PyPhi Documentation

Release v1.1.0

William GP Mayner

May 30, 2018

Usage and Examples

1 Installation

Python Module Index

PyPhi is a Python library for computing integrated information.

To report issues, use the issue tracker on the GitHub repository. Bug reports and pull requests are welcome.

For general discussion, you are welcome to join the pyphi-users group.

CHAPTER 1

Installation

To install the latest stable release, run

pip install pyphi

To install the latest development version, which is a work in progress and may have bugs, run

pip install "git+https://github.com/wmayner/pyphi@develop#egg=pyphi"

Tip: For detailed instructions on how to install PyPhi on macOS, see the Detailed installation guide for macOS.

Note: Windows users: PyPhi is only supported on Linux and macOS operating systems. However, you can run it on Windows by using the Anaconda Python distribution and installing PyPhi with conda: conda install -c wmayner pyphi

1.1 Installation

To install the latest stable release, run

pip install pyphi

To install the latest development version, which is a work in progress and may have bugs, run

pip install "git+https://github.com/wmayner/pyphi@develop#egg=pyphi"

Tip: For detailed instructions on how to install PyPhi on macOS, see the Detailed installation guide for macOS.

Note: Windows users: PyPhi is only supported on Linux and macOS operating systems. However, you can run it on Windows by using the Anaconda Python distribution and installing PyPhi with conda: conda install -c wmayner pyphi

1.2 Getting started

To explore the following examples, install IPython by running pip install ipython on the command line. Then run it with the command ipython.

Lines of code beginning with >>> and . . . can be pasted directly into IPython.

1.3 Basic Usage

Let's make a simple 3-node network and compute its Φ .

To make a network, we need a TPM and (optionally) a connectivity matrix. The TPM can be in more than one form; see the documentation for *Network*. Here we'll use the 2-dimensional state-by-node form.

```
>>> import pyphi
>>> import numpy as np
>>> tpm = np.array([
         [0, 0, 0],
. . .
         [0, 0, 1],
. . .
         [1, 0, 1],
. . .
. . .
         [1, 0, 0],
         [1, 1, 0],
. . .
         [1, 1, 1],
. . .
         [1, 1, 1],
. . .
         [1, 1, 0]
. . .
...])
```

The connectivity matrix is a square matrix such that the (i, j)th entry is 1 if there is a connection from node *i* to node *j*, and 0 otherwise.

```
>>> cm = np.array([
... [0, 0, 1],
... [1, 0, 1],
... [1, 1, 0]
... ])
```

We'll also make labels for the network nodes so that PyPhi's output is easier to read.

>>> labels = ('A', 'B', 'C')

Now we construct the network itself with the arguments we just created:

>>> network = pyphi.Network(tpm, cm=cm, node_labels=labels)

The next step is to define a subsystem for which we want to evaluate Φ . To make a subsystem, we need the network that it belongs to, the state of that network, and the indices of the subset of nodes which should be included.

The state should be an *n*-tuple, where *n* is the number of nodes in the network, and where the i^{th} element is the state of the i^{th} node in the network.

>>> state = (1, 0, 0)

In this case, we want the Φ of the entire network, so we simply include every node in the network in our subsystem:

```
>>> node_indices = (0, 1, 2)
>>> subsystem = pyphi.Subsystem(network, state, node_indices)
```

Tip: If you do not explicitly provide node indices to a *Subsystem* the system will, by default, cover the entire network. For example, the following is equivalent to the above definition of subsystem:

```
>>> subsystem = pyphi.Subsystem(network, state)
```

Tip: Node labels can be used instead of indices when constructing a *Subsystem*:

```
>>> pyphi.Subsystem(network, state, ('B', 'C'))
Subsystem(B, C)
```

Now we use the *phi* () function to compute the Φ of our subsystem:

```
>>> pyphi.compute.phi(subsystem)
2.3125
```

If we want to take a deeper look at the integrated-information-theoretic properties of our network, we can access all the intermediate quantities and structures that are calculated in the course of arriving at a final Φ value by using *sia()*. This returns a nested object, *SystemIrreducibilityAnalysis*, that contains data about the subsystem's cause-effect structure, cause and effect repertoires, etc.

>>> sia = pyphi.compute.sia(subsystem)

For instance, we can see that this network has 4 concepts:

```
>>> len(sia.ces)
4
```

See the documentation for *SystemIrreducibilityAnalysis* and *Concept* for more information on these objects.

Tip: The network and subsystem discussed here are returned by the *pyphi.examples.basic_network()* and *pyphi.examples.basic_subsystem()* functions.

1.4 IIT 3.0 Paper (2014)

This section is meant to serve as a companion to the paper From the Phenomenology to the Mechanisms of Consciousness: Integrated Information Theory 3.0 by Oizumi, Albantakis, and Tononi, and as a demonstration of how to use PyPhi. Readers are encouraged to follow along and analyze the systems shown in the figures, in order to become more familiar with both the theory and the software. Install IPython by running pip install ipython on the command line. Then run it with the command ipython.

Lines of code beginning with >>> and . . . can be pasted directly into IPython.

We begin by importing PyPhi and NumPy:

```
>>> import pyphi
>>> import numpy as np
```

1.4.1 Figure 1

Existence: Mechanisms in a state having causal power.

For the first figure, we'll demonstrate how to set up a network and a candidate set. In PyPhi, networks are built by specifying a transition probability matrix and (optionally) a connectivity matrix. (If no connectivity matrix is given, full connectivity is assumed.) So, to set up the system shown in Figure 1, we'll start by defining its TPM.

Note: The TPM in the figure is given in **state-by-state** form; there is a row and a column for each state. However, in PyPhi, we use a more compact representation: **state-by-node** form, in which there is a row for each state, but a column for each node. The (i, j)th entry gives the probability that the jth node is ON in the ith state. For more information on how TPMs are represented in PyPhi, see *Transition probability matrix conventions*.

In the figure, the TPM is shown only for the candidate set. We'll define the entire network's TPM. Also, nodes D, E and F are not assigned mechanisms; for the purposes of this example we will assume they are OR gates. With that assumption, we get the following TPM (before copying and pasting, see note below):

-								
>>>	tpm	= nj	p.a	rra	y([
		[0,	Ο,	Ο,	Ο,	Ο,	0],	
•••		[0,	Ο,	1,	Ο,	Ο,	0],	
•••		[1,	Ο,	1,	Ο,	1,	0],	
•••		[1,	Ο,	Ο,	Ο,	1,	0],	
•••		[1,	Ο,	Ο,	Ο,	Ο,	0],	
•••		[1,					0],	
•••		[1,	Ο,	1,	Ο,	1,	0],	
•••		[1,	1,	Ο,	Ο,	1,	0],	
•••		[1,	Ο,	Ο,	Ο,	Ο,	0],	
•••		[1,	Ο,	1,	Ο,	Ο,	0],	
•••		[1,	Ο,	1,	Ο,	1,	0],	
•••		[1,	Ο,	Ο,	Ο,	1,	0],	
•••		[1,	Ο,	Ο,	Ο,	Ο,	0],	
•••		[1,	1,	1,	Ο,	Ο,	0],	
•••		[1,	Ο,	1,	Ο,	1,	0],	
•••		[1,	1,	Ο,	Ο,	1,	0],	
•••		[0,	Ο,	Ο,	Ο,	Ο,	0],	
•••		[0,				Ο,		
•••		[1,	Ο,	1,			0],	
•••		[1,	Ο,	Ο,	Ο,	1,	0],	
• • •		[1,	Ο,			Ο,	0],	
•••		[1,	1,	1,	Ο,	Ο,	0],	
•••		[1,	Ο,	1,	Ο,	1,	0],	
		[1,	1,	Ο,		1,		
		[1,	Ο,	Ο,	Ο,	Ο,	0],	
•••		[1,	Ο,	1,	Ο,	Ο,	0],	
•••		[1,	Ο,	1,	Ο,	1,	0],	

(continues on next page)

(continued from previous page)

		(continued from previous page)
	[1, 0, 0, 0, 1, 0],	
	[1, 0, 0, 0, 0],	
	[1, 1, 1, 0, 0, 0],	
	[1, 0, 1, 0, 1, 0],	
	[1, 1, 0, 0, 1, 0],	
	[0, 0, 0, 0, 0],	
•••	[0, 0, 1, 0, 0, 0],	
	[1, 0, 1, 0, 1, 0],	
	[1, 0, 0, 0, 1, 0],	
•••	[1, 0, 0, 0, 0],	
•••	[1, 1, 1, 0, 0],	
•••	[1, 0, 1, 0, 1, 0],	
•••	[1, 1, 0, 0, 1, 0],	
•••	[1, 0, 0, 0, 0, 0],	
•••	[1, 0, 1, 0, 0, 0],	
•••	[1, 0, 1, 0, 1, 0],	
•••	[1, 0, 0, 0, 1, 0],	
•••	[1, 0, 0, 0, 0, 0],	
•••	[1, 1, 1, 0, 0, 0],	
•••	$[1, 0, 1, 0, 1, 0], \\ [1, 1, 0, 0, 1, 0],$	
	[0, 0, 0, 0, 0, 0],	
	[0, 0, 1, 0, 0, 0],	
	[1, 0, 1, 0, 1, 0],	
	[1, 0, 0, 1, 0],	
	[1, 0, 0, 0, 0, 0],	
	[1, 1, 1, 0, 0, 0],	
	[1, 0, 1, 0, 1, 0],	
	[1, 1, 0, 0, 1, 0],	
	[1, 0, 0, 0, 0],	
	[1, 0, 1, 0, 0, 0],	
	[1, 0, 1, 0, 1, 0],	
	[1, 0, 0, 0, 1, 0],	
	[1, 0, 0, 0, 0],	
	[1, 1, 1, 0, 0],	
	[1, 0, 1, 0, 1, 0],	
	[1, 1, 0, 0, 1, 0]	
])		

Note: This network is already built for you; you can get it from the *examples* module with network = pyphi. examples.fig0a(). The TPM can then be accessed with network.tpm.

Next we'll define the connectivity matrix. In PyPhi, the $(i, j)^{\text{th}}$ entry in a connectivity matrix indicates whether node i is connected to node j. Thus, this network's connectivity matrix is

>>> cm = np.array([
... [0, 1, 1, 0, 0, 0],
... [1, 0, 1, 0, 1, 0],
... [1, 1, 0, 0, 0, 0],
... [1, 0, 0, 0, 0, 0],
... [0, 0, 0, 0, 0, 0],
... [0, 0, 0, 0, 0, 0],
...])

Now we can pass the TPM and connectivity matrix as arguments to the network constructor:

>>> network = pyphi.Network(tpm, cm=cm)

Now the network shown in the figure is stored in a variable called network. You can find more information about the network object we just created by running help (network) or by consulting the documentation for *Network*.

The next step is to define the candidate set shown in the figure, consisting of nodes A, B and C. In PyPhi, a candidate set for Φ evaluation is represented by the *Subsystem* class. Subsystems are built by giving the network it is a part of, the state of the network, and indices of the nodes to be included in the subsystem. So, we define our candidate set like so:

>>> state = (1, 0, 0, 0, 1, 0)
>>> ABC = pyphi.Subsystem(network, state, [0, 1, 2])

For more information on the subsystem object, see the documentation for Subsystem.

That covers the basic workflow with PyPhi and introduces the two types of objects we use to represent and analyze networks. First you define the network of interest with a TPM and connectivity matrix; then you define a candidate set you want to analyze.

1.4.2 Figure 3

Information requires selectivity.

(A)

We'll start by setting up the subsystem depicted in the figure and labeling the nodes. In this case, the subsystem is just the entire network.

```
>>> network = pyphi.examples.fig3a()
>>> state = (1, 0, 0, 0)
>>> subsystem = pyphi.Subsystem(network, state)
>>> A, B, C, D = subsystem.node_indices
```

Since the connections are noisy, we see that A = 1 is unselective; all previous states are equally likely:

```
>>> subsystem.cause_repertoire((A,), (B, C, D))
array([[[0.125, 0.125],
       [0.125, 0.125]],
       [[0.125, 0.125],
       [0.125, 0.125]]])
```

And this gives us zero cause information:

```
>>> subsystem.cause_info((A,), (B, C, D))
0.0
```

(B)

The same as (A) but without noisy connections:

```
>>> network = pyphi.examples.fig3b()
>>> subsystem = pyphi.Subsystem(network, state)
>>> A, B, C, D = subsystem.node_indices
```

Now, A's cause repertoire is maximally selective.

```
>>> cr = subsystem.cause_repertoire((A,), (B, C, D))
>>> cr
array([[[[0., 0.],
       [0., 0.]],
       [[0., 0.],
       [0., 1.]]]))
```

Since the cause repertoire is over the purview BCD, the first dimension (which corresponds to A's states) is a singleton. We can squeeze out A's singleton dimension with

```
>>> cr = cr.squeeze()
```

and now we can see that the probability of *B*, *C*, and *D* having been all ON is 1:

```
>>> cr[(1, 1, 1)]
1.0
```

Now the cause information specified by A = 1 is 1.5:

```
>>> subsystem.cause_info((A,), (B, C, D))
1.5
```

(C)

The same as (B) but with A = 0:

```
>>> state = (0, 0, 0, 0)
>>> subsystem = pyphi.Subsystem(network, state)
>>> A, B, C, D = subsystem.node_indices
```

And here the cause repertoire is minimally selective, only ruling out the state where B, C, and D were all ON:

```
>>> subsystem.cause_repertoire((A,), (B, C, D))
array([[[0.14285714, 0.14285714],
       [0.14285714, 0.14285714]],
       [[0.14285714, 0.14285714],
       [0.14285714, 0. ]]]))
```

And so we have less cause information:

```
>>> subsystem.cause_info((A,), (B, C, D))
0.214284
```

1.4.3 Figure 4

Information: "Differences that make a difference to a system from its own intrinsic perspective."

First we'll get the network from the *examples* module, set up a subsystem, and label the nodes, as usual:

```
>>> network = pyphi.examples.fig4()
>>> state = (1, 0, 0)
>>> subsystem = pyphi.Subsystem(network, state)
>>> A, B, C = subsystem.node_indices
```

Then we'll compute the cause and effect repertoires of mechanism A over purview ABC:

```
>>> subsystem.cause_repertoire((A,), (A, B, C))
array([[[0. , 0.16666667],
       [0.16666667, 0.16666667]],
       [0.16666667, 0.16666667]])
>>> subsystem.effect_repertoire((A,), (A, B, C))
array([[[0.0625, 0.0625],
       [0.0625, 0.0625]],
       [[0.1875, 0.1875],
       [0.1875, 0.1875],
       [0.1875, 0.1875]]])
```

And the unconstrained repertoires over the same (these functions don't take a mechanism; they only take a purview):

```
>>> subsystem.unconstrained_cause_repertoire((A, B, C))
array([[0.125, 0.125],
       [0.125, 0.125]],
       [[0.125, 0.125]]])
>>> subsystem.unconstrained_effect_repertoire((A, B, C))
array([[[0.09375, 0.09375],
       [0.03125, 0.03125]],
       [[0.28125, 0.28125],
       [[0.09375, 0.09375]]])
```

The Earth Mover's distance between them gives the cause and effect information:

```
>>> subsystem.cause_info((A,), (A, B, C))
0.333332
>>> subsystem.effect_info((A,), (A, B, C))
0.25
```

And the minimum of those gives the cause-effect information:

```
>>> subsystem.cause_effect_info((A,), (A, B, C))
0.25
```

1.4.4 Figure 5

A mechanism generates information only if it has both selective causes and selective effects within the system.

(A)

```
>>> network = pyphi.examples.fig5a()
>>> state = (1, 1, 1)
>>> subsystem = pyphi.Subsystem(network, state)
>>> A, B, C = subsystem.node_indices
```

A has inputs, so its cause repertoire is selective and it has cause information:

```
>>> subsystem.cause_repertoire((A,), (A, B, C))
array([[[0., 0.],
            [0., 0.5]],
            [[0., 0.5]]])
>>> subsystem.cause_info((A,), (A, B, C))
1.0
```

But because it has no outputs, its effect repertoire no different from the unconstrained effect repertoire, so it has no effect information:

```
>>> np.array_equal(subsystem.effect_repertoire((A,), (A, B, C)),
... subsystem.unconstrained_effect_repertoire((A, B, C)))
True
>>> subsystem.effect_info((A,), (A, B, C))
0.0
```

And thus its cause effect information is zero.

```
>>> subsystem.cause_effect_info((A,), (A, B, C))
0.0
```

(B)

```
>>> network = pyphi.examples.fig5b()
>>> state = (1, 0, 0)
>>> subsystem = pyphi.Subsystem(network, state)
>>> A, B, C = subsystem.node_indices
```

Symmetrically, A now has outputs, so its effect repertoire is selective and it has effect information:

```
>>> subsystem.effect_repertoire((A,), (A, B, C))
array([[[0., 0.],
            [0., 0.]],
            [[0., 0.],
            [0., 1.]]])
>>> subsystem.effect_info((A,), (A, B, C))
0.5
```

But because it now has no inputs, its cause repertoire is no different from the unconstrained effect repertoire, so it has no cause information:

```
>>> np.array_equal(subsystem.cause_repertoire((A,), (A, B, C)),
... subsystem.unconstrained_cause_repertoire((A, B, C)))
True
>>> subsystem.cause_info((A,), (A, B, C))
0.0
```

And its cause effect information is again zero.

```
>>> subsystem.cause_effect_info((A,), (A, B, C))
0.0
```

1.4.5 Figure 6

Integrated information: The information generated by the whole that is irreducible to the information generated by its parts.

```
>>> network = pyphi.examples.fig6()
>>> state = (1, 0, 0)
>>> subsystem = pyphi.Subsystem(network, state)
>>> ABC = subsystem.node_indices
```

Here we demonstrate the functions that find the minimum information partition a mechanism over a purview:

```
>>> mip_c = subsystem.cause_mip(ABC, ABC)
>>> mip_e = subsystem.effect_mip(ABC, ABC)
```

These objects contain the $\varphi_{\text{cause}}^{\text{MIP}}$ and $\varphi_{\text{effect}}^{\text{MIP}}$ values in their respective phi attributes, and the minimal partitions in their partition attributes:

```
>>> mip_c.phi
0.4999999
>>> mip_c.partition
A B,C
A,B,C
>>> mip_e.phi
0.25
>>> mip_e.partition
A,B,C
B A,C
```

For more information on these objects, see the documentation for the *RepertoireIrreducibilityAnalysis* class, or use help(mip_c).

Note that the minimal partition found for the cause is

$$\frac{A^c}{\varnothing} \times \frac{BC^c}{ABC^p},$$

rather than the one shown in the figure. However, both partitions result in a difference of 0.5 between the unpartitioned and partitioned cause repertoires. So we see that in small networks like this, there can be multiple choices of partition that yield the same, minimal φ^{MIP} . In these cases, which partition the software chooses is left undefined.

1.4.6 Figure 7

A mechanism generates integrated information only if it has both integrated causes and integrated effects.

It is left as an exercise for the reader to use the subsystem methods cause_mip and effect_mip, introduced in the previous section, to demonstrate the points made in Figure 7.

To avoid building TPMs and connectivity matrices by hand, you can use the graphical user interface for PyPhi available online at http://integratedinformationtheory.org/calculate.html. You can build the networks shown in the figure there,

and then use the **Export** button to obtain a JSON file representing the network. You can then import the file into Python like so:

network = pyphi.network.from_json('path/to/network.json')

1.4.7 Figure 8

The maximally integrated cause repertoire over the power set of purviews is the "core cause" specified by a mechanism.

```
>>> network = pyphi.examples.fig8()
>>> state = (1, 0, 0)
>>> subsystem = pyphi.Subsystem(network, state)
>>> A, B, C = subsystem.node_indices
```

In PyPhi, the "core cause" is called the *maximally-irreducible cause* (MIC). To find the MIC of a mechanism over all purviews, use the *mic()* method:

```
>>> mic = subsystem.mic((B, C))
>>> mic.phi
0.333334
```

Similarly, the mie () method returns the "core effect" or maximally-irreducible effect (MIE).

For a detailed description of the MIC and MIE objects returned by these methods, see the documentation for *MaximallyIrreducibleCause* or use help(subsystem.mic) and help(subsystem.mie).

1.4.8 Figure 9

A mechanism that specifies a maximally irreducible cause-effect repertoire.

This figure and the next few use the same network as in Figure 8, so we don't need to reassign the network and subsystem variables.

Together, the MIC and MIE of a mechanism specify a *concept*. In PyPhi, this is represented by the *Concept* object. Concepts are computed using the *concept* () method of a subsystem:

```
>>> concept_A = subsystem.concept((A,))
>>> concept_A.phi
0.166667
```

As usual, please consult the documentation or use help(concept_A) for a detailed description of the *Concept* object.

1.4.9 Figure 10

Information: A conceptual structure C (constellation of concepts) is the set of all concepts generated by a set of elements in a state.

For functions of entire subsystems rather than mechanisms within them, we use the *compute* module. In this figure, we see the constellation of concepts of the powerset of *ABC*'s mechanisms. A constellation of concepts is represented in PyPhi by a *CauseEffectStructure*. We can compute the cause-effect structure of the subsystem like so:

```
>>> ces = pyphi.compute.ces(subsystem)
```

And verify that the φ values match:

```
>>> ces.labeled_mechanisms
(['A'], ['B'], ['C'], ['A', 'B'], ['B', 'C'], ['A', 'B', 'C'])
>>> ces.phis
[0.166667, 0.166667, 0.25, 0.25, 0.333334, 0.499999]
```

The null concept (the small black cross shown in concept-space) is available as an attribute of the subsystem:

```
>>> subsystem.null_concept.phi
0.0
```

1.4.10 Figure 11

Assessing the conceptual information CI of a conceptual structure (constellation of concepts).

Conceptual information can be computed using the function named, as you might expect, conceptual_info():

```
>>> pyphi.compute.conceptual_info(subsystem)
2.111109
```

1.4.11 Figure 12

Assessing the integrated conceptual information Φ of a constellation C.

To calculate Φ^{MIP} for a candidate set, we use the function *sia()*:

```
>>> sia = pyphi.compute.sia(subsystem)
```

The returned value is a large object containing the Φ^{MIP} value, the minimal cut, the cause-effect structure of the whole set and that of the partitioned set $C_{\rightarrow}^{\text{MIP}}$, the total calculation time, the calculation time for just the unpartitioned cause-effect structure, a reference to the subsystem that was analyzed, and a reference to the subsystem with the minimal unidirectional cut applied. For details see the documentation for *SystemIrreducibilityAnalysis* or use help(sia).

We can verify that the Φ^{MIP} value and minimal cut are as shown in the figure:

```
>>> sia.phi
1.916665
>>> sia.cut
Cut [A, B] / / [C]
```

Note: This Cut represents removing any connections from the nodes with indices 0 and 1 to the node with index 2.

1.4.12 Figure 13

A set of elements generates integrated conceptual information Φ only if each subset has both causes and effects in the rest of the set.

It is left as an exercise for the reader to demonstrate that of the networks shown, only (B) has $\Phi > 0$.

1.4.13 Figure 14

A complex: A local maximum of integrated conceptual information Φ .

>>> network = pyphi.examples.fig14()
>>> state = (1, 0, 0, 0, 1, 0)

To find the subsystem within a network that is the major complex, we use the function of that name, which returns a *SystemIrreducibilityAnalysis* object:

>>> major_complex = pyphi.compute.major_complex(network, state)

And we see that the nodes in the complex are indeed A, B, and C:

```
>>> major_complex.subsystem.nodes
(A, B, C)
```

1.4.14 Figure 15

A quale: The maximally irreducible conceptual structure (MICS) generated by a complex.

You can use the visual interface at http://integratedinformationtheory.org/calculate.html to view a conceptual structure structure in a 3D projection of qualia space. The network in the figure is already built for you; click the **Load Example** button and select "IIT 3.0 Paper, Figure 1" (this network is the same as the candidate set in Figure 1).

1.4.15 Figure 16

A system can condense into a major complex and minor complexes that may or may not interact with it.

For this figure, we omit nodes H, I, J, K and L, since the TPM of the full 12-node network is very large, and the point can be illustrated without them.

```
>>> network = pyphi.examples.fig16()
>>> state = (1, 0, 0, 1, 1, 1, 0)
```

To find the maximal set of non-overlapping complexes that a network condenses into, use condensed ():

>>> condensed = pyphi.compute.condensed(network, state)

We find that there are two complexes: the major complex ABC with $\Phi \approx 1.92$, and a minor complex FG with $\Phi \approx 0.069$ (note that there is typo in the figure: FG's Φ value should be 0.069). Furthermore, the program has been updated to only consider background conditions of current states, not previous states; as a result the minor complex DE shown in the paper no longer exists.

```
>>> len(condensed)
2
>>> ABC, FG = condensed
>>> (ABC.subsystem.nodes, ABC.phi)
((A, B, C), 1.916665)
>>> (FG.subsystem.nodes, FG.phi)
((F, G), 0.069445)
```

There are several other functions available for working with complexes; see the documentation for *subsystems()*, *all_complexes()*, *possible_complexes()*, and *complexes()*.

1.5 Conditional Independence

Conditional independence is the property of a TPM that each node's state at time t + 1 must be independent of the state of the others, given the state of the network at time t:

$$\Pr(S_{t+1} \mid S_t = s_t) = \prod_{N \in S} \Pr(N_{t+1} \mid S_t = s_t), \quad \forall \ s_t \in S.$$

This example explores the assumption of conditional independence, and the behaviour of the program when it is not satisfied.

Every state-by-node TPM corresponds to a unique state-by-state TPM which satisfies the conditional independence property (see *Transition probability matrix conventions* for a discussion of the different TPM forms). If a state-by-node TPM is given as input for a *Network*, PyPhi assumes that it is from a system with the corresponding conditionally independent state-by-state TPM.

When a state-by-state TPM is given as input for a *Network*, the state-by-state TPM is first converted to a state-by-node TPM. PyPhi then assumes that the system corresponds to the unique conditionally independent representation of the state-by-node TPM.

Note: Every deterministic state-by-state TPM satisfies the conditional independence property.

Consider a system of two binary nodes (A and B) which do not change if they have the same value, but flip with probability 50% if they have different values.

We'll load the state-by-state TPM for such a system from the *examples* module:

```
>>> import pyphi
>>> tpm = pyphi.examples.cond_depend_tpm()
>>> print(tpm)
[[1. 0. 0. 0. ]
[0. 0.5 0.5 0. ]
[0. 0.5 0.5 0. ]
[0. 0. 0. 1. ]]
```

This system does not satisfy the conditional independence property; given a previous state of (1, 0), the current state of node A depends on whether or not B has flipped.

If a conditionally dependent TPM is used to create a *Network*, PyPhi will raise an error:

```
>>> network = pyphi.Network(tpm)
Traceback (most recent call last):
    ...
pyphi.exceptions.ConditionallyDependentError: TPM is not conditionally independent.
See the conditional independence example in the documentation for more info.
```

To see the conditionally independent TPM that corresponds to the conditionally dependent TPM, convert it to stateby-node form and then back to state-by-state form:

```
>>> sbn_tpm = pyphi.convert.state_by_state2state_by_node(tpm)
>>> print(sbn_tpm)
[[[0. 0. ]
    [0.5 0.5]]
[[0.5 0.5]
    [1. 1. ]]]
```

(continues on next page)

(continued from previous page)

```
>>> sbs_tpm = pyphi.convert.state_by_node2state_by_state(sbn_tpm)
>>> print(sbs_tpm)
[[1. 0. 0. 0. ]
[0.25 0.25 0.25 0.25]
[0.25 0.25 0.25 0.25]
[0. 0. 0. 1. ]]
```

A system which does not satisfy the conditional independence property exhibits "instantaneous causality." In such situations, there must be additional exogenous variable(s) which explain the dependence.

Now consider the above example, but with the addition of a third node (C) which is equally likely to be ON or OFF, and such that when nodes A and B are in different states, they will flip when C is ON, but stay the same when C is OFF.

```
>>> tpm2 = pyphi.examples.cond_independ_tpm()
>>> print(tpm2)
[[0.5 0. 0. 0. 0.5 0. 0. 0. ]
[0. 0.5 0. 0. 0. 0.5 0. 0. ]
[0. 0. 0.5 0. 0. 0. 0.5 0. ]
[0. 0. 0. 0.5 0. 0. 0. 0.5]
[0.5 0. 0. 0. 0.5 0. 0. 0. ]
[0. 0. 0.5 0. 0. 0. 0.5 0. ]
[0. 0. 5 0. 0. 0. 0.5 0. 0. ]
[0. 0. 0.5 0. 0. 0. 0.5 0. ]
[0. 0. 0.5 0. 0. 0. 0.5 0. ]
[0. 0. 0. 0.5 0. 0. 0. 0.5]]
```

The resulting state-by-state TPM now satisfies the conditional independence property.

```
>>> sbn_tpm2 = pyphi.convert.state_by_state2state_by_node(tpm2)
>>> print(sbn_tpm2)
[[[[0. 0. 0.5]]
[[0. 1. 0.5]]
[[1. 0. 0.5]]]
[[1. 0. 0.5]]
[[1. 1. 0.5]]
[[1. 1. 0.5]]]
```

The node indices are 0 and 1 for A and B, and 2 for C:

```
>>> AB = [0, 1]
>>> C = [2]
```

From here, if we marginalize out the node C;

>>> tpm2_marginalizeC = pyphi.tpm.marginalize_out(C, sbn_tpm2)

And then restrict the purview to only nodes A and B;

```
>>> import numpy as np
>>> tpm2_purviewAB = np.squeeze(tpm2_marginalizeC[:,:,:,AB])
```

We get back the original state-by-node TPM from the system with just A and B.

```
>>> np.all(tpm2_purviewAB == sbn_tpm)
True
```

1.6 XOR Network

This example describes a system of three fully connected XOR nodes, A, B and C (no self-connections).

First let's create the XOR network:

```
>>> import pyphi
>>> network = pyphi.examples.xor_network()
```

We'll consider the state with all nodes OFF.

>>> state = (0, 0, 0)

According to IIT, existence is a holistic notion; the whole is more important than its parts. The first step is to confirm the existence of the whole, by finding the major complex of the network:

>>> major_complex = pyphi.compute.major_complex(network, state)

The major complex exists ($\Phi > 0$),

```
>>> major_complex.phi
1.874999
```

and it consists of the entire network:

```
>>> major_complex.subsystem
Subsystem(A, B, C)
```

Knowing what exists at the system level, we can now investigate the existence of concepts within the complex.

```
>>> ces = major_complex.ces
>>> len(ces)
3
>>> ces.labeled_mechanisms
(['A', 'B'], ['A', 'C'], ['B', 'C'])
```

There are three concepts in the cause-effect structure. They are all the possible second order mechanisms: AB, AC and BC.

Focusing on the concept specified by mechanism AB, we investigate existence, and the irreducible cause and effect. Based on the symmetry of the network, the results will be similar for the other second order mechanisms.

```
>>> concept = ces[0]
>>> concept.mechanism
(0, 1)
>>> concept.phi
0.5
```

The concept has $\varphi = \frac{1}{2}$.

```
>>> concept.cause.purview
(0, 1, 2)
>>> concept.cause.repertoire
array([[[0.5, 0. ],
        [0. , 0. ]],
        [[0. , 0. ],
        [0. , 0.5]]])
```

So we see that the cause purview of this mechanism is the whole system ABC, and that the repertoire shows a 0.5 of probability the previous state being (0, 0, 0) and the same for (1, 1, 1):

```
>>> concept.cause.repertoire[(0, 0, 0)]
0.5
>>> concept.cause.repertoire[(1, 1, 1)]
0.5
```

This tells us that knowing both A and B are currently OFF means that the previous state of the system was either all OFF or all ON with equal probability.

For any reduced purview, we would still have the same information about the elements in the purview (either all ON or all OFF), but we would lose the information about the elements outside the purview.

```
>>> concept.effect.purview
(2,)
>>> concept.effect.repertoire
array([[[1., 0.]]])
```

The effect purview of this concept is the node C. The mechanism AB is able to completely specify the next state of C. Since both nodes are OFF, the next state of C will be OFF.

The mechanism AB does not provide any information about the next state of either A or B, because the relationship depends on the value of C. That is, the next state of A (or B) may be either ON or OFF, depending on the value of C. Any purview larger than C would be reducible by pruning away the additional elements.

Major Complex: ABC with $\Phi = 1.875$							
Mechanism	φ	Cause Purview	Effect Purview				
AB	0.5	ABC	C				
AC	0.5	ABC	В				
BC	0.5	ABC	A				

An analysis of the *intrinsic existence* of this system reveals that the major complex of the system is the entire network of XOR nodes. Furthermore, the concepts which exist within the complex are those specified by the second-order mechanisms *AB*, *AC*, and *BC*.

To understand the notion of intrinsic existence, in addition to determining what exists for the system, it is useful to consider also what does not exist.

Specifically, it may be surprising that none of the first order mechanisms A, B or C exist. This physical system of XOR gates is sitting on the table in front of me; I can touch the individual elements of the system, so how can it be that they do not exist?

