IAST Documentation

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This Python package, pyIAST, predicts mixed-gas adsorption isotherms from a set of pure-component gas adsorption isotherms in a nanoporous material using Ideal Adsorbed Solution Theory (IAST).

pyIAST characterizes a pure-component adsorption isotherm from a set of simulated or experimental data points by:

- 1. fitting an analytical model to the data [e.g., Langmuir, quadratic, BET, Sips, or Dual-site Langmuir Freundlich].
- 2. linearly interpolating the data.

Then, pyIAST performs IAST calculations to predict the mixed-gas adsorption isotherms on the basis of these purecomponent adsorption isotherm characterizations.

pyIAST can handle an arbitrary number of components.

Please see our article for theoretical details and consider citing our article if you used pyIAST in your research:

3. Simon, B. Smit, M. Haranczyk. pyIAST: Ideal Adsorbed Solution Theory (IAST) Python Package. Submitted to Computer Physics Communications.

For example, consider that we have pure-component methane and ethane adsorption isotherms in metal-organic framework IRMOF-1 at 298 K, shown in Fig. 1.

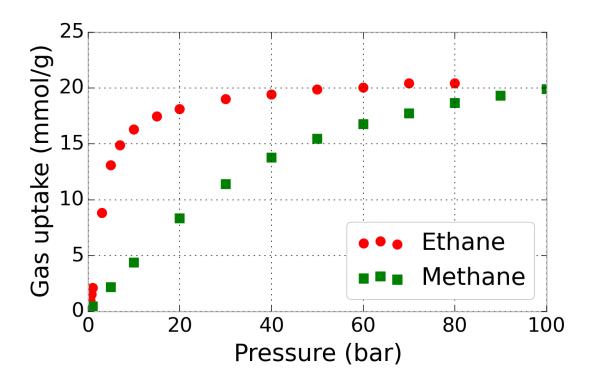


Fig. 1: Figure 1. Pure-component methane and ethane adsorption isotherms – the amount of gas adsorbed as a function of pressure– in metal-organic framework IRMOF-1. Simulated data.

Using the pure-component isotherm data in Fig. 1, pyIAST can predict the methane and ethane uptake in IRMOF-1 in the presence of a *mixture* of ethane and methane at 298 K under a variety of compositions. For example, for a mixture at 65.0 bar, Fig. 2 shows that the mixed-gas adsorption isotherms in IRMOF-1 predicted by pyIAST (lines) agree with binary component Grand-canonical Monte Carlo simulations (points).

To ask a question, request an additional feature, report a bug, or suggest an improvement, submit an issue on Github or discuss on Gitter.

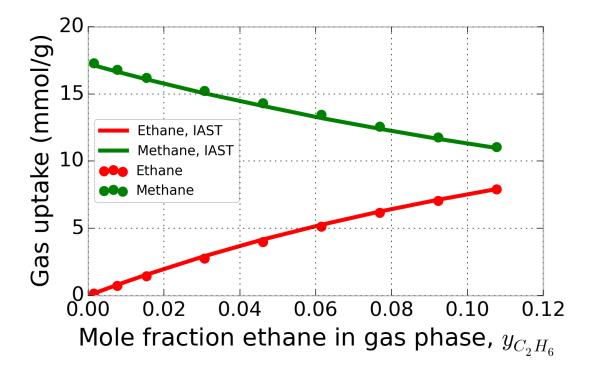


Fig. 2: Figure 2. Methane and ethane adsorption in IRMOF-1 in the presence of a mixture of methane and ethane at 65.0 bar and 298 K. The x-axis shows the composition of ethane in the mixture. The data points are from binary grand-canonical Monte Carlo simulations; the lines are from pyIAST.

Installation

To install pyIAST, use the Python package manager pip:

sudo pip install pyiast

pyIAST runs on Python 2.6 and 2.7.

As an alternative method to install pyIAST, clone the repository on Github. *cd* into the main directory *pyIAST* and run the *setup.py* script in the terminal:

sudo python setup.py install

If on Windows, run the setup file from a command prompt (Start -> Accessories):

setup.py install

New to Python?

