
pydgrid Documentation

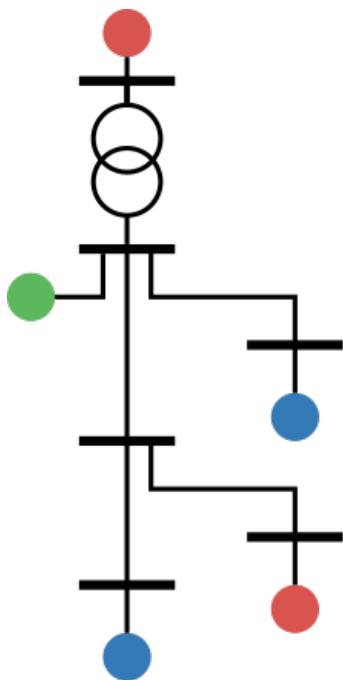
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pydgrid

Nov 26, 2018

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pydgrid

Python Distribution
System Simulator

pydgrid is an open source (MIT) electric distribution grid simulator. Grid elements are represented in phasor coordinates. Some futures are:

- Balanced and unbalanced power flow
- Time series simulation
- Time domain simulation

The [source code](#) is hosted on GitHub, and all contributions and feedback are more than welcome. You can test pydgrid in your browser using binder, a cloud Jupyter notebook server:

CHAPTER 1

Getting started

1.1 Requirements

pydgrid requires the following Python packages:

- NumPy, for basic numerical routines
- numba, for accelerating the code
- json, for reading network data
- matplotlib, for results plotting
- bokeh, for results visualization
- pytest, for running the tests from the package

pydgrid is usually tested on Linux and Windows on Python 3.5 and 3.6 against latest NumPy.

1.2 Installation

The easiest and fastest way to get the package up and running is to install anaconda with Python 3.5 or earlier.

Then you can install pydgrid from PyPI using pip:

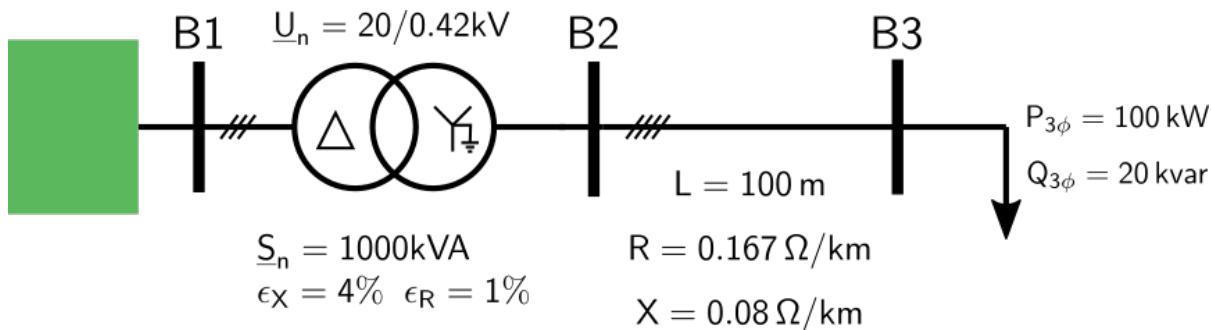
```
$ pip install pydgrid
```

Warning: It is recommended that you **never ever use sudo** with distutils, pip, setuptools and friends in Linux because you might seriously break your system [1][2][3][4]. Options are `per user directories`, `virtualenv` or `local installations`.

CHAPTER 2

User guide

The simplest use can be understood with an example. Suppose we want to calculate the power flow of the following system:



The following steps should be considered:

1. Import modules
2. Define or load grid parameters
3. Generate a grid instance
4. Read grid parameters
5. Run power flow
6. Post process results
7. Plot results

2.1 Import modules

First of all, we have to import the relevant modules and classes:

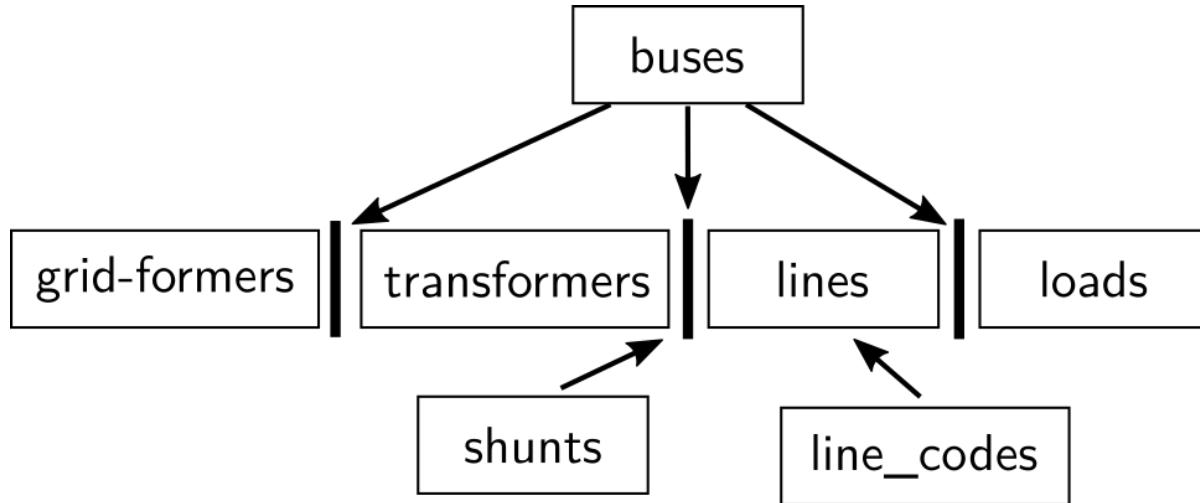
```
import numpy as np
from pydgrid import grid
```

2.2 Define or write grid parameters

The network can be introduced in two ways:

- Python dictionary
- json file with the same structure as in the case of the previous python dictionary

For the proposed system example the following elements from pydgrid should be considered:



```
data = {
    "buses": [
        {"bus": "B1", "pos_x": 0, "pos_y": 0, "units": "m", "U_kV": 20.0}
    ],
    "grid_formers": [
        {"bus": "B1",
         "bus_nodes": [1, 2, 3], "deg": [0, -120, -240],
         "kV": [11.547, 11.547, 11.547]}
    ],
    "transformers": [
        {"bus_j": "B1", "bus_k": "B2", "S_n_kVA": 1000.0, "U_j_kV": 20, "U_k_kV": 0.42,
         "R_cc_pu": 0.01, "X_cc_pu": 0.04, "connection": "Dyn11",
         "conductors_j": 3, "conductors_k": 4},
    ],
    "lines": [
        {"bus_j": "B2", "bus_k": "B3", "code": "lv_cu_150", "m": 100.0},
    ],
    "loads": [
        {"bus": "B3", "kVA": 300.0, "pf": 0.85, "type": "3P+N"}
    ]
}
```

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```
"shunts": [
    {"bus": "B2", "R": 0.001, "X": 0.0, "bus_nodes": [4, 0]}
],
"line_codes":
    {"lv_cu_150": {"Rph": 0.167, "Xph": 0.08, "Rn": 0.167, "Xn": 0.08}}
}
```

2.3 Generate a grid instance

```
grid_1 = grid()
```

2.4 Read grid parameters

```
grid_1.read(data)
```

2.5 Execute power flow

```
grid_1.pf()
```

2.6 Plot results

In the case of using jupyter notebook results can be visualized with a bokeh plot that includes hover tools.