That sort of existence is what we term *extrinsic existence*. The XOR gates exist for me as an observer, external to the system. I am able to manipulate them, and observe their causes and effects, but the question that matters for *intrinsic* existence is, do they have irreducible causes and effects within the system? There are two reasons a mechanism may have no irreducible cause-effect power: either the cause-effect power is completely reducible, or there was no cause-effect power to begin with. In the case of elementary mechanisms, it must be the latter.

To see this, again due to symmetry of the system, we will focus only on the mechanism A.

```
>>> subsystem = pyphi.examples.xor_subsystem()
>>> A = (0,)
>>> ABC = (0, 1, 2)
```

In order to exist, a mechanism must have irreducible cause and effect power within the system.

```
>>> subsystem.cause_info(A, ABC)
0.5
>>> subsystem.effect_info(A, ABC)
0.0
```

The mechanism has no effect power over the entire subsystem, so it cannot have effect power over any purview within the subsystem. Furthermore, if a mechanism has no effect power, it certainly has no irreducible effect power. The first-order mechanisms of this system do not exist intrinsically, because they have no effect power (having causal power is not enough).

To see why this is true, consider the effect of A. There is no self-loop, so A can have no effect on itself. Without knowing the current state of A, in the next state B could be either ON or OFF. If we know that the current state of A is ON, then B could still be either ON or OFF, depending on the state of C. Thus, on its own, the current state of A does not provide any information about the next state of B. A similar result holds for the effect of A on C. Since A has no effect power over any element of the system, it does not exist from the intrinsic perspective.

To complete the discussion, we can also investigate the potential third order mechanism ABC. Consider the cause information over the purview ABC:

```
>>> subsystem.cause_info(ABC, ABC)
0.749999
```

Since the mechanism has nonzero cause information, it has causal power over the system—but is it irreducible?

```
>>> mip = subsystem.cause_mip(ABC, ABC)
>>> mip.phi
0.0
>>> mip.partition
A B,C
A,B,C
```

The mechanism has ci = 0.75, but it is completely reducible ($\varphi = 0$) to the partition

$$\frac{A}{\varnothing} \times \frac{BC}{ABC}$$

This result can be understood as follows: knowing that B and C are OFF in the current state is sufficient to know that A, B, and C were all OFF in the previous state; there is no additional information gained by knowing that A is currently OFF.

Similarly for any other potential purview, the current state of B and C being (0, 0) is always enough to fully specify the previous state, so the mechanism is reducible for all possible purviews, and hence does not exist.

1.7 Emergence (coarse-graining and blackboxing)

1.7.1 Coarse-graining

We'll use the *macro* module to explore alternate spatial scales of a network. The network under consideration is a 4-node non-deterministic network, available from the *examples* module.

```
>>> import pyphi
>>> network = pyphi.examples.macro_network()
```

The connectivity matrix is all-to-all:

```
>>> network.cm
array([[1., 1., 1., 1.],
        [1., 1., 1., 1.],
        [1., 1., 1., 1.],
        [1., 1., 1., 1.]])
```

We'll set the state so that nodes are OFF.

>>> state = (0, 0, 0, 0)

At the "micro" spatial scale, we can compute the major complex, and determine the Φ value:

```
>>> major_complex = pyphi.compute.major_complex(network, state)
>>> major_complex.phi
0.113889
```

The question is whether there are other spatial scales which have greater values of Φ . This is accomplished by considering all possible coarse-graining of micro-elements to form macro-elements. A coarse-graining of nodes is any partition of the elements of the micro system. First we'll get a list of all possible coarse-grainings:

>>> grains = list(pyphi.macro.all_coarse_grains(network.node_indices))

We start by considering the first coarse grain:

>>> coarse_grain = grains[0]

Each *CoarseGrain* has two attributes: the partition of states into macro elements, and the grouping of micro-states into macro-states. Let's first look at the partition:

```
>>> coarse_grain.partition
((0, 1, 2), (3,))
```

There are two macro-elements in this partition: one consists of micro-elements (0, 1, 2) and the other is simply micro-element 3.

We must then determine the relationship between micro-elements and macro-elements. When coarse-graining the system we assume that the resulting macro-elements do not differentiate the different micro-elements. Thus any correspondence between states must be stated solely in terms of the number of micro-elements which are ON, and not depend on which micro-elements are ON.

For example, consider the macro-element (0, 1, 2). We may say that the macro-element is ON if at least one micro-element is ON, or if all micro-elements are ON; however, we may not say that the macro-element is ON if micro-element 1 is ON, because this relationship involves identifying specific micro-elements.

The grouping attribute of the *CoarseGrain* describes how the state of micro-elements describes the state of macro-elements:

```
>>> grouping = coarse_grain.grouping
>>> grouping
((((0, 1, 2), (3,)), ((0,), (1,)))
```

The grouping consists of two lists, one for each macro-element:

```
>>> grouping[0]
((0, 1, 2), (3,))
```

For the first macro-element, this grouping means that the element will be OFF if zero, one or two of its micro-elements are ON, and will be ON if all three micro-elements are ON.

```
>>> grouping[1]
((0,), (1,))
```

For the second macro-element, the grouping means that the element will be OFF if its micro-element is OFF, and ON if its micro-element is ON.

One we have selected a partition and grouping for analysis, we can create a mapping between micro-states and macrostates:

```
>>> mapping = coarse_grain.make_mapping()
>>> mapping
array([0, 0, 0, 0, 0, 0, 0, 1, 2, 2, 2, 2, 2, 2, 3])
```

The interpretation of the mapping uses the little-endian convention of indexing (see Little-endian convention).

>>> mapping[7] 1

This says that micro-state 7 corresponds to macro-state 1:

```
>>> pyphi.convert.le_index2state(7, 4)
(1, 1, 1, 0)
```

```
>>> pyphi.convert.le_index2state(1, 2)
(1, 0)
```

In micro-state 7, all three elements corresponding to the first macro-element are ON, so that macro-element is ON. The micro-element corresponding to the second macro-element is OFF, so that macro-element is OFF.

The *CoarseGrain* object uses the mapping internally to create a state-by-state TPM for the macro-system corresponding to the selected partition and grouping

```
>>> coarse_grain.macro_tpm(network.tpm)
Traceback (most recent call last):
    ...
pyphi.exceptions.ConditionallyDependentError...
```

However, this macro-TPM does not satisfy the conditional independence assumption, so this particular partition and grouping combination is not a valid coarse-graining of the system. Constructing a *MacroSubsystem* with this coarse-graining will also raise a *ConditionallyDependentError*.

Let's consider a different coarse-graining instead.

```
>>> coarse_grain = grains[14]
>>> coarse_grain.partition
```

(continues on next page)

(continued from previous page)

```
((0, 1), (2, 3))
>>> coarse_grain.grouping
(((0, 1), (2,)), ((0, 1), (2,)))
```

```
>>> mapping = coarse_grain.make_mapping()
>>> mapping
array([0, 0, 0, 1, 0, 0, 0, 1, 0, 0, 0, 1, 2, 2, 2, 3])
```

We can now construct a *MacroSubsystem* using this coarse-graining:

We can then consider the integrated information of this macro-network and compare it to the micro-network.

```
>>> macro_sia = pyphi.compute.sia(macro_subsystem)
>>> macro_sia.phi
0.597212
```

The integrated information of the macro subsystem ($\Phi = 0.597212$) is greater than the integrated information of the micro system ($\Phi = 0.113889$). We can conclude that a macro-scale is appropriate for this system, but to determine which one, we must check all possible partitions and all possible groupings to find the maximum of integrated information across all scales.

```
>>> M = pyphi.macro.emergence(network, state)
>>> M.emergence
0.483323
>>> M.system
(0, 1, 2, 3)
>>> M.coarse_grain.partition
((0, 1), (2, 3))
>>> M.coarse_grain.grouping
(((0, 1), (2,)), ((0, 1), (2,)))
```

The analysis determines the partition and grouping which results in the maximum value of integrated information, as well as the emergence (increase in Φ) from the micro-scale to the macro-scale.

1.7.2 Blackboxing

• pyphi.examples.blackbox_network()

The *macro* module also provides tools for studying the emergence of systems using blackboxing.

```
>>> import pyphi
>>> network = pyphi.examples.blackbox_network()
```

We consider the state where all nodes are OFF:

>>> state = (0, 0, 0, 0, 0, 0)

The system has minimal Φ without blackboxing:

```
>>> subsys = pyphi.Subsystem(network, state)
>>> pyphi.compute.phi(subsys)
0.215278
```

We will consider the blackbox system consisting of two blackbox elements, ABC and DEF, where C and F are output elements and AB and DE are hidden within their respective blackboxes.

Blackboxing is done with a Blackbox object. As with CoarseGrain, we pass it a partition of micro-elements:

```
>>> partition = ((0, 1, 2), (3, 4, 5))
>>> output_indices = (2, 5)
>>> blackbox = pyphi.macro.Blackbox(partition, output_indices)
```

Blackboxes have a few convenient attributes and methods. The hidden_indices attribute returns the elements which are hidden within blackboxes:

```
>>> blackbox.hidden_indices
(0, 1, 3, 4)
```

The micro_indices attribute lists all the micro-elements in the box:

```
>>> blackbox.micro_indices
(0, 1, 2, 3, 4, 5)
```

The macro_indices attribute generates a set of indices which index the blackbox macro-elements. Since there are two blackboxes in our example, and each has one output element, there are two macro-indices:

```
>>> blackbox.macro_indices
(0, 1)
```

The macro_state method converts a state of the micro elements to the state of the macro-elements. The macro-state of a blackbox system is simply the state of the system's output elements:

```
>>> micro_state = (0, 0, 0, 0, 0, 1)
>>> blackbox.macro_state(micro_state)
(0, 1)
```

Let us also define a time scale over which to perform our analysis:

>>> time_scale = 2

As in the coarse-graining example, the blackbox and time scale are passed to MacroSubsystem:

```
>>> macro_subsystem = pyphi.macro.MacroSubsystem(network, state,
... blackbox=blackbox,
... time_scale=time_scale)
```

We can now compute Φ for this macro system:

```
>>> pyphi.compute.phi(macro_subsystem)
0.638888
```

We find that the macro subsystem has greater integrated information ($\Phi = 0.638888$) than the micro system ($\Phi = 0.215278$)—the system demonstrates emergence.

1.8 Actual Causation

This section demonstrates how to use PyPhi to evaluate actual causation as described in

Albantakis L, Marshall W, Hoel E, Tononi G (2017). What caused what? An irreducible account of actual causation. arXiv:1708.06716 [cs.AI].

```
>>> import pyphi
>>> from pyphi import actual, config, Direction
```

1.8.1 Configuration

Before we begin we need to set some configuration values. The correct way of partitioning for actual causation is using the 'ALL' partitions setting; 'TRI'-partitions are a reasonable approximation. In case of ties the smaller purview should be chosen. IIT 3.0 style bipartitions will give incorrect results.

```
>>> config.PARTITION_TYPE = 'TRI'
>>> config.PICK_SMALLEST_PURVIEW = True
```

When calculating a causal account of the transition between a set of elements X at time t - 1 and a set of elements Y at time t, with X and Y being subsets of the same system, the transition should be valid according to the system's TPM. However, the state of X at t - 1 does not necessarily need to have a valid previous state so we can disable state validation:

```
>>> config.VALIDATE_SUBSYSTEM_STATES = False
```

1.8.2 Computation

We will look at how to perform computations over the basic OR-AND network introduced in Figure 1 of the paper.

```
>>> network = pyphi.examples.actual_causation()
```

This is a standard PyPhi Network so we can look at its TPM:

```
>>> pyphi.convert.state_by_node2state_by_state(network.tpm)
array([[1., 0., 0., 0.],
       [0., 1., 0., 0.],
       [0., 1., 0., 0.],
       [0., 0., 0., 1.]])
```

The OR gate is element 0, and the AND gate is element 1 in the network.

>>> OR = 0 >>> AND = 1

We want to observe both elements at t - 1 and t, with OR ON and AND OFF in both observations:

>>> X = Y = (OR, AND)
>>> X_state = Y_state = (1, 0)

The *Transition* object is the core of all actual causation calculations. To instantiate a *Transition*, we pass it a *Network*, the state of the network at t - 1 and t, and elements of interest at t - 1 and t. Note that PyPhi requires the state to be the state of the entire network, not just the state of the nodes in the transition.

>>> transition = actual.Transition(network, X_state, Y_state, X, Y)

Cause and effect repertoires can be obtained for the transition. For example, as shown on the right side of Figure 2B, we can compute the effect repertoire to see how $X_{t-1} = \{OR = 1\}$ constrains the probability distribution of the purview $Y_t = \{OR, AND\}$:

Similarly, as in Figure 2C, we can compute the cause repertoire of $Y_t = \{OR, AND = 10\}$ to see how it constrains the purview $X_{t-1} = \{OR\}$:

```
>>> transition.cause_repertoire((OR, AND), (OR,))
array([[0.5],
       [0.5]])
```

Note: In all *Transition* methods the constraining occurence is passed as the mechanism argument and the constrained occurence is the purview argument. This mirrors the terminology introduced in the IIT code.

Transition also provides methods for computing cause and effect ratios. For example, the effect ratio of $X_{t-1} = \{OR = 1\}$ constraining $Y_t = \{OR\}$ (as shown in Figure 3A) is computed as follows:

```
>>> transition.effect_ratio((OR,), (OR,))
0.415037
```

The effect ratio of $X_{t-1} = \{OR = 1\}$ constraining $Y_t = \{AND\}$ is negative:

```
>>> transition.effect_ratio((OR,), (AND,))
-0.584963
```

And the cause ratio of $Y_t = \{OR = 1\}$ constraining $X_{t-1} = \{OR, AND\}$ (Figure 3B) is:

```
>>> transition.cause_ratio((OR,), (OR, AND))
0.415037
```

We can evaluate α for a particular pair of occurences, as in Figure 3C. For example, to find the irreducible effect ratio of $\{OR, AND\} \rightarrow \{OR, AND\}$, we use the find_mip method:

>>> link = transition.find_mip(Direction.EFFECT, (OR, AND), (OR, AND))

This returns a *AcRepertoireIrreducibilityAnalysis* object, with a number of useful properties. This particular MIP is reducible, as we can see by checking the value of α :

```
>>> link.alpha
```

The partition property shows the minimum information partition that reduces the occurence and candidate effect:

```
>>> link.partition
OR AND
```

(continues on next page)

(continued from previous page)

OR AND

Let's look at the MIP for the irreducible occurence $Y_t = \{OR, AND\}$ constraining $X_{t-1} = \{OR, AND\}$ (Figure 3D). This candidate causal link has positive α :

```
>>> link = transition.find_mip(Direction.CAUSE, (OR, AND), (OR, AND))
>>> link.alpha
0.169925
```

To find the actual cause or actual effect of a particular occurence, use the find_actual_cause or find_actual_effect methods:

```
>>> transition.find_actual_cause((OR, AND))
CausalLink
\alpha = 0.1699 [OR, AND] [OR, AND]
```

1.8.3 Accounts

The complete causal account of our transition can be computed with the account function:

We see that this function produces the causal links shown in Figure 4. The *Account* object is a subclass of tuple, and can manipulated the same:

```
>>> len(account) 5
```

1.8.4 Irreducible Accounts

The irreducibility of the causal account of our transition of interest can be evaluated using the following function:

```
>>> sia = actual.sia(transition)
>>> sia.alpha
0.169925
```

As shown in Figure 4, the second order occurence $Y_t = \{OR, AND = 10\}$ is destroyed by the MIP:

```
>>> sia.partitioned_account
Account (4 causal links)
```

(continues on next page)

(continued from previous page)

The partition of the MIP is available in the cut property:

```
>>> sia.cut
KCut CAUSE
OR AND
OR AND
```

To find all irreducible accounts within the transition of interest, use nexus:

>>> all_accounts = actual.nexus(network, X_state, Y_state)

This computes \mathcal{A} for all permutations of of elements in X_{t-1} and Y_t and returns a tuple of all AcSystemIrreducibilityAnalysis objects with $\mathcal{A} > 0$:

```
>>> for n in all_accounts:
... print(n.transition, n.alpha)
Transition([OR] [OR]) 2.0
Transition([AND] [AND]) 2.0
Transition([OR, AND] [OR, AND]) 0.169925
```

The causal_nexus function computes the maximally irreducible account for the transition of interest:

```
>>> cn = actual.causal_nexus(network, X_state, Y_state)
>>> cn.alpha
2.0
>>> cn.transition
Transition([OR] [OR])
```

1.8.5 Disjunction of conjunctions

If you are interested in exploring further, the disjunction of conjunctions network from Figure 7 is provided as well:

```
>>> network = pyphi.examples.disjunction_conjunction_network()
>>> cn = actual.causal_nexus(network, (1, 0, 1, 0), (0, 0, 0, 1))
```

The only irreducible transition is from $X_{t-1} = C$ to $Y_t = D$, with A of 2.0:

```
>>> cn.transition
Transition([C] [D])
>>> cn.alpha
2.0
```

1.9 Residue

This example describes a system containing two AND gates, A and B, with a single overlapping input node.

First let's create the subsystem corresponding to the residue network, with all nodes OFF in the current and previous states.

```
>>> import pyphi
>>> subsystem = pyphi.examples.residue_subsystem()
```

Next, we can define the mechanisms of interest. Mechanisms and purviews are represented by tuples of node indices in the network:

```
>>> A = (0,)
>>> B = (1,)
>>> AB = (0, 1)
```

And the possible cause purviews that we're interested in:

```
>>> CD = (2, 3)
>>> DE = (3, 4)
>>> CDE = (2, 3, 4)
```

We can then evaluate the cause information for each of the mechanisms over the cause purview CDE.

```
>>> subsystem.cause_info(A, CDE)
0.333332
```

```
>>> subsystem.cause_info(B, CDE)
0.333332
```

```
>>> subsystem.cause_info(AB, CDE)
0.5
```

The composite mechanism AB has greater cause information than either of the individual mechanisms. This contradicts the idea that AB should exist minimally in this system.

Instead, we can quantify existence as the irreducible cause information of a mechanism. The MIP of a mechanism is the partition of mechanism and purview which makes the least difference to the cause repertoire (see the documentation for the *RepertoireIrreducibilityAnalysis* object). The irreducible cause information is the distance between the unpartitioned and partitioned repertoires.

To analyze the irreducibility of the mechanism AB on the cause side:

```
>>> mip_AB = subsystem.cause_mip(AB, CDE)
```

We can then determine what the specific partition is.

```
>>> mip_AB.partition

______A,B

______C D,E
```

The indices (0, 1, 2, 3, 4) correspond to nodes A, B, C, D, E respectively. Thus the MIP is $\frac{AB}{DE} \times \frac{\emptyset}{C}$, where \emptyset denotes the empty mechanism.

The partitioned repertoire of the MIP can also be retrieved:

```
>>> mip_AB.partitioned_repertoire
array([[[[0.2, 0.2],
        [0.1, 0. ]],
        [[0.2, 0.2],
        [0.1, 0. ]]]])
```

And we can then calculate the irreducible cause information as the difference between partitioned and unpartitioned repertoires.

```
>>> mip_AB.phi
0.1
```

One counterintuitive result that merits discussion is that since irreducible cause information is what defines existence, we must also evaluate the irreducible cause information of the mechanisms A and B.

The mechanism A over the purview CDE is completely reducible to $\frac{A}{CD} \times \frac{\emptyset}{E}$ because E has no effect on A, so it has zero φ .

Instead, we should evaluate A over the purview CD.

>>> mip_A = subsystem.cause_mip(A, CD)

In this case, there is a well-defined MIP

```
>>> mip_A.partition

A

C
D
```

which is $\frac{\emptyset}{C} \times \frac{A}{D}$. It has partitioned repertoire

and irreducible cause information

```
>>> mip_A.phi
0.166667
```

A similar result holds for *B*. Thus the mechanisms *A* and *B* exist at levels of $\varphi = \frac{1}{6}$, while the higher-order mechanism *AB* exists only as the residual of causes, at a level of $\varphi = \frac{1}{10}$.

1.10 Magic Cuts

This example explores a system of three fully connected elements A, B and C, which follow the logic of the Rule 110 cellular automaton. The point of this example is to highlight an unexpected behaviour of system cuts: that the minimum information partition of a system can result in new concepts being created.

First let's create the Rule 110 network, with all nodes OFF in the current state.

```
>>> import pyphi
>>> network = pyphi.examples.rule110_network()
>>> state = (0, 0, 0)
```

Next, we want to identify the spatial scale and major complex of the network:

```
>>> macro = pyphi.macro.emergence(network, state)
>>> print(macro.emergence)
-1.112671
```

Since the emergence value is negative, there is no macro scale which has greater integrated information than the original micro scale. We can now analyze the micro scale to determine the major complex of the system:

```
>>> major_complex = pyphi.compute.major_complex(network, state)
>>> major_complex.subsystem
Subsystem(A, B, C)
>>> print(major_complex.phi)
1.35708
```

The major complex of the system contains all three nodes of the system, and it has integrated information $\Phi = 1.35708$. Now that we have identified the major complex of the system, we can explore its cause-effect structure and the effect of the MIP.

>>> ces = major_complex.ces

There two equivalent cuts for this system; for concreteness we sever all connections from elements A and B to C.

```
>>> cut = pyphi.models.Cut(from_nodes=(0, 1), to_nodes=(2,))
>>> cut_subsystem = pyphi.Subsystem(network, state, cut=cut)
>>> cut_ces = pyphi.compute.ces(cut_subsystem)
```

Let's investigate the concepts in the unpartitioned cause-effect structure,

```
>>> ces.labeled_mechanisms
(['A'], ['B'], ['C'], ['A', 'B'], ['A', 'C'], ['B', 'C'])
>>> ces.phis
[0.125, 0.125, 0.125, 0.499999, 0.499999, 0.499999]
>>> sum(ces.phis)
1.874997000000002
```

and also the concepts of the partitioned cause-effect structure.

```
>>> cut_ces.labeled_mechanisms
(['A'], ['B'], ['C'], ['A', 'B'], ['B', 'C'], ['A', 'B', 'C'])
>>> cut_ces.phis
[0.125, 0.125, 0.125, 0.499999, 0.2666666, 0.333333]
>>> sum(_)
1.4749980000000003
```

The unpartitioned cause-effect structure includes all possible first and second order concepts, but there is no third order concept. After applying the cut and severing the connections from A and B to C, the third order concept ABC is created and the second order concept AC is destroyed. The overall amount of φ in the system decreases from 1.875 to 1.475.

Let's explore the concept which was created to determine why it does not exist in the unpartitioned cause-effect structure and what changed in the partitioned cause-effect structure.

```
>>> subsystem = major_complex.subsystem
>>> ABC = subsystem.node_indices
>>> subsystem.cause_info(ABC, ABC)
0.749999
>>> subsystem.effect_info(ABC, ABC)
1.875
```

The mechanism does have cause and effect power over the system. But, since it doesn't specify a concept, it must be that this power is reducible:

```
>>> mic = subsystem.mic(ABC)
>>> mic.phi
0.0
>>> mie = subsystem.mie(ABC)
>>> mie.phi
0.625
```

The reason ABC does not exist as a concept is that its cause is reducible. Looking at the TPM of the system, there are no possible states where two elements are OFF. This means that knowing two elements are OFF is enough to know that the third element must also be OFF, and thus the third element can always be cut from the concept without a loss of information. This will be true for any purview, so the cause information is reducible.

```
>>> BC = (1, 2)
>>> A = (0,)
>>> repertoire = subsystem.cause_repertoire(ABC, ABC)
>>> cut_repertoire = (subsystem.cause_repertoire(BC, ABC) *
... subsystem.cause_repertoire(A, ()))
>>> pyphi.distance.hamming_emd(repertoire, cut_repertoire)
0.0
```

Next, let's look at the cut subsystem to understand how the new concept comes into existence.

```
>>> ABC = (0, 1, 2)
>>> C = (2,)
>>> AB = (0, 1)
```

The cut applied to the subsystem severs the connections going to C from either A or B. In this circumstance, knowing the state of A or B does not tell us anything about the state of C; only the previous state of C can tell us about the next state of C. C_node.tpm_on gives us the probability of C being ON in the next state, while C_node.tpm_off would give us the probability of C being OFF.

```
>>> C_node = cut_subsystem.indices2nodes(C)[0]
>>> C_node.tpm_on.flatten()
array([0.5 , 0.75])
```

This states that C has a 50% chance of being ON in the next state if it currently OFF, but a 75% chance of being ON in the next state if it is currently ON. Thus, unlike the unpartitioned case, knowing the current state of C gives us additional information over and above knowing the state of A or B.

```
>>> repertoire = cut_subsystem.cause_repertoire(ABC, ABC)
>>> cut_repertoire = (cut_subsystem.cause_repertoire(AB, ABC) *
...
cut_subsystem.cause_repertoire(C, ()))
>>> print(pyphi.distance.hamming_emd(repertoire, cut_repertoire))
0.500001
```

With this partition, the integrated information is $\varphi = 0.5$, but we must check all possible partitions to find the maximally-irreducible cause:

```
>>> mic = cut_subsystem.mic(ABC)
>>> mic.purview
(0, 1, 2)
>>> mic.phi
0.3333333
```

It turns out that the MIP of the maximally-irreducible cause is

$$\frac{AB}{\varnothing} \times \frac{C}{ABC}$$

and the integrated information of mechanism ABC is $\varphi = 1/3$.

Note that in order for a new concept to be created by a cut, there must be a within-mechanism connection severed by the cut.

In the previous example, the MIP created a new concept, but the amount of φ in the cause-effect structure still decreased. This is not always the case. Next we will look at an example of system whoes MIP increases the amount of φ . This example is based on a five-node network that implements the logic of the Rule 154 cellular automaton. Let's first load the network:

```
>>> network = pyphi.examples.rule154_network()
>>> state = (1, 0, 0, 0, 0)
```

For this example, it is the subsystem consisting of A, B, and E that we explore. This is not the major complex of the system, but it serves as a proof of principle regardless.

```
>>> subsystem = pyphi.Subsystem(network, state, (0, 1, 4))
```

Calculating the MIP of the system,

```
>>> sia = pyphi.compute.sia(subsystem)
>>> sia.phi
0.217829
>>> sia.cut
Cut [A, E] / / [B]
```

we see that this subsystem has a Φ value of 0.15533, and the MIP cuts the connections from AE to B. Investigating the concepts in both the partitioned and unpartitioned cause-effect structures,

```
>>> sia.ces.labeled_mechanisms
(['A'], ['B'], ['A', 'B'])
>>> sia.ces.phis
[0.25, 0.166667, 0.178572]
>>> print(sum(_))
0.595239000000001
```

We see that the unpartitioned cause-effect structure has mechanisms A, B and AB with $\sum \varphi = 0.595239$.

```
>>> sia.partitioned_ces.labeled_mechanisms
(['A'], ['B'], ['A', 'B'])
>>> sia.partitioned_ces.phis
[0.25, 0.166667, 0.214286]
>>> print(sum(_))
0.630953
```

The partitioned cause-effect structure has mechanisms A, B and AB but with $\sum \varphi = 0.630953$. There are the same number of concepts in both cause-effect structures, over the same mechanisms; however, the partitioned cause-effect structure has a greater φ value for the concept AB, resulting in an overall greater $\sum \varphi$ for the partitioned cause-effect structure.

Although situations described above are rare, they do occur, so one must be careful when analyzing the integrated information of physical systems not to dismiss the possibility of partitions creating new concepts or increasing the amount of φ ; otherwise, an incorrect major complex may be identified.

1.11 Detailed installation guide for macOS

This is a step-by-step guide intended for those unfamiliar with Python or the command-line (a.k.a. the "shell").

A shell can be opened by opening a new tab in the Terminal app (located in Utilities). Text that is formatted like code is meant to be copied and pasted into the terminal (hit the Enter key to run the command).

The fist step is to install the versions of Python that we need. The most convenient way of doing this is to use the OS X package manager Homebrew. Install Homebrew by running this command:

```
/usr/bin/ruby -e "$(curl -fsSL https://raw.githubusercontent.com/Homebrew/install/

→master/install)"
```

Now you should have access to the brew command. First, we need to install Python 2 and 3. Using these socalled "brewed" Python versions, rather than the version of Python that comes with your computer, will protect your computer's Python version from unwanted changes that could interfere with other applications.

brew install python python3

Then we need to ensure that the terminal "knows about" the newly-installed Python versions:

```
brew link --overwrite python
brew link --overwrite python3
```

Now that we're using our shiny new Python versions, it is highly recommended to set up a **virtual environment** in which to install PyPhi. Virtual environments allow different projects to isolate their dependencies from one another, so that they don't interact in unexpected ways. Please see this guide for more information.

To do this, you must install virtualenvwrapper, a tool for manipulating virtual environments. This tool is available on PyPI, the Python package index, and can be installed with pip, the command-line utility for installing and managing Python packages (pip was installed automatically with the brewed Python):

pip install virtualenvwrapper

Now we need to edit your shell startup file. This is a file that runs automatically every time you open a new shell (a new window or tab in the Terminal app). This file should be in your home directory, though it will be invisible in the Finder because the filename is preceded by a period. On most Macs it is called .bash_profile. You can open this in a text editor by running this command:

```
open -a TextEdit ~/.bash_profile
```

If you get an error that says the file doesn't exist, then run touch ~/.bash_profile first to create it.

Now, you'll add three lines to the shell startup file. These lines will set the location where the virtual environments will live, the location of your development project directories, and the location of the script installed with this package, respectively. Note: The location of the script can be found by running which virtualenvwrapper.sh.

The filepath after the equals sign on the second line will different for everyone, but here is an example:

```
export WORKON_HOME=$HOME/.virtualenvs
export PROJECT_HOME=$HOME/dev
source /usr/local/bin/virtualenvwrapper.sh
```

After editing the startup file and saving it, open a new terminal shell by opening a new tab or window (or just reload the startup file by running source ~/.bash_profile).

Now that virtualenvwrapper is fully installed, use it to create a Python 3 virtual environment, like so:

mkvirtualenv -p `which python3` <name_of_your_project>

The option -p `which python3` ensures that when the virtual environment is activated, the commands python and pip will refer to their Python 3 counterparts.

The virtual environment should have been activated automatically after creating it. Virtual environments can be manually activated with workon <name_of_your_project>, and deactivated with deactivate.

Important: Remember to activate the virtual environment with the workon command every time you begin working on your project. Also, note that the currently active virtual environment is *not* associated with any particular folder; it is associated with a terminal shell. In other words, each time you open a new Terminal tab or terminal window, you need to run workon <name_of_your_project (with some extra setup, this can be done automatically; see here). When a virtual environment is active, your command-line prompt will be prepended with the name of the virtual environment in parentheses.

Once you've checked that the new virtual environment is active, you're finally ready to install PyPhi into it (note that this may take a few minutes):

```
pip install pyphi
```

Congratulations, you've just installed PyPhi!

To play around with the software, ensure that you've activated the virtual environment with workon <name_of_your_project>. Then run python to start a Python 3 interpreter. Then, in the interpreter's command-line (which is preceded by the >>> prompt), run

import pyphi

Optionally, you can also install IPython with pip install ipython to get a more useful Python interpreter that offers things like tab-completion. Once you've installed it, you can start the IPython interpreter with the command ipython.

Next, please see the documentation for some examples of how to use PyPhi and information on how to configure it.

1.12 Transition probability matrix conventions

A *Network* can be created with a transition probability matrix (TPM) in any of the three forms described below. However, in PyPhi the canonical TPM representation is **multidimensional state-by-node form**. The TPM will be converted to this form when the *Network* is built.

Tip: Functions for converting TPMs from one form to another are available in the *convert* module.

1.12.1 State-by-node form

A TPM in **state-by-node form** is a matrix where the entry (i, j) gives the probability that the j^{th} node will be ON at time t + 1 if the system is in the i^{th} state at time t.

1.12.2 Multidimensional state-by-node form

A TPM in **multidimensional state-by-node** form is a state-by-node form that has been reshaped so that it has n + 1 dimensions instead of two. The first n dimensions correspond to each of the n nodes at time t, while the last dimension corresponds to the probabilities of each node being ON at t + 1.

With this form, we can take advantage of NumPy array indexing and use a network state as an index directly:

```
>>> from pyphi.examples import basic_noisy_selfloop_network
>>> tpm = basic_noisy_selfloop_network().tpm
>>> state = (0, 0, 1)  # A network state is a binary tuple
>>> tpm[state]
array([0.919, 0.91, 0.756])
```

This tells us that if the current state is $N_0 = 0, N_1 = 0, N_2 = 1$, then the for the next state, $\Pr(N_0 = 1) = 0.919$, $\Pr(N_1 = 1) = 0.91$ and $\Pr(N_2 = 1) = 0.756$.

Important: The multidimensional state-by-node form is used throughout PyPhi, regardless of the form that was used to create the *Network*.

1.12.3 State-by-state form

A TPM in **state-by-state form** is a matrix where the entry (i, j) gives the probability that the state at time t + 1 will be j if the state at time t is labeled by i.

Warning: When converting a state-by-state TPM to one of the other forms, information may be lost!

This is because the space of possible state-by-state TPMs is larger than the space of state-by-node TPMs (so the conversion cannot be injective). However, if we restrict the state-by-state TPMs to only those that satisfy the conditional independence property, then the mapping becomes bijective.

See Conditional Independence for a more detailed discussion.

1.12.4 Little-endian convention

Even after choosing one of the above representations, there are several ways to write down the TPM.