If new to Python, I *highly* recommend working in the IPython Notebook; test scripts and tutorials for this code are written in IPython Notebooks. The instructions for getting started with Python for scientific computing are here.

pyIAST tutorial

For this tutorial on pyIAST, enter the */test* directory of pyIAST. While you can type this code into the Python shell, I highly recommend instead opening an IPython Notebook. First, import pyIAST into Python after installation.

import pyiast

For our tutorial, we have the pure-component methane and ethane adsorption isotherm data for metal-organic framework IRMOF-1 in Fig 1. We seek to predict the methane and ethane uptake in the presence of a binary mixture of methane and ethane in IRMOF-1 at the same temperature. As an example for this tutorial, we seek to predict the methane and ethane uptake of IRMOF-1 in the presence a 5/95 mol % ethane/methane mixture at a total pressure of 65.0 bar and 298 K.

3.1 Import the pure-component isotherm data

First, we load the pure-component isotherm data into Python so we can pass it into pyIAST. The data in Fig. 1 (from single component grand-canonical Monte Carlo simulations) are present in the CSV files:

- IRMOF-1_ethane_isotherm_298K.csv
- IRMOF-1_methane_isotherm_298K.csv

To import this data into Python, use the *Pandas* package (documentation for Pandas). The following code will return a Pandas DataFrame instance, which is useful for storing and manipulating tabular data.

```
import pandas as pd
df_ch4 = pd.read_csv("IRMOF-1_methane_isotherm_298K.csv")
df_ch3ch3 = pd.read_csv("IRMOF-1_ethane_isotherm_298K.csv")
```

You can check that your data has loaded correctly by looking at the head of the DataFrame:

df_ch4.head()

The units for pressure and loading in both DataFrames must be consistent; loading of gas must be in a molar quantity for IAST to apply (e.g. mmol/g or mmol/cm³). pyIAST will then work with these units throughout.

To load data into a Pandas DataFrame that is not *CSV*, see the documentation for Pandas. Pandas is generally a very useful tool for manipulating data. See 10 Minutes to pandas.

3.2 Construct pure-component isotherm objects

Next, we use pyIAST to translate the pure-component methane and ethane adsorption isotherm data into a model, which we will subsequently feed into pyIAST's IAST calculator.

There are two different pure-component isotherm data characterizations in pyIAST:

- 1. pyiast.ModelIsotherm
- 2. pyiast.InterpolatorIsotherm

In the first, an analytical model (e.g. Langmuir) is fit to the data, and the isotherm thereafter is characterized by this fitted analytical model. In the second, pyIAST linearly interpolates the data and uses numerical quadrature to compute the spreading pressure, which is an integration involving the isotherm for IAST calculations.

Note that pyIAST allows you to mix isotherm models for an IAST calculation (e.g. use Langmuir for methane but interpolate for ethane).

For both *ModelIsotherm* and *InterpolatorIsotherm*, we construct the instance by passing the Pandas DataFrame with the pure-component adsorption isotherm data and the names of the columns that correspond to the loading and pressure.

3.2.1 Modellsotherm

Here, in the construction of the instance of a *ModelIsotherm*, the data fitting to the analytical model is done under the hood. As an example, to construct a *ModelIsotherm* using the Langmuir adsorption model for methane (see Fig. 1), we pass the DataFrame df_ch4 and the names (keys) of the columns that correspond to the loading and pressure. In *IRMOF-1_methane_isotherm_298K.csv*, the name of the loading and pressure column is *Loading(mmol/g)* and *Pressure(bar)*, respectively. (e.g., in Pandas, $df_ch4['Pressure(bar)']$ will return the column corresponding to the pressure.)

A Langmuir model has been fit to the data in df_ch4 . You can access a dictionary of the model parameters identified by least squares fitting to the data by:

```
ch4_isotherm.params # dictionary of identified parameters
# {'K': 0.021312451202830915, 'M': 29.208535025975138}
```

or print them:

```
ch4_isotherm.print_params() # print parameters
# Langmuir identified model parameters:
# K = 0.021312
# M = 29.208535
# RMSE = 0.270928487851
```

pyIAST will plot the isotherm data points and resuling model fit by:

pyiast.plot_isotherm(ch3ch3_isotherm)

To predict the loading at a new pressure using the identified model, for example at 40.0 bar, one can call:

```
ch4_isotherm.loading(40.0) # returns predicted loading at 40 bar.
# 13.441427980586377 (same units as in df_ch4, mmol/g)
```

or the reduced spreading pressure (used for IAST calculations) via:

```
ch4_isotherm.spreading_pressure(40.0)
# 18.008092685521699 (mmol/g)
```

pyIAST fits other models (see the list *pyiast._MODELS* for available models), for example, the quadratic isotherm model, by passing *model="Quadratic"* into the construction of the *ModelIsotherm* instance.