```
from pydgrid.plot_bokeh import plot_results
plot_results(grid_1)
```

An on-line working jupyter notebook with the same example can be obtained here:

CHAPTER 3

Definitions

3.1 Buses and Nodes

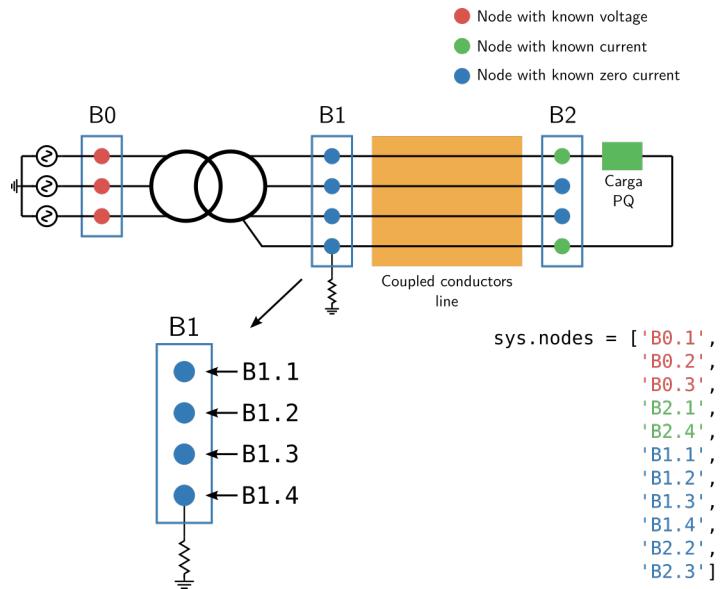
to_do

3.2 Nodes order

The nodes order in the voltages and currents vectors V_{node} and I_{node} is as follows:

- nodes with grid formers (known voltages)
- nodes with loads or greed feeders (known currents)
- transition nodes (zeros current injections)

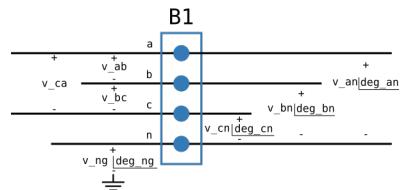
3.2.1 Example



V_known has the nodes with grid formers sources V_unknown has the rest of the nodes

V_sorted ... Buses order is as defined in the key buses of the .json file or data dictionary.

3.3 Buses results voltages

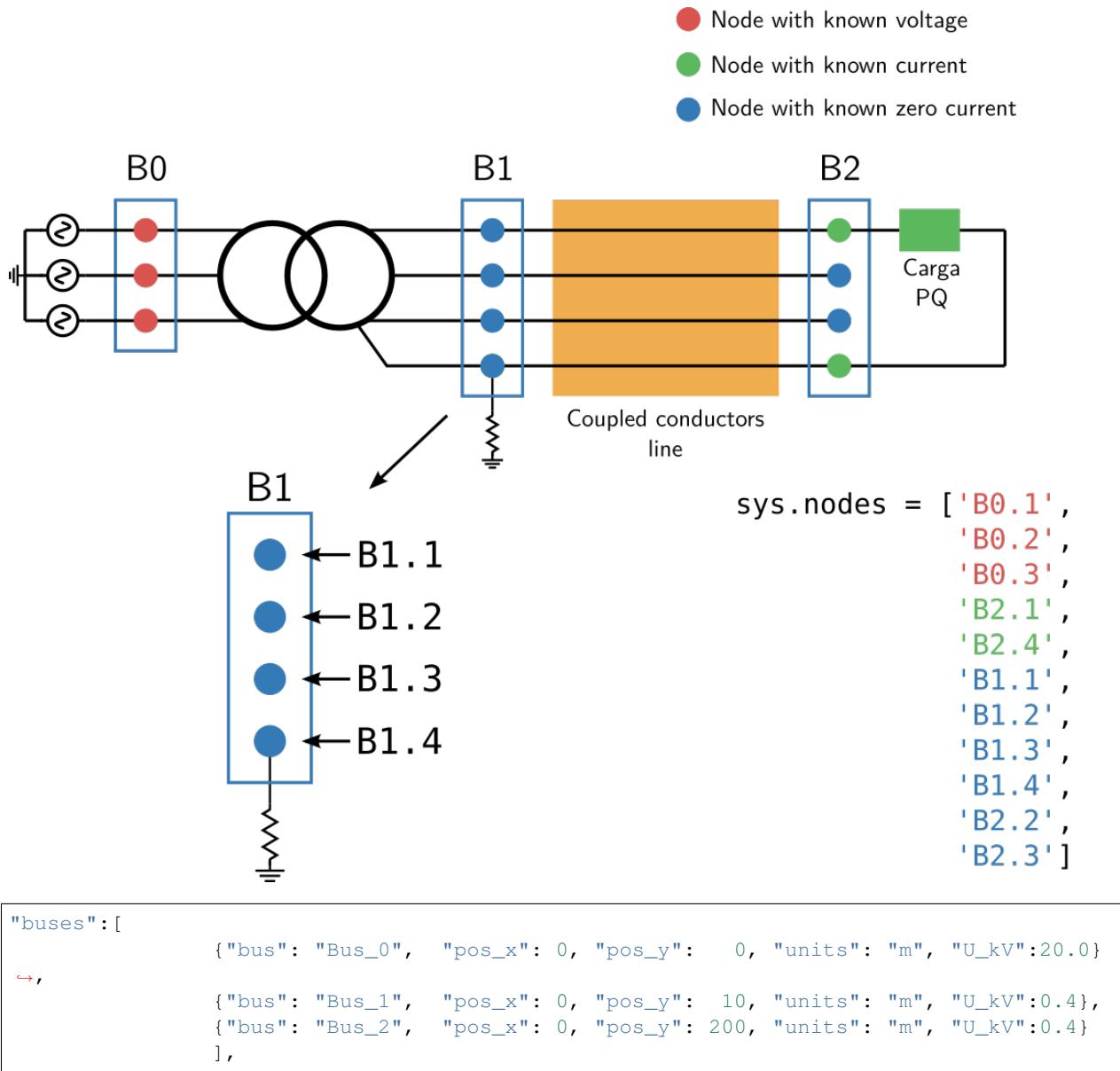


CHAPTER 4

Elements

4.1 Buses

Buses are composed by nodes.



where:

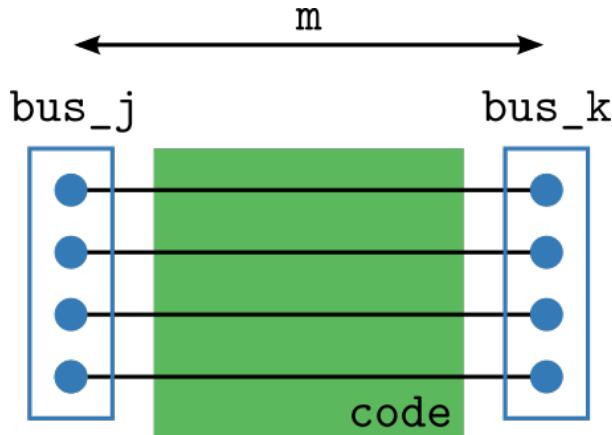
- "bus": name of the bus
- "pos_x": x position of the bus
- "pos_y": y position of the bus
- "units": units for positions (only m is available)
- "U_kV": RMS phase-phase base voltage (kV)

4.1.1 Indices and tables

- genindex
- modindex

- search

4.2 Lines