With both state-by-state and state-by-node TPMs, one is confronted with a choice about which rows correspond to which states. In state-by-state TPMs, this choice must also be made for the columns.

State at t	$\Pr(N = ON)$ at $t + 1$		
A, B	A	В	
(0, 0)	0.1	0.2	
(1, 0)	0.3	0.4	
(0, 1)	0.5	0.6	
(1, 1)	0.7	0.8	

There are two possible choices for the rows. Either the first node changes state every other row:

Or the last node does:

State at t	$\Pr(N = ON)$ at $t + 1$		
A, B	A	В	
(0, 0)	0.1	0.2	
(0, 1)	0.5	0.6	
(1, 0)	0.3	0.4	
(1, 1)	0.7	0.8	

Note that the index i of a row in a TPM encodes a network state: convert the index to binary, and each bit gives the state of a node. The question is, which node?

Throughout PyPhi, we always choose the first convention—the state of the first node (the one with the lowest index) varies the fastest. So, the least-significant bit—the one's place—gives the state of the lowest-index node.

This is analogous to the little-endian convention in organizing computer memory. The other convention, where the highest-index node varies the fastest, is analogous to the big-endian convention (see Endianness).

The rationale for this choice of convention is that the little-endian mapping is stable under changes in the number of nodes, in the sense that the same bit always corresponds to the same node index. The big-endian mapping does not have this property.

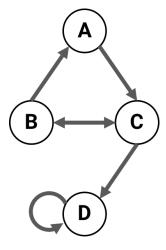
Tip: Functions to convert states to indices and vice versa, according to either the little-endian or big-endian convention, are available in the *convert* module.

Note: This applies to only situations where decimal indices are encoding states. Whenever a network state is represented as a list or tuple, we use the only sensible convention: the i^{th} element gives the state of the i^{th} node.

1.13 Connectivity matrix conventions

Throughout PyPhi, if CM is a connectivity matrix, then $[CM]_{i,j} = 1$ means that there is a directed edge (i, j) from node i to node j, and $[CM]_{i,j} = 0$ means there is no edge from i to j.

For example, this network of four nodes



has the following connectivity matrix:

>>>	cm =	[[0,	Ο,	1,	0],
		[1,	Ο,	1,	0],
		[0,	1,	Ο,	1],
		[0,	Ο,	Ο,	111

1.14 Loading a configuration

Various aspects of PyPhi's behavior can be configured.

When PyPhi is imported, it checks for a YAML file named pyphi_config.yml in the current directory and automatically loads it if it exists; otherwise the default configuration is used.

The various settings are listed here with their defaults.

```
>>> import pyphi
>>> defaults = pyphi.config.defaults()
```

Print the config object to see the current settings:

```
>>> print(pyphi.config)
{ 'ASSUME_CUTS_CANNOT_CREATE_NEW_CONCEPTS': False,
    'CACHE_SIAS': False,
    'CACHE_POTENTIAL_PURVIEWS': True,
    'CACHING_BACKEND': 'fs',
    ...
```

Setting can be changed on the fly by assigning them a new value:

>>> pyphi.config.PROGRESS_BARS = False

It is also possible to manually load a configuration file:

```
>>> pyphi.config.load_file('pyphi_config.yml')
```

Or load a dictionary of configuration values:

```
>>> pyphi.config.load_dict({'PRECISION': 1})
```

1.15 Approximations and theoretical options

These settings control the algorithms PyPhi uses.

- ASSUME_CUTS_CANNOT_CREATE_NEW_CONCEPTS
- CUT_ONE_APPROXIMATION
- MEASURE
- PARTITION_TYPE
- PICK_SMALLEST_PURVIEW
- USE_SMALL_PHI_DIFFERENCE_FOR_CES_DISTANCE
- SYSTEM_CUTS
- SINGLE_MICRO_NODES_WITH_SELFLOOPS_HAVE_PHI
- VALIDATE_SUBSYSTEM_STATES
- VALIDATE_CONDITIONAL_INDEPENDENCE

1.16 Parallelization and system resources

These settings control how much processing power and memory is available for PyPhi to use. The default values may not be appropriate for your use-case or machine, so **please check these settings before running anything**. Otherwise, there is a risk that simulations might crash (potentially after running for a long time!), resulting in data loss.

- PARALLEL_CONCEPT_EVALUATION
- PARALLEL_CUT_EVALUATION
- PARALLEL_COMPLEX_EVALUATION
- NUMBER_OF_CORES
- MAXIMUM_CACHE_MEMORY_PERCENTAGE

Important: Only one of PARALLEL_CONCEPT_EVALUATION, PARALLEL_CUT_EVALUATION, and PARALLEL_COMPLEX_EVALUATION can be set to True at a time.

For most networks, PARALLEL_CUT_EVALUATION is the most efficient. This is because the algorithm is exponential time in the number of nodes, so the most of the time is spent on the largest subsystem.

You should only parallelize concept evaluation if you are just computing a CauseEffectStructure.

1.17 Memoization and caching

PyPhi provides a number of ways to cache intermediate results.

- CACHE_SIAS
- CACHE_REPERTOIRES
- CACHE_POTENTIAL_PURVIEWS
- CLEAR_SUBSYSTEM_CACHES_AFTER_COMPUTING_SIA

- CACHING_BACKEND
- FS_CACHE_VERBOSITY
- FS_CACHE_DIRECTORY
- MONGODB_CONFIG
- REDIS_CACHE
- REDIS_CONFIG

1.18 Logging

These settings control how PyPhi handles log messages. Logs can be written to standard output, a file, both, or none. If these simple default controls are not flexible enough for you, you can override the entire logging configuration. See the documentation on Python's logger for more information.

- LOG_STDOUT_LEVEL
- LOG_FILE_LEVEL
- LOG_FILE
- PROGRESS_BARS
- REPR_VERBOSITY
- PRINT_FRACTIONS

1.19 Numerical precision

• PRECISION

1.20 The config API

class pyphi.conf.**Option** (*default*, *values=None*, *on_change=None*, *doc=None*) A descriptor implementing PyPhi configuration options.

Parameters default - The default value of this Option.

Keyword Arguments

- **values** (*list*) Allowed values for this option. A ValueError will be raised if values is not None and the option is set to be a value not in the list.
- **on_change** (*function*) Optional callback that is called when the value of the option is changed. The Config instance is passed as the only argument to the callback.
- **doc** (*str*) Optional docstring for the option.
- class pyphi.conf.ConfigMeta(cls_name, bases, namespace)
 Metaclass for Config.

Responsible for setting the name of each Option when a subclass of Config is created; because Option objects are defined on the class, not the instance, their name should only be set once.

Python 3.6 handles this exact need with the special descriptor method <u>__set_name__</u> (see PEP 487). We should use that once we drop support for 3.4 & 3.5.

class pyphi.conf.Config

Base configuration object.

See PyphiConfig for usage.

classmethod options()

Return a dictionary the Option objects for this config

defaults()

Return the default values of this configuration.

load_dict (dct)

Load a dictionary of configuration values.

load_file (filename)
Load config from a YAML file.

snapshot()

Return a snapshot of the current values of this configuration.

```
override (**new_values)
```

Decorator and context manager to override configuration values.

The initial configuration values are reset after the decorated function returns or the context manager completes it block, even if the function or block raises an exception. This is intended to be used by tests which require specific configuration values.

Example

```
>>> from pyphi import config
>>> @config.override(PRECISION=20000)
... def test_something():
... assert config.PRECISION == 20000
...
>>> test_something()
>>> with config.override(PRECISION=100):
... assert config.PRECISION == 100
...
```

pyphi.conf.configure_logging(conf)

Reconfigure PyPhi logging based on the current configuration.

class pyphi.conf.PyphiConfig

pyphi.config is an instance of this class.

ASSUME_CUTS_CANNOT_CREATE_NEW_CONCEPTS

default=False

In certain cases, making a cut can actually cause a previously reducible concept to become a proper, irreducible concept. Assuming this can never happen can increase performance significantly, however the obtained results are not strictly accurate.

CUT_ONE_APPROXIMATION

default=False

When determining the MIP for Φ , this restricts the set of system cuts that are considered to only those that cut the inputs or outputs of a single node. This restricted set of cuts scales linearly with the size of the system; the full set of all possible bipartitions scales exponentially. This approximation is more likely to give theoretically accurate results with modular, sparsely-connected, or homogeneous networks.

MEASURE

default='EMD'

The measure to use when computing distances between repertoires and concepts. A full list of currently installed measures is available by calling print (pyphi.distance.measures.all()). Note that some measures cannot be used for calculating Φ because they are asymmetric.

Custom measures can be added using the pyphi.distance.measures.register decorator. For example:

```
from pyphi.distance import measures
@measures.register('ALWAYS_ZERO')
def always_zero(a, b):
    return 0
```

This measures can then be used by setting config.MEASURE = 'ALWAYS_ZERO'.

If the measure is asymmetric you should register it using the asymmetric keyword argument. See *distance* for examples.

PARALLEL_CONCEPT_EVALUATION

default=False

Controls whether concepts are evaluated in parallel when computing cause-effect structures.

PARALLEL_CUT_EVALUATION

default=True

Controls whether system cuts are evaluated in parallel, which is faster but requires more memory. If cuts are evaluated sequentially, only two *SystemIrreducibilityAnalysis* instances need to be in memory at once.

PARALLEL_COMPLEX_EVALUATION

default=False

Controls whether systems are evaluated in parallel when computing complexes.

NUMBER_OF_CORES

default=-1

Controls the number of CPU cores used to evaluate unidirectional cuts. Negative numbers count backwards from the total number of available cores, with -1 meaning 'use all available cores.'

MAXIMUM_CACHE_MEMORY_PERCENTAGE

default=50

PyPhi employs several in-memory caches to speed up computation. However, these can quickly use a lot of memory for large networks or large numbers of them; to avoid thrashing, this setting limits the percentage of a system's RAM that the caches can collectively use.

CACHE_SIAS

default=False

PyPhi is equipped with a transparent caching system for *SystemIrreducibilityAnalysis* objects which stores them as they are computed to avoid having to recompute them later. This makes it easy to play around interactively with the program, or to accumulate results with minimal effort. For larger projects, however, it is recommended that you manage the results explicitly, rather than relying on the cache. For this reason it is disabled by default.

CACHE_REPERTOIRES

default=True

PyPhi caches cause and effect repertoires. This greatly improves speed, but can consume a significant amount of memory. If you are experiencing memory issues, try disabling this.

CACHE_POTENTIAL_PURVIEWS

default=True

Controls whether the potential purviews of mechanisms of a network are cached. Caching speeds up computations by not recomputing expensive reducibility checks, but uses additional memory.

CLEAR_SUBSYSTEM_CACHES_AFTER_COMPUTING_SIA

default=False

Controls whether a *Subsystem*'s repertoire and MICE caches are cleared with *clear_caches()* after computing the *SystemIrreducibilityAnalysis*. If you don't need to do any more computations after running *sia()*, then enabling this may help conserve memory.

CACHING_BACKEND

default='fs'

Controls whether precomputed results are stored and read from a local filesystem-based cache in the current directory or from a database. Set this to fs' for the filesystem, db' for the database.

FS_CACHE_VERBOSITY

default=0

Controls how much caching information is printed if the filesystem cache is used. Takes a value between 0 and 11.

FS_CACHE_DIRECTORY

default='__pyphi_cache__'

If the filesystem is used for caching, the cache will be stored in this directory. This directory can be copied and moved around if you want to reuse results *e.g.* on a another computer, but it must be in the same directory from which Python is being run.

MONGODB_CONFIG

```
default={'collection_name' -- 'cache', 'host' -- 'localhost', 'port':
27017, 'database_name': 'pyphi'}
```

Set the configuration for the MongoDB database backend (only has an effect if CACHING_BACKEND is 'db').

REDIS_CACHE

default=False

Specifies whether to use Redis to cache MaximallyIrreducibleCauseOrEffect.

REDIS_CONFIG

```
default={'test_db' -- 1, 'db' -- 0, 'host': 'localhost', 'port':
6379}
```

Configure the Redis database backend. These are the defaults in the provided redis.conf file.

LOG_FILE

default='pyphi.log', on_change=configure_logging

Controls the name of the log file.

LOG_FILE_LEVEL

default='INFO', on_change=configure_logging

Controls the level of log messages written to the log file. This setting has the same possible values as LOG_STDOUT_LEVEL.

LOG_STDOUT_LEVEL

default='WARNING', on_change=configure_logging

Controls the level of log messages written to standard output. Can be one of 'DEBUG', 'INFO', 'WARNING', 'ERROR', 'CRITICAL', or None. 'DEBUG' is the least restrictive level and will show the most log messages. 'CRITICAL' is the most restrictive level and will only display information about fatal errors. If set to None, logging to standard output will be disabled entirely.

PROGRESS_BARS

default=True

Controls whether to show progress bars on the console.

Tip: If you are iterating over many systems rather than doing one long-running calculation, consider disabling this for speed.

PRECISION

default=6

If MEASURE is EMD, then the Earth Mover's Distance is calculated with an external C++ library that a numerical optimizer to find a good approximation. Consequently, systems with analytically zero Φ will sometimes be numerically found to have a small but non-zero amount. This setting controls the number of decimal places to which PyPhi will consider EMD calculations accurate. Values of Φ lower than 10e-PRECISION will be considered insignificant and treated as zero. The default value is about as accurate as the EMD computations get.

VALIDATE_SUBSYSTEM_STATES

default=True

Controls whether PyPhi checks if the subsystems's state is possible (reachable with nonzero probability from some previous state), given the subsystem's TPM (which is conditioned on background conditions). If this is turned off, then calculated Φ values may not be valid, since they may be associated with a subsystem that could never be in the given state.

VALIDATE_CONDITIONAL_INDEPENDENCE

default=True

Controls whether PyPhi checks if a system's TPM is conditionally independent.

SINGLE_MICRO_NODES_WITH_SELFLOOPS_HAVE_PHI

default=False

If set to True, the Φ value of single micro-node subsystems is the difference between their unpartitioned CauseEffectStructure (a single concept) and the null concept. If set to False, their Φ is defined to be zero. Single macro-node subsystems may always be cut, regardless of circumstances.

REPR_VERBOSITY

default=2, values=[0, 1, 2]

Controls the verbosity of ___repr__ methods on PyPhi objects. Can be set to 0, 1, or 2. If set to 1, calling repr on PyPhi objects will return pretty-formatted and legible strings, excluding repertoires. If set to 2, repr calls also include repertoires.

Although this breaks the convention that <u>__repr__</u> methods should return a representation which can reconstruct the object, readable representations are convenient since the Python REPL calls repr to represent all objects in the shell and PyPhi is often used interactively with the REPL. If set to 0, repr returns more traditional object representations.

PRINT_FRACTIONS

default=True

Controls whether numbers in a repr are printed as fractions. Numbers are still printed as decimals if the fraction's denominator would be large. This only has an effect if $REPR_VERBOSITY > 0$.

PARTITION_TYPE

default='BI'

Controls the type of partition used for φ computations.

If set to 'BI', partitions will have two parts.

If set to 'TRI', partitions will have three parts. In addition, computations will only consider partitions that strictly partition the mechanism the mechanism. That is, for the mechanism (A, B) and purview (B, C, D) the partition:

A, B B C, D

is not considered, but:

A B B C, D

is. The following is also valid:

In addition, this setting introduces "wedge" tripartitions of the form:

A B B C D

where the mechanism in the third part is always empty.

In addition, in the case of a φ -tie when computing a *MaximallyIrreducibleCause* or *MaximallyIrreducibleEffect*, The 'TRIPARTITION' setting choses the MIP with smallest purview instead of the largest (which is the default).

Finally, if set to 'ALL', all possible partitions will be tested.

PICK_SMALLEST_PURVIEW

default=False

When computing a *MaximallyIrreducibleCause* or *MaximallyIrreducibleEffect*, it is possible for several MIPs to have the same φ value. If this setting is set to True the MIP with the smallest purview is chosen; otherwise, the one with largest purview is chosen.

USE_SMALL_PHI_DIFFERENCE_FOR_CES_DISTANCE

default=False

If set to True, the distance between cause-effect structures (when computing a SystemIrreducibilityAnalysis) is calculated using the difference between the sum of φ in the cause-effect structures instead of the extended EMD.

SYSTEM_CUTS

```
default='3.0_STYLE', values=['3.0_STYLE', 'CONCEPT_STYLE']
```

If set to '3.0_STYLE', then traditional IIT 3.0 cuts will be used when computing Φ . If set to 'CONCEPT_STYLE', then experimental concept-style system cuts will be used instead.

log()

Log current settings.

1.21 actual

Methods for computing actual causation of subsystems and mechanisms.

```
pyphi.actual.log2(x)
Rounded version of log2.
```

A state transition between two sets of nodes in a network.

A *Transition* is implemented with two *Subsystem* objects: one representing the system at time t-1 used to compute effect coefficients, and another representing the system at time t which is used to compute cause coefficients. These subsystems are accessed with the effect_system and cause_system attributes, and are mapped to the causal directions via the system attribute.

Parameters

- network (Network) The network the subsystem belongs to.
- **before_state** (tuple[int]) The state of the network at time t 1.
- **after_state** (*tuple[int]*) The state of the network at time *t*.
- **cause_indices** (tuple[int] or tuple[str]) Indices of nodes in the cause system. (TODO: clarify)
- **effect_indices** (tuple[int] or tuple[str]) Indices of nodes in the effect system. (TODO: clarify)
- Keyword Arguments noise_background (bool) If True, background conditions are noised instead of frozen.

node_indices

tuple[int] – The indices of the nodes in the system.

network

Network – The network the system belongs to.

before_state

tuple[int] – The state of the network at time t - 1.

after_state

tuple[int] – The state of the network at time *t*.

effect_system

Subsystem – The system in before_state used to compute effect repertoires and coefficients.

cause_system

Subsystem – The system in after_state used to compute cause repertoires and coefficients.

cause_system

Subsystem

system

dict – A dictionary mapping causal directions to the system used to compute repertoires in that direction.

cut

ActualCut - The cut that has been applied to this transition.

Note: During initialization, both the cause and effect systems are conditioned on before_state as the background state. After conditioning the effect_system is then properly reset to after_state.

node_labels

to_json()

Return a JSON-serializable representation.

- **apply_cut** (*cut*) Return a cut version of this transition.
- **cause_repertoire** (*mechanism*, *purview*) Return the cause repertoire.
- effect_repertoire (mechanism, purview) Return the effect repertoire.
- unconstrained_cause_repertoire (*purview*) Return the unconstrained cause repertoire of the occurence.
- **unconstrained_effect_repertoire** (*purview*) Return the unconstrained effect repertoire of the occurence.

repertoire (*direction*, *mechanism*, *purview*)

Return the cause or effect repertoire function based on a direction.

Parameters direction (*str*) – The temporal direction, specifying the cause or effect repertoire.

state_probability(direction, repertoire, purview)

Compute the probability of the purview in its current state given the repertoire.

Collapses the dimensions of the repertoire that correspond to the purview nodes onto their state. All other dimension are already singular and thus receive 0 as the conditioning index.

Returns A single probabilty.

Return type float

probability (direction, mechanism, purview)

Probability that the purview is in it's current state given the state of the mechanism.

unconstrained_probability (*direction*, *purview*) Unconstrained probability of the purview.

purview_state(direction)

The state of the purview when we are computing coefficients in direction.

For example, if we are computing the cause coefficient of a mechanism in after_state, the direction is "CAUSE" and the purview_state is before_state.

mechanism_state(direction)

The state of the mechanism when computing coefficients in direction.

mechanism_indices(direction)

The indices of nodes in the mechanism system.

purview_indices(direction)

The indices of nodes in the purview system.

- cause_ratio (mechanism, purview)
 The cause ratio of the purview given mechanism.
- effect_ratio (mechanism, purview)

The effect ratio of the purview given mechanism.

partitioned_repertoire (*direction*, *partition*) Compute the repertoire over the partition in the given direction.

partitioned_probability (*direction*, *partition*) Compute the probability of the mechanism over the purview in the partition.

find_mip (direction, mechanism, purview, allow_neg=False)
Find the ratio minimum information partition for a mechanism over a purview.

Parameters

- direction (*str*) *CAUSE* or *EFFECT*
- mechanism (tuple[int]) A mechanism.
- **purview** (tuple[int]) A purview.
- Keyword Arguments allow_neg (boolean) If true, alpha is allowed to be negative. Otherwise, negative values of alpha will be treated as if they were 0.

Returns The irreducibility analysis for the mechanism.

Return type *AcRepertoireIrreducibilityAnalysis*

potential_purviews (direction, mechanism, purviews=False)

Return all purviews that could belong to the MaximallyIrreducibleCause/MaximallyIrreducibleEffect.

Filters out trivially-reducible purviews.

Parameters

- **direction** (*str*) Either *CAUSE* or *EFFECT*.
- mechanism (tuple[int]) The mechanism of interest.

Keyword Arguments purviews (tuple[int]) – Optional subset of purviews of interest.

find_causal_link (direction, mechanism, purviews=False, allow_neg=False)

Return the maximally irreducible cause or effect ratio for a mechanism.

Parameters

- **direction** (*str*) The temporal direction, specifying cause or effect.
- mechanism (tuple[int]) The mechanism to be tested for irreducibility.
- **Keyword Arguments purviews** (*tuple[int]*) Optionally restrict the possible purviews to a subset of the subsystem. This may be useful for _e.g._ finding only concepts that are "about" a certain subset of nodes.

Returns The maximally-irreducible actual cause or effect.

Return type *CausalLink*

find_actual_cause (mechanism, purviews=False) Return the actual cause of a mechanism.

find_mice (*args, **kwargs)
Backwards-compatible alias for find_causal_link().

pyphi.actual.directed_account (transition, direction, mechanisms=False, purviews=False, al-

low_neg=False)

Return the set of all *CausalLink* of the specified direction.

pyphi.actual.account (transition, direction=<Direction.BIDIRECTIONAL: 2>)
 Return the set of all causal links for a Transition.

Parameters transition (Transition) – The transition of interest.

Keyword Arguments direction (Direction) – By default the account contains actual causes and actual effects.

pyphi.actual.account_distance(A1, A2)

Return the distance between two accounts. Here that is just the difference in sum(alpha)

Parameters

- A1 (Account) The first account.
- A2 (Account) The second account

Returns The distance between the two accounts.

Return type float

pyphi.actual.sia(transition, direction=<Direction.BIDIRECTIONAL: 2>)

Return the minimal information partition of a transition in a specific direction.

Parameters transition (Transition) – The candidate system.

Returns A nested structure containing all the data from the intermediate calculations. The top level contains the basic irreducibility information for the given subsystem.

Return type *AcSystemIrreducibilityAnalysis*

class pyphi.actual.**ComputeACSystemIrreducibility** (*iterable*, **context*) Computation engine for AC SIAs.

description = 'Evaluating AC cuts'

- static compute (cut, transition, direction, unpartitioned_account)
 Map over a single object from self.iterable.
- process_result (new_sia, min_sia)

Reduce handler.

Every time a new result is generated by compute, this method is called with the result and the previous (accumulated) result. This method compares or collates these two values, returning the new result.

Setting self.done to True in this method will abort the remainder of the computation, returning this final result.

pyphi.actual.transitions (*network*, *before_state*, *after_state*) Return a generator of all possible transitions of a network.

pyphi.actual.nexus (network, before_state, after_state, direction=<Direction.BIDIRECTIONAL: 2>)
 Return a tuple of all irreducible nexus of the network.

pyphi.actual.causal_nexus (network, before_state, after_state, direction=<Direction.BIDIRECTIONAL: 2>) Return the causal nexus of the network.

pyphi.actual.nice_true_ces(tc)
Format a true CauseEffectStructure.

pyphi.actual.events (network, previous_state, current_state, next_state, nodes, mechanisms=False)
Find all events (mechanisms with actual causes and actual effects).

pyphi.actual.true_ces (subsystem, previous_state, next_state)
 Set of all sets of elements that have true causes and true effects.

Note: Since the true *CauseEffectStructure* is always about the full system, the background conditions don't matter and the subsystem should be conditioned on the current state.

pyphi.actual.true_events (network, previous_state, current_state, next_state, indices=None, major_complex=None)

Return all mechanisms that have true causes and true effects within the complex.

Parameters

- **network** (Network) The network to analyze.
- **previous_state** (*tuple[int]*) The state of the network at t 1.
- **current_state** (*tuple[int]*) The state of the network at t.
- **next_state** (*tuple[int]*) The state of the network at t + 1.

Keyword Arguments

- **indices** (*tuple[int]*) The indices of the major complex.
- major_complex (AcSystemIrreducibilityAnalysis) The major complex. If major_complex is given then indices is ignored.

Returns List of true events in the major complex.

```
Return type tuple[Event]
```

pyphi.actual.extrinsic_events (network, previous_state, current_state, next_state, indices=None,

major_complex=None)

Set of all mechanisms that are in the major complex but which have true causes and effects within the entire network.

Parameters

- **network** (Network) The network to analyze.
- **previous_state** (*tuple[int]*) The state of the network at t 1.
- **current_state** (*tuple[int]*) The state of the network at t.
- **next_state** (*tuple[int]*) The state of the network at t + 1.

Keyword Arguments

- **indices** (*tuple[int]*) The indices of the major complex.
- major_complex (AcSystemIrreducibilityAnalysis) The major complex. If major_complex is given then indices is ignored.

Returns List of extrinsic events in the major complex.

Return type tuple(actions)

1.22 cache

Memoization and caching utilities.

```
pyphi.cache.memory_full()
    Check if the memory is too full for further caching.
```

```
pyphi.cache.cache (cache={}, maxmem=50, typed=False)
Memory-limited cache decorator.
```

maxmem is a float between 0 and 100, inclusive, specifying the maximum percentage of physical memory that the cache can use.

If typed is True, arguments of different types will be cached separately. For example, f(3.0) and f(3) will be treated as distinct calls with distinct results.

Arguments to the cached function must be hashable.

View the cache statistics named tuple (hits, misses, currsize) with f.cache_info(). Clear the cache and statistics with f.cache_clear(). Access the underlying function with f._wrapped__.

class pyphi.cache.DictCache

A generic dictionary-based cache.

Intended to be used as an object-level cache of method results.

 $\verb+clear()$

size()

Number of items in cache

info()

Return info about cache hits, misses, and size

get (key)

Get a value out of the cache.

Returns None if the key is not in the cache. Updates cache statistics.

set (key, value)

Set a value in the cache

key (**args*, _*prefix=None*, ***kwargs*) Get the cache key for the given function args.

Kwargs: prefix: A constant to prefix to the key.

pyphi.cache.redis_init(db)

pyphi.cache.redis_available()

Check if the Redis server is connected.

class pyphi.cache.RedisCache

clear()

Flush the cache.

static size()

Size of the Redis cache.

Note: This is the size of the entire Redis database.

info()

Return cache information.

Note: This is not the cache info for the entire Redis key space.

get (key)

Get a value from the cache.

Returns None if the key is not in the cache.

set (key, value)

Set a value in the cache.

key()

Delegate to subclasses.

pyphi.cache.validate_parent_cache (parent_cache)

class pyphi.cache.RedisMICECache(subsystem, parent_cache=None)

A Redis-backed cache for find_mice().

See *MICECache* for more info.

get (key)

Get a value from the cache.

If the *MaximallyIrreducibleCauseOrEffect* cannot be found in this cache, try and find it in the parent cache.

set (key, value)

Only need to set if the subsystem is uncut.

Caches are only inherited from uncut subsystems.

key (*direction*, *mechanism*, *purviews=False*, *_prefix=None*) Cache key. This is the call signature of find_mice().

class pyphi.cache.DictMICECache (subsystem, parent_cache=None)

A subsystem-local cache for MaximallyIrreducibleCauseOrEffect objects.

See *MICECache* for more info.

set (key, mice)

Set a value in the cache.

Only cache if:

- The subsystem is uncut (caches are only inherited from uncut subsystems so there is no reason to cache on cut subsystems.)
- $\varphi > 0$. Ideally we would cache all mice, but the size of the cache grows way too large, making parallel computations incredibly inefficient because the caches have to be passed between process. This will be changed once global caches are implemented.
- Memory is not too full.

key (*direction, mechanism, purviews=False, _prefix=None*) Cache key. This is the call signature of *find_mice()*.

pyphi.cache.MICECache (subsystem, parent_cache=None)

Construct a MaximallyIrreducibleCauseOrEffect cache.

Uses either a Redis-backed cache or a local dict cache on the object.

Parameters subsystem (Subsystem) - The subsystem that this is a cache for.

Kwargs:

parent_cache (MICECache): The cache generated by the uncut version of subsystem. Any cached MaximallyIrreducibleCauseOrEffect which are unaffected by the cut are reused in this cache. If None, the cache is initialized empty.

class pyphi.cache.PurviewCache

A network-level cache for possible purviews.

- set (*key*, *value*) Only set if purview caching is enabled
- pyphi.cache.**method** (*cache_name*, *key_prefix=None*) Caching decorator for object-level method caches.

Cache key generation is delegated to the cache.

Parameters

- **cache_name** (*str*) The name of the (already-instantiated) cache on the decorated object which should be used to store results of this method.
- *key_prefix A constant to use as part of the cache key in addition to the method arguments.

1.23 compute

See pyphi.compute.subsystem, pyphi.compute.network, pyphi.compute.distance, and pyphi.compute.parallel for documentation.

```
pyphi.compute.all_complexes
```

Alias for pyphi.compute.network.all_complexes().

- pyphi.compute.ces
 Alias for pyphi.compute.subsystem.ces().
- pyphi.compute.ces_distance Alias for pyphi.compute.distance.ces_distance().

```
pyphi.compute.complexes
```

Alias for pyphi.compute.network.complexes().

pyphi.compute.concept_distance

Alias for pyphi.compute.distance.concept_distance().

pyphi.compute.conceptual_info

Alias for pyphi.compute.subsystem.conceptual_info().

pyphi.compute.condensed Alias for pyphi.compute.network.condensed().

pyphi.compute.evaluate_cut

Alias for pyphi.compute.subsystem.evaluate_cut().

```
pyphi.compute.major_complex
Alias for pyphi.compute.network.major_complex().
```

pyphi.compute.phi
 Alias for pyphi.compute.subsystem.phi().

```
pyphi.compute.possible_complexes
    Alias for pyphi.compute.network.possible_complexes().
```

pyphi.compute.sia Alias for pyphi.compute.subsystem.sia().

```
pyphi.compute.subsystems
    Alias for pyphi.compute.network.subsystems().
```

1.24 compute.distance

Functions for computing distances between various PyPhi objects.

```
pyphi.compute.distance.concept_distance (c1, c2)
Return the distance between two concepts in concept space.
```

Parameters

- **c1** (Concept) The first concept.
- c2 (Concept) The second concept.

Returns The distance between the two concepts in concept space.

Return type float

```
pyphi.compute.distance.ces_distance(C1, C2)
```

Return the distance between two cause-effect structures.

Parameters

- C1 (CauseEffectStructure) The first CauseEffectStructure.
- C2 (CauseEffectStructure) The second CauseEffectStructure.

Returns The distance between the two cause-effect structures in concept space.

Return type float

```
pyphi.compute.distance.small_phi_ces_distance(C1, C2)
Return the difference in \varphi between CauseEffectStructure.
```

1.25 compute.network

Functions for computing network-level properties.

```
pyphi.compute.network.subsystems (network, state)
Return a generator of all possible subsystems of a network.
```

Note: Does not return subsystems that are in an impossible state (after conditioning the subsystem TPM on the state of the other nodes).

Parameters

- network (Network) The Network of interest.
- **state** (*tuple[int]*) The state of the network (a binary tuple).

Yields *Subsystem* – A *Subsystem* for each subset of nodes in the network, excluding subsystems that would be in an impossible state.

pyphi.compute.network.possible_complexes(network, state)

Return a generator of subsystems of a network that could be a complex.

This is the just powerset of the nodes that have at least one input and output (nodes with no inputs or no outputs cannot be part of a main complex, because they do not have a causal link with the rest of the subsystem in the previous or next timestep, respectively).

Note: Does not return subsystems that are in an impossible state (after conditioning the subsystem TPM on the state of the other nodes).

Parameters

- network (Network) The Network of interest.
- **state** (*tuple[int]*) The state of the network (a binary tuple).

Yields Subsystem – The next subsystem that could be a complex.

class pyphi.compute.network.**FindAllComplexes** (*iterable*, **context*) Computation engine for finding all complexes.

description = 'Finding complexes'

empty_result()

Return the default result with which to begin the computation.

static compute(subsystem)

Map over a single object from self.iterable.

process_result (new_sia, sias)

Reduce handler.

Every time a new result is generated by compute, this method is called with the result and the previous (accumulated) result. This method compares or collates these two values, returning the new result.

Setting self.done to True in this method will abort the remainder of the computation, returning this final result.

pyphi.compute.network.**all_complexes** (*network*, *state*) Return a generator for all complexes of the network.

Note: Includes reducible, zero- Φ complexes (which are not, strictly speaking, complexes at all).

Parameters

- **network** (Network) The Network of interest.
- **state** (*tuple[int]*) The state of the network (a binary tuple).