A nonlinear data-fitting routine is used in pyIAST to fit the model parameters to the data. pyIAST uses heuristics for starting guesses for these model parameters. But, you can pass your own parameter guesses in the form of a dictionary *param_guess* when you construct the instance. For example, to use 25.0 as a starting guess for the *M* parameter in the Langmuir model:

You may need to pass your own starting guess for the parameters if the default guesses in pyIAST were not good enough for convergence when solving the nonlinear equations of IAST. You can see the naming convention for model parameters in pyIAST in the dictionary *pyiast._MODEL_PARAMS* as well as in the documentation for the *ModelIsotherm* class at the end of this page. Further, you can change the method used to solve the IAST equations by passing e.g. *optimization_method="Powell"* if you encounter convergence problems. For a list of optimization methods, see the Scipy website.

3.2.2 InterpolatorIsotherm

The *InterpolatorIsotherm*, where pyIAST linearly interpolates the isotherm data, is constructed very similary to the *ModelIsotherm*, but now there is not a need to pass a string *model* to indicate which model to use.

This *InterpolatorIsotherm* object behaves analogously to the *ModelIsotherm*; for example *ch4_isotherm.loading(40.0)* returns the loading at 40.0 bar via linear interpolation and *pyiast.plot_isotherm(ch4_isotherm)* still plots the isotherm and linear interpolation. When we attempt to extrapolate beyond the data point with the highest pressure, the *ch4_isotherm* above will throw an exception.

The *InterpolatorIsotherm* has an additional, optional argument *fill_value* that tells us what loading to assume when we attempt to extrapolate beyond the highest pressure observed in the pure-component isotherm data. For example, if the isotherm looks reasonably saturated, we can assume that the loading at the highest pressure point is equal to the largest loading in the data:

3.2.3 Should I use Modellsotherm or Interpolatorlsotherm?

See the discussion in our manuscript:

3. Simon, B. Smit, M. Haranczyk. pyIAST: Ideal Adsorbed Solution Theory (IAST) Python Package. Submitted to Computer Physics Communications.

3.3 Peform an IAST calculation

Given the pure-component isotherm characterizations constructed with pyIAST, we now illustrate how to use pyIAST to predict gas uptake when the material is in equilibrium with a *mixture* of gases. We have *ch4_isotherm* as above and an analogously constructed pure-component ethane adsorption isotherm object *ch3ch3_isotherm*.

As an example, we seek the loading in the presence of a 5/95 mol% ethane/methane mixture at a temperature of 298 K [the same temperature as the pure-component isotherms] and a total pressure of 65.0 bar. The function pyiast.iast() takes as input the partial pressures of the gases in the mixture and a list of the pure-component isotherms characterized by pyIAST. For convenience, we define the total pressure first as *total_pressure* and the gas phase mole fractions as y.

```
total_pressure = 65.0 # total pressure (bar)
y = np.array([0.05, 0.95]) # gas mole fractions
# partial pressures are now P_total * y
# Perform IAST calculation
q = pyiast.iast(total_pressure * y, [ch3ch3_isotherm, ch4_isotherm], verboseflag=True)
# returns q = array([4.4612935, 13.86364776])
```

The function *pyiast.iast()* returns *q*, an array of component loadings at these mixture conditions predicted by IAST. Since we passed the ethane partial pressures and isotherm first, entry 0 will correspond to ethane; entry 1 will correspond to methane. The flag *verboseflag* will print details of the IAST calculation. When the result required an extrapolation of the pressure beyond the highest pressure observed in the data, pyIAST will print a warning to the user. It may be necessary to collect pure-component isotherm data at higher pressures for the conditions in which you are interested (see our manuscript).