```
"lines": [
    {"bus_j": "Bus_1", "bus_k": "Bus_2", "code": "UG1", "m": 200.0}
]
```

where:

- "bus_j": name of the j bus
- "bus_k": name of the k bus
- "code": line code
- "m": line length in meters

4.3 Line codes

Two types of lines models can be considered:

- Serie Impedance (only R and X)
- PI Section Line (R, X and shunt C)

Line parameters can be introduced as:

- Sequence coordinates
- Primitive matrices
- Unitary voltage drop for p.f.= 1.0 and p.f.= 0.8

4.3.1 Serie impedance sequence parameters

Sequence coordinates

```
"line_codes":  
    { "mv_al_50": { "R1":0.8, "X1": 0.148, "R0":0.8, "X0": 0.148},  
     "mv_al_95": { "R1":0.403, "X1": 0.129, "R0":0.403, "X0": 0.129},  
     "mv_al_120": { "R1":0.321, "X1": 0.123, "R0":0.321, "X0": 0.321},  
     "mv_al_185": { "R1":0.209, "X1": 0.113, "R0":0.209, "X0": 0.209},  
     "mv_al_300": { "R1":0.128, "X1": 0.105, "R0":0.128, "X0": 0.128}  
    }
```

where:

- "R1": Positive sequence resistance (Ω/km)
- "X1": Positive sequence reactance (Ω/km)
- "R0": Zero sequence resistance (Ω/km)
- "X0": Zero sequence reactance (Ω/km)

Primitive matrices

```
"line_codes":  
    { "UG1":  
        { "R": [[ 0.211,  0.049,  0.049,  0.049],  
                [ 0.049,  0.211,  0.049,  0.049],  
                [ 0.049,  0.049,  0.211,  0.049],  
                [ 0.049,  0.049,  0.049,  0.211]],  
         "X": [[ 0.747,  0.673,  0.651,  0.673],  
                [ 0.673,  0.747,  0.673,  0.651],  
                [ 0.651,  0.673,  0.747,  0.673],  
                [ 0.673,  0.651,  0.673,  0.747]]  
        },  
     "UG3":  
        { "R": [[ 0.871,  0.049,  0.049,  0.049],  
                [ 0.049,  0.871,  0.049,  0.049],  
                [ 0.049,  0.049,  0.871,  0.049],  
                [ 0.049,  0.049,  0.049,  0.871]],  
         "X": [[ 0.797,  0.719,  0.697,  0.719],  
                [ 0.719,  0.797,  0.719,  0.697],  
                [ 0.697,  0.719,  0.797,  0.719],  
                [ 0.719,  0.697,  0.719,  0.797]]  
        }  
    }
```

where:

- "R": Resistance primitive (Ω/km)
- "X": Reactance primitive (Ω/km)

Unitary voltage drop