Yields *SystemIrreducibilityAnalysis* – A *SystemIrreducibilityAnalysis* for each *Subsystem* of the *Network*.

class pyphi.compute.network.**FindIrreducibleComplexes** (*iterable*, **context*) Computation engine for finding irreducible complexes of a network.

process_result (new_sia, sias)

Reduce handler.

Every time a new result is generated by compute, this method is called with the result and the previous (accumulated) result. This method compares or collates these two values, returning the new result.

Setting self.done to True in this method will abort the remainder of the computation, returning this final result.

pyphi.compute.network.complexes(network, state)

Return all irreducible complexes of the network.

Parameters

- **network** (Network) The Network of interest.
- **state** (*tuple[int]*) The state of the network (a binary tuple).

Yields SystemIrreducibilityAnalysis – A SystemIrreducibilityAnalysis for each Subsystem of the Network, excluding those with $\Phi = 0$.

pyphi.compute.network.major_complex(network, state)

Return the major complex of the network.

Parameters

- **network** (Network) The Network of interest.
- **state** (*tuple[int]*) The state of the network (a binary tuple).

Returns The *SystemIrreducibilityAnalysis* for the *Subsystem* with maximal Φ .

Return type SystemIrreducibilityAnalysis

pyphi.compute.network.condensed(network, state)

Return a list of maximal non-overlapping complexes.

Parameters

- **network** (Network) The Network of interest.
- **state** (*tuple[int]*) The state of the network (a binary tuple).
- **Returns** A list of *SystemIrreducibilityAnalysis* for non-overlapping complexes with maximal Φ values.

Return type list[SystemIrreducibilityAnalysis]

1.26 compute.parallel

Utilities for parallel computation.

```
class pyphi.compute.parallel.ExceptionWrapper(exception)
```

A picklable wrapper suitable for passing exception tracebacks through instances of multiprocessing. Queue.

Parameters exception (*Exception*) – The exception to wrap.

```
reraise()
```

Re-raise the exception.

```
class pyphi.compute.parallel.MapReduce(iterable, *context)
```

An engine for doing heavy computations over an iterable.

This is similar to multiprocessing.Pool, but allows computations to shortcircuit, and supports both parallel and sequential computations.

Parameters

- iterable (Iterable) A collection of objects to perform a computation over.
- ***context** Any additional data necessary to complete the computation.

Any subclass of MapReduce must implement three methods:

```
- ``empty_result``,
- ``compute``, (map), and
- ``process_result`` (reduce).
```

The engine includes a builtin tqdm progress bar; this can be disabled by setting pyphi.config. PROGRESS_BARS to False.

Parallel operations start a daemon thread which handles log messages sent from worker processes.

Subprocesses spawned by MapReduce cannot spawn more subprocesses; be aware of this when composing nested computations. This is not an issue in practice because it is typically most efficient to only parallelize the top level computation.

```
description = ''
```

```
empty_result (*context)
```

Return the default result with which to begin the computation.

```
static compute (obj, *context)
```

Map over a single object from self.iterable.

process_result (new_result, old_result)

Reduce handler.

Every time a new result is generated by compute, this method is called with the result and the previous (accumulated) result. This method compares or collates these two values, returning the new result.

Setting self.done to True in this method will abort the remainder of the computation, returning this final result.

```
init_progress_bar()
```

Initialize and return a progress bar.

static worker(compute, task_queue, result_queue, log_queue, complete, *context)
A worker process, run by multiprocessing.Process.

```
start_parallel()
```

Initialize all queues and start the worker processes and the log thread.

initialize_tasks()

Load the input queue to capacity.

Overfilling causes a deadlock when *queue.put* blocks when full, so further tasks are enqueued as results are returned.

maybe_put_task()

Enqueue the next task, if there are any waiting.

run_parallel()

Perform the computation in parallel, reading results from the output queue and passing them to process_result.

finish_parallel()

Orderly shutdown of workers.

run_sequential()

Perform the computation sequentially, only holding two computed objects in memory at a time.

run (parallel=True)

Perform the computation.

Keyword Arguments parallel (*boolean*) – If True, run the computation in parallel. Otherwise, operate sequentially.

class pyphi.compute.parallel.LogThread(q)

 $Thread \ which \ handles \ log \ records \ sent \ from \ {\tt MapReduce} \ processes.$

It listens to an instance of multiprocessing. Queue, rewriting log messages to the PyPhi log handler.

run()

Method representing the thread's activity.

You may override this method in a subclass. The standard run() method invokes the callable object passed to the object's constructor as the target argument, if any, with sequential and keyword arguments taken from the args and kwargs arguments, respectively.

```
pyphi.compute.parallel.configure_worker_logging(queue)
    Configure a worker process to log all messages to queue.
```

1.27 compute.subsystem

Functions for computing subsystem-level properties.

```
class pyphi.compute.subsystem.ComputeCauseEffectStructure(iterable, *context)
Engine for computing a CauseEffectStructure.
```

```
description = 'Computing concepts'
```

subsystem

```
empty_result (*args)
```

Return the default result with which to begin the computation.

static compute (mechanism, subsystem, purviews, cause_purviews, effect_purviews)
Compute a Concept for a mechanism, in this Subsystem with the provided purviews.

```
process_result (new_concept, concepts)
```

Save all concepts with non-zero φ to the CauseEffectStructure.

pyphi.compute.subsystem.ces (subsystem, mechanisms=False, purviews=False, cause_purviews=False, effect_purviews=False, parallel=False)

Return the conceptual structure of this subsystem, optionally restricted to concepts with the mechanisms and purviews given in keyword arguments.

If you don't need the full *CauseEffectStructure*, restricting the possible mechanisms and purviews can make this function much faster.

Parameters subsystem (Subsystem) - The subsystem for which to determine the CauseEffectStructure.

Keyword Arguments

- **mechanisms** (*tuple[tuple[int]]*) Restrict possible mechanisms to those in this list.
- **purviews** (tuple[tuple[int]]) Same as in concept().
- **cause_purviews** (tuple[tuple[int]]) Same as in concept().
- **effect_purviews** (tuple[tuple[int]]) Same as in concept().
- **parallel** (*bool*) Whether to compute concepts in parallel. If True, overrides config.PARALLEL_CONCEPT_EVALUATION.

Returns A tuple of every *Concept* in the cause-effect structure.

Return type *CauseEffectStructure*

This is the distance from the subsystem's *CauseEffectStructure* to the null concept.

pyphi.compute.subsystem.evaluate_cut (uncut_subsystem, cut, unpartitioned_ces) Compute the system irreducibility for a given cut.

Parameters

- uncut_subsystem (Subsystem) The subsystem without the cut applied.
- **cut** (Cut) The cut to evaluate.
- **unpartitioned_ces** (CauseEffectStructure) The cause-effect structure of the uncut subsystem.

Returns The SystemIrreducibilityAnalysis for that cut.

Return type SystemIrreducibilityAnalysis

class pyphi.compute.subsystem.**ComputeSystemIrreducibility** (*iterable*, **context*) Computation engine for system-level irreducibility.

description = 'Evaluating Φ cuts'

empty_result (*subsystem*, *unpartitioned_ces*) Begin with a *SystemIrreducibilityAnalysis* with infinite Φ ; all actual SIAs will have less.

- **static compute** (*cut*, *subsystem*, *unpartitioned_ces*) Evaluate a cut.
- **process_result** (*new_sia*, *min_sia*) Check if the new SIA has smaller Φ than the standing result.

pyphi.compute.subsystem.sia_bipartitions (*nodes*, *node_labels=None*) Return all Φ cuts for the given nodes.

This value changes based on config.CUT_ONE_APPROXIMATION.

Parameters nodes (*tuple[int]*) – The node indices to partition.

Returns All unidirectional partitions.

Return type list[Cut]

pyphi.compute.subsystem.sia(cache_key, subsystem)

Return the minimal information partition of a subsystem.

Parameters subsystem (Subsystem) - The candidate set of nodes.

Returns A nested structure containing all the data from the intermediate calculations. The top level contains the basic irreducibility information for the given subsystem.

Return type SystemIrreducibilityAnalysis

pyphi.compute.subsystem.**phi** (*subsystem*) Return the Φ value of a subsystem.

class pyphi.compute.subsystem.**ConceptStyleSystem**(*subsystem*, *direction*, *cut=None*) A functional replacement for Subsystem implementing concept-style system cuts.

apply_cut (cut)

____getattr___(*name*) Pass attribute access through to the basic subsystem.

cause_system

effect_system

concept (*mechanism*, *purviews=False*, *cause_purviews=False*, *effect_purviews=False*) Compute a concept, using the appropriate system for each side of the cut.

pyphi.compute.subsystem.concept_cuts (direction, node_indices, node_labels=None)
Generator over all concept-syle cuts for these nodes.

pyphi.compute.subsystem.directional_sia (*subsystem*, *direction*, *unpartitioned_ces=None*) Calculate a concept-style SystemIrreducibilityAnalysisCause or SystemIrreducibilityAnalysisEffect.

Represents a SystemIrreducibilityAnalysis computed using concept-style system cuts.

min_sia

__getattr___(*name*) Pass attribute access through to the minimal SIA.

unorderable_unless_eq = ['network']

order_by()

Return a list of values to compare for ordering.

The first value in the list has the greatest priority; if the first objects are equal the second object is compared, etc.

pyphi.compute.subsystem.sia_concept_style(subsystem)
Compute a concept-style SystemIrreducibilityAnalysis

1.28 conf

1.28.1 Loading a configuration

Various aspects of PyPhi's behavior can be configured.

When PyPhi is imported, it checks for a YAML file named pyphi_config.yml in the current directory and automatically loads it if it exists; otherwise the default configuration is used.

The various settings are listed here with their defaults.

```
>>> import pyphi
>>> defaults = pyphi.config.defaults()
```

Print the config object to see the current settings:

```
>>> print(pyphi.config)
{ 'ASSUME_CUTS_CANNOT_CREATE_NEW_CONCEPTS': False,
    'CACHE_SIAS': False,
    'CACHE_POTENTIAL_PURVIEWS': True,
    'CACHING_BACKEND': 'fs',
    ...
```

Setting can be changed on the fly by assigning them a new value:

>>> pyphi.config.PROGRESS_BARS = False

It is also possible to manually load a configuration file:

>>> pyphi.config.load_file('pyphi_config.yml')

Or load a dictionary of configuration values:

```
>>> pyphi.config.load_dict({'PRECISION': 1})
```

1.28.2 Approximations and theoretical options

These settings control the algorithms PyPhi uses.

- ASSUME_CUTS_CANNOT_CREATE_NEW_CONCEPTS
- CUT_ONE_APPROXIMATION
- MEASURE
- PARTITION_TYPE
- PICK_SMALLEST_PURVIEW
- USE_SMALL_PHI_DIFFERENCE_FOR_CES_DISTANCE
- SYSTEM_CUTS
- SINGLE_MICRO_NODES_WITH_SELFLOOPS_HAVE_PHI
- VALIDATE_SUBSYSTEM_STATES
- VALIDATE_CONDITIONAL_INDEPENDENCE

1.28.3 Parallelization and system resources

These settings control how much processing power and memory is available for PyPhi to use. The default values may not be appropriate for your use-case or machine, so **please check these settings before running anything**. Otherwise, there is a risk that simulations might crash (potentially after running for a long time!), resulting in data loss.

• PARALLEL_CONCEPT_EVALUATION

- PARALLEL_CUT_EVALUATION
- PARALLEL_COMPLEX_EVALUATION
- NUMBER_OF_CORES
- MAXIMUM_CACHE_MEMORY_PERCENTAGE

Important: Only one of PARALLEL_CONCEPT_EVALUATION, PARALLEL_CUT_EVALUATION, and PARALLEL_COMPLEX_EVALUATION can be set to True at a time.

For most networks, PARALLEL_CUT_EVALUATION is the most efficient. This is because the algorithm is exponential time in the number of nodes, so the most of the time is spent on the largest subsystem.

You should only parallelize concept evaluation if you are just computing a CauseEffectStructure.

1.28.4 Memoization and caching

PyPhi provides a number of ways to cache intermediate results.

- CACHE_SIAS
- CACHE_REPERTOIRES
- CACHE_POTENTIAL_PURVIEWS
- CLEAR_SUBSYSTEM_CACHES_AFTER_COMPUTING_SIA
- CACHING_BACKEND
- FS_CACHE_VERBOSITY
- FS_CACHE_DIRECTORY
- MONGODB_CONFIG
- REDIS_CACHE
- REDIS_CONFIG

1.28.5 Logging

These settings control how PyPhi handles log messages. Logs can be written to standard output, a file, both, or none. If these simple default controls are not flexible enough for you, you can override the entire logging configuration. See the documentation on Python's logger for more information.

- LOG_STDOUT_LEVEL
- LOG_FILE_LEVEL
- LOG_FILE
- PROGRESS_BARS
- REPR_VERBOSITY
- PRINT_FRACTIONS

1.28.6 Numerical precision

• PRECISION

1.28.7 The config API

class pyphi.conf.**Option** (*default*, *values=None*, *on_change=None*, *doc=None*) A descriptor implementing PyPhi configuration options.

Parameters default - The default value of this Option.

Keyword Arguments

- **values** (*list*) Allowed values for this option. A ValueError will be raised if values is not None and the option is set to be a value not in the list.
- **on_change** (*function*) Optional callback that is called when the value of the option is changed. The Config instance is passed as the only argument to the callback.
- **doc** (*str*) Optional docstring for the option.

```
class pyphi.conf.ConfigMeta(cls_name, bases, namespace)
    Metaclass for Config.
```

Responsible for setting the name of each Option when a subclass of Config is created; because Option objects are defined on the class, not the instance, their name should only be set once.

Python 3.6 handles this exact need with the special descriptor method <u>__set_name__</u> (see PEP 487). We should use that once we drop support for 3.4 & 3.5.

class pyphi.conf.Config

Base configuration object.

See PyphiConfig for usage.

classmethod options()

Return a dictionary the Option objects for this config

defaults()

Return the default values of this configuration.

load_dict (dct)

Load a dictionary of configuration values.

load_file (filename)

Load config from a YAML file.

snapshot()

Return a snapshot of the current values of this configuration.

override (**new_values)

Decorator and context manager to override configuration values.

The initial configuration values are reset after the decorated function returns or the context manager completes it block, even if the function or block raises an exception. This is intended to be used by tests which require specific configuration values.

Example

```
>>> from pyphi import config
>>> @config.override(PRECISION=20000)
... def test_something():
... assert config.PRECISION == 20000
...
>>> test_something()
>>> with config.override(PRECISION=100):
... assert config.PRECISION == 100
...
```

pyphi.conf.configure_logging(conf)

Reconfigure PyPhi logging based on the current configuration.

class pyphi.conf.PyphiConfig

pyphi.config is an instance of this class.

ASSUME_CUTS_CANNOT_CREATE_NEW_CONCEPTS

default=False

In certain cases, making a cut can actually cause a previously reducible concept to become a proper, irreducible concept. Assuming this can never happen can increase performance significantly, however the obtained results are not strictly accurate.

CUT_ONE_APPROXIMATION

default=False

When determining the MIP for Φ , this restricts the set of system cuts that are considered to only those that cut the inputs or outputs of a single node. This restricted set of cuts scales linearly with the size of the system; the full set of all possible bipartitions scales exponentially. This approximation is more likely to give theoretically accurate results with modular, sparsely-connected, or homogeneous networks.

MEASURE

default='EMD'

The measure to use when computing distances between repertoires and concepts. A full list of currently installed measures is available by calling print (pyphi.distance.measures.all()). Note that some measures cannot be used for calculating Φ because they are asymmetric.

Custom measures can be added using the pyphi.distance.measures.register decorator. For example:

```
from pyphi.distance import measures
@measures.register('ALWAYS_ZERO')
def always_zero(a, b):
    return 0
```

This measures can then be used by setting config.MEASURE = 'ALWAYS_ZERO'.

If the measure is asymmetric you should register it using the asymmetric keyword argument. See *distance* for examples.

PARALLEL_CONCEPT_EVALUATION

default=False

Controls whether concepts are evaluated in parallel when computing cause-effect structures.

PARALLEL_CUT_EVALUATION

default=True

Controls whether system cuts are evaluated in parallel, which is faster but requires more memory. If cuts are evaluated sequentially, only two *SystemIrreducibilityAnalysis* instances need to be in memory at once.

PARALLEL_COMPLEX_EVALUATION

default=False

Controls whether systems are evaluated in parallel when computing complexes.

NUMBER_OF_CORES

default=-1

Controls the number of CPU cores used to evaluate unidirectional cuts. Negative numbers count backwards from the total number of available cores, with -1 meaning 'use all available cores.'

MAXIMUM_CACHE_MEMORY_PERCENTAGE

default=50

PyPhi employs several in-memory caches to speed up computation. However, these can quickly use a lot of memory for large networks or large numbers of them; to avoid thrashing, this setting limits the percentage of a system's RAM that the caches can collectively use.

CACHE_SIAS

default=False

PyPhi is equipped with a transparent caching system for *SystemIrreducibilityAnalysis* objects which stores them as they are computed to avoid having to recompute them later. This makes it easy to play around interactively with the program, or to accumulate results with minimal effort. For larger projects, however, it is recommended that you manage the results explicitly, rather than relying on the cache. For this reason it is disabled by default.

CACHE_REPERTOIRES

default=True

PyPhi caches cause and effect repertoires. This greatly improves speed, but can consume a significant amount of memory. If you are experiencing memory issues, try disabling this.

CACHE_POTENTIAL_PURVIEWS

default=True

Controls whether the potential purviews of mechanisms of a network are cached. Caching speeds up computations by not recomputing expensive reducibility checks, but uses additional memory.

CLEAR_SUBSYSTEM_CACHES_AFTER_COMPUTING_SIA

default=False

Controls whether a *Subsystem*'s repertoire and MICE caches are cleared with *clear_caches()* after computing the *SystemIrreducibilityAnalysis*. If you don't need to do any more computations after running *sia()*, then enabling this may help conserve memory.

CACHING_BACKEND

default='fs'

Controls whether precomputed results are stored and read from a local filesystem-based cache in the current directory or from a database. Set this to 'fs' for the filesystem, 'db' for the database.

FS_CACHE_VERBOSITY

default=0

Controls how much caching information is printed if the filesystem cache is used. Takes a value between 0 and 11.

FS_CACHE_DIRECTORY

default='__pyphi_cache__'

If the filesystem is used for caching, the cache will be stored in this directory. This directory can be copied and moved around if you want to reuse results *e.g.* on a another computer, but it must be in the same directory from which Python is being run.

MONGODB_CONFIG

```
default={'collection_name' -- 'cache', 'host' -- 'localhost', 'port':
27017, 'database_name': 'pyphi'}
```

Set the configuration for the MongoDB database backend (only has an effect if CACHING_BACKEND is 'db').

REDIS_CACHE

default=False

Specifies whether to use Redis to cache MaximallyIrreducibleCauseOrEffect.

REDIS_CONFIG

```
default={'test_db' -- 1, 'db' -- 0, 'host': 'localhost', 'port':
6379}
```

Configure the Redis database backend. These are the defaults in the provided redis.conf file.

LOG_FILE

default='pyphi.log', on_change=configure_logging

Controls the name of the log file.

LOG_FILE_LEVEL

default='INFO', on_change=configure_logging

Controls the level of log messages written to the log file. This setting has the same possible values as LOG_STDOUT_LEVEL.

LOG_STDOUT_LEVEL

default='WARNING', on_change=configure_logging

Controls the level of log messages written to standard output. Can be one of 'DEBUG', 'INFO', 'WARNING', 'ERROR', 'CRITICAL', or None. 'DEBUG' is the least restrictive level and will show the most log messages. 'CRITICAL' is the most restrictive level and will only display information about fatal errors. If set to None, logging to standard output will be disabled entirely.

PROGRESS_BARS

default=True

Controls whether to show progress bars on the console.

Tip: If you are iterating over many systems rather than doing one long-running calculation, consider disabling this for speed.

PRECISION

default=6

If MEASURE is EMD, then the Earth Mover's Distance is calculated with an external C++ library that a numerical optimizer to find a good approximation. Consequently, systems with analytically zero Φ will sometimes be numerically found to have a small but non-zero amount. This setting controls the number of decimal places to which PyPhi will consider EMD calculations accurate. Values of Φ lower than 10e-PRECISION will be considered insignificant and treated as zero. The default value is about as accurate as the EMD computations get.

VALIDATE_SUBSYSTEM_STATES

default=True

Controls whether PyPhi checks if the subsystems's state is possible (reachable with nonzero probability from some previous state), given the subsystem's TPM (which is conditioned on background conditions). If this is turned off, then calculated Φ values may not be valid, since they may be associated with a subsystem that could never be in the given state.

VALIDATE_CONDITIONAL_INDEPENDENCE

default=True

Controls whether PyPhi checks if a system's TPM is conditionally independent.

SINGLE_MICRO_NODES_WITH_SELFLOOPS_HAVE_PHI

default=False

If set to True, the Φ value of single micro-node subsystems is the difference between their unpartitioned *CauseEffectStructure* (a single concept) and the null concept. If set to False, their Φ is defined to be zero. Single macro-node subsystems may always be cut, regardless of circumstances.

REPR_VERBOSITY

default=2, values=[0, 1, 2]

Controls the verbosity of <u>repr</u> methods on PyPhi objects. Can be set to 0, 1, or 2. If set to 1, calling repr on PyPhi objects will return pretty-formatted and legible strings, excluding repertoires. If set to 2, repr calls also include repertoires.

Although this breaks the convention that <u>__repr__</u> methods should return a representation which can reconstruct the object, readable representations are convenient since the Python REPL calls repr to represent all objects in the shell and PyPhi is often used interactively with the REPL. If set to 0, repr returns more traditional object representations.

PRINT_FRACTIONS

default=True

Controls whether numbers in a repr are printed as fractions. Numbers are still printed as decimals if the fraction's denominator would be large. This only has an effect if $REPR_VERBOSITY > 0$.

PARTITION_TYPE

default='BI'

Controls the type of partition used for φ computations.

If set to 'BI', partitions will have two parts.

If set to 'TRI', partitions will have three parts. In addition, computations will only consider partitions that strictly partition the mechanism the mechanism. That is, for the mechanism (A, B) and purview (B, C, D) the partition:

A, B ______ B C, D

is not considered, but:

A B B C,D

is. The following is also valid:

In addition, this setting introduces "wedge" tripartitions of the form:

A B _____ B C D

where the mechanism in the third part is always empty.

In addition, in the case of a φ -tie when computing a *MaximallyIrreducibleCause* or *MaximallyIrreducibleEffect*, The 'TRIPARTITION' setting choses the MIP with smallest purview instead of the largest (which is the default).

Finally, if set to 'ALL', all possible partitions will be tested.

PICK_SMALLEST_PURVIEW

default=False

When computing a *MaximallyIrreducibleCause* or *MaximallyIrreducibleEffect*, it is possible for several MIPs to have the same φ value. If this setting is set to True the MIP with the smallest purview is chosen; otherwise, the one with largest purview is chosen.

USE_SMALL_PHI_DIFFERENCE_FOR_CES_DISTANCE

default=False

If set to True, the distance between cause-effect structures (when computing a SystemIrreducibilityAnalysis) is calculated using the difference between the sum of φ in the cause-effect structures instead of the extended EMD.

SYSTEM_CUTS

default='3.0_STYLE', values=['3.0_STYLE', 'CONCEPT_STYLE']

If set to '3.0_STYLE', then traditional IIT 3.0 cuts will be used when computing Φ . If set to 'CONCEPT_STYLE', then experimental concept-style system cuts will be used instead.

log()

Log current settings.

1.29 connectivity

Functions for determining network connectivity properties.

- pyphi.connectivity.get_outputs_from_cm (*index*, cm) Return indices of the outputs of node with the given index.
- pyphi.connectivity.relevant_connections (n, _from, to)
 Construct a connectivity matrix.

Parameters

- **n** (*int*) The dimensions of the matrix
- _from (tuple[int]) Nodes with outgoing connections to to
- to (tuple[int]) Nodes with incoming connections from _from

Returns An $N \times N$ connectivity matrix with the (i, j)th entry is 1 if i is in _from and j is in to, and 0 otherwise.

Return type np.ndarray

pyphi.connectivity.block_cm(cm)

Return whether cm can be arranged as a block connectivity matrix.

If so, the corresponding mechanism/purview is trivially reducible. Technically, only square matrices are "block diagonal", but the notion of connectivity carries over.

We test for block connectivity by trying to grow a block of nodes such that:

- · 'source' nodes only input to nodes in the block
- 'sink' nodes only receive inputs from source nodes in the block

For example, the following connectivity matrix represents connections from nodes1 = A, B, Ctonodes2 = D, E, F, G (without loss of generality, note that nodes1 and nodes2 may share elements):

```
D E F G
A [1, 1, 0, 0]
B [1, 1, 0, 0]
C [0, 0, 1, 1]
```

Since nodes AB only connect to nodes DE, and node C only connects to nodes FG, the subgraph is reducible, because the cut

A,B	С
D,E	F,G

does not change the structure of the graph.

pyphi.connectivity.block_reducible(cm, nodes1, nodes2)

Return whether connections from nodes1 to nodes2 are reducible.

Parameters

- **cm** (*np*.*ndarray*) The network's connectivity matrix.
- **nodes1** (tuple[int]) Source nodes
- nodes2 (tuple[int]) Sink nodes

```
pyphi.connectivity.is_strong(cm, nodes=None)
```

Return whether the connectivity matrix is strongly connected.

Remember that a singleton graph is strongly connected.

Parameters cm (*np.ndarray*) – A square connectivity matrix.

Keyword Arguments nodes (*tuple[int]*) – A subset of nodes to consider.

pyphi.connectivity.is_weak(cm, nodes=None)

Return whether the connectivity matrix is weakly connected.

Parameters cm(*np*.*ndarray*) – A square connectivity matrix.

Keyword Arguments nodes (tuple[int]) - A subset of nodes to consider.

pyphi.connectivity.is_full(cm, nodes1, nodes2)

Test connectivity of one set of nodes to another.

Parameters

- cm (np.ndarrray) The connectivity matrix
- **nodes1** (*tuple[int]*) The nodes whose outputs to nodes2 will be tested.
- **nodes2** (*tuple[int]*) The nodes whose inputs from nodes1 will be tested.
- **Returns** True if all elements in nodes1 output to some element in nodes2 and all elements in nodes2 have an input from some element in nodes1, or if either set of nodes is empty; False otherwise.

Return type bool

1.30 constants

Package-wide constants.

```
pyphi.constants.EPSILON = 1e-06
The threshold below which we consider differences in phi values to be zero.
```

```
pyphi.constants.FILESYSTEM = 'fs'
```

Label for the filesystem cache backend.

pyphi.constants.**DATABASE = 'db'** Label for the MongoDB cache backend.

```
pyphi.constants.PICKLE_PROTOCOL = 4
The protocol used for pickling objects.
```

```
pyphi.constants.joblib_memory = Memory(cachedir='__pyphi_cache__/joblib')
The joblib Memory object for persistent caching without a database.
```

```
pyphi.constants.OFF = (0,)
    Node states
```

1.31 convert

Conversion functions.

See the documentation on PyPhi *Transition probability matrix conventions* for information on the different representations that these functions convert between.

Examples

```
>>> reverse_bits(12, 7)
24
>>> reverse_bits(0, 1)
```

```
>>> reverse_bits(1, 2)
2
```

```
pyphi.convert.nodes2indices (nodes)
Convert nodes to a tuple of their indices.
```

```
pyphi.convert.nodes2state (nodes)
Convert nodes to a tuple of their states.
```

```
pyphi.convert.be2le(i, n)
Convert between big-endian and little-endian for indices in range(n).
```

```
pyphi.convert.le2be(i, n)
```

Convert between big-endian and little-endian for indices in range (n).

```
pyphi.convert.state2be_index(state)
```

Convert a PyPhi state-tuple to a decimal index according to the big-endian convention.

Parameters state (tuple[int]) - A state-tuple where the i^{th} element of the tuple gives the state of the i^{th} node.

Returns A decimal integer corresponding to a network state under the big-endian convention.

Return type int

Examples

```
>>> state2be_index((1, 0, 0, 0, 0))
16
>>> state2be_index((1, 1, 1, 0, 0, 0, 0, 0))
224
```

pyphi.convert.state2le_index(state)

Convert a PyPhi state-tuple to a decimal index according to the little-endian convention.

Parameters state (tuple[int]) - A state-tuple where the i^{th} element of the tuple gives the state of the i^{th} node.

Returns A decimal integer corresponding to a network state under the little-endian convention.

Return type int

Examples

```
>>> state2le_index((1, 0, 0, 0, 0))
1
>>> state2le_index((1, 1, 1, 0, 0, 0, 0, 0))
7
```

pyphi.convert.le_index2state(i, number_of_nodes)

Convert a decimal integer to a PyPhi state tuple with the little-endian convention.

The output is the reverse of be_index2state().

Parameters i (*int*) – A decimal integer corresponding to a network state under the little-endian convention.

Returns A state-tuple where the i^{th} element of the tuple gives the state of the i^{th} node.

Return type tuple[int]

Examples

```
>>> number_of_nodes = 5
>>> le_index2state(1, number_of_nodes)
(1, 0, 0, 0, 0)
>>> number_of_nodes = 8
>>> le_index2state(7, number_of_nodes)
(1, 1, 1, 0, 0, 0, 0, 0)
```

pyphi.convert.be_index2state(i, number_of_nodes)

Convert a decimal integer to a PyPhi state tuple using the big-endian convention that the most-significant bits correspond to low-index nodes.

The output is the reverse of le_index2state().

Parameters i (*int*) – A decimal integer corresponding to a network state under the big-endian convention.

Returns A state-tuple where the i^{th} element of the tuple gives the state of the i^{th} node.

Return type tuple[int]

Examples

```
>>> number_of_nodes = 5
>>> be_index2state(1, number_of_nodes)
(0, 0, 0, 0, 1)
>>> number_of_nodes = 8
>>> be_index2state(7, number_of_nodes)
(0, 0, 0, 0, 0, 1, 1, 1)
```

pyphi.convert.be2le_state_by_state(tpm)

Convert a state-by-state TPM from big-endian to little-endian or vice versa.

Parameters tpm (*np.ndarray*) – A state-by-state TPM.

Returns The state-by-state TPM in the other indexing format.

Return type np.ndarray

Example

```
>>> tpm = np.arange(16).reshape([4, 4])
>>> be2le_state_by_state(tpm)
array([[ 0., 1., 2., 3.],
       [ 8., 9., 10., 11.],
       [ 4., 5., 6., 7.],
       [12., 13., 14., 15.]])
```

pyphi.convert.le2be_state_by_state(tpm)

Convert a state-by-state TPM from big-endian to little-endian or vice versa.

Parameters tpm (*np*.*ndarray*) – A state-by-state TPM.

Returns The state-by-state TPM in the other indexing format.

Return type np.ndarray

Example

```
>>> tpm = np.arange(16).reshape([4, 4])
>>> be2le_state_by_state(tpm)
array([[ 0., 1., 2., 3.],
       [ 8., 9., 10., 11.],
       [ 4., 5., 6., 7.],
       [12., 13., 14., 15.]])
```

pyphi.convert.to_multidimensional(tpm)

Reshape a state-by-node TPM to the multidimensional form.

See documentation for the *Network* object for more information on TPM formats.

pyphi.convert.to_2dimensional(tpm)

Reshape a state-by-node TPM to the 2-dimensional form.

See *Transition probability matrix conventions* and documentation for the *Network* object for more information on TPM representations.

```
pyphi.convert.state_by_state2state_by_node (tpm)
Convert a state hu state TPM to a state hu mode TPM
```

Convert a state-by-state TPM to a state-by-node TPM.

Danger: Many nondeterministic state-by-state TPMs can be represented by a single a state-by-state TPM. However, the mapping can be made to be one-to-one if we assume the state-by-state TPM is conditionally independent, as this function does. **If the given TPM is not conditionally independent, the conditional dependencies will be silently lost.**

Note: The indices of the rows and columns of the state-by-state TPM are assumed to follow the little-endian convention. The indices of the rows of the resulting state-by-node TPM also follow the little-endian convention. See the documentation on PyPhi the *Transition probability matrix conventions* more information.

Parameters tpm (*list*[*list*] or *np*.*ndarray*) – A square state-by-state TPM with row and column indices following the little-endian convention.

Returns A state-by-node TPM, with row indices following the little-endian convention.

Return type np.ndarray

Example

```
>>> tpm = np.array([[0.5, 0.5, 0.0, 0.0],
... [0.0, 1.0, 0.0, 0.0],
... [0.0, 0.2, 0.0, 0.8],
... [0.0, 0.3, 0.7, 0.0]])
>>> state_by_state2state_by_node(tpm)
```

```
array([[[0.5, 0. ],
[1., 0.8]],
[[1., 0. ],
[0.3, 0.7]]])
```

pyphi.convert.state_by_node2state_by_state(tpm)

Convert a state-by-node TPM to a state-by-state TPM.

Important: A nondeterministic state-by-node TPM can have more than one representation as a state-bystate TPM. However, the mapping can be made to be one-to-one if we assume the TPMs to be conditionally independent. Therefore, **this function returns the corresponding conditionally independent state-by-state TPM.**

Note: The indices of the rows of the state-by-node TPM are assumed to follow the little-endian convention, while the indices of the columns follow the big-endian convention. The indices of the rows and columns of the resulting state-by-state TPM both follow the big-endian convention. See the documentation on PyPhi *Transition probability matrix conventions* for more info.