3.4 Reverse IAST calculation

In reverse IAST, we specify the mole fractions of gas in the *adsorbed* phase and the total bulk gas pressure, then calculate the bulk gas composition that yields these adsorbed mole fractions. This is useful e.g. in catalysis, where one seeks to control the composition of gas adsorbed in the material.

As an example, we seek the bulk gas composition [at 298 K, the same temperature as the pure-component isotherms] that will yield a 20/80 mol% ethane/methane mixture in the *adsorbed phase* at a total bulk gas pressure of 65.0. The code for this is:

```
total_pressure = 65.0 # total pressure (bar)
x = [0.2, 0.8] # list/array of desired mole fractions in adsorbed phase
y, q = pyiast.reverse_iast(x, total_pressure, [ch3ch3_isotherm, ch4_isotherm])
# returns (array([ 0.03911984,  0.96088016]), array([ 3.62944368,  14.51777472]))
```

which will return y, the required bulk gas phase mole fractions, and q, an array of component loadings at these mixture conditions predicted by IAST. Entry 0 will correspond to ethane; entry 1 will correspond to methane.

A variant of this tutorial, where we generate Fig. 2, is available in this IPython Notebook.

Theory

Ideal Adsorbed Solution Theory was developed by Myers and Prausnitz:

A. L. Myers and J. M. Prausnitz (1965). Thermodynamics of mixed-gas adsorption. AIChE Journal, 11(1), 121-127.

In our IAST calculations, we follow the method to solve the equations outlined in the more accessible reference:

A. Tarafder and M. Mazzotti. A method for deriving explicit binary isotherms obeying ideal adsorbed solution theory. Chem. Eng. Technol. 2012, 35, No. 1, 102-108.

We provide an accessible derivation of IAST and discuss practical issues in applying IAST in our manuscript:

C. Simon, B. Smit, M. Haranczyk. pyIAST: Ideal Adsorbed Solution Theory (IAST) Python Package. Submitted to Computer Physics Communications.

Tests

In the /test directory, you will find IPython Notebooks that test pyIAST in various ways.

5.1 Methane/ethane mixture test

'test/Methane and ethane test.ipynb'

This IPython Notebook compares pyIAST calculations to binary component grand-canonical Monte Carlo simulations for a methane/ethane mixture. This notebook reproduces Fig. 2, which confirms that pyIAST yields component loadings consistent with the binary grand-canonical Monte Carlo simulations.

5.2 Isotherm fitting tests

test/Isotherm tests.ipynb

This IPython Notebook generates synthetic data for each isotherm model, stores the data in a Pandas DataFrame, and uses pyIAST to construct a *ModelIsotherm* using this data; this notebook checks for consistency between the identified model parameters and those used to generate the synthetic data. This ensures that the data fitting routine in pyIAST is behaving correctly.

5.3 Competitive Langmuir adsorption

test/Test IAST for Langmuir case.ipynb

In that case that the pure-component adsorption isotherm $L_i(P)$ for species *i* follows a Langmuir isotherm with saturation loading *M* and Langmuir constant K_i :

$$L_i(P) = M \frac{K_i P}{1 + K_i P},$$

i.e. equal saturation loadings among all components, it follows from IAST that the mixed gas adsorption isotherm $N_i(p_i)$ follows the competitive Langmuir model:

$$N_i(p_i) = M \frac{K_i p_i}{1 + \sum_j K_j p_j}.$$

In this IPython Notebook, we generate synthetic data that follows three Langmuir adsorption isotherm models with the same saturation loading but different Langmuir constants. We then use pyIAST to predict the mixed gas adsorption isotherm and check that it is consistent with the competitive Langmuir adsorption model above.

Class documentation and details

This module contains objects to characterize the pure-component adsorption isotherms from experimental or simulated data. These will be fed into the IAST functions in pyiast.py.

Class to characterize pure-component isotherm data with an analytical model. Data fitting is done during instantiation.

Models supported are as follows. Here, L is the gas uptake, P is pressure (fugacity technically).