```
"line_codes":  
    {  
        "lv_cu_150": { "u90_pf10":0.27, "u90_pf08":0.31, 'T_deg':90.0, 'alpha':0.004},  
        "lv_cu_240": { "u90_pf10":0.17, "u90_pf08":0.27, 'T_deg':90.0, 'alpha':0.004}  
    }
```

where:

- "u90_pf10": Unitary voltage drop with load $\cos(\phi) = 1.0$ at 90°C (V/(km A))
- "u90_pf08": Unitary voltage drop with load $\cos(\phi) = 0.8$ at 90°C (V/(km A))
- "T_deg": Current conductor temperature (°C)
- "alpha": Temperature coefficient (1/°C)

PI section sequence parameters

```
"line_codes":
{
    "mv_cu_50_pi": {"R1":0.387, "X1": 0.152, "R0":0.387, "X0": 0.152, "C_1_muF":0.135, "C_0_muF":0.135},
    "mv_cu_95_pi": {"R1":0.193, "X1": 0.136, "R0":0.193, "X0": 0.136, "C_1_muF":0.175, "C_0_muF":0.175},
    "mv_cu_120_pi": {"R1":0.153, "X1": 0.132, "R0":0.153, "X0": 0.132, "C_1_muF":0.186, "C_0_muF":0.186},
    "mv_cu_185_pi": {"R1":0.099, "X1": 0.121, "R0":0.099, "X0": 0.121, "C_1_muF":0.226, "C_0_muF":0.226},
    "mv_cu_300_pi": {"R1":0.060, "X1": 0.112, "R0":0.060, "X0": 0.112, "C_1_muF":0.275, "C_0_muF":0.275}
}
```

where:

- "R1": Positive sequence resistance (Ω/km)
- "X1": Positive sequence reactance (Ω/km)
- "R0": Zero sequence resistance (Ω/km)
- "X0": Zero sequence reactance (Ω/km)
- "C_1_muF": Zero sequence resistance ($\mu\text{F}/\text{km}$)
- "C_0_muF": Zero sequence reactance ($\mu\text{F}/\text{km}$)

Serie impedance primitives

PI section sequence parameters