- **Parameters tpm** (*list[list]* or *np.ndarray*) A state-by-node TPM with row indices following the little-endian convention and column indices following the big-endian convention.
- **Returns** A state-by-state TPM, with both row and column indices following the big-endian convention.

Return type np.ndarray

```
>>> tpm = np.array([[1, 1, 0],
                     [0, 0, 1],
. . .
                     [0, 1, 1],
. . .
                     [1, 0, 0],
. . .
                     [0, 0, 1],
. . .
                     [1, 0, 0],
. . .
. . .
                     [1, 1, 1],
                     [1, 0, 1]])
>>> state_by_node2state_by_state(tpm)
array([[0., 0., 0., 1., 0., 0., 0.],
       [0., 0., 0., 0., 1., 0., 0., 0.],
       [0., 0., 0., 0., 0., 0., 1., 0.],
       [0., 1., 0., 0., 0., 0., 0., 0.],
       [0., 0., 0., 0., 1., 0., 0., 0.],
       [0., 1., 0., 0., 0., 0., 0., 0.],
       [0., 0., 0., 0., 0., 0., 0., 1.],
       [0., 0., 0., 0., 0., 1., 0., 0.]])
```

pyphi.convert.b21(i, n)

Convert between big-endian and little-endian for indices in range (n).

```
pyphi.convert.l2b(i, n)
```

Convert between big-endian and little-endian for indices in range (n).

```
pyphi.convert.l2s(i, number_of_nodes)
```

Convert a decimal integer to a PyPhi state tuple with the little-endian convention.

The output is the reverse of *be_index2state()*.

Parameters i (*int*) – A decimal integer corresponding to a network state under the little-endian convention.

Returns A state-tuple where the i^{th} element of the tuple gives the state of the i^{th} node.

Return type tuple[int]

Examples

```
>>> number_of_nodes = 5
>>> le_index2state(1, number_of_nodes)
(1, 0, 0, 0, 0)
>>> number_of_nodes = 8
>>> le_index2state(7, number_of_nodes)
(1, 1, 1, 0, 0, 0, 0, 0)
```

pyphi.convert.b2s(i, number_of_nodes)

Convert a decimal integer to a PyPhi state tuple using the big-endian convention that the most-significant bits correspond to low-index nodes.

The output is the reverse of le_index2state().

Parameters i (*int*) – A decimal integer corresponding to a network state under the big-endian convention.

Returns A state-tuple where the i^{th} element of the tuple gives the state of the i^{th} node.

Return type tuple[int]

Examples

```
>>> number_of_nodes = 5
>>> be_index2state(1, number_of_nodes)
(0, 0, 0, 0, 1)
>>> number_of_nodes = 8
>>> be_index2state(7, number_of_nodes)
(0, 0, 0, 0, 0, 1, 1, 1)
```

pyphi.convert.s21(state)

Convert a PyPhi state-tuple to a decimal index according to the little-endian convention.

Parameters state (tuple[int]) - A state-tuple where the i^{th} element of the tuple gives the state of the i^{th} node.

Returns A decimal integer corresponding to a network state under the little-endian convention.

Return type int

Examples

```
>>> state2le_index((1, 0, 0, 0, 0))
1
>>> state2le_index((1, 1, 1, 0, 0, 0, 0, 0))
7
```

pyphi.convert.s2b(state)

Convert a PyPhi state-tuple to a decimal index according to the big-endian convention.

Parameters state (tuple[int]) - A state-tuple where the ith element of the tuple gives the state of the ith node.

Returns A decimal integer corresponding to a network state under the big-endian convention.

Return type int

Examples

```
>>> state2be_index((1, 0, 0, 0, 0))
16
>>> state2be_index((1, 1, 1, 0, 0, 0, 0, 0))
224
```

pyphi.convert.b21_sbs(tpm)

Convert a state-by-state TPM from big-endian to little-endian or vice versa.

Parameters tpm (*np.ndarray*) – A state-by-state TPM.

Returns The state-by-state TPM in the other indexing format.

Return type np.ndarray

Example

```
>>> tpm = np.arange(16).reshape([4, 4])
>>> be2le_state_by_state(tpm)
array([[ 0., 1., 2., 3.],
       [ 8., 9., 10., 11.],
       [ 4., 5., 6., 7.],
       [12., 13., 14., 15.]])
```

pyphi.convert.l2b_sbs(tpm)

Convert a state-by-state TPM from big-endian to little-endian or vice versa.

Parameters tpm (*np.ndarray*) – A state-by-state TPM.

Returns The state-by-state TPM in the other indexing format.

Return type np.ndarray

Example

```
>>> tpm = np.arange(16).reshape([4, 4])
>>> be2le_state_by_state(tpm)
array([[ 0., 1., 2., 3.],
       [ 8., 9., 10., 11.],
       [ 4., 5., 6., 7.],
       [12., 13., 14., 15.]])
```

pyphi.convert.to_md(tpm)

Reshape a state-by-node TPM to the multidimensional form.

See documentation for the *Network* object for more information on TPM formats.

pyphi.convert.to_2d(tpm)

Reshape a state-by-node TPM to the 2-dimensional form.

See *Transition probability matrix conventions* and documentation for the *Network* object for more information on TPM representations.

pyphi.convert.sbn2sbs(tpm)

Convert a state-by-node TPM to a state-by-state TPM.

Important: A nondeterministic state-by-node TPM can have more than one representation as a state-bystate TPM. However, the mapping can be made to be one-to-one if we assume the TPMs to be conditionally independent. Therefore, **this function returns the corresponding conditionally independent state-by-state TPM.**

Note: The indices of the rows of the state-by-node TPM are assumed to follow the little-endian convention, while the indices of the columns follow the big-endian convention. The indices of the rows and columns of the resulting state-by-state TPM both follow the big-endian convention. See the documentation on PyPhi *Transition probability matrix conventions* for more info.

Parameters tpm (*list[list]* or *np.ndarray*) – A state-by-node TPM with row indices following the little-endian convention and column indices following the big-endian convention.

Returns A state-by-state TPM, with both row and column indices following the big-endian convention.

Return type np.ndarray

```
>>> tpm = np.array([[1, 1, 0],
                     [0, 0, 1],
. . .
                     [0, 1, 1],
. . .
                     [1, 0, 0],
. . .
                     [0, 0, 1],
. . .
                     [1, 0, 0],
. . .
. . .
                     [1, 1, 1],
                     [1, 0, 1]])
. . .
>>> state_by_node2state_by_state(tpm)
array([[0., 0., 0., 1., 0., 0., 0.],
       [0., 0., 0., 0., 1., 0., 0., 0.],
       [0., 0., 0., 0., 0., 0., 1., 0.],
       [0., 1., 0., 0., 0., 0., 0., 0.],
       [0., 0., 0., 0., 1., 0., 0., 0.],
       [0., 1., 0., 0., 0., 0., 0., 0.],
       [0., 0., 0., 0., 0., 0., 0., 1.],
       [0., 0., 0., 0., 0., 1., 0., 0.]])
```

pyphi.convert.sbs2sbn(tpm)

Convert a state-by-state TPM to a state-by-node TPM.

Danger: Many nondeterministic state-by-state TPMs can be represented by a single a state-by-state TPM. However, the mapping can be made to be one-to-one if we assume the state-by-state TPM is conditionally independent, as this function does. **If the given TPM is not conditionally independent, the conditional dependencies will be silently lost.**

Note: The indices of the rows and columns of the state-by-state TPM are assumed to follow the little-endian convention. The indices of the rows of the resulting state-by-node TPM also follow the little-endian convention. See the documentation on PyPhi the *Transition probability matrix conventions* more information.

Parameters tpm (*list*[*list*] or *np.ndarray*) – A square state-by-state TPM with row and column indices following the little-endian convention.

Returns A state-by-node TPM, with row indices following the little-endian convention.

Return type np.ndarray

Example

```
>>> tpm = np.array([[0.5, 0.5, 0.0, 0.0],
... [0.0, 1.0, 0.0, 0.0],
... [0.0, 0.2, 0.0, 0.8],
... [0.0, 0.3, 0.7, 0.0]])
>>> state_by_state2state_by_node(tpm)
array([[[0.5, 0. ],
[1. , 0.8]],
[[1. , 0. ],
[0.3, 0.7]]])
```

1.32 direction

Causal directions.

```
class pyphi.direction.Direction
Constant that parametrizes cause and effect methods.
Accessed using Direction.CAUSE and Direction.EFFECT, etc.
CAUSE = 0
```

011002 0

EFFECT = 1

BIDIRECTIONAL = 2

1.33 distance

Functions for measuring distances.

```
class pyphi.distance.MeasureRegistry
Storage for measures registered with PyPhi.
```

Users can define custom measures:

Examples

```
>>> @measures.register('ALWAYS_ZERO')
... def always_zero(a, b):
... return 0
```

And use them by setting config.MEASURE = 'ALWAYS_ZERO'.

desc = 'measures'

register(name, asymmetric=False)

Decorator for registering a measure with PyPhi.

Parameters name (*string*) – The name of the measure.

Keyword Arguments asymmetric (boolean) – True if the measure is asymmetric.

asymmetric()

Return a list of asymmetric measures.

class pyphi.distance.np_suppress

Decorator to suppress NumPy warnings about divide-by-zero and multiplication of NaN.

Note: This should only be used in cases where you are *sure* that these warnings are not indicative of deeper issues in your code.

pyphi.distance.hamming_emd(d1, d2)

Return the Earth Mover's Distance between two distributions (indexed by state, one dimension per node) using the Hamming distance between states as the transportation cost function.

Singleton dimensions are sqeezed out.

pyphi.distance.effect_emd(d1, d2)

Compute the EMD between two effect repertoires.

Because the nodes are independent, the EMD between effect repertoires is equal to the sum of the EMDs between the marginal distributions of each node, and the EMD between marginal distribution for a node is the absolute difference in the probabilities that the node is OFF.

Parameters

- **d1** (*np*.*ndarray*) The first repertoire.
- **d2** (*np*.*ndarray*) The second repertoire.

Returns The EMD between d1 and d2.

Return type float

pyphi.distance.**l1**(*d1*, *d*2)

Return the L1 distance between two distributions.

Parameters

- **d1** (*np.ndarray*) The first distribution.
- **d2** (*np*.*ndarray*) The second distribution.

Returns The sum of absolute differences of d1 and d2.

Return type float

pyphi.distance.kld(d1, d2)

Return the Kullback-Leibler Divergence (KLD) between two distributions.

Parameters

- **d1** (*np.ndarray*) The first distribution.
- **d2** (*np.ndarray*) The second distribution.

Returns The KLD of d1 from d2.

Return type float

pyphi.distance.entropy_difference (d1, d2)Return the difference in entropy between two distributions.

pyphi.distance.**psq2**(d1,d2)

Compute the PSQ2 measure.

Parameters

- **d1** (*np.ndarray*) The first distribution.
- **d2** (*np.ndarray*) The second distribution.

pyphi.distance.mp2q(p, q)

Compute the MP2Q measure.

Parameters

- **p** (*np*.*ndarray*) The unpartitioned repertoire
- q (np.ndarray) The partitioned repertoire

pyphi.distance.bld(p,q)

Compute the Buzz Lightyear (Billy-Leo) Divergence.

```
pyphi.distance.directional_emd(direction, d1, d2)
```

Compute the EMD between two repertoires for a given direction.

The full EMD computation is used for cause repertoires. A fast analytic solution is used for effect repertoires.

Parameters

- direction (Direction) CAUSE or EFFECT.
- **d1** (*np.ndarray*) The first repertoire.
- **d2** (*np.ndarray*) The second repertoire.

Returns The EMD between d1 and d2, rounded to PRECISION.

Return type float

Raises ValueError - If direction is invalid.

pyphi.distance.repertoire_distance(direction, r1, r2)

Compute the distance between two repertoires for the given direction.

Parameters

- direction (Direction) CAUSE or EFFECT.
- **r1** (*np.ndarray*) The first repertoire.
- **r2** (*np.ndarray*) The second repertoire.

Returns The distance between d1 and d2, rounded to PRECISION.

Return type float

pyphi.distance.system_repertoire_distance(r1, r2)

Compute the distance between two repertoires of a system.

Parameters

- **r1** (*np.ndarray*) The first repertoire.
- **r2** (*np*.*ndarray*) The second repertoire.

Returns The distance between r1 and r2.

Return type float

1.34 distribution

Functions for manipulating probability distributions.

pyphi.distribution.normalize(a) Normalize a distribution.

Parameters a (*np*.*ndarray*) – The array to normalize.

Returns a normalized so that the sum of its entries is 1.

Return type np.ndarray

```
pyphi.distribution.uniform_distribution(number_of_nodes)
```

Return the uniform distribution for a set of binary nodes, indexed by state (so there is one dimension per node, the size of which is the number of possible states for that node).

Parameters nodes (*np*.*ndarray*) – A set of indices of binary nodes.

Returns The uniform distribution over the set of nodes.

Return type np.ndarray

```
pyphi.distribution.marginal (repertoire, node_index)
Get the marginal distribution for a node.
```

```
pyphi.distribution.independent (repertoire)
Check whether the repertoire is independent.
```

pyphi.distribution.purview(repertoire)
The second sec

The purview of the repertoire.

Parameters repertoire (*np.ndarray*) – A repertoire

Returns The purview that the repertoire was computed over.

Return type tuple[int]

pyphi.distribution.**purview_size** (*repertoire*) Return the size of the purview of the repertoire.

Parameters repertoire (*np.ndarray*) – A repertoire

Returns The size of purview that the repertoire was computed over.

Return type int

pyphi.distribution.repertoire_shape (purview, N)

Return the shape a repertoire.

Parameters

- **purview** (*tuple[int]*) The purview over which the repertoire is computed.
- **N** (*int*) The number of elements in the system.
- **Returns** The shape of the repertoire. Purview nodes have two dimensions and non-purview nodes are collapsed to a unitary dimension.

Return type list[int]

Example

```
>>> purview = (0, 2)
>>> N = 3
>>> repertoire_shape(purview, N)
[2, 1, 2]
```

pyphi.distribution.flatten (repertoire, big_endian=False)
Flatten a repertoire, removing empty dimensions.

By default, the flattened repertoire is returned in little-endian order.

Parameters repertoire (*np.ndarray* or *None*) – A repertoire.

Keyword Arguments big_endian (boolean) – If True, flatten the repertoire in big-endian order.

Returns The flattened repertoire.

Return type np.ndarray

pyphi.distribution.max_entropy_distribution (*node_indices, number_of_nodes*) Return the maximum entropy distribution over a set of nodes.

This is different from the network's uniform distribution because nodes outside node_indices are fixed and treated as if they have only 1 state.

Parameters

- **node_indices** (*tuple[int]*) The set of node indices over which to take the distribution.
- **number_of_nodes** (*int*) The total number of nodes in the network.

Returns The maximum entropy distribution over the set of nodes.

Return type np.ndarray

1.35 examples

Example networks and subsystems to go along with the documentation.

A 3-node network of logic gates.

Diagram:

TPM:

Previous state	Current state
A, B, C	A, B, C
0, 0, 0	0, 0, 0
1, 0, 0	0, 0, 1
0, 1, 0	1, 0, 1
1, 1, 0	1, 0, 0
0, 0, 1	1, 1, 0
1, 0, 1	1, 1, 1
0, 1, 1	1, 1, 1
1, 1, 1	1, 1, 0

Connectivity matrix:

•	Α	В	C
A	0	0	1
В	1	0	1
C	1	1	0

Note: $[CM]_{i,j} = 1$ means that there is a directed edge (i, j) from node *i* to node *j* and $[CM]_{i,j} = 0$ means there is no edge from *i* to *j*.

```
pyphi.examples.basic_state()
```

The state of nodes in *basic_network()*.

```
pyphi.examples.basic_subsystem()
```

A subsystem containing all the nodes of the *basic_network()*.

```
pyphi.examples.basic_noisy_selfloop_network()
```

Based on the basic_network, but with added selfloops and noisy edges.

Nodes perform deterministic functions of their inputs, but those inputs may be flipped (i.e. what should be a 0 becomes a 1, and vice versa) with probability epsilon (eps = 0.1 here).

Diagram:

```
+~~+
| v
+~~~~~+
+~~~~>| A |<~~~~+
| | (OR) +~~~+ |
```

```
+~~~~+ | |
                    v
   +~~~+~+
 + \sim + \sim \sim \sim \sim \sim \sim +
 B | <~~~~+ C |
+>| (COPY) +~~~~~>| (XOR) |<+
           +~~~~+
 +~~~~+
+~~~+
                      + \sim \sim \sim +
```

pyphi.examples.basic_noisy_selfloop_subsystem()

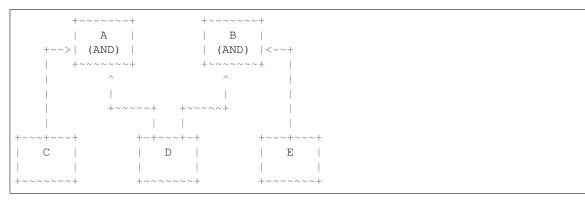
A subsystem containing all the nodes of the basic_noisy_selfloop_network().

```
pyphi.examples.residue_network()
```

The network for the residue example.

Current and previous state are all nodes OFF.

Diagram:



Connectivity matrix:

•	Α	В	С	D	E
A	0	0	0	0	0
В	0	0	0	0	0
С	1	0	0	0	0
D	1	1	0	0	0
E	0	1	0	0	0

pyphi.examples.residue_subsystem()

The subsystem containing all the nodes of the residue_network().

pyphi.examples.xor_network()

A fully connected system of three XOR gates. In the state (0, 0, 0), none of the elementary mechanisms exist.

Diagram:

```
+~~~~+ +~~~~+ B |
| (XOR) +~~~~~> | (XOR) |
+~+~~~+ +~~~+ +~~+
| ^ ^ ^ /
```

```
| | +~~~~+ | |
| +~~~+ C +~~~+ |
+~~~~>| (XOR) +<~~~+
+~~~~+
```

Connectivity matrix:

•	Α	В	C
A	0	1	1
В	1	0	1
С	1	1	0

pyphi.examples.xor_subsystem()

The subsystem containing all the nodes of the *xor_network()*.

pyphi.examples.cond_depend_tpm()

A system of two general logic gates A and B such if they are in the same state they stay the same, but if they are in different states, they flip with probability 50%.

Diagram:

```
+~~~~+ +~~~~+
| A |<~~~~~+ B |
| +~~~~~>| |
+~~~~+ +~~~~+
```

TPM:

	(0, 0)	(1, 0)	(0, 1)	(1, 1)
(0, 0)	1.0	0.0	0.0	0.0
(1, 0)	0.0	0.5	0.5	0.0
(0, 1)	0.0	0.5	0.5	0.0
(1, 1)	0.0	0.0	0.0	1.0

Connectivity matrix:

•	А	В
Α	0	1
В	1	0

pyphi.examples.cond_independ_tpm()

A system of three general logic gates A, B and C such that: if A and B are in the same state then they stay the same; if they are in different states, they flip if C is ON and stay the same if C is OFF; and C is ON 50% of the time, independent of the previous state.

Diagram:

```
+~~~~+ +~~~~+
| A +~~~~~>| B |
| |<~~~~~+ |
+~+~~+ +~~~+
| ^ ^ |
| +~~+~~+ |
```

```
| ~~~~+ C +~~~+ |
+~~~~>| | <~~~~+
```

TPM:

	(0, 0, 0)	(1, 0, 0)	(0, 1, 0)	(1, 1, 0)	(0, 0, 1)	(1, 0, 1)	(0, 1, 1)	(1, 1, 1)
(0, 0, 0)	0.5	0.0	0.0	0.0	0.5	0.0	0.0	0.0
(1, 0, 0)	0.0	0.5	0.0	0.0	0.0	0.5	0.0	0.0
(0, 1, 0)	0.0	0.0	0.5	0.0	0.0	0.0	0.5	0.0
(1, 1, 0)	0.0	0.0	0.0	0.5	0.0	0.0	0.0	0.5
(0, 0, 1)	0.5	0.0	0.0	0.0	0.5	0.0	0.0	0.0
(1, 0, 1)	0.0	0.0	0.5	0.0	0.0	0.0	0.5	0.0
(0, 1, 1)	0.0	0.5	0.0	0.0	0.0	0.5	0.0	0.0
(1, 1, 1)	0.0	0.0	0.0	0.5	0.0	0.0	0.0	0.5

Connectivity matrix:

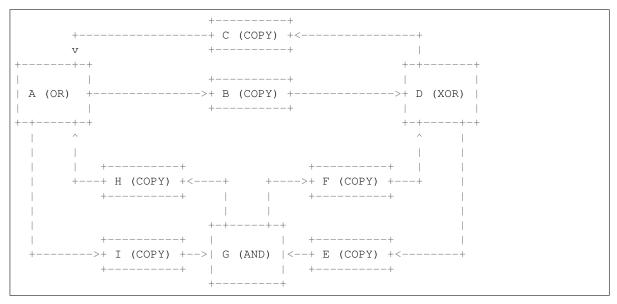
•	Α	В	С
A	0	1	0
В	1	0	0
С	1	1	0

pyphi.examples.propagation_delay_network()

A version of the primary example from the IIT 3.0 paper with deterministic COPY gates on each connection. These copy gates essentially function as propagation delays on the signal between OR, AND and XOR gates from the original system.

The current and previous states of the network are also selected to mimic the corresponding states from the IIT 3.0 paper.

Diagram:



Connectivity matrix:

•	Α	В	C	D	E	F	G	H	Ι
Α	0	1	0	0	0	0	0	0	1
В	0	0	0	1	0	0	0	0	0
C	1	0	0	0	0	0	0	0	0
D	0	0	1	0	1	0	0	0	0
E	0	0	0	0	0	0	1	0	0
F	0	0	0	1	0	0	0	0	0
G	0	0	0	0	0	1	0	1	0
Η	1	0	0	0	0	0	0	0	0
Ι	0	0	0	0	0	0	1	0	0

States:

In the IIT 3.0 paper example, the previous state of the system has only the XOR gate ON. For the propagation delay network, this corresponds to a state of (0, 0, 0, 1, 0, 0, 0, 0, 0).

The current state of the IIT 3.0 example has only the OR gate ON. By advancing the propagation delay system two time steps, the current state (1, 0, 0, 0, 0, 0, 0, 0, 0, 0) is achieved, with corresponding previous state (0, 0, 1, 0, 1, 0, 0, 0, 0, 0).

```
pyphi.examples.macro_network()
```

A network of micro elements which has greater integrated information after coarse graining to a macro scale.

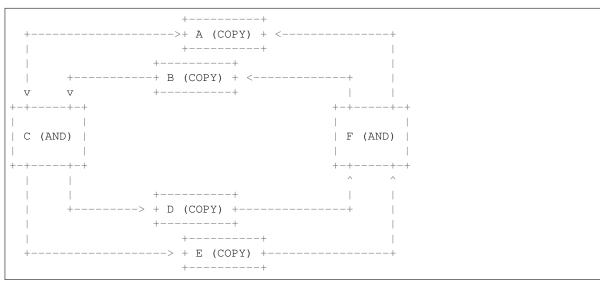
```
pyphi.examples.macro_subsystem()
```

A subsystem containing all the nodes of macro_network().

```
pyphi.examples.blackbox_network()
```

A micro-network to demonstrate blackboxing.

Diagram:



Connectivity Matrix:

•	А	В	C	D	E	F
Α	0	0	1	0	0	0
В	0	0	1	0	0	0
С	0	0	0	1	1	0
D	0	0	0	0	0	1
E	0	0	0	0	0	1
F	1	1	0	0	0	0

In the documentation example, the state is (0, 0, 0, 0, 0, 0).

pyphi.examples.rule110_network()

A network of three elements which follows the logic of the Rule 110 cellular automaton with current and previous state (0, 0, 0).

pyphi.examples.rule154_network()

A network of three elements which follows the logic of the Rule 154 cellular automaton.

```
pyphi.examples.figla()
```

The network shown in Figure 1A of the 2014 IIT 3.0 paper.

```
pyphi.examples.fig3a()
```

The network shown in Figure 3A of the 2014 IIT 3.0 paper.

```
pyphi.examples.fig3b()
```

The network shown in Figure 3B of the 2014 IIT 3.0 paper.

```
pyphi.examples.fig4()
```

The network shown in Figure 4 of the 2014 IIT 3.0 paper.

Diagram:

```
+~~~~+
+~~~~>| A |<~~~~+
| +~~~+ (OR) +~~~+
| | +~~~+ (OR) +~~~+
| | +~~~~+
| | v v v
+~+~~+
| B |<~~~~~+ C |
| (AND) +~~~~~>| (XOR) |
+~~~~~+
```

pyphi.examples.fig5a()

The network shown in Figure 5A of the 2014 IIT 3.0 paper.

Diagram:

```
+~~~~+
+~~~~> | A | <~~~~+
| | (AND) | |
| +~~~~~+ |
| | |
+~~+
| B | <~~~~+ C |
| (COPY) +~~~~> | (COPY) |
+~~~+ +~~~~+
```

pyphi.examples.fig5b()

The network shown in Figure 5B of the 2014 IIT 3.0 paper.

Diagram:

```
+----+
+---+
| (AND) | |
| +----+
v v
+----+
| B |<----+
C |
| (COPY) +----->
+---+
+---+
+---+
+----+
```

pyphi.examples.fig6()

The network shown in Figure 4 of the 2014 IIT 3.0 paper.

Diagram:

pyphi.examples.fig8()

The network shown in Figure 4 of the 2014 IIT 3.0 paper.

Diagram:

pyphi.examples.fig9()

The network shown in Figure 4 of the 2014 IIT 3.0 paper.

Diagram:

```
+~~~~+
+~~~~+
| +~~~+ (OR) +~~~+
| +~~~+ (OR) +~~~+
| | +~~~~+
| | +~~~~+
| v v |
+~+~~~+
| B |<~~~~+
C |
| (AND) +~~~~>
| (XOR) |
+~~~~+
```

pyphi.examples.fig10()

The network shown in Figure 4 of the 2014 IIT 3.0 paper.

Diagram:

```
pyphi.examples.fig14()
```

The network shown in Figure 1A of the 2014 IIT 3.0 paper.

```
pyphi.examples.fig16()
```

The network shown in Figure 5B of the 2014 IIT 3.0 paper.

```
pyphi.examples.actual_causation()
```

The actual causation example network, consisting of an OR and AND gate with self-loops.

```
pyphi.examples.disjunction_conjunction_network()
```

The disjunction-conjunction example from Actual Causation Figure 7.

A network of four elements, one output D with three inputs A B C. The output turns ON if A AND B are ON or if C is ON.

```
pyphi.examples.prevention()
```

The Transition for the prevention example from Actual Causation Figure 5D.

1.36 exceptions

PyPhi exceptions.

```
exception pyphi.exceptions.StateUnreachableError(state)
The current state cannot be reached from any previous state.
```

exception pyphi.exceptions.**ConditionallyDependentError** The TPM is conditionally dependent.

exception pyphi.exceptions.**JSONVersionError** JSON was serialized with a different version of PyPhi.

```
exception pyphi.exceptions.WrongDirectionError
The wrong direction was provided.
```

1.37 jsonify

PyPhi- and NumPy-aware JSON serialization.

To be properly serialized and deserialized, PyPhi objects must implement a to_json method which returns a dictionary of attribute names and attribute values. These attributes should be the names of arguments passed to the object constructor. If the constructor takes additional, fewer, or different arguments, the object needs to implement a custom

classmethod called from_json that takes a Python dictionary as an argument and returns a PyPhi object. For example:

```
class Phi:
    def __init__(self, phi):
        self.phi = phi
    def to_json(self):
        return {'phi': self.phi, 'twice_phi': 2 * self.phi}
    @classmethod
    def from_json(cls, json):
        return Phi(json['phi'])
```

The object must also be added to jsonify._loadable_models.

The JSON encoder adds the name of the object and the current PyPhi version to the JSON stream. The JSON decoder uses this metadata to recursively deserialize the stream to a nested PyPhi object structure. The decoder will raise an exception if current PyPhi version doesn't match the version in the JSON data.

pyphi.jsonify.jsonify(obj)

Return a JSON-encodable representation of an object, recursively using any available to_json methods, converting NumPy arrays and datatypes to native lists and types along the way.

class pyphi.jsonify.PyPhiJSONEncoder	(skipkeys=False,		ensure_ascii=True,
	allow_nan=True,		
	sort_keys=False,	indent=None,	separators=None,
	default=None)		
JSONEncoder that allows serializing PyPhi obje	cts with jsonify.		

Constructor for JSONEncoder, with sensible defaults.

If skipkeys is false, then it is a TypeError to attempt encoding of keys that are not str, int, float or None. If skipkeys is True, such items are simply skipped.

If ensure_ascii is true, the output is guaranteed to be str objects with all incoming non-ASCII characters escaped. If ensure_ascii is false, the output can contain non-ASCII characters.

If check_circular is true, then lists, dicts, and custom encoded objects will be checked for circular references during encoding to prevent an infinite recursion (which would cause an OverflowError). Otherwise, no such check takes place.

If allow_nan is true, then NaN, Infinity, and -Infinity will be encoded as such. This behavior is not JSON specification compliant, but is consistent with most JavaScript based encoders and decoders. Otherwise, it will be a ValueError to encode such floats.

If sort_keys is true, then the output of dictionaries will be sorted by key; this is useful for regression tests to ensure that JSON serializations can be compared on a day-to-day basis.

If indent is a non-negative integer, then JSON array elements and object members will be pretty-printed with that indent level. An indent level of 0 will only insert newlines. None is the most compact representation.

If specified, separators should be an (item_separator, key_separator) tuple. The default is (`, `, `: `) if *indent* is None and (`, `, `: `) otherwise. To get the most compact JSON representation, you should specify (`, `, `:`) to eliminate whitespace.

If specified, default is a function that gets called for objects that can't otherwise be serialized. It should return a JSON encodable version of the object or raise a TypeError.

encode (*obj*)

Encode the output of jsonify with the default encoder.

iterencode (*obj*, ***kwargs*) Analog to *encode* used by json.dump.

- pyphi.jsonify.**dumps** (*obj*, **user_kwargs) Serialize obj as JSON-formatted stream.
- pyphi.jsonify.dump(obj, fp, **user_kwargs)
 Serialize obj as a JSON-formatted stream and write to fp (a .write()-supporting file-like object.
- **class** pyphi.jsonify.**PyPhiJSONDecoder** (**args*, ***kwargs*) Extension of the default encoder which automatically deserializes PyPhi JSON to the appropriate model classes.
- pyphi.jsonify.loads (*string*) Deserialize a JSON string to a Python object.

pyphi.jsonify.load (*fp*) Deserialize a JSON stream to a Python object.

1.38 macro

Methods for coarse-graining systems to different levels of spatial analysis.

```
pyphi.macro.reindex (indices)
Generate a new set of node indices, the size of indices.
```

```
pyphi.macro.remove_singleton_dimensions (tpm)
Remove singleton dimensions from the TPM.
```

Singleton dimensions are created by conditioning on a set of elements. This removes those elements from the TPM, leaving a TPM that only describes the non-conditioned elements.

Note that indices used in the original TPM must be reindexed for the smaller TPM.

```
pyphi.macro.run_tpm (system, steps, blackbox)
Iterate the TPM for the given number of timesteps.
```

Returns tpm * (noise_tpm^(t-1))

Return type np.ndarray

class pyphi.macro.SystemAttrs

An immutable container that holds all the attributes of a subsystem.

Versions of this object are passed down the steps of the micro-to-macro pipeline.

Create new instance of SystemAttrs(tpm, cm, node_indices, state)

node_labels

Return the labels for macro nodes.

nodes

static pack(system)

apply (system)

A subclass of *Subsystem* implementing macro computations.

This subsystem performs blackboxing and coarse-graining of elements.

Unlike *Subsystem*, whose TPM has dimensionality equal to that of the subsystem's network and represents nodes external to the system using singleton dimensions, *MacroSubsystem* squeezes the TPM to remove these singletons. As a result, the node indices of the system are also squeezed to 0...n so they properly index the TPM, and the state-tuple is reduced to the size of the system.

After each macro update (temporal blackboxing, spatial blackboxing, and spatial coarse-graining) the TPM, CM, nodes, and state are updated so that they correctly represent the updated system.

cut_indices

The indices of this system to be cut for Φ computations.

For macro computations the cut is applied to the underlying micro-system.

cut_mechanisms

The mechanisms of this system that are currently cut.

Note that although cut_indices returns micro indices, this returns macro mechanisms.

Yields tuple[int]

cut_node_labels

Labels for the nodes that can be cut.

These are the labels of the micro elements.

apply_cut (cut)

Return a cut version of this MacroSubsystem.

Parameters cut (Cut) – The cut to apply to this *MacroSubsystem*.

Returns The cut version of this MacroSubsystem.

Return type MacroSubsystem

potential_purviews (direction, mechanism, purviews=False)

Override Subsystem implementation using Network-level indices.

macro2micro(macro_indices)

Return all micro indices which compose the elements specified by macro_indices.

macro2blackbox_outputs (macro_indices)

Given a set of macro elements, return the blackbox output elements which compose these elements.