•Langmuir isotherm model

$$L(P) = M \frac{KP}{1 + KP},$$

•Quadratic isotherm model

$$L(P) = M \frac{(K_a + 2K_b P)P}{1 + K_a P + K_b P^2}$$

•Brunauer-Emmett-Teller (BET) adsorption isotherm

$$L(P) = M \frac{K_A P}{(1 - K_B P)(1 - K_B P + K_A P)}$$

•Sips adsorption isotherm

$$L(P) = M \frac{K^n P^n}{1 + K^n P^n}$$

•Dual-site Langmuir-Fruendlich (DSLF) adsorption isotherm

$$L(P) = M_1 \frac{(K_1 P)^{n_1}}{1 + (K_1 P)^{n_1}} + M_2 \frac{(K_2 P)^{n_2}}{1 + (K_2 P)^{n_2}}$$

•Henry's law. Only use if your data is linear, and do not necessarily trust IAST results from Henry's law if the result required an extrapolation of your data; Henry's law is unrealistic because the adsorption sites will saturate at higher pressures.

$$L(P) = K_H P$$

•Freundlich Isotherm. Do not necessarily trust IAST results from the Freundlich isotherm if the result required an extrapolation of your data; the Freundlich isotherm is unrealistic because the adsorption sites will saturate at higher pressures.

$$L(P) = KP^a$$

Instantiation. A *ModelIsotherm* class is instantiated by passing it the pure-component adsorption isotherm in the form of a Pandas DataFrame. The least squares data fitting is done here.

Parameters

- df DataFrame pure-component adsorption isotherm data
- loading_key String key for loading column in df
- pressure_key String key for pressure column in df
- param_guess Dict starting guess for model parameters in the data fitting routine
- method SciPy mini- optimization_method String in mization function to use in fitting model to data. See [here](http://docs.scipy.org/doc/scipy/reference/optimize.html#module-scipy.optimize).

Returns self

Return type ModelIsotherm

df = None

Pandas DataFrame on which isotherm was fit

loading (pressure)

Given stored model parameters, compute loading at pressure P.

Parameters pressure – Float or Array pressure (in corresponding units as df in instantiation)

Returns predicted loading at pressure P (in corresponding units as df in instantiation) using fitted model params in *self.params*.

Return type Float or Array

loading_key = None

name of column in df that contains loading

model = None

Name of analytical model to fit to data to characterize pure-component adsorption isotherm

pressure_key = None

name of column in df that contains pressure

print_params()

Print identified model parameters

spreading_pressure (pressure)

Calculate reduced spreading pressure at a bulk gas pressure P.

The reduced spreading pressure is an integral involving the isotherm L(P):

$$\Pi(p) = \int_0^p \frac{L(\hat{p})}{\hat{p}} d\hat{p},$$

which is computed analytically, as a function of the model isotherm parameters.

Parameters pressure – float pressure (in corresponding units as df in instantiation)

Returns spreading pressure, Π

Return type Float

class isotherms. InterpolatorIsotherm (df,

(df, loading_key=None, fill value=None) pressure key=None,

Interpolator isotherm object to store pure-component adsorption isotherm.

Here, the isotherm is characterized by linear interpolation of data.

Loading = 0.0 at pressure = 0.0 is enforced here automatically for interpolation at low pressures.

Default for extrapolating isotherm beyond highest pressure in available data is to throw an exception. Pass a value for *fill_value* in instantiation to extrapolate loading as *fill_value*.

__init__ (df, loading_key=None, pressure_key=None, fill_value=None)

Instantiation. InterpolatorIsotherm is instantiated by passing it the pure-component adsorption isotherm data in the form of a Pandas DataFrame.

Linear interpolation done with *interp1d* function in Scipy.

e.g. to extrapolate loading beyond highest pressure point as 100.0, pass fill_value=100.0.

Parameters

- **df** DataFrame adsorption isotherm data
- loading_key String key for loading column in df
- pressure_key String key for pressure column in df
- **fill_value** Float value of loading to assume when an attempt is made to interpolate at a pressure greater than the largest pressure observed in the data

Returns self

Return type InterpolatorIsotherm

df = None

Pandas DataFrame on which isotherm was fit

fill_value = None

value of loading to assume beyond highest pressure in the data

loading(pressure)

Linearly interpolate isotherm to compute loading at pressure P.