```
"line_codes":
{
    "K1":
        {"R": [[0.8667, 0.2955, 0.2907],
               [0.2955, 0.8837, 0.2992],
               [0.2907, 0.2992, 0.8741]],
         "X": [[2.0417, 0.9502, 0.7290],
               [0.9502, 1.9852, 0.8023],
               [0.7290, 0.8023, 2.0172]],
         "B_mu": [[10.7409, -3.4777, -1.3322],
                   [-3.4777, 11.3208, -2.2140],
                   [-1.3322, -2.2140, 10.2104]]}
}
```

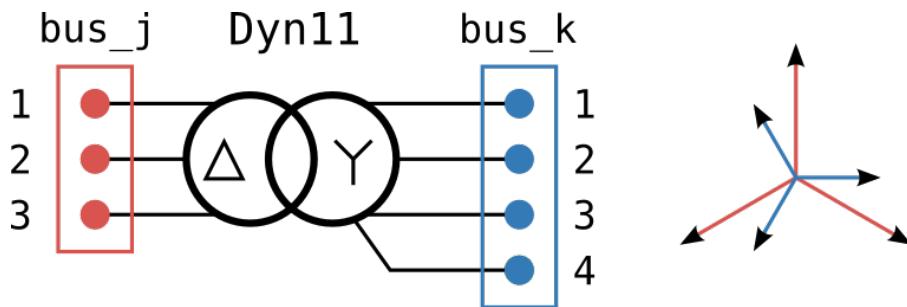
where:

- "R": Resistance primitive (Ω/km)
- "X": Reactance primitive (Ω/km)
- "B_mu": Zero sequence resistance ($\mu\text{S}/\text{km}$)

4.4 Transformers

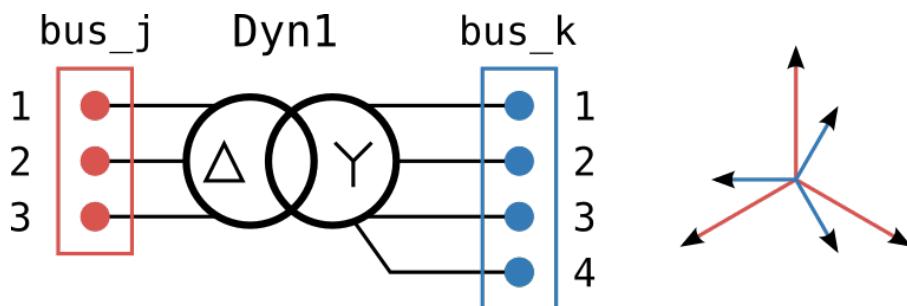
Transformers are modeled as in [T1].

4.4.1 Dyn11



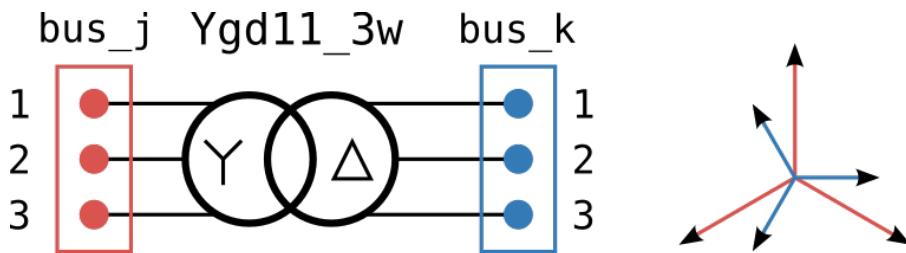
```
"transformers": [  
    {"bus_j": "Bus_0", "bus_k": "Bus_1", "S_n_kVA": 1000.0, "U_j_kv": 20, "U_k_kv": 0.42,  
     "R_cc_pu": 0.01, "X_cc_pu": 0.04, "connection": "Dyn11", "conductors_j": 3,  
     "conductors_k": 4},  
],
```

4.4.2 Dyn1



```
"transformers": [  
    {"bus_j": "Bus_0", "bus_k": "Bus_1", "S_n_kVA": 1000.0, "U_j_kv": 20, "U_k_kv": 0.42,  
     "R_cc_pu": 0.01, "X_cc_pu": 0.04, "connection": "Dyn1", "conductors_j": 3,  
     "conductors_k": 4},  
],
```

4.4.3 Ygd11_3w



```
"transformers": [
    {"bus_j": "Bus_0", "bus_k": "Bus_1", "S_n_kVA": 2500.0, "U_j_kv": 20, "U_k_kv": 0.69,
     "R_cc_pu": 0.01, "X_cc_pu": 0.04, "connection": "Ygd11_3w", "conductors_j": 3, "conductors_k": 3},
],
```

where:

- "bus_j": name of the j bus
- "bus_k": name of the k bus
- "pos_x": x position of the bus
- "pos_y": y position of the bus
- "S_n_kVA": based power in kVA
- "U_j_kv": HV side nominal RMS phase-phase voltage in kV
- "U_k_kv": LV side nominal RMS phase-phase voltage in kV
- "connection": connection type (see available connections)
- "conductors_j": HV side conductors
- "conductors_k": LV side conductors

4.5 Grid formers

Grid formers are considered as fix voltage sources in the power flow calculation.

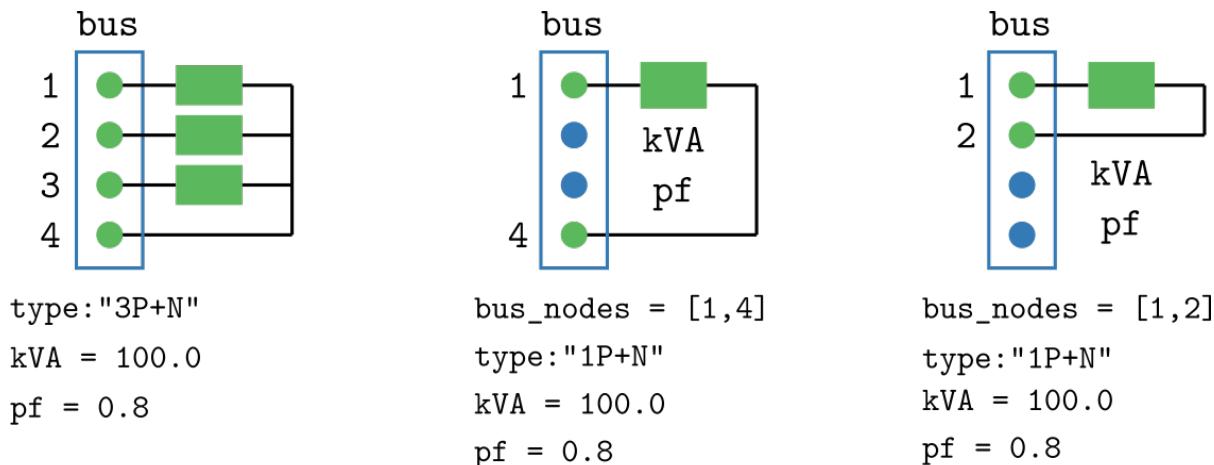
```
"grid_formers": [
    {"bus": "Bus_1",
     "bus_nodes": [1, 2, 3], "deg": [0, -120, -240],
     "kV": [0.23094, 0.23094, 0.23094]}
]
```

where:

- "bus": name of the bus
- "bus_nodes": list of nodes where the grid former source is connected
- "kV": phase-neutral RMS voltages list (kV)
- "deg": phase-neutral voltage angles list (deg)

4.6 Loads

Loads.