__eq__(other)

Two macro systems are equal if each underlying Subsystem is equal and all macro attributes are equal.

class pyphi.macro.CoarseGrain

Represents a coarse graining of a collection of nodes.

partition

tuple[tuple] – The partition of micro-elements into macro-elements.

grouping

tuple[tuple[tuple]] – The grouping of micro-states into macro-states.

Create new instance of CoarseGrain(partition, grouping)

micro_indices

Indices of micro elements represented in this coarse-graining.

macro_indices

Indices of macro elements of this coarse-graining.

reindex()

Re-index this coarse graining to use squeezed indices.

The output grouping is translated to use indices $0 \dots n$, where n is the number of micro indices in the coarse-graining. Re-indexing does not effect the state grouping, which is already index-independent.

Returns A new CoarseGrain object, indexed from 0...n.

Return type CoarseGrain

Example

```
>>> partition = ((1, 2),)
>>> grouping = (((0,), (1, 2)),)
>>> coarse_grain = CoarseGrain(partition, grouping)
>>> coarse_grain.reindex()
CoarseGrain(partition=((0, 1),), grouping=(((0,), (1, 2)),))
```

macro_state (micro_state)

Translate a micro state to a macro state

Parameters micro_state (*tuple[int]*) – The state of the micro nodes in this coarsegraining.

Returns The state of the macro system, translated as specified by this coarse-graining.

Return type tuple[int]

Example

```
>>> coarse_grain = CoarseGrain(((1, 2),), (((0,), (1, 2)),))
>>> coarse_grain.macro_state((0, 0))
(0,)
>>> coarse_grain.macro_state((1, 0))
(1,)
>>> coarse_grain.macro_state((1, 1))
(1,)
```

make_mapping()

Return a mapping from micro-state to the macro-states based on the partition and state grouping of this coarse-grain.

Returns A mapping from micro-states to macro-states. The i^{th} entry in the mapping is the macro-state corresponding to the i^{th} micro-state.

```
Return type (nd.ndarray)
```

```
macro_tpm_sbs(state_by_state_micro_tpm)
```

Create a state-by-state coarse-grained macro TPM.

Parameters micro_tpm(*nd.array*) – The state-by-state TPM of the micro-system.

Returns The state-by-state TPM of the macro-system.

Return type np.ndarray

```
macro_tpm (micro_tpm, check_independence=True)
Create a coarse-grained macro TPM.
```

Parameters

- micro_tpm (nd.array) The TPM of the micro-system.
- **check_independence** (*bool*) Whether to check that the macro TPM is conditionally independent.

Raises ConditionallyDependentError – If check_independence is True and the macro TPM is not conditionally independent.

Returns The state-by-node TPM of the macro-system.

Return type np.ndarray

class pyphi.macro.Blackbox

Class representing a blackboxing of a system.

partition

tuple[tuple[int]] – The partition of nodes into boxes.

output_indices

tuple[int] - Outputs of the blackboxes.

Create new instance of Blackbox(partition, output_indices)

hidden_indices

All elements hidden inside the blackboxes.

micro_indices

Indices of micro-elements in this blackboxing.

macro_indices

Fresh indices of macro-elements of the blackboxing.

outputs_of (partition_index)

The outputs of the partition at partition_index.

Note that this returns a tuple of element indices, since coarse- grained blackboxes may have multiple outputs.

reindex()

Squeeze the indices of this blackboxing to 0..n.

Returns a new, reindexed *Blackbox*.

Return type Blackbox

Example

```
>>> partition = ((3,), (2, 4))
>>> output_indices = (2, 3)
>>> blackbox = Blackbox(partition, output_indices)
>>> blackbox.reindex()
Blackbox(partition=((1,), (0, 2)), output_indices=(0, 1))
```

macro_state (micro_state)

Compute the macro-state of this blackbox.

This is just the state of the blackbox's output indices.

```
Parameters micro_state (tuple[int]) – The state of the micro-elements in the blackbox.
```

Returns The state of the output indices.

Return type tuple[int]

in_same_box (*a*, *b*) Return True if nodes a and b` are in the same box.

hidden_from (a, b)Return True if a is hidden in a different box than b.

pyphi.macro.all_partitions (indices)

Return a list of all possible coarse grains of a network.

Parameters indices (*tuple[int]*) – The micro indices to partition.

Yields *tuple[tuple]* – A possible partition. Each element of the tuple is a tuple of micro-elements which correspond to macro-elements.

pyphi.macro.all_groupings (partition)

Return all possible groupings of states for a particular coarse graining (partition) of a network.

Parameters partition (tuple[tuple]) - A partition of micro-elements into macro elements.

Yields tuple[tuple]] - A grouping of micro-states into macro states of system.

TODO: document exactly how to interpret the grouping.

pyphi.macro.all_coarse_grains(indices)

Generator over all possible CoarseGrain of these indices.

Parameters indices (*tuple[int]*) – Node indices to coarse grain.

Yields CoarseGrain – The next CoarseGrain for indices.

pyphi.macro.all_coarse_grains_for_blackbox(blackbox)

Generator over all *CoarseGrain* for the given blackbox.

If a box has multiple outputs, those outputs are partitioned into the same coarse-grain macro-element.

pyphi.macro.all_blackboxes(indices)

Generator over all possible blackboxings of these indices.

Parameters indices (tuple[int]) – Nodes to blackbox.

Yields *Blackbox* – The next *Blackbox* of indices.

A coarse-grained network of nodes.

See the *Emergence* (coarse-graining and blackboxing) example in the documentation for more information.

network

Network - The network object of the macro-system.

phi

float – The Φ of the network's major complex.

micro_network

Network - The network object of the corresponding micro system.

micro_phi

float – The Φ of the major complex of the corresponding micro-system.

coarse_grain

CoarseGrain - The coarse-graining of micro-elements into macro-elements.

time_scale

int - The time scale the macro-network run over.

blackbox

Blackbox – The blackboxing of micro elements in the network.

emergence

float – The difference between the Φ of the macro- and the micro-system.

emergence

Difference between the Φ of the macro and micro systems

pyphi.macro.coarse_graining(network, state, internal_indices)

Find the maximal coarse-graining of a micro-system.

Parameters

- **network** (Network) The network in question.
- **state** (*tuple[int]*) The state of the network.
- **internal_indices** (*tuple[int]*) Nodes in the micro-system.

Returns The phi-value of the maximal *CoarseGrain*.

Return type tuple[int, *CoarseGrain*]

Generator over all possible macro-systems for the network.

pyphi.macro.emergence (network, state, do_blackbox=False, do_coarse_grain=True, time_scales=None)

Check for the emergence of a micro-system into a macro-system.

Checks all possible blackboxings and coarse-grainings of a system to find the spatial scale with maximum integrated information.

Use the do_blackbox and do_coarse_grain args to specify whether to use blackboxing, coarse-graining, or both. The default is to just coarse-grain the system.

Parameters

- **network** (Network) The network of the micro-system under investigation.
- **state** (*tuple[int]*) The state of the network.
- **do_blackbox** (*bool*) Set to True to enable blackboxing. Defaults to False.
- do_coarse_grain (bool) Set to True to enable coarse-graining. Defaults to True.
- time_scales (list[int]) List of all time steps over which to check for emergence.

Returns The maximal macro-system generated from the micro-system.

Return type MacroNetwork

pyphi.macro.phi_by_grain(network, state)

pyphi.macro.effective_info(network)

Return the effective information of the given network.

Note: For details, see:

Hoel, Erik P., Larissa Albantakis, and Giulio Tononi. "Quantifying causal emergence shows that macro can beat micro." Proceedings of the National Academy of Sciences 110.49 (2013): 19790-19795.

Available online: doi: 10.1073/pnas.1314922110.

1.39 models

See pyphi.models.subsystem, pyphi.models.mechanism, and pyphi.models.cuts for documen- tation.
<pre>pyphi.models.Account Alias for pyphi.models.actual_causation.Account.</pre>
<pre>pyphi.models.AcRepertoireIrreducibilityAnalysis Alias for pyphi.models.actual_causation.AcRepertoireIrreducibilityAnalysis.</pre>
<pre>pyphi.models.AcSystemIrreducibilityAnalysis Alias for pyphi.models.actual_causation.AcSystemIrreducibilityAnalysis.</pre>
<pre>pyphi.models.ActualCut Alias for pyphi.models.cuts.ActualCut.</pre>
<pre>pyphi.models.Bipartition Alias for pyphi.models.cuts.Bipartition.</pre>
<pre>pyphi.models.CausalLink Alias for pyphi.models.actual_causation.CausalLink.</pre>
<pre>pyphi.models.CauseEffectStructure Alias for pyphi.models.subsystem.CauseEffectStructure.</pre>
<pre>pyphi.models.Concept Alias for pyphi.models.mechanism.Concept.</pre>
<pre>pyphi.models.Cut Alias for pyphi.models.cuts.Cut.</pre>
<pre>pyphi.models.DirectedAccount Alias for pyphi.models.actual_causation.DirectedAccount.</pre>
pyphi.models. MaximallyIrreducibleCause Alias for pyphi.models.mechanism.MaximallyIrreducibleCause.
<pre>pyphi.models.MaximallyIrreducibleEffect Alias for pyphi.models.mechanism.MaximallyIrreducibleEffect.</pre>
<pre>pyphi.models.MaximallyIrreducibleCauseOrEffect Alias for pyphi.models.mechanism.MaximallyIrreducibleCauseOrEffect.</pre>
pyphi.models. Part Alias for pyphi.models.cuts.Part.
<pre>pyphi.models.RepertoireIrreducibilityAnalysis Alias for pyphi.models.mechanism.RepertoireIrreducibilityAnalysis.</pre>
<pre>pyphi.models.SystemIrreducibilityAnalysis Alias for pyphi.models.subsystem.SystemIrreducibilityAnalysis.</pre>

$1.40 \ {\tt models.actual_causation}$

Objects that represent structures used in actual causation.

pyphi.models.actual_causation.greater_than_zero (*alpha*) Return True if alpha is greater than zero, accounting for numerical errors.

class pyphi.models.actual_causation.AcRepertoireIrreducibilityAnalysis	(alpha,
	state,
	di-
	rec-
	tion,
	mech-
	<i>a</i> -
	nism,
	purview,
	par-
	ti-
	tion,
	prob-
	<i>a</i> -
	bil-
	ity,
	par-
	ti-
	tioned_probability,
	node_labels=None)
A minimum information partition for ac_coef calculation.	

These can be compared with the built-in Python comparison operators (<, >, etc.). First, α values are compared. Then, if these are equal up to PRECISION, the size of the mechanism is compared.

alpha

float – This is the difference between the mechanism's unpartitioned and partitioned actual probability.

state

tuple[int] - state of system in specified direction (cause, effect)

direction

str – The temporal direction specifying whether this analysis should be calculated with cause or effect repertoires.

mechanism

tuple[int] – The mechanism to analyze.

purview

tuple[int] – The purview over which the unpartitioned actual probability differs the least from the actual probability of the partition.

partition

tuple[Part, Part] - The partition that makes the least difference to the mechanism's repertoire.

probability

float - The probability of the state in the previous/next timestep.

partitioned_probability

float - The probability of the state in the partitioned repertoire.

unorderable_unless_eq = ['direction']

order_by()

Return a list of values to compare for ordering.

The first value in the list has the greatest priority; if the first objects are equal the second object is compared, etc.

```
__bool__()
An AcRepertoireIrreducibilityAnalysis is True if it has <math>\alpha > 0.
```

phi

Alias for α for PyPhi utility functions.

to_json()

Return a JSON-serializable representation.

class pyphi.models.actual_causation.CausalLink(ria)

A maximally irreducible actual cause or effect.

These can be compared with the built-in Python comparison operators (<, >, etc.). First, α values are compared. Then, if these are equal up to PRECISION, the size of the mechanism is compared.

alpha

float – The difference between the mechanism's unpartitioned and partitioned actual probabilities.

phi

Alias for α for PyPhi utility functions.

direction

Direction – Either CAUSE or EFFECT.

mechanism

list[int] – The mechanism for which the action is evaluated.

purview

list[int] – The purview over which this mechanism's α is maximal.

ria

AcRepertoireIrreducibilityAnalysis – The irreducibility analysis for this mechanism.

node_labels

unorderable_unless_eq = ['direction']

order_by()

Return a list of values to compare for ordering.

The first value in the list has the greatest priority; if the first objects are equal the second object is compared, etc.

__bool__()

An CausalLink is True if $\alpha > 0$.

to_json()

Return a JSON-serializable representation.

class pyphi.models.actual_causation.Event

A mechanism which has both an actual cause and an actual effect.

actual_cause

CausalLink - The actual cause of the mechanism.

actual_effect

CausalLink – The actual effect of the mechanism.

Create new instance of Event(actual_cause, actual_effect)

mechanism

The mechanism of the event.

class pyphi.models.actual_causation.Account(causal_links)

The set of *CausalLink* with $\alpha > 0$. This includes both actual causes and actual effects.

irreducible_causes

The set of irreducible causes in this Account.

irreducible_effects

The set of irreducible effects in this Account.

to_json()

classmethod from_json(dct)

class pyphi.models.actual_causation.**DirectedAccount** (*causal_links*) The set of *CausalLink* with $\alpha > 0$ for one direction of a transition.

class pyphi.models.actual_causation.AcSystemIrreducibilityAnalysis(alpha=None,

direction=None, account=None, partitioned_account=None, transition=None, cut=None)

An analysis of transition-level irreducibility (\mathcal{A}) .

Contains the A value of the *Transition*, the causal account, and all the intermediate results obtained in the course of computing them.

alpha

float – The A value for the transition when taken against this analysis, *i.e.* the difference between the unpartitioned account and this analysis's partitioned account.

account

Account - The account of the whole transition.

partitioned_account

Account – The account of the partitioned transition.

transition

Transition – The transition this analysis was calculated for.

\mathtt{cut}

ActualCut – The minimal partition.

before_state

Return the actual previous state of the *Transition*.

after_state

Return the actual current state of the Transition.

unorderable_unless_eq = ['direction']

order_by()

Return a list of values to compare for ordering.

The first value in the list has the greatest priority; if the first objects are equal the second object is compared, etc.

__bool__()

An AcSystemIrreducibilityAnalysis is True if it has $\mathcal{A} > 0$.

to_json()

1.41 models.cuts

Objects that represent partitions of sets of nodes.

```
class pyphi.models.cuts.NullCut (indices, node_labels=None)
```

The cut that does nothing.

is_null

This is the only cut where is_null == True.

indices

Indices of the cut.

cut_matrix (*n*) Return a matrix of zeros.

to_json()

class pyphi.models.cuts.**Cut** (*from_nodes*, *to_nodes*, *node_labels=None*) Represents a unidirectional cut.

from_nodes

tuple[int] – Connections from this group of nodes to those in to_nodes are from_nodes.

to_nodes

tuple[int] – Connections to this group of nodes from those in from_nodes are from_nodes.

from_nodes

to_nodes

node_labels

indices

Indices of this cut.

cut_matrix(n)

Compute the cut matrix for this cut.

The cut matrix is a square matrix which represents connections severed by the cut.

Parameters n (*int*) – The size of the network.

Example

to_json()

Return a JSON-serializable representation.

class pyphi.models.cuts.**KCut** (*direction*, *partition*, *node_labels=None*) A cut that severs all connections between parts of a K-partition.

indices

Indices of this cut.

cut_matrix(n)

The matrix of connections that are severed by this cut.

to_json()

```
class pyphi.models.cuts.ActualCut (direction, partition, node_labels=None)
Represents an cut for a Transition.
```

indices

Indices of this cut.

class pyphi.models.cuts.Part

Represents one part of a *Bipartition*.

mechanism

tuple[int] – The nodes in the mechanism for this part.

purview

tuple[int] – The nodes in the mechanism for this part.

Example

When calculating φ of a 3-node subsystem, we partition the system in the following way:

mechanism: A,C B _________ purview: B A,C

This class represents one term in the above product.

Create new instance of Part(mechanism, purview)

```
to_json()
```

Return a JSON-serializable representation.

class pyphi.models.cuts.**KPartition**(**parts*, *node_labels=None*) A partition with an arbitrary number of parts.

parts

node_labels

mechanism

tuple[int] – The nodes of the mechanism in the partition.

purview

tuple[int] – The nodes of the purview in the partition.

normalize()

Normalize the order of parts in the partition.

to_json()

classmethod from_json(dct)

class pyphi.models.cuts.**Bipartition** (**parts*, *node_labels=None*) A bipartition of a mechanism and purview.

part0

Part – The first part of the partition.

part1

Part – The second part of the partition.

to_json() Return a JSON-serializable representation.

classmethod from_json(dct)

node_labels

parts

class pyphi.models.cuts.**Tripartition**(**parts*, *node_labels=None*) A partition with three parts.

node_labels

parts

1.42 models.mechanism

Mechanism-level objects.

class pyphi.models.mechanism.RepertoireIrreducibilityAnalys	is(phi, a	lirection,	
	mechanis	mechanism,	
	purview,	par-	
	tition,	reper-	
	toire,	parti-	
	tioned_re	pertoire,	
		node_labels=None)	
An analysis of the irreducibility (φ) of a mechanism over a purview, for a given	n partition, ir	one temporal	
direction.			

These can be compared with the built-in Python comparison operators (<, >, etc.). First, φ values are compared. Then, if these are equal up to PRECISION, the size of the mechanism is compared (see the

phi

float – This is the difference between the mechanism's unpartitioned and partitioned repertoires.

direction

Direction – *CAUSE* or *EFFECT*.

PICK_SMALLEST_PURVIEW option in config.)

mechanism

tuple[int] – The mechanism that was analyzed.

purview

tuple[int] – The purview over which the mechanism was analyzed.

partition

KPartition – The partition of the mechanism-purview pair that was analyzed.

repertoire

np.ndarray - The repertoire of the mechanism over the purview.

partitioned_repertoire

np.ndarray – The partitioned repertoire of the mechanism over the purview. This is the product of the repertoires of each part of the partition.

node_labels

NodeLabels for this system.

unorderable_unless_eq = ['direction']

order_by()

Return a list of values to compare for ordering.

The first value in the list has the greatest priority; if the first objects are equal the second object is compared, etc.

```
__bool__()
```

```
A RepertoireIrreducibilityAnalysis is True if it has \varphi > 0.
```

to_json()

class pyphi.models.mechanism.**MaximallyIrreducibleCauseOrEffect** (*ria*) A maximally irreducible cause or effect (MICE).

These can be compared with the built-in Python comparison operators (<, >, etc.). First, φ values are compared. Then, if these are equal up to PRECISION, the size of the mechanism is compared (see the PICK_SMALLEST_PURVIEW option in config.)

phi

float - The difference between the mechanism's unpartitioned and partitioned repertoires.

direction

Direction – *CAUSE* or *EFFECT*.

mechanism

list[int] – The mechanism for which the MICE is evaluated.

purview

list[int] – The purview over which this mechanism's φ is maximal.

mip

KPartition – The partition that makes the least difference to the mechanism's repertoire.

repertoire

np.ndarray - The unpartitioned repertoire of the mechanism over the purview.

partitioned_repertoire

np.ndarray – The partitioned repertoire of the mechanism over the purview.

ria

RepertoireIrreducibilityAnalysis - The irreducibility analysis for this mechanism.

unorderable_unless_eq = ['direction']

order_by()

Return a list of values to compare for ordering.

The first value in the list has the greatest priority; if the first objects are equal the second object is compared, etc.

to_json()

damaged_by_cut (subsystem)

Return True if this MICE is affected by the subsystem's cut.

The cut affects the MICE if it either splits the MICE's mechanism or splits the connections between the purview and mechanism.

class pyphi.models.mechanism.**MaximallyIrreducibleCause** (*ria*) A maximally irreducible cause (MIC).

These can be compared with the built-in Python comparison operators (<, >, etc.). First, φ values are compared. Then, if these are equal up to PRECISION, the size of the mechanism is compared (see the PICK_SMALLEST_PURVIEW option in config.)

direction

Direction – CAUSE.

class pyphi.models.mechanism.**MaximallyIrreducibleEffect** (*ria*) A maximally irreducible effect (MIE).

These can be compared with the built-in Python comparison operators (<, >, etc.). First, φ values are compared. Then, if these are equal up to PRECISION, the size of the mechanism is compared (see the PICK_SMALLEST_PURVIEW option in config.)

direction

Direction – EFFECT.

class pyphi.models.mechanism.Concept (mechanism=None, cause=None, effect=None, subsys-

tem=None, *time=None*)

The maximally irreducible cause and effect specified by a mechanism.

These can be compared with the built-in Python comparison operators (<, >, etc.). First, φ values are compared. Then, if these are equal up to PRECISION, the size of the mechanism is compared.

mechanism

tuple[int] – The mechanism that the concept consists of.

cause

MaximallyIrreducibleCause – The *MaximallyIrreducibleCause* representing the maximallyirreducible cause of this concept.

effect

MaximallyIrreducibleEffect – The *MaximallyIrreducibleEffect* representing the maximallyirreducible effect of this concept.

subsystem

Subsystem – This concept's parent subsystem.

time

float – The number of seconds it took to calculate.

phi

float – The size of the concept.

This is the minimum of the φ values of the concept's MaximallyIrreducibleCause and MaximallyIrreducibleEffect.

cause_purview

tuple[int] – The cause purview.

effect_purview

tuple[int] – The effect purview.

cause_repertoire

np.ndarray – The cause repertoire.

effect_repertoire

np.ndarray – The effect repertoire.

mechanism_state

tuple(int) – The state of this mechanism.

unorderable_unless_eq = ['subsystem']

order_by()

Return a list of values to compare for ordering.

The first value in the list has the greatest priority; if the first objects are equal the second object is compared, etc.

```
__bool__()
```

A concept is True if $\varphi > 0$.

```
eq_repertoires(other)
```

Return whether this concept has the same repertoires as another.

Warning: This only checks if the cause and effect repertoires are equal as arrays; mechanisms, purviews, or even the nodes that the mechanism and purview indices refer to, might be different.

```
emd_eq(other)
```

Return whether this concept is equal to another in the context of an EMD calculation.

```
expand_cause_repertoire (new_purview=None)
See expand_repertoire ().
```

expand_effect_repertoire (new_purview=None)
See expand repertoire().

```
expand_partitioned_cause_repertoire()
    See expand_repertoire().
```

```
expand_partitioned_effect_repertoire()
```

See expand_repertoire().

```
to_json()
```

Return a JSON-serializable representation.

classmethod from_json(dct)

1.43 models.subsystem

Subsystem-level objects.

```
class pyphi.models.subsystem.CauseEffectStructure(concepts=(), subsystem=None,
```

time=None)

A collection of concepts.

order_by()

Return a list of values to compare for ordering.

The first value in the list has the greatest priority; if the first objects are equal the second object is compared, etc.

to_json()

mechanisms

The mechanism of each concept.

phis

The φ values of each concept.

labeled_mechanisms

The labeled mechanism of each concept.

An analysis of system irreducibility (Φ).

Contains the Φ value of the *Subsystem*, the cause-effect structure, and all the intermediate results obtained in the course of computing them.

These can be compared with the built-in Python comparison operators (<, >, etc.). First, Φ values are compared. Then, if these are equal up to PRECISION, the one with the larger subsystem is greater.

phi

float – The Φ value for the subsystem when taken against this analysis, *i.e.* the difference between the cause-effect structure and the partitioned cause-effect structure for this analysis.

ces

CauseEffectStructure – The cause-effect structure of the whole subsystem.

partitioned_ces

CauseEffectStructure - The cause-effect structure when the subsystem is cut.

subsystem

Subsystem – The subsystem this analysis was calculated for.

cut_subsystem

Subsystem – The subsystem with the minimal cut applied.

time

float - The number of seconds it took to calculate.

print (ces=True)

Print this SystemIrreducibilityAnalysis, optionally without cause-effect structures.

small_phi_time

The number of seconds it took to calculate the CES.

cut

The unidirectional cut that makes the least difference to the subsystem.

network

The network the subsystem belongs to.

unorderable_unless_eq = ['network']

order_by()

Return a list of values to compare for ordering.

The first value in the list has the greatest priority; if the first objects are equal the second object is compared, etc.

__bool__()

A SystemIrreducibilityAnalysis is True if it has $\Phi > 0$.

to_json()

Return a JSON-serializable representation.

classmethod from_json(dct)

1.44 network

Represents the network of interest. This is the primary object of PyPhi and the context of all φ and Φ computation.

class pyphi.network.Network(tpm, cm=None, node_labels=None, purview_cache=None)
 A network of nodes.

Represents the network under analysis and holds auxilary data about it.

Parameters tpm (*np*.*ndarray*) – The transition probability matrix of the network.

The TPM can be provided in any of three forms: **state-by-state**, **state-by-node**, or **multidimensional state-by-node** form. In the state-by-node forms, row indices must follow the little-endian convention (see *Little-endian convention*). In state-by-state form, column indices must also follow the little-endian convention.

If the TPM is given in state-by-node form, it can be either 2-dimensional, so that tpm[i] gives the probabilities of each node being ON if the previous state is encoded by *i* according to the little-endian convention, or in multidimensional form, so that tpm[(0, 0, 1)] gives the probabilities of each node being ON if the previous state is $N_0 = 0, N_1 = 0, N_2 = 1$.

The shape of the 2-dimensional form of a state-by-node TPM must be (s, n), and the shape of the multidimensional form of the TPM must be [2] * n + [n], where s is the number of states and n is the number of nodes in the network.

Keyword Arguments

- cm (np.ndarray) A square binary adjacency matrix indicating the connections between nodes in the network. cm[i][j] == 1 means that node *i* is connected to node *j* (see *Connectivity matrix conventions*). If no connectivity matrix is given, PyPhi assumes that every node is connected to every node (including itself).
- **node_labels** (tuple[str] or NodeLabels) Human-readable labels for each node in the network.

Example

In a 3-node network, the_network.tpm[(0, 0, 1)] gives the transition probabilities for each node at t given that state at t - 1 was $N_0 = 0$, $N_1 = 0$, $N_2 = 1$.

tpm

np.ndarray - The network's transition probability matrix, in multidimensional form.

cm

np.ndarray – The network's connectivity matrix.

A square binary adjacency matrix indicating the connections between nodes in the network.

connectivity_matrix

np.ndarray - Alias for cm.

causally_significant_nodes

See pyphi.connectivity.causally_significant_nodes().

size

int – The number of nodes in the network.

num_states

int – The number of possible states of the network.

node_indices

tuple[int] – The indices of nodes in the network.

This is equivalent to tuple (range (network.size)).

node_labels

tuple[str] – The labels of nodes in the network.

potential_purviews (direction, mechanism)

All purviews which are not clearly reducible for mechanism.

Parameters

- direction (Direction) CAUSE or EFFECT.
- mechanism (tuple[int]) The mechanism which all purviews are checked for reducibility over.

Returns All purviews which are irreducible over mechanism.

Return type list[tuple[int]]

__len_()

int: The number of nodes in the network.

__eq__(other)

Return whether this network equals the other object.

Networks are equal if they have the same TPM and CM.

to_json()

Return a JSON-serializable representation.

classmethod from_json(json_dict)

Return a *Network* object from a JSON dictionary representation.

pyphi.network.irreducible_purviews (*cm*, *direction*, *mechanism*, *purviews*) Return all purviews which are irreducible for the mechanism.

Parameters

- **cm** (np.ndarray) An $N \times N$ connectivity matrix.
- direction (Direction) CAUSE or EFFECT.
- **purviews** (*list*[*tuple*[*int*]]) The purviews to check.
- **mechanism** (*tuple[int]*) The mechanism in question.

Returns All purviews in purviews which are not reducible over mechanism.

Return type list[tuple[int]]

Raises ValueError – If direction is invalid.

pyphi.network.from_json(filename)

Convert a JSON network to a PyPhi network.

Parameters filename (*str*) – A path to a JSON file representing a network.

Returns The corresponding PyPhi network object.

Return type Network

1.45 node

Represents a node in a network. Each node has a unique index, its position in the network's list of nodes.

class pyphi.node.Node(tpm, cm, index, state, node_labels)

A node in a subsystem.

Parameters

- tpm (*np*.ndarray) The TPM of the subsystem.
- **cm** (*np*.*ndarray*) The CM of the subsystem.
- **index** (*int*) The node's index in the network.
- **state** (*int*) The state of this node.
- node_labels (NodeLabels) Labels for these nodes.

tpm

np.ndarray – The node TPM is a 2^(n_inputs)-by-2 matrix, where node.tpm[i][j] gives the marginal probability that the node is in state j at t+1 if the state of its inputs is i at t. If the node is a single element with a cut selfloop, (i.e. it has no inputs), the tpm is simply its unconstrained effect repertoire.

tpm_off

The TPM of this node containing only the 'OFF' probabilities.

tpm_on

The TPM of this node containing only the 'ON' probabilities.

inputs

The set of nodes with connections to this node.

outputs

The set of nodes this node has connections to.

label

The textual label for this node.

__eq__(other)

Return whether this node equals the other object.

Two nodes are equal if they belong to the same subsystem and have the same index (their TPMs must be the same in that case, so this method doesn't need to check TPM equality).

Labels are for display only, so two equal nodes may have different labels.

to_json()

Return a JSON-serializable representation.

pyphi.node.generate_nodes(tpm, cm, network_state, indices, node_labels=None)

Generate *Node* objects for a subsystem.

Parameters

- tpm (np.ndarray) The system's TPM
- **cm** (*np.ndarray*) The corresponding CM.
- **network_state** (*tuple*) The state of the network.
- **indices** (*tuple[int]*) Indices to generate nodes for.

Keyword Arguments node_labels (NodeLabels) - Textual labels for each node.

Returns The nodes of the system.

Return type tuple[Node]

```
pyphi.node.expand_node_tpm(tpm)
```

Broadcast a node TPM over the full network.

This is different from broadcasting the TPM of a full system since the last dimension (containing the state of the node) contains only the probability of *this* node being on, rather than the probabilities for each node.

1.46 partition

Functions for generating partitions.

pyphi.partition.**partitions** (*collection*) Generate all set partitions of a collection.

Example

```
>>> list(partitions(range(3)))
[[[0, 1, 2]],
[[0], [1, 2]],
[[0, 1], [2]],
[[1], [0, 2]],
[[0], [1], [2]]]
```

pyphi.partition.bipartition_indices(N)

Return indices for undirected bipartitions of a sequence.

Parameters N(int) – The length of the sequence.

Returns A list of tuples containing the indices for each of the two parts.

Return type list

Example

```
>>> N = 3
>>> bipartition_indices(N)
[((), (0, 1, 2)), ((0,), (1, 2)), ((1,), (0, 2)), ((0, 1), (2,))]
```

pyphi.partition.bipartition(seq)

Return a list of bipartitions for a sequence.

Parameters a (*Iterable*) – The sequence to partition.

Returns A list of tuples containing each of the two partitions.

Return type list[tuple[tuple]]

Example

```
>>> bipartition((1,2,3))
[((), (1, 2, 3)), ((1,), (2, 3)), ((2,), (1, 3)), ((1, 2), (3,))]
```

```
pyphi.partition.directed_bipartition_indices (N)
Return indices for directed bipartitions of a sequence.
```

Parameters N(int) – The length of the sequence.

Returns A list of tuples containing the indices for each of the two parts.

Return type list

Example

```
>>> N = 3
>>> directed_bipartition_indices(N)
[((), (0, 1, 2)),
((0,), (1, 2)),
((1,), (0, 2)),
((0, 1), (2,)),
((2,), (0, 1)),
((2,), (0, 1)),
((1, 2), (0,)),
((0, 1, 2), ())]
```

pyphi.partition.directed_bipartition(seq, nontrivial=False) Return a list of directed bipartitions for a sequence.

Parameters seq(*Iterable*) – The sequence to partition.

Returns A list of tuples containing each of the two parts.

Return type list[tuple[tuple]]

Example

```
>>> directed_bipartition((1, 2, 3))
[((), (1, 2, 3)),
 ((1,), (2, 3)),
 ((2,), (1, 3)),
 ((1, 2), (3,)),
 ((3,), (1, 2)),
 ((1, 3), (2,)),
 ((2, 3), (1,)),
 ((1, 2, 3), ())]
```

```
pyphi.partition.bipartition_of_one (seq)
Generate bipartitions where one part is of length 1.
```

```
pyphi.partition.reverse_elements (seq)
Reverse the elements of a sequence.
```

```
pyphi.partition.directed_bipartition_of_one (seq)
Generate directed bipartitions where one part is of length 1.
```

Parameters seq(*Iterable*) – The sequence to partition.

Returns A list of tuples containing each of the two partitions.

Return type list[tuple[tuple]]

Example

```
>>> partitions = directed_bipartition_of_one((1, 2, 3))
>>> list(partitions)
[((1,), (2, 3)),
  ((2,), (1, 3)),
  ((3,), (1, 2)),
  ((2, 3), (1,)),
  ((1, 3), (2,)),
  ((1, 2), (3,))]
```

Parameters N(int) – The length of the sequence.

Returns A list of tuples containing the indices for each partition.

Return type list[tuple]

Example

```
>>> N = 1
>>> directed_tripartition_indices(N)
[((0,), (), ()), ((), (0,), ()), ((), (), (0,))]
```

pyphi.partition.directed_tripartition (seq) Generator over all directed tripartitions of a sequence.