Parameters pressure – float pressure (in corresponding units as df in instantiation)

Returns predicted loading at pressure P (in corresponding units as df in instantiation)

Return type Float or Array

loading_key = None

name of loading column

pressure_key = None

name of pressure column

spreading_pressure (pressure)

Calculate reduced spreading pressure at a bulk gas pressure P. (see Tarafder eqn 4)

Use numerical quadrature on isotherm data points to compute the reduced spreading pressure via the integral:

$$\Pi(p) = \int_0^p \frac{q(\hat{p})}{\hat{p}} d\hat{p}.$$

In this integral, the isotherm $q(\hat{p})$ is represented by a linear interpolation of the data.

See C. Simon, B. Smit, M. Haranczyk. pyIAST: Ideal Adsorbed Solution Theory (IAST) Python Package. Computer Physics Communications.

Parameters pressure – float pressure (in corresponding units as df in instantiation)

Returns spreading pressure, Π

Return type Float

isotherms.plot_isotherm(isotherm, withfit=True, xlogscale=False, ylogscale=False, pressure=None)

Plot isotherm data and fit using Matplotlib.

Parameters

- isotherm pyIAST isotherm object
- withfit Bool plot fit as well
- **pressure** numpy.array optional pressure array to pass for plotting
- **xlogscale** Bool log-scale on x-axis
- **ylogscale** Bool log-scale on y-axis

isotherms.plot_isotherm (isotherm, withfit=True, xlogscale=False, ylogscale=False, pressure=None)

Plot isotherm data and fit using Matplotlib.

Parameters

- isotherm pyIAST isotherm object
- withfit Bool plot fit as well
- pressure numpy.array optional pressure array to pass for plotting
- **xlogscale** Bool log-scale on x-axis
- **ylogscale** Bool log-scale on y-axis

This module performs the heart of the IAST calculations, given the pure-component adsorption isotherm models from the *isotherms* module.

pyiast.iast (partial_pressures, isotherms, verboseflag=False, warningoff=False, adsorbed_mole_fraction_guess=None)

Perform IAST calculation to predict multi-component adsorption isotherm from pure component adsorption isotherms.

The material is now in equilibrium with a mixture of gases with partial pressures in the array *partial_pressures* in units corresponding to those passed in the list of isotherms.

Pass a list of pure-component adsorption isotherms.

Parameters

• **partial_pressures** – Array or list partial pressures of gas components, e.g. [5.0, 10.0] (bar)

- **isotherms** list pure-component adsorption isotherms. e.g. [methane_isotherm, ethane_isotherm]
- verboseflag Bool print off a lot of information
- warningoff Bool when False, warnings will print when the IAST calculation result required extrapolation of the pure-component adsorption isotherm beyond the highest pressure in the data
- **adsorbed_mole_fraction_guess** Array or List, starting guesses for adsorbed phase mole fractions that *pyiast.iast* solves for

Returns loadings: predicted uptakes of each component

Return type Array

pyiast.**print_selectivity** (*component_loadings*, *partial_pressures*) Calculate selectivity as a function of component loadings and bulk gas pressures

Parameters

- component_loadings numpy array of component loadings
- partial_pressures partial pressures of components

Perform reverse IAST to predict gas phase composition at total pressure *total_pressure* that will yield adsorbed mole fractions *adsorbed_mole_fractions*.

Pass a list of pure-component adsorption isotherms.

Parameters

- adsorbed_mole_fractions Array desired adsorbed mole fractions, e.g. [.5, .5]
- total_pressure Float total bulk gas pressure
- **isotherms** list of pure-component adsorption isotherms. e.g. [ethane_isotherm, methane_isotherm]
- verboseflag Bool print stuff
- **warningoff** Bool when False, warnings will print when the IAST calculation result required extrapolation of the pure-component adsorption isotherm beyond the highest pressure in the data
- **gas_mole_fraction_guess** Array or List, starting guesses for gas phase mole fractions that *pyiast.reverse_iast* solves for

Returns gas_mole_fractions, loadings: bulk gas mole fractions that yield

desired adsorbed mole fractions *adsorbed_mole_fractions* at *total_pressure*, adsorbed component loadings according to reverse IAST :rtype: Array, Array

CHAPTER 7

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