```
"loads": [
    {"bus": "Bus_2", "kVA": 50.0, "pf": 0.85, "type": "1P+N", "bus_nodes": [1,4]},
    {"bus": "Bus_2", "kVA": 30.0, "pf": 0.85, "type": "1P+N", "bus_nodes": [2,4]},
    {"bus": "Bus_2", "kVA": 20.0, "pf": 0.85, "type": "1P+N", "bus_nodes": [3,4]}
],
```

where:

- "bus": name of the bus
- "bus_nodes": list of nodes where the load is connected
- "type": available types are: - "3P+N": three phase load with neutral - "3P": three phase load without neutral
- "1P+N": single phase load connected between one phase and other or neutral
- "kVA": apparent power (kW)
- "pf": load power factor

4.7 Grid feeders

Grid feeders are considered as fix power or current sources in the power flow calculation.

```
"grid_feeders": [{"bus": "Bus_2", "bus_nodes": [1, 2, 3, 4],
                  "kW": [0.5, 0.5, 0.5], "kvar": [0, 0, 0],
                  "kA": [0, 0, 0], "phi_deg": [30, 30, 30]}]
```

where:

- "bus": name of the bus
- "bus_nodes": list of nodes where the grid former source is connected
- "kW": active power for each phase
- "kvar": reactive power for each phase
- "kA": RMS value of the current in each phase

- "phi_deg": angle between voltages and currents

4.7.1 Voltage Source Converter (VSC)

```
"grid_feeders": [{"bus": "Bus_2", "bus_nodes": [1, 2, 3],
                  "type": "vsc", "control_mode": "pq_leon",
                  "kW": 500.0, "kvar": 200.0,
                  "L": 400e-6, "R": 0.01, "V_dc": 800.0}
                 ]
```

4.8 Shunt elements

Impedances that can be connected between phases, phases and neutral and phases and neutral and ground.

```
"shunts": [
    {"bus": "Bus_1", "R": 0.001, "X": 0.0, "bus_nodes": [4, 0]},
    {"bus": "Bus_2", "R": 40.0, "X": 0.0, "bus_nodes": [4, 0]}
]
```

where:

- "bus": name of the bus
- "bus_node": list of nodes where the shunt element is connected
- "R": shunt element resistance (Ω)
- "X": shunt element reactance (Ω)

CHAPTER 5

Jupyter Notebooks

```
In [1]: import numpy as np
from pydgrid.pydgrid import grid
from pydgrid.pf import pf_eval,time_serie
```

5.1 Kersting book example 6.1

5.1.1 Data