Parameters seq(*Iterable*) – a sequence.

Yields tuple[tuple] - A tripartition of seq.

Example

```
>>> seq = (2, 5)
>>> list(directed_tripartition(seq))
[((2, 5), (), ()),
((2,), (5,), ()),
((2,), (), (5,)),
((5,), (2,), ()),
((), (2, 5), ()),
((), (2,), (5,)),
((5,), (), (2,)),
((), (5,), (2,)),
((), (2, 5))]
```

pyphi.partition.k_partitions (collection, k)
Generate all k-partitions of a collection.

Example

```
>>> list(k_partitions(range(3), 2))
[[[0, 1], [2]], [[0], [1, 2]], [[0, 2], [1]]]
```

class pyphi.partition.PartitionRegistry Storage for partition schemes registered with PyPhi.

Users can define custom partitions:

Examples

```
>>> @partition_registry.register('NONE')
... def no_partitions(mechanism, purview):
... return []
```

And use them by setting config.PARTITION_TYPE = 'NONE'

desc = 'partitions'

pyphi.partition.mip_partitions (mechanism, purview, node_labels=None) Return a generator over all mechanism-purview partitions, based on the current configuration.

pyphi.partition.mip_bipartitions (mechanism, purview, node_labels=None) Return an generator of all φ bipartitions of a mechanism over a purview.

Excludes all bipartitions where one half is entirely empty, *e.g*:

А _____

is not valid, but

is.

Parameters

- **mechanism** (*tuple[int]*) The mechanism to partition
- **purview** (*tuple[int]*) The purview to partition

Yields Bipartition -

Where each bipartition is:

<pre>bipart[0].mechanism</pre>	<pre>bipart[1].mechanism</pre>
bipart[0].purview	bipart[1].purview

Example

```
>>> mechanism = (0,)
>>> purview = (2, 3)
>>> for partition in mip_bipartitions(mechanism, purview):
... print(partition, '\n')
_____0
```

(continues on next page)

(continued from previous page)

```
\begin{array}{c} 2 & 3 \\ \hline 0 \\ \hline 3 & 2 \\ \hline 0 \\ \hline 2, 3 \end{array}
```

pyphi.partition.wedge_partitions (mechanism, purview, node_labels=None)
Return an iterator over all wedge partitions.

These are partitions which strictly split the mechanism and allow a subset of the purview to be split into a third partition, e.g.:

A B B C D

See PARTITION_TYPE in config for more information.

Parameters

- mechanism (tuple[int]) A mechanism.
- **purview** (tuple[int]) A purview.

Yields Tripartition - all unique tripartitions of this mechanism and purview.

Partitions can consist of any number of parts.

Parameters

- **mechanism** (*tuple[int]*) A mechanism.
- **purview** (tuple[int]) A purview.

Yields KPartition – A partition of this mechanism and purview into k parts.

1.47 subsystem

Represents a candidate system for φ and Φ evaluation.

A set of nodes in a network.

Parameters

- **network** (Network) The network the subsystem belongs to.
- **state** (*tuple[int]*) The state of the network.

Keyword Arguments

- nodes (tuple[int] or tuple[str]) The nodes of the network which are in this subsystem. Nodes can be specified either as indices or as labels if the *Network* was passed node_labels. If this is None then the full network will be used.
- cut (Cut) The unidirectional *Cut* to apply to this subsystem.

network

Network – The network the subsystem belongs to.

tpm

np.ndarray – The TPM conditioned on the state of the external nodes.

cm

np.ndarray – The connectivity matrix after applying the cut.

state

tuple[int] – The state of the network.

node_indices

tuple[int] – The indices of the nodes in the subsystem.

cut

Cut – The cut that has been applied to this subsystem.

null_cut

Cut – The cut object representing no cut.

nodes

tuple[*Node*] – The nodes in this *Subsystem*.

proper_state

tuple[int] – The state of the subsystem.

proper_state[i] gives the state of the i^{th} node in the subsystem. Note that this is not the state of nodes[i].

connectivity_matrix

np.ndarray – Alias for cm.

size

int – The number of nodes in the subsystem.

is_cut

bool – True if this Subsystem has a cut applied to it.

cut_indices

tuple[int] – The nodes of this subsystem to cut for Φ computations.

This was added to support MacroSubsystem, which cuts indices other than node_indices.

Yields tuple[int]

cut_mechanisms

list[tuple[int]] – The mechanisms that are cut in this system.

cut_node_labels

NodeLabels - Labels for the nodes of this system that will be cut.

tpm_size

int – The number of nodes in the TPM.

$\verb+cache_info()$

Report repertoire cache statistics.

clear_caches()

Clear the mice and repertoire caches.

__bool__()

Return False if the Subsystem has no nodes, True otherwise.

___eq___(other)

Return whether this Subsystem is equal to the other object.

Two Subsystems are equal if their sets of nodes, networks, and cuts are equal.

___lt__(other)

Return whether this subsystem has fewer nodes than the other.

__gt_(other)

Return whether this subsystem has more nodes than the other.

__len_()

Return the number of nodes in this Subsystem.

to_json()

Return a JSON-serializable representation.

apply_cut (cut)

Return a cut version of this Subsystem.

Parameters cut (Cut) – The cut to apply to this Subsystem.

Returns The cut subsystem.

Return type Subsystem

indices2nodes(indices)

Return *Node* for these indices.

Parameters indices (*tuple[int]*) – The indices in question.

Returns The *Node* objects corresponding to these indices.

Return type tuple[Node]

Raises ValueError – If requested indices are not in the subsystem.

cause_repertoire (mechanism, purview)

Return the cause repertoire of a mechanism over a purview.

Parameters

- **mechanism** (*tuple[int]*) The mechanism for which to calculate the cause repertoire.
- **purview** (*tuple[int]*) The purview over which to calculate the cause repertoire.

Returns The cause repertoire of the mechanism over the purview.

Return type np.ndarray

Note: The returned repertoire is a distribution over purview node states, not the states of the whole network.

effect_repertoire (mechanism, purview)

Return the effect repertoire of a mechanism over a purview.

Parameters

- **mechanism** (*tuple[int]*) The mechanism for which to calculate the effect repertoire.
- **purview** (*tuple[int]*) The purview over which to calculate the effect repertoire.

Returns The effect repertoire of the mechanism over the purview.

Return type np.ndarray

Note: The returned repertoire is a distribution over purview node states, not the states of the whole network.

repertoire (*direction*, *mechanism*, *purview*)

Return the cause or effect repertoire based on a direction.

Parameters

- direction (Direction) CAUSE or EFFECT.
- mechanism (tuple[int]) The mechanism for which to calculate the repertoire.
- **purview** (*tuple[int]*) The purview over which to calculate the repertoire.

Returns The cause or effect repertoire of the mechanism over the purview.

Return type np.ndarray

Raises ValueError - If direction is invalid.

unconstrained_repertoire (direction, purview)

Return the unconstrained cause/effect repertoire over a purview.

unconstrained_cause_repertoire(purview)

Return the unconstrained cause repertoire for a purview.

This is just the cause repertoire in the absence of any mechanism.

unconstrained_effect_repertoire (purview)

Return the unconstrained effect repertoire for a purview.

This is just the effect repertoire in the absence of any mechanism.

partitioned_repertoire(direction, partition)

Compute the repertoire of a partitioned mechanism and purview.

expand_repertoire (*direction*, *repertoire*, *new_purview=None*) Distribute an effect repertoire over a larger purview.

Parameters

- direction (Direction) CAUSE or EFFECT.
- **repertoire** (*np.ndarray*) The repertoire to expand.
- Keyword Arguments new_purview (tuple[int]) The new purview to expand the repertoire over. If None (the default), the new purview is the entire network.
- **Returns** A distribution over the new purview, where probability is spread out over the new nodes.

Return type np.ndarray

Raises ValueError – If the expanded purview doesn't contain the original purview.

expand_cause_repertoire (repertoire, new_purview=None)
Alias for expand_repertoire () with direction set to CAUSE.

expand_effect_repertoire(repertoire, new_purview=None)

Alias for expand_repertoire() with direction set to EFFECT.

- **cause_info** (*mechanism*, *purview*) Return the cause information for a mechanism over a purview.
- **effect_info** (*mechanism*, *purview*) Return the effect information for a mechanism over a purview.

cause_effect_info(mechanism, purview)

Return the cause-effect information for a mechanism over a purview.

This is the minimum of the cause and effect information.

evaluate_partition (*direction*, *mechanism*, *purview*, *partition*, *repertoire=None*) Return the φ of a mechanism over a purview for the given partition.

Parameters

- direction (Direction) CAUSE or EFFECT.
- **mechanism** (*tuple[int]*) The nodes in the mechanism.
- **purview** (*tuple[int]*) The nodes in the purview.
- **partition** (Bipartition) The partition to evaluate.
- **Keyword Arguments repertoire** (*np.array*) The unpartitioned repertoire. If not supplied, it will be computed.
- **Returns** The distance between the unpartitioned and partitioned repertoires, and the partitioned repertoire.

Return type tuple[int, np.ndarray]

find_mip (direction, mechanism, purview)

Return the minimum information partition for a mechanism over a purview.

Parameters

- direction (Direction) CAUSE or EFFECT.
- **mechanism** (tuple[int]) The nodes in the mechanism.
- **purview** (*tuple[int]*) The nodes in the purview.
- **Returns** The irreducibility analysis for the mininum-information partition in one temporal direction.

Return type RepertoireIrreducibilityAnalysis

cause_mip(mechanism, purview)

Return the irreducibility analysis for the cause MIP.

Alias for find_mip() with direction set to CAUSE.

effect_mip (mechanism, purview)

Return the irreducibility analysis for the effect MIP.

Alias for find_mip() with direction set to EFFECT.

phi_cause_mip (*mechanism*, *purview*) Return the φ of the cause MIP. This is the distance between the unpartitioned cause repertoire and the MIP cause repertoire.

phi_effect_mip (*mechanism*, *purview*) Return the φ of the effect MIP.

This is the distance between the unpartitioned effect repertoire and the MIP cause repertoire.

phi (mechanism, purview)

Return the φ of a mechanism over a purview.

```
potential_purviews (direction, mechanism, purviews=False)
```

Return all purviews that could belong to the MaximallyIrreducibleCause/MaximallyIrreducibleEffect.

Filters out trivially-reducible purviews.

Parameters

- direction (Direction) CAUSE or EFFECT.
- mechanism (tuple[int]) The mechanism of interest.

Keyword Arguments purviews (tuple[int]) – Optional subset of purviews of interest.

find_mice (direction, mechanism, purviews=False)

Return the *MaximallyIrreducibleCause* or *MaximallyIrreducibleEffect* for a mechanism.

Parameters

- direction (Direction) -: CAUSE or EFFECT.
- mechanism (tuple[int]) The mechanism to be tested for irreducibility.
- **Keyword Arguments purviews** (*tuple[int]*) Optionally restrict the possible purviews to a subset of the subsystem. This may be useful for _e.g._ finding only concepts that are "about" a certain subset of nodes.

Returns The MaximallyIrreducibleCause or MaximallyIrreducibleEffect.

Return type MaximallyIrreducibleCauseOrEffect

mic (mechanism, purviews=False)

Return the mechanism's maximally-irreducible cause (MaximallyIrreducibleCause).

Alias for find_mice() with direction set to CAUSE.

mie (mechanism, purviews=False)

Return the mechanism's maximally-irreducible effect (MaximallyIrreducibleEffect).

Alias for find_mice() with direction set to EFFECT.

phi_max(mechanism)

Return the φ^{\max} of a mechanism.

This is the maximum of φ taken over all possible purviews.

null_concept

Return the null concept of this subsystem.

The null concept is a point in concept space identified with the unconstrained cause and effect repertoire of this subsystem.

concept (*mechanism*, *purviews=False*, *cause_purviews=False*, *effect_purviews=False*) Return the concept specified by a mechanism within this subsytem.

Parameters mechanism (tuple[int]) – The candidate set of nodes.

Keyword Arguments

- **purviews** (*tuple[tuple[int]]*) Restrict the possible purviews to those in this list.
- **cause_purviews** (*tuple[tuple[int]]*) Restrict the possible cause purviews to those in this list. Takes precedence over purviews.
- **effect_purviews** (*tuple[tuple[int]]*) Restrict the possible effect purviews to those in this list. Takes precedence over purviews.
- **Returns** The pair of maximally irreducible cause/effect repertoires that constitute the concept specified by the given mechanism.

Return type *Concept*

1.48 timescale

Functions for converting the timescale of a TPM.

pyphi.timescale.sparse(matrix, threshold=0.1)

pyphi.timescale.sparse_time(tpm, time_scale)

pyphi.timescale.dense_time(tpm, time_scale)

pyphi.timescale.run_tpm(tpm, time_scale)
Iterate a TPM by the specified number of time steps.

Parameters

- **tpm** (*np*.*ndarray*) A state-by-node tpm.
- time_scale (*int*) The number of steps to run the tpm.

Returns np.ndarray

pyphi.timescale.run_cm(cm, time_scale)
 Iterate a connectivity matrix the specified number of steps.

Parameters

- **cm** (*np*.*ndarray*) A connectivity matrix.
- **time_scale** (*int*) The number of steps to run.

Returns The connectivity matrix at the new timescale.

Return type np.ndarray

1.49 tpm

Functions for manipulating transition probability matrices.

```
pyphi.tpm.tpm_indices(tpm)
Return the indices of nodes in the TPM.
```

```
pyphi.tpm.is_state_by_state(tpm)
```

Return True if tpm is in state-by-state form, otherwise False.

```
pyphi.tpm.condition_tpm(tpm, fixed_nodes, state)
```

Return a TPM conditioned on the given fixed node indices, whose states are fixed according to the given statetuple.

The dimensions of the new TPM that correspond to the fixed nodes are collapsed onto their state, making those dimensions singletons suitable for broadcasting. The number of dimensions of the conditioned TPM will be the same as the unconditioned TPM.

```
pyphi.tpm.expand_tpm(tpm)
```

Broadcast a state-by-node TPM so that singleton dimensions are expanded over the full network.

```
pyphi.tpm.marginalize_out (node_indices, tpm)
```

Marginalize out nodes from a TPM.

Parameters

- **node_indices** (*list[int]*) The indices of nodes to be marginalized out.
- tpm (*np.ndarray*) The TPM to marginalize the node out of.

Returns A TPM with the same number of dimensions, with the nodes marginalized out.

Return type np.ndarray

pyphi.tpm.infer_edge(tpm, a, b, contexts)

Infer the presence or absence of an edge from node A to node B.

Let S be the set of all nodes in a network. Let $A' = S - \{A\}$. We call the state of A' the context C of A. There is an edge from A to B if there exists any context C(A) such that $Pr(B \mid C(A), A = 0) \neq Pr(B \mid C(A), A = 1)$.

Parameters

- tpm (*np*.*ndarray*) The TPM in state-by-node, multidimensional form.
- **a** (*int*) The index of the putative source node.
- **b** (*int*) The index of the putative sink node.

Returns True if the edge $A \rightarrow B$ exists, False otherwise.

Return type bool

```
pyphi.tpm.infer_cm(tpm)
```

Infer the connectivity matrix associated with a state-by-node TPM in multidimensional form.

1.50 utils

Functions used by more than one PyPhi module or class, or that might be of external use.

pyphi.utils.all_states (n, big_endian=False)
Return all binary states for a system.

Parameters

- **n** (*int*) The number of elements in the system.
- **big_endian** (*bool*) Whether to return the states in big-endian order instead of littleendian order.
- Yields *tuple[int]* The next state of an n-element system, in little-endian order unless big_endian is True.

```
pyphi.utils.np_immutable(a)
Make a NumPy array immutable.
```

```
pyphi.utils.np_hash(a)
Return a hash of a NumPy array.
```

class pyphi.utils.**np_hashable** (*array*) A hashable wrapper around a NumPy array.

```
pyphi.utils.eq(x, y)
Compare two values up to PRECISION.
```

pyphi.utils.combs(a, r)
 NumPy implementation of itertools.combinations.

Return successive r-length combinations of elements in the array a.

Parameters

• **a** (*np.ndarray*) – The array from which to get combinations.

• **r** (*int*) – The length of the combinations.

Returns An array of combinations.

Return type np.ndarray

```
pyphi.utils.comb_indices(n, k)
```

n-dimensional version of itertools.combinations.

Parameters

- **a** (*np.ndarray*) The array from which to get combinations.
- **k** (*int*) The desired length of the combinations.

Returns Indices that give the k-combinations of n elements.

Return type np.ndarray

Example

pyphi.utils.powerset (iterable, nonempty=False, reverse=False)
Generate the power set of an iterable.

Parameters iterable (*Iterable*) – The iterable from which to generate the power set.

Keyword Arguments

- nonempty (boolean) If True, don't include the empty set.
- **reverse** (*boolean*) If True, reverse the order of the powerset.

Returns An iterator over the power set.

Return type Iterable

Example

```
>>> ps = powerset(np.arange(2))
>>> list(ps)
[(), (0,), (1,), (0, 1)]
>>> ps = powerset(np.arange(2), nonempty=True)
>>> list(ps)
[(0,), (1,), (0, 1)]
>>> ps = powerset(np.arange(2), nonempty=True, reverse=True)
>>> list(ps)
[(1, 0), (1,), (0,)]
```

pyphi.utils.load_data (*directory*, num) Load numpy data from the data directory.

The files should stored in .../data/<dir> and named 0.npy, 1.npy, ... <num - 1>.npy.

Returns A list of loaded data, such that list [i] contains the the contents of i.npy.

Return type list

```
pyphi.utils.time_annotated(func, *args, **kwargs)
```

Annotate the decorated function or method with the total execution time.

The result is annotated with a *time* attribute.

1.51 validate

Methods for validating arguments.

pyphi.validate.direction (direction, allow_bi=False)
Validate that the given direction is one of the allowed constants.

If allow_bi is True then Direction.BIDIRECTIONAL is acceptable.

pyphi.validate.tpm(tpm, check_independence=True)
Validate a TPM.

The TPM can be in

- 2-dimensional state-by-state form,
- 2-dimensional state-by-node form, or
- multidimensional state-by-node form.

```
pyphi.validate.conditionally_independent(tpm)
Validate that the TPM is conditionally independent.
```

pyphi.validate.connectivity_matrix(cm)
Validate the given connectivity matrix.

```
pyphi.validate.node_labels (node_labels, node_indices)
Validate that there is a label for each node.
```

```
pyphi.validate.network(n)
Validate a Network.
```

Checks the TPM and connectivity matrix.

- pyphi.validate.is_network (network)
 Validate that the argument is a Network.
- pyphi.validate.node_states (state)
 Check that the state contains only zeros and ones.

```
pyphi.validate.state_length(state, size)
            Check that the state is the given size.
```

- pyphi.validate.**state_reachable** (*subsystem*) Return whether a state can be reached according to the network's TPM.
- pyphi.validate.cut (cut, node_indices)
 Check that the cut is for only the given nodes.
- pyphi.validate.subsystem(s)
 Validate a Subsystem.

Checks its state and cut.

pyphi.validate.time_scale(time_scale)
Validate a macro temporal time scale.

- pyphi.validate.partition (partition)
 Validate a partition used by blackboxes and coarse grains.
- pyphi.validate.coarse_grain (coarse_grain) Validate a macro coarse-graining.
- pyphi.validate.blackbox(blackbox)
 Validate a macro blackboxing.
- pyphi.validate.blackbox_and_coarse_grain (*blackbox, coarse_grain*) Validate that a coarse-graining properly combines the outputs of a blackboxing.

Python Module Index

р

pyphi.actual,46 pyphi.cache,51 pyphi.compute, 53 pyphi.compute.distance,54 pyphi.compute.network, 54 pyphi.compute.parallel,56 pyphi.compute.subsystem, 58 pyphi.conf, 38 pyphi.connectivity,68 pyphi.constants,70 pyphi.convert,70 pyphi.direction,78 pyphi.distance,78 pyphi.distribution,81 pyphi.examples,82 pyphi.exceptions,90 pyphi.jsonify,90 pyphi.macro,92 pyphi.models,98 pyphi.models.actual_causation,98 pyphi.models.cuts, 102 pyphi.models.mechanism, 104 pyphi.models.subsystem, 107 pyphi.network, 109 pyphi.node, 111 pyphi.partition, 112 pyphi.subsystem, 116 pyphi.timescale, 122 pyphi.tpm, 122 pyphi.utils, 123 pyphi.validate,125

Index

Symbols	pyphi.models.actual_causation), 101
bool() (pyphi.models.actual_causation.AcRepertoireIn method), 99	pypin.models), 98
bool() (pyphi.models.actual_causation.AcSystemIrred method), 101	actual_cause (pyphi.models.actual_causation.Event at-
bool() (pyphi.models.actual_causation.CausalLink method), 100	tribute), 100 actual_effect (pyphi.models.actual_causation.Event at-
bool() (pyphi.models.mechanism.Concept method), 107	tribute), 100 ActualCut (class in pyphi.models.cuts), 103
bool() (pyphi.models.mechanism.RepertoireIrreducibi method), 105	and state (pyphi.actual. manshion attribute), 40
bool() (pyphi.models.subsystem.SystemIrreducibility/ method), 108	Antersistate (pyphi.models.actual_causation.AcSystemIrreducibilityAnalysis attribute), 101
bool() (pyphi.subsystem.Subsystem method), 118 eq() (pyphi.macro.MacroSubsystem method), 93	all_blackboxes() (in module pyphi.macro), 96 all_coarse_grains() (in module pyphi.macro), 96
eq() (pyphi.network.Network method), 110 eq() (pyphi.node.Node method), 111	all_coarse_grains_for_blackbox() (in module pyphi.macro), 96
eq() (pyphi.subsystem.Subsystem method), 118 getattr() (pyphi.compute.subsystem.ConceptStyleSyst	all_complexes (in module pyphi.compute), 53 endl_complexes() (in module pyphi.compute.network), 55
method), 60 getattr() (pyphi.compute.subsystem.SystemIrreducibil	ingly matching () (in module pyphimacro), 96
method), 60 gt() (pyphi.subsystem.Subsystem method), 118	all_partitions() (in module pyphi.macro), 96 all_partitions() (in module pyphi.partition), 116
len() (pyphi.network.Network method), 110 len() (pyphi.subsystem.Subsystem method), 118	all_states() (in module pyphi.utils), 123 alpha (pyphi.models.actual_causation.AcRepertoireIrreducibilityAnalysis
lt() (pyphi.subsystem.Subsystem method), 118	attribute), 99 alpha (pyphi.models.actual_causation.AcSystemIrreducibilityAnalysis
A Account (class in pyphi.models.actual_causation), 100	attribute), 101 alpha (pyphi.models.actual_causation.CausalLink at-
Account (in module pyphi.models), 98 account (pyphi.models.actual_causation.AcSystemIrreduci attribute), 101	tribute), 100 , apply() (pyphi.macro.SystemAttrs method), 92 bilityAnalysis apply_boundary_conditions_to_cm() (in module
account() (in module pyphi.actual), 49 account_distance() (in module pyphi.actual), 49	pyphi.connectivity), 68 apply_cut() (pyphi.actual.Transition method), 47
AcRepertoireIrreducibilityAnalysis (class in pyphi.models.actual_causation), 99	apply_cut() (pyphi.compute.subsystem.ConceptStyleSystem method), 60
AcRepertoireIrreducibilityAnalysis (in module pyphi.models), 98	apply_cut() (pyphi.macro.MacroSubsystem method), 93 apply_cut() (pyphi.subsystem.Subsystem method), 118
AcSystemIrreducibilityAnalysis (class in	ASSUME_CUTS_CANNOT_CREATE_NEW_CONCEPTS (pyphi.conf.PyphiConfig attribute), 41

asymmetric() (pyphi.distance.MeasureRegistry method), 79	CAUSE (pyphi.direction.Dir cause (pyphi.models.mechan
В	cause_effect_info() method), 120
b2l() (in module pyphi.convert), 74	cause_info() (pyphi.subsyste
b21_sbs() (in module pyphi.convert), 76	cause_mip() (pyphi.subsyste
b2s() (in module pyphi.convert), 75	cause_purview (pyphi
basic_network() (in module pyphi.examples), 82	attribute), 106
basic_noisy_selfloop_network() (in module	cause_ratio() (pyphi.actual.7
pyphi.examples), 83	cause_repertoire (pyphi.mo
basic_noisy_selfloop_subsystem() (in module	tribute), 106
pyphi.examples), 84	cause_repertoire() (pyphi.ac
basic_state() (in module pyphi.examples), 83	cause_repertoire() (pyphi.su
basic_subsystem() (in module pyphi.examples), 83	118
be2le() (in module pyphi.convert), 71	cause_system (pyphi.actual.
be2le_state_by_state() (in module pyphi.convert), 72	cause_system (pyphi.compu
be_index2state() (in module pyphi.convert), 72	attribute), 60
before_state (pyphi.actual.Transition attribute), 46	CauseEffectStructure (class
before_state (pyphi.actual.rialisticin attribute), 40	
attribute), 101	CauseEffectStructure (in mo
BIDIRECTIONAL (pyphi.direction.Direction attribute),	ces (in module pyphi.compu
	ces (pyphi.models.subsysten
Bipartition (class in pyphi.models.cuts), 103	attribute), 108
Bipartition (in module pyphi.models), 98	ces() (in module pyphi.comp
bipartition() (in module pyphi.nodels), 98	ces_distance (in module pyphiconic
bipartition() (in module pyphi.partition), 112 bipartition_indices() (in module pyphi.partition), 112	ces_distance() (in module pyp
	clear() (pyphi.cache.DictCac
bipartition_of_one() (in module pyphi.partition), 113	clear() (pyphi.cache.RedisCa
Blackbox (class in pyphi.macro), 95	clear_caches() (pyphi.subs
blackbox (pyphi.macro.MacroNetwork attribute), 97	117
blackbox() (in module pyphi.validate), 126	CLEAR_SUBSYSTEM_CA
blackbox_and_coarse_grain() (in module pyphi.validate), 126	(pyphi.conf.Pyphi
	cm (pyphi.network.Network
blackbox_network() (in module pyphi.examples), 87	cm (pyphi.subsystem.Subsys
bld() (in module pyphi.distance), 80	coarse_grain (pyphi.macro.M
block_cm() (in module pyphi.connectivity), 69	
block_reducible() (in module pyphi.connectivity), 69	coarse_grain() (in module py
С	coarse_graining() (in module
	CoarseGrain (class in pyphi.
cache() (in module pyphi.cache), 51	comb_indices() (in module p
cache_info() (pyphi.subsystem.Subsystem method), 117	combs() (in module pyphi.ut
CACHE_POTENTIAL_PURVIEWS	complexes (in module pyphi
(pyphi.conf.PyphiConfig attribute), 43	complexes() (in module pyper compute() (pyphi.actual.Com
CACHE_REPERTOIRES (pyphi.conf.PyphiConfig at-	1 0 1 7 1
tribute), 42	static method), 49
CACHE_SIAS (pyphi.conf.PyphiConfig attribute), 42	compute() (pyphi.compute
CACHING_BACKEND (pyphi.conf.PyphiConfig at-	static method), 55
tribute), 43	compute() (pyphi.compute
causal_nexus() (in module pyphi.actual), 49	method), 57
CausalLink (class in pyphi.models.actual_causation), 100	compute() (pyphi.compute.s
CausalLink (in module pyphi.models), 98	static method), 58
causally_significant_nodes (pyphi.network.Network at-	compute() (pyphi.compute.s
tribute), 109	static method), 59

causally_significant_nodes() (in module pyphi.connectivity), 68

Index

ComputeACSystemIrreducibility (class in pyphi.actual),

49

direction.Direction attribute), 78 odels.mechanism.Concept attribute), 106 (pyphi.subsystem.Subsystem fo() od), 120 yphi.subsystem.Subsystem method), 120 yphi.subsystem.Subsystem method), 120 (pyphi.models.mechanism.Concept ute), 106 yphi.actual.Transition method), 47 e (pyphi.models.mechanism.Concept ate), 106 e() (pyphi.actual.Transition method), 47 e() (pyphi.subsystem.Subsystem method), pyphi.actual.Transition attribute), 46 pyphi.compute.subsystem.ConceptStyleSystem ute), 60 ucture (class in pyphi.models.subsystem), sis ucture (in module pyphi.models), 98 pyphi.compute), 53 els.subsystem.SystemIrreducibilityAnalysis ute), 108 e pyphi.compute.subsystem), 58 n module pyphi.compute), 53 in module pyphi.compute.distance), 54 ache.DictCache method), 51 ache.RedisCache method), 51 (pyphi.subsystem.Subsystem method), YSTEM_CACHES_AFTER_COMPUTING_SIA i.conf.PyphiConfig attribute), 43 ork.Network attribute), 109 ystem.Subsystem attribute), 117 vphi.macro.MacroNetwork attribute), 96 (in module pyphi.validate), 126 g() (in module pyphi.macro), 97 lass in pyphi.macro), 93 (in module pyphi.utils), 124 dule pyphi.utils), 124 nodule pyphi.compute), 53 module pyphi.compute.network), 56 hi.actual.ComputeACSystemIrreducibility method), 49 yphi.compute.network.FindAllComplexes method), 55 yphi.compute.parallel.MapReduce static od), 57 hi.compute.subsystem.ComputeCauseEffectStructure method), 58 hi.compute.subsystem.ComputeSystemIrreducibility

ComputeCauseEffectStructure (class in pyphi.compute.subsystem), 58 ComputeSystemIrreducibility (class in pyphi.compute.subsystem), 59 Concept (class in pyphi.models.mechanism), 106 Concept (in module pyphi.models), 98 method), 60 concept() (pyphi.subsystem.Subsystem method), 121 concept_cuts() (in module pyphi.compute.subsystem), 60 concept_distance (in module pyphi.compute), 53 concept_distance() (in module pyphi.compute.distance), 54 ConceptStyleSystem (class in pyphi.compute.subsystem), conceptual_info (in module pyphi.compute), 53 conceptual_info() (in module pyphi.compute.subsystem), 59 cond_depend_tpm() (in module pyphi.examples), 85 cond independ tpm() (in module pyphi.examples), 85 condensed (in module pyphi.compute), 53 condensed() (in module pyphi.compute.network), 56 condition_tpm() (in module pyphi.tpm), 122 conditionally independent() (in module pyphi.validate), 125 ConditionallyDependentError, 90 Config (class in pyphi.conf), 41 ConfigMeta (class in pyphi.conf), 40 configure_logging() (in module pyphi.conf), 41 configure_worker_logging() module (in pyphi.compute.parallel), 58 connectivity_matrix (pyphi.network.Network attribute), 109 connectivity_matrix (pyphi.subsystem.Subsystem attribute), 117 connectivity_matrix() (in module pyphi.validate), 125 Cut (class in pyphi.models.cuts), 102 Cut (in module pyphi.models), 98 cut (pyphi.actual.Transition attribute), 46 cut (pyphi.models.actual_causation.AcSystemIrreducibilityAnalysis pyphi.models.actual_causation), 101 attribute), 101 cut (pyphi.models.subsystem.SystemIrreducibilityAnalysis attribute), 108 cut (pyphi.subsystem.Subsystem attribute), 117 cut() (in module pyphi.validate), 126 cut_indices (pyphi.macro.MacroSubsystem attribute), 93 cut_indices (pyphi.subsystem.Subsystem attribute), 117 cut_matrix() (pyphi.models.cuts.Cut method), 102 cut_matrix() (pyphi.models.cuts.KCut method), 102 cut_matrix() (pyphi.models.cuts.NullCut method), 102 cut_mechanisms (pyphi.macro.MacroSubsystem attribute), 93 cut mechanisms (pyphi.subsystem.Subsystem attribute), 117

(pyphi.macro.MacroSubsystem cut node labels attribute), 93 cut node labels (pyphi.subsystem.Subsystem attribute), 117 CUT ONE APPROXIMATION (pyphi.conf.PyphiConfig attribute), 41 concept() (pyphi.compute.subsystem.ConceptStyleSystem cut subsystem(pyphi.models.subsystem.SystemIrreducibilityAnalysis attribute), 108 D damaged by cut() (pyphi.models.mechanism.MaximallyIrreducibleCauseC method), 105 DATABASE (in module pyphi.constants), 70 defaults() (pyphi.conf.Config method), 41 dense_time() (in module pyphi.timescale), 122 desc (pyphi.distance.MeasureRegistry attribute), 79 desc (pyphi.partition.PartitionRegistry attribute), 115 description (pyphi.actual.ComputeACSystemIrreducibility attribute), 49 description (pyphi.compute.network.FindAllComplexes attribute), 55 description (pyphi.compute.parallel.MapReduce attribute), 57 description (pyphi.compute.subsystem.ComputeCauseEffectStructure attribute), 58 description (pyphi.compute.subsystem.ComputeSystemIrreducibility attribute), 59 DictCache (class in pyphi.cache), 51 DictMICECache (class in pyphi.cache), 52 directed account() (in module pyphi.actual), 49 directed_bipartition() (in module pyphi.partition), 113 directed bipartition indices() module (in pyphi.partition), 112 directed bipartition of one() (in module pyphi.partition), 113 directed_tripartition() (in module pyphi.partition), 114 directed_tripartition_indices() (in module pyphi.partition), 114 in DirectedAccount (class DirectedAccount (in module pyphi.models), 98 Direction (class in pyphi.direction), 78 direction (pyphi.models.actual_causation.AcRepertoireIrreducibilityAnalys attribute), 99 direction (pyphi.models.actual causation.CausalLink attribute), 100 direction (pyphi.models.mechanism.MaximallyIrreducibleCause attribute), 105 direction (pyphi.models.mechanism.MaximallyIrreducibleCauseOrEffect attribute), 105 direction (pyphi.models.mechanism.MaximallyIrreducibleEffect attribute), 106 direction (pyphi.models.mechanism.RepertoireIrreducibilityAnalysis

attribute), 104

direction() (in module pyphi.validate), 125

directional emd() (in module pyphi.distance), 80

- directional sia() (in module pyphi.compute.subsystem), 60
- disjunction conjunction network() (in module pyphi.examples), 90
- dump() (in module pyphi.isonify), 92

dumps() (in module pyphi.jsonify), 92

F

EFFECT (pyphi.direction.Direction attribute), 78 effect (pyphi.models.mechanism.Concept attribute), 106 effect_emd() (in module pyphi.distance), 79 effect_info() (pyphi.subsystem.Subsystem method), 120 effect_mip() (pyphi.subsystem.Subsystem method), 120 effect purview (pyphi.models.mechanism.Concept attribute), 106 effect_ratio() (pyphi.actual.Transition method), 48 effect repertoire (pyphi.models.mechanism.Concept attribute), 106 effect repertoire() (pyphi.actual.Transition method), 47 effect repertoire() (pyphi.subsystem.Subsystem method), 118 effect system (pyphi.actual.Transition attribute), 46 effect_system (pyphi.compute.subsystem.ConceptStyleSystem14() (in module pyphi.examples), 90 attribute), 60 effective_info() (in module pyphi.macro), 97 emd eq() (pyphi.models.mechanism.Concept method), 107 emergence (pyphi.macro.MacroNetwork attribute), 97 emergence() (in module pyphi.macro), 97 empty_result() (pyphi.actual.ComputeACSystemIrreducibilifig5b() (in module pyphi.examples), 88 method), 49 empty_result() (pyphi.compute.network.FindAllComplexes fig8() (in module pyphi.examples), 89 method), 55 (pyphi.compute.parallel.MapReduce empty_result() method), 57 method), 58 empty_result() (pyphi.compute.subsystem.ComputeSystemIfindunihidt)/(pyphi.actual.Transition method), 48 method). 59 encode() (pyphi.jsonify.PyPhiJSONEncoder method), 91 entropy difference() (in module pyphi.distance), 80 EPSILON (in module pyphi.constants), 70 eq() (in module pyphi.utils), 124 eq_repertoires() (pyphi.models.mechanism.Concept method), 107 evaluate_cut (in module pyphi.compute), 53 evaluate_cut() (in module pyphi.compute.subsystem), 59 evaluate partition() (pyphi.subsystem.Subsystem method), 120 Event (class in pyphi.models.actual_causation), 100 events() (in module pyphi.actual), 50 ExceptionWrapper (class in pyphi.compute.parallel), 56

expand cause repertoire() (pyphi.models.mechanism.Concept method). 107 expand_cause_repertoire() (pyphi.subsystem.Subsystem method), 119 expand effect repertoire() (pyphi.models.mechanism.Concept method). 107 expand_effect_repertoire() (pyphi.subsystem.Subsystem method), 120 expand_node_tpm() (in module pyphi.node), 112 expand_partitioned_cause_repertoire() (pyphi.models.mechanism.Concept method), 107 expand_partitioned_effect_repertoire() (pyphi.models.mechanism.Concept method), 107 expand repertoire() (pyphi.subsystem.Subsystem method), 119 expand tpm() (in module pyphi.tpm), 123 extrinsic events() (in module pyphi.actual), 50

F

fig10() (in module pyphi.examples), 89 fig16() (in module pyphi.examples), 90 fig1a() (in module pyphi.examples), 88 fig3a() (in module pyphi.examples), 88 fig3b() (in module pyphi.examples), 88 fig4() (in module pyphi.examples), 88 fig5a() (in module pyphi.examples), 88 fig6() (in module pyphi.examples), 89 fig9() (in module pyphi.examples), 89 FILESYSTEM (in module pyphi.constants), 70 find_actual_cause() (pyphi.actual.Transition method), 48 empty_result() (pyphi.compute.subsystem.ComputeCauseEffect() (pyphi.actual.Transition method), 48 find causal link() (pyphi.actual.Transition method), 48 find mice() (pyphi.subsystem.Subsystem method), 121 find mip() (pyphi.actual.Transition method), 48 find mip() (pyphi.subsystem.Subsystem method), 120 FindAllComplexes (class in pyphi.compute.network), 55 FindIrreducibleComplexes (class in pyphi.compute.network), 56 finish_parallel() (pyphi.compute.parallel.MapReduce method), 58 flatten() (in module pyphi.distribution), 82 from_json() (in module pyphi.network), 110 (pyphi.models.actual causation.Account from_json() class method), 101 from_json() (pyphi.models.cuts.Bipartition class method), 104

- from json() (pyphi.models.cuts.KPartition class method), 103
- from json() (pyphi.models.mechanism.Concept class method), 107
- from json() (pyphi.models.subsystem.SystemIrreducibilityAsamydis(pyphi.models.cuts.NullCut attribute), 102 class method), 108
- from ison() (pyphi.network.Network class method), 110 from nodes (pyphi.models.cuts.Cut attribute), 102
- FS CACHE DIRECTORY (pyphi.conf.PyphiConfig attribute), 43
- FS_CACHE_VERBOSITY (pyphi.conf.PyphiConfig attribute), 43

G

generate_nodes() (in module pyphi.node), 111 get() (pyphi.cache.DictCache method), 51 get() (pyphi.cache.RedisCache method), 52 get() (pyphi.cache.RedisMICECache method), 52 get inputs from cm() (in module pyphi.connectivity), 68 get_num_processes() (in module pyphi.compute.parallel), 56 get outputs from cm() (in module pyphi.connectivity), 68 greater_than_zero() (in module pyphi.models.actual causation), 98 grouping (pyphi.macro.CoarseGrain attribute), 93

н

hamming_emd() (in module pyphi.distance), 79 hidden_from() (pyphi.macro.Blackbox method), 96 hidden_indices (pyphi.macro.Blackbox attribute), 95

attribute), 107 in same box() (pyphi.macro.Blackbox method), 96 le2be() (in module pyphi.convert), 71 independent() (in module pyphi.distribution), 81 le2be_state_by_state() (in module pyphi.convert), 72 indices (pyphi.models.cuts.ActualCut attribute), 103 le_index2state() (in module pyphi.convert), 71 indices (pyphi.models.cuts.Cut attribute), 102 load() (in module pyphi.jsonify), 92 indices (pyphi.models.cuts.KCut attribute), 102 load data() (in module pyphi.utils), 125 indices (pyphi.models.cuts.NullCut attribute), 102 load_dict() (pyphi.conf.Config method), 41 indices2nodes() (pyphi.subsystem.Subsystem method), load_file() (pyphi.conf.Config method), 41 118 loads() (in module pyphi.jsonify), 92 infer_cm() (in module pyphi.tpm), 123 log() (pyphi.conf.PyphiConfig method), 46 infer_edge() (in module pyphi.tpm), 123 log2() (in module pyphi.actual), 46 info() (pyphi.cache.DictCache method), 51 LOG_FILE (pyphi.conf.PyphiConfig attribute), 43 info() (pyphi.cache.RedisCache method), 52 LOG_FILE_LEVEL (pyphi.conf.PyphiConfig attribute), init_progress_bar() (pyphi.compute.parallel.MapReduce 43 method), 57 LOG_STDOUT_LEVEL (pyphi.conf.PyphiConfig initialize tasks() (pyphi.compute.parallel.MapReduce attribute), 43 method), 57 LogThread (class in pyphi.compute.parallel), 58 inputs (pyphi.node.Node attribute), 111 irreducible_causes (pyphi.models.actual_causation.Account attribute), 100 irreducible_effects (pyphi.models.actual_causation.Accountmacro2blackbox_outputs() attribute), 101 (pyphi.macro.MacroSubsystem method),

irreducible purviews() (in module pyphi.network), 110 is cut (pyphi.subsystem.Subsystem attribute), 117 is full() (in module pyphi.connectivity), 70 is_network() (in module pyphi.validate), 126 is state by state() (in module pyphi.tpm), 122 is strong() (in module pyphi.connectivity), 69 is weak() (in module pyphi.connectivity), 69

iterencode() (pyphi.jsonify.PyPhiJSONEncoder method), 91

J

joblib_memory (in module pyphi.constants), 70 jsonify() (in module pyphi.jsonify), 91 JSONVersionError, 90

Κ

k_partitions() (in module pyphi.partition), 114 KCut (class in pyphi.models.cuts), 102 key() (pyphi.cache.DictCache method), 51 key() (pyphi.cache.DictMICECache method), 52 key() (pyphi.cache.RedisCache method), 52 key() (pyphi.cache.RedisMICECache method), 52 kld() (in module pyphi.distance), 79 KPartition (class in pyphi.models.cuts), 103

11() (in module pyphi.distance), 79 12b() (in module pyphi.convert), 74 12b sbs() (in module pyphi.convert), 76 12s() (in module pyphi.convert), 74 label (pyphi.node.Node attribute), 111 labeled mechanisms (pyphi.models.subsystem.CauseEffectStructure

93 macro2micro() (pyphi.macro.MacroSubsystem method), 93 macro_indices (pyphi.macro.Blackbox attribute), 95 macro indices (pyphi.macro.CoarseGrain attribute), 93 macro network() (in module pyphi.examples), 87 macro_state() (pyphi.macro.Blackbox method), 95 macro_state() (pyphi.macro.CoarseGrain method), 94 macro subsystem() (in module pyphi.examples), 87 macro_tpm() (pyphi.macro.CoarseGrain method), 94 macro_tpm_sbs() (pyphi.macro.CoarseGrain method), 94 MacroNetwork (class in pyphi.macro), 96 MacroSubsystem (class in pyphi.macro), 92 major_complex (in module pyphi.compute), 53 major_complex() (in module pyphi.compute.network), 56 make_mapping() (pyphi.macro.CoarseGrain method), 94 MapReduce (class in pyphi.compute.parallel), 57 marginal() (in module pyphi.distribution), 81 marginal_zero() (in module pyphi.distribution), 81 marginalize out() (in module pyphi.tpm), 123 max_entropy_distribution() (in module pyphi.distribution), 82 MaximallyIrreducibleCause (class in pyphi.models.mechanism), 105 MaximallyIrreducibleCause (in module pyphi.models), 98 MaximallyIrreducibleCauseOrEffect (class in pyphi.models.mechanism), 105 MaximallyIrreducibleCauseOrEffect module (in pyphi.models), 98 MaximallyIrreducibleEffect (class in pyphi.models.mechanism), 106 MaximallyIrreducibleEffect (in module pyphi.models), 98 MAXIMUM CACHE MEMORY PERCENTAGE (pyphi.conf.PyphiConfig attribute), 42 maybe put task() (pyphi.compute.parallel.MapReduce method), 58 MEASURE (pyphi.conf.PyphiConfig attribute), 41 MeasureRegistry (class in pyphi.distance), 78 mechanism (pyphi.models.actual_causation.AcRepertoireIrradueihility.enebyphi.subsystem.Subsystem attribute), 117 attribute), 99 mechanism (pyphi.models.actual causation.CausalLink attribute), 100 (pyphi.models.actual_causation.Event atmechanism tribute), 100 mechanism (pyphi.models.cuts.KPartition attribute), 103 mechanism (pyphi.models.cuts.Part attribute), 103 mechanism (pyphi.models.mechanism.Concept attribute), 106 attribute), 105

mechanism indices() (pyphi.actual.Transition method), 47 mechanism state (pyphi.models.mechanism.Concept attribute), 106 mechanism state() (pyphi.actual.Transition method), 47 mechanisms (pyphi.models.subsystem.CauseEffectStructure attribute), 107 memory full() (in module pyphi.cache), 51 method() (in module pyphi.cache), 53 mic() (pyphi.subsystem.Subsystem method), 121 MICECache() (in module pyphi.cache), 52 micro_indices (pyphi.macro.Blackbox attribute), 95 micro_indices (pyphi.macro.CoarseGrain attribute), 93 micro_network (pyphi.macro.MacroNetwork attribute), 96 micro_phi (pyphi.macro.MacroNetwork attribute), 96 mie() (pyphi.subsystem.Subsystem method), 121 min sia (pyphi.compute.subsystem.SystemIrreducibilityAnalysisConceptSt attribute). 60 mip (pyphi.models.mechanism.MaximallyIrreducibleCauseOrEffect attribute), 105 mip bipartitions() (in module pyphi.partition), 115 mip_partitions() (in module pyphi.partition), 115 MONGODB CONFIG (pyphi.conf.PyphiConfig attribute), 43 mp2q() (in module pyphi.distance), 80

Ν

Network (class in pyphi.network), 109 network (pyphi.actual.Transition attribute), 46 network (pyphi.macro.MacroNetwork attribute), 96 network (pyphi.models.subsystem.SystemIrreducibilityAnalysis attribute), 108 network (pyphi.subsystem.Subsystem attribute), 117 network() (in module pyphi.validate), 125 nexus() (in module pyphi.actual), 49 nice_true_ces() (in module pyphi.actual), 50 Node (class in pyphi.node), 111 node indices (pyphi.actual.Transition attribute), 46 node indices (pyphi.network.Network attribute), 109 node_labels (pyphi.actual.Transition attribute), 47 node labels (pyphi.macro.SystemAttrs attribute), 92 node_labels (pyphi.models.actual_causation.CausalLink attribute), 100 node_labels (pyphi.models.cuts.Bipartition attribute), 104 node_labels (pyphi.models.cuts.Cut attribute), 102 node_labels (pyphi.models.cuts.KPartition attribute), 103 node_labels (pyphi.models.cuts.Tripartition attribute), 104 mechanism (pyphi.models.mechanism.MaximallyIrreducible Gause Aveistics phi.models.mechanism.RepertoireIrreducibilityAnalysis attribute), 104

mechanism (pyphi.models.mechanism.RepertoireIrreducibility denators (pyphi.network.Network attribute), 110 attribute), 104 node_labels() (in module pyphi.validate), 125

node_states() (in module pyphi.validate), 126 nodes (pyphi.macro.SystemAttrs attribute), 92 nodes (pyphi.subsystem.Subsystem attribute), 117 nodes2indices() (in module pyphi.convert), 71 nodes2state() (in module pyphi.distribution), 81 normalize() (pyphi.models.cuts.KPartition method), 103 np_hash() (in module pyphi.utils), 124 np_hashable (class in pyphi.utils), 124 np_immutable() (in module pyphi.utils), 123	Part (in module pyphi.models), 98 part0 (pyphi.models.cuts.Bipartition attribute), 103 part1 (pyphi.models.cuts.Bipartition attribute), 103 partition (pyphi.macro.Blackbox attribute), 95 partition (pyphi.macro.CoarseGrain attribute), 93 partition (pyphi.models.actual_causation.AcRepertoireIrreducibilityAnalys attribute), 99 partition (pyphi.models.mechanism.RepertoireIrreducibilityAnalysis attribute), 104 partition() (in module pyphi.validate), 126
np_suppress (class in pyphi.distance), 79	PARTITION_TYPE (pyphi.conf.PyphiConfig attribute),
null_concept (pyphi.subsystem.Subsystem attribute), 121 null_cut (pyphi.subsystem.Subsystem attribute), 117 NullCut (class in pyphi.models.cuts), 102	45 partitioned_account (pyphi.models.actual_causation.AcSystemIrreducibility attribute), 101
num_states (pyphi.network.Network attribute), 109 NUMBER_OF_CORES (pyphi.conf.PyphiConfig at-	partitioned_ces (pyphi.models.subsystem.SystemIrreducibilityAnalysis attribute), 108
tribute), 42	partitioned_probability (pyphi.models.actual_causation.AcRepertoireIrredu attribute), 99
0	partitioned_probability() (pyphi.actual.Transition
OFF (in module pyphi.constants), 70 Option (class in pyphi.conf), 40 options() (pyphi.conf.Config class method), 41	method), 48 partitioned_repertoire (pyphi.models.mechanism.MaximallyIrreducibleCau attribute), 105
method), 60	Anatitioned neepersoire (pyphi.models.mechanism.RepertoireIrreducibilityAnattribute), 104
order_by() (pyphi.models.actual_causation.AcRepertoireIrr method), 99	RELEASE () (pyphi.actual.Transition method), 48
order_by() (pyphi.models.actual_causation.AcSystemIrredumethod), 101	newtitionellyspertoire() (pyphi.subsystem.Subsystem method), 119
order_by() (pyphi.models.actual_causation.CausalLink method), 100	PartitionRegistry (class in pyphi.partition), 114 partitions() (in module pyphi.partition), 112
order_by() (pyphi.models.mechanism.Concept method), 106	parts (pyphi.models.cuts.Bipartition attribute), 104 parts (pyphi.models.cuts.KPartition attribute), 103
order_by() (pyphi.models.mechanism.MaximallyIrreducible method), 105	phi (in module pyphi.compute), 54
order_by() (pyphi.models.mechanism.RepertoireIrreducibil method), 104	phi (pyphi.models.actual_causation.AcRepertoireIrreducibilityAnalysis
order_by() (pyphi.models.subsystem.CauseEffectStructure method), 107	attribute), 100 phi (pyphi.models.actual_causation.CausalLink at-
order_by() (pyphi.models.subsystem.SystemIrreducibilityA method), 108	nalysis tribute), 100 phi (pyphi.models.mechanism.Concept attribute), 106
output_indices (pyphi.macro.Blackbox attribute), 95	phi (pyphi.models.mechanism.MaximallyIrreducibleCauseOrEffect
outputs (pyphi.node.Node attribute), 111 outputs_of() (pyphi.macro.Blackbox method), 95 override() (pyphi.conf.Config method), 41	attribute), 105 phi (pyphi.models.mechanism.RepertoireIrreducibilityAnalysis attribute), 104
P	phi (pyphi.models.subsystem.SystemIrreducibilityAnalysis attribute), 108
pack() (pyphi.macro.SystemAttrs static method), 92 PARALLEL_COMPLEX_EVALUATION (pyphi.conf.PyphiConfig attribute), 42	phi() (in module pyphi.compute.subsystem), 60 phi() (pyphi.subsystem.Subsystem method), 121 phi_by_grain() (in module pyphi.macro), 97 phi_cause_mip() (pyphi.subsystem.Subsystem method),
PARALLEL_CONCEPT_EVALUATION (pyphi.conf.PyphiConfig attribute), 42	120 phi_effect_mip() (pyphi.subsystem.Subsystem method),
PARALLEL_CUT_EVALUATION (pyphi.conf.PyphiConfig attribute), 42 Part (class in pyphi.models.cuts), 103	121 phi_max() (pyphi.subsystem.Subsystem method), 121

which (much i models when the Course Effect Structure of	and in the second distribution of
phis (pyphi.models.subsystem.CauseEffectStructure at- tribute), 107	purview() (in module pyphi.distribution), 81 purview_indices() (pyphi.actual.Transition method), 47
PICK_SMALLEST_PURVIEW	purview_size() (in module pyphi.distribution), 81
(pyphi.conf.PyphiConfig attribute), 45	purview_state() (minioude pypin.distribution), 81 purview_state() (pyphi.actual.Transition method), 47
PICKLE_PROTOCOL (in module pyphi.constants), 70	PurviewCache (class in pyphi.cache), 53
possible_complexes (in module pyphi.compute), 54	pyphi.actual (module), 46
possible_complexes() (in module pypineoinpute), 94 module	pyphi.cache (module), 51
pyphi.compute.network), 55	pyphi.compute (module), 53
potential_purviews() (pyphi.actual.Transition method),	pyphi.compute.distance (module), 54
48	pyphi.compute.network (module), 54
potential_purviews() (pyphi.macro.MacroSubsystem	pyphi.compute.parallel (module), 56
method), 93	pyphi.compute.subsystem (module), 58
potential_purviews() (pyphi.network.Network method),	pyphi.conf (module), 38
110	pyphi.connectivity (module), 68
potential_purviews() (pyphi.subsystem.Subsystem	pyphi.constants (module), 70
method), 121	pyphi.convert (module), 70
powerset() (in module pyphi.utils), 124	pyphi.direction (module), 78
PRECISION (pyphi.conf.PyphiConfig attribute), 44	pyphi.distance (module), 78
prevention() (in module pyphi.examples), 90	pyphi.distribution (module), 81
print() (pyphi.models.subsystem.SystemIrreducibilityAnal	yşiyphi.examples (module), 82
method), 108	pyphi.exceptions (module), 90
PRINT_FRACTIONS (pyphi.conf.PyphiConfig at-	pyphi.jsonify (module), 90
tribute), 44	pyphi.macro (module), 92
probability (pyphi.models.actual_causation.AcRepertoireIn	
attribute), 99	pyphi.models.actual_causation (module), 98
probability() (pyphi.actual.Transition method), 47	pyphi.models.cuts (module), 102
process_result() (pyphi.actual.ComputeACSystemIrreducil	
method), 49	pyphi.models.subsystem (module), 107
process_result() (pyphi.compute.network.FindAllComplex	
method), 55	pyphi.node (module), 111
process_result() (pyphi.compute.network.FindIrreducibleC	
method), 56	pyphi.subsystem (module), 116
process_result() (pyphi.compute.parallel.MapReduce	pyphi.timescale (module), 122
method), 57	pyphi.tpm (module), 122
process_result() (pyphi.compute.subsystem.ComputeCause method), 58	pyphi.validate (module), 125
process_result() (pyphi.compute.subsystem.ComputeSyste	
method), 59	PyPhiJSONDecoder (class in pyphi.jsonify), 92
PROGRESS_BARS (pyphi.conf.PyphiConfig attribute),	PyPhiJSONEncoder (class in pyphi.jsonify), 92
44	r yr misorveneoder (class in pyphi.jsonny), 91
propagation_delay_network() (in module	R
pyphi.examples), 86	
proper_state (pyphi.subsystem.Subsystem attribute), 117	rebuild_system_tpm() (in module pyphi.macro), 92
psq2() (in module pyphi.distance), 80	redis_available() (in module pyphi.cache), 51 REDIS_CACHE (pyphi.conf.PyphiConfig attribute), 43
purview (pyphi.models.actual_causation.AcRepertoireIrred	REDIS_CACHE (pyphi.conf.ryphiConfig attribute), 43
attribute), 99	redis_init() (in module pyphi.cache), 51
purview (pyphi.models.actual_causation.CausalLink at-	RedisCache (class in pyphi.cache), 51
tribute), 100	RedisMICECache (class in pyphi.cache), 52
purview (pyphi.models.cuts.KPartition attribute), 103	register() (pyphi.distance.MeasureRegistry method), 79
purview (pyphi.models.cuts.Part attribute), 103	reindex() (in module pyphi.macro), 92
purview (pyphi.models.mechanism.MaximallyIrreducibleC	Cause Province Province (1, 22)
attribute), 105	reindex() (pyphi.macro.CoarseGrain method), 93
purview (pyphi.models.mechanism.RepertoireIrreducibility	Actel at f_connections() (in module pyphi.connectivity),
attribute), 104	68

	sia_concept_style() (in module				
pyphi.macro), 92	pyphi.compute.subsystem), 60				
	ecsineodefMacRo_NODES_WITH_SELFLOOPS_HAVE_PHI				
attribute), 105 (pyphi.conf.PyphiConfig attribute), 44					
repertoire (pyphi.models.mechanism.RepertoireIrreducibilityikna(pysphi.network.Network attribute), 109					
attribute), 104	size (pyphi.subsystem.Subsystem attribute), 117				
repertoire() (pyphi.actual.Transition method), 47	size() (pyphi.cache.DictCache method), 51				
repertoire() (pyphi.subsystem.Subsystem method), 119	size() (pyphi.cache.RedisCache static method), 51				
repertoire_distance() (in module pyphi.distance), 80	small_phi_ces_distance() (in module				
repertoire_shape() (in module pyphi.distribution), 81	pyphi.compute.distance), 54				
RepertoireIrreducibilityAnalysis (class in	small_phi_time (pyphi.models.subsystem.SystemIrreducibilityAnalysis				
pyphi.models.mechanism), 104	attribute), 108				
RepertoireIrreducibilityAnalysis (in module	snapshot() (pyphi.conf.Config method), 41				
pyphi.models), 98	sparse() (in module pyphi.timescale), 122				
REPR_VERBOSITY (pyphi.conf.PyphiConfig attribute),	sparse_time() (in module pyphi.timescale), 122				
44	start_parallel() (pyphi.compute.parallel.MapReduce				
reraise() (pyphi.compute.parallel.ExceptionWrapper	method), 57				
method), 57	state (pyphi.models.actual_causation.AcRepertoireIrreducibilityAnalysis				
residue_network() (in module pyphi.examples), 84	attribute), 99				
residue_subsystem() (in module pyphi.examples), 84	state (pyphi.subsystem.Subsystem attribute), 117				
reverse_bits() (in module pyphi.convert), 70	<pre>state2be_index() (in module pyphi.convert), 71</pre>				
reverse_elements() (in module pyphi.partition), 113	<pre>state2le_index() (in module pyphi.convert), 71</pre>				
ria (pyphi.models.actual_causation.CausalLink attribute),	state_by_node2state_by_state() (in module				
100	pyphi.convert), 74				
ria (pyphi.models.mechanism.MaximallyIrreducibleCause	OsEaffee_dby_state2state_by_node() (in module				
attribute), 105	pyphi.convert), 73				
rule110_network() (in module pyphi.examples), 88	state_length() (in module pyphi.validate), 126				
rule154_network() (in module pyphi.examples), 88	state_of() (in module pyphi.utils), 123				
run() (pyphi.compute.parallel.LogThread method), 58	state_probability() (pyphi.actual.Transition method), 47				
run() (pyphi.compute.parallel.MapReduce method), 58	state_reachable() (in module pyphi.validate), 126				
run_cm() (in module pyphi.timescale), 122	StateUnreachableError, 90				
run_parallel() (pyphi.compute.parallel.MapReduce	Subsystem (class in pyphi.subsystem), 116				
method), 58	subsystem (pyphi.compute.subsystem.ComputeCauseEffectStructure				
run_sequential() (pyphi.compute.parallel.MapReduce	attribute), 58				
method), 58	subsystem (pyphi.models.mechanism.Concept attribute),				
run_tpm() (in module pyphi.macro), 92	106				
<pre>run_tpm() (in module pyphi.timescale), 122</pre>	subsystem (pyphi.models.subsystem.SystemIrreducibilityAnalysis				
0	attribute), 108				
S	subsystem() (in module pyphi.validate), 126				
s2b() (in module pyphi.convert), 75	subsystems (in module pyphi.compute), 54				
s2l() (in module pyphi.convert), 75	subsystems() (in module pyphi.compute.network), 54				
sbn2sbs() (in module pyphi.convert), 77	system (pyphi.actual.Transition attribute), 46				
sbs2sbn() (in module pyphi.convert), 77	SYSTEM_CUTS (pyphi.conf.PyphiConfig attribute), 45				
set() (pyphi.cache.DictCache method), 51	system_repertoire_distance() (in module pyphi.distance),				
set() (pyphi.cache.DictMICECache method), 52	81				
set() (pyphi.cache.PurviewCache method), 53	SystemAttrs (class in pyphi.macro), 92				
set() (pyphi.cache.RedisCache method), 52	SystemIrreducibilityAnalysis (class in				
set() (pyphi.cache.RedisMICECache method), 52	pyphi.models.subsystem), 107				
sia (in module pyphi.compute), 54	SystemIrreducibilityAnalysis (in module pyphi.models),				
sia() (in module pyphi.actual), 49	98				
sia() (in module pyphi.compute.subsystem), 60	SystemIrreducibilityAnalysisConceptStyle (class in				
sia_bipartitions() (in module pyphi.compute.subsystem),	pyphi.compute.subsystem), 60				
59					

Т

true_events() (in module pyphi.actual), 50 time (pyphi.models.mechanism.Concept attribute), 106 time (pyphi.models.subsystem.SystemIrreducibilityAnalysis unconstrained_cause_repertoire() attribute), 108 (pyphi.actual.Transition method), 47 time_annotated() (in module pyphi.utils), 125 unconstrained_cause_repertoire() time_scale (pyphi.macro.MacroNetwork attribute), 96 time_scale() (in module pyphi.validate), 126 (pyphi.subsystem.Subsystem method), 119 to_2d() (in module pyphi.convert), 77 unconstrained_effect_repertoire() (pyphi.actual.Transition method), 47 to_2dimensional() (in module pyphi.convert), 73 unconstrained_effect_repertoire() to json() (pyphi.actual.Transition method), 47 (pyphi.models.actual_causation.Account (pyphi.subsystem.Subsystem method), 119 to json() unconstrained_probability() (pyphi.actual.Transition method), 101 to_json() (pyphi.models.actual_causation.AcRepertoireIrreducibilityAmethod), 47 unconstrained_repertoire() (pyphi.subsystem.Subsystem method), 100 to_json() (pyphi.models.actual_causation.AcSystemIrreducibilityAnalmethod), 119 uniform_distribution() (in module pyphi.distribution), 81 method), 101unorderable_unless_eq (pyphi.compute.subsystem.SystemIrreducibilityAna to_json() (pyphi.models.actual_causation.CausalLink method), 100 attribute), 60 unorderable_unless_eq (pyphi.models.actual_causation.AcRepertoireIrredu to_json() (pyphi.models.cuts.Bipartition method), 103 attribute), 99 to_json() (pyphi.models.cuts.Cut method), 102 unorderable_unless_eq (pyphi.models.actual_causation.AcSystemIrreducib to_json() (pyphi.models.cuts.KCut method), 103 attribute), 101 to_json() (pyphi.models.cuts.KPartition method), 103 to_json() (pyphi.models.cuts.NullCut method), 102 unorderable_unless_eq (pyphi.models.actual_causation.CausalLink to_json() (pyphi.models.cuts.Part method), 103 attribute), 100 unorderable_unless_eq (pyphi.models.mechanism.Concept to_json() (pyphi.models.mechanism.Concept method), attribute), 106 107 attribute), 105 method), 105 to_json() (pyphi.models.mechanism.RepertoireIrreducibilityAnorthesiable_unless_eq (pyphi.mechanism.RepertoireIrreducibilityAnorthesiable_unless_eq (pyphi.mechanism.RepertoireIrreducibilityAnorthesiable_unless_eq (pyphi.mechanism.RepertoireIrreducibilityAnorthesiable_unless_eq (pyphi.mechanism.RepertoireIrreducibilityAnorthesiable_unless_eq (pyphi.mechanism.RepertoireIrreducibilityAnorthesiable_unless_eq (pyphi.mechanism.RepertoireIrreducibilityAnorthesiable_unless_eq (pyphi.mechanism.RepertoireIrreducibilityAnorthesiable_unless_eq (pyphi.mechanism.RepertoireIrreducibilityAnorthesiable_unless_eq (pyphi.mechanism.RepertoireIrreducibilityAnorthesiable_unless_eq (pyphi.mech attribute), 104 method), 105 to_json() (pyphi.models.subsystem.CauseEffectStructure unorderable_unless_eq (pyphi.models.subsystem.SystemIrreducibilityAnalyzer) attribute), 108 method), 107 to_json() (pyphi.models.subsystem.SystemIrreducibilityAnallyses_SMALL_PHI_DIFFERENCE_FOR_CES_DISTANCE method), 108 (pyphi.conf.PyphiConfig attribute), 45 to_json() (pyphi.network.Network method), 110 V to_json() (pyphi.node.Node method), 111 to_json() (pyphi.subsystem.Subsystem method), 118 VALIDATE_CONDITIONAL_INDEPENDENCE to_md() (in module pyphi.convert), 76 (pyphi.conf.PyphiConfig attribute), 44 to_multidimensional() (in module pyphi.convert), 73 validate_parent_cache() (in module pyphi.cache), 52 to_nodes (pyphi.models.cuts.Cut attribute), 102 VALIDATE_SUBSYSTEM_STATES tpm (pyphi.network.Network attribute), 109 (pyphi.conf.PyphiConfig attribute), 44 tpm (pyphi.node.Node attribute), 111 W tpm (pyphi.subsystem.Subsystem attribute), 117 tpm() (in module pyphi.validate), 125 wedge_partitions() (in module pyphi.partition), 116 tpm_indices() (in module pyphi.tpm), 122 worker() (pyphi.compute.parallel.MapReduce static tpm_off (pyphi.node.Node attribute), 111 method), 57 tpm_on (pyphi.node.Node attribute), 111 WrongDirectionError, 90 tpm_size (pyphi.subsystem.Subsystem attribute), 117 Transition (class in pyphi.actual), 46 Х transition (pyphi.models.actual_causation.AcSystemIrreducibilityAnalysis xor_network() (in module pyphi.examples), 84 attribute), 101 xor_subsystem() (in module pyphi.examples), 85 transitions() (in module pyphi.actual), 49 Tripartition (class in pyphi.models.cuts), 104

true_ces() (in module pyphi.actual), 50