```
In [2]: data = {
    "lines": [
        {"bus_j": "Bus_1", "bus_k": "Bus_2", "code": "Kersting", "m": 1609.34}
    ],
    "buses": [
        {"bus": "Bus_1", "pos_x": 10, "pos_y": 0, "units": "m", "U_kv": 12.47},
        {"bus": "Bus_2", "pos_x": 200, "pos_y": 0, "units": "m", "U_kv": 12.47}
    ],
    "grid_formers": [
        {"bus": "Bus_1", "bus_nodes": [1, 2, 3],
         "kV": [7.53869, 7.45125, 7.48512],
         "deg": [1.57248, -118.30047, 121.93184]}
    ],
    "loads": [
        {"bus": "Bus_2", "kVA": 6000.0, "pf": 0.9, "type": "3P"}
    ],
    "line_codes": [
        {"Kersting": [
            {"R": [
                [0.8667, 0.2955, 0.2907],
                [0.2955, 0.8837, 0.2992],
                [0.2907, 0.2992, 0.8741]
            ]},
            {"X": [
                [0.5, 0.5, 0.5],
                [0.5, 0.5, 0.5],
                [0.5, 0.5, 0.5]
            ]},
            {"B": [
                [0.0, 0.0, 0.0],
                [0.0, 0.0, 0.0],
                [0.0, 0.0, 0.0]
            ]},
            {"G": [
                [0.0, 0.0, 0.0],
                [0.0, 0.0, 0.0],
                [0.0, 0.0, 0.0]
            ]}
        ]},
        {"3P": [
            {"R": [
                [0.8667, 0.2955, 0.2907],
                [0.2955, 0.8837, 0.2992],
                [0.2907, 0.2992, 0.8741]
            ]},
            {"X": [
                [0.5, 0.5, 0.5],
                [0.5, 0.5, 0.5],
                [0.5, 0.5, 0.5]
            ]},
            {"B": [
                [0.0, 0.0, 0.0],
                [0.0, 0.0, 0.0],
                [0.0, 0.0, 0.0]
            ]},
            {"G": [
                [0.0, 0.0, 0.0],
                [0.0, 0.0, 0.0],
                [0.0, 0.0, 0.0]
            ]}
        ]}
    ]
}
```

```
"X": [
    [2.0417, 0.9502, 0.7290],
    [0.9502, 1.9852, 0.8023],
    [0.7290, 0.8023, 2.0172]
],
"B_mu": [
    [10.7409, -3.4777, -1.3322],
    [-3.4777, 11.3208, -2.2140],
    [-1.3322, -2.2140, 10.2104]
],
"unit": "miles"
}
}
```

5.1.2 Execute power flow

```
In [3]: grid_1 = grid()
grid_1.read(data) # Load data
grid_1.pf_solver = 2
grid_1.pf() # solve power flow
```

5.1.3 Graph with obtained results

```
In [4]: from pydgrid.plot_bokeh import plot_results
plot_results(grid_1)
```

Data type cannot be displayed: application/vnd.bokehjs_load.v0+json, application/javascript

Data type cannot be displayed: application/vnd.bokehjs_exec.v0+json, application/javascript

```
Out[4]: Figure(id='1003', ...)
```

5.1.4 Get element transformers results

```
In [6]: grid_1.buses
Out[6]: [{"bus": "Bus_1",
  "pos_x": 10,
  "pos_y": 0,
  "units": "m",
  "U_kV": 12.47,
  "N_nodes": 3,
  "v_an": 7538.69,
  "v_bn": 7451.25,
  "v_cn": 7485.12,
  "v_ng": 0.0,
  "deg_an": 1.57248,
  "deg_bn": -118.30046999999999,
  "deg_cn": 121.93184,
  "deg_ng": 0.0},
```

```
'v_ab': 12973.42498856987,
'v_bc': 12920.120310382239,
'v_ca': 13034.52171783379,
'p_a': 1858935.7393203387,
'p_b': 1835419.9515336645,
'p_c': 1839830.0481158614,
'q_a': 963491.4173624129,
'q_b': 956338.0192537266,
'q_c': 968270.9001076091},
{'bus': 'Bus_2',
'pos_x': 200,
'pos_y': 0,
'units': 'm',
'U_kv': 12.47,
'N_nodes': 3,
'v_an': 7199.551320077657,
'v_bn': 7199.557391530307,
'v_cn': 7199.55602482274,
'v_ng': 0.0,
'deg_an': -3.170444377827802e-05,
'deg_bn': -120.00002917542324,
'deg_cn': 119.9999628259816,
'deg_ng': 0.0,
'v_ab': 12469.993777213469,
'v_bc': 12469.998513070677,
'v_ca': 12469.992408860844,
'p_a': -1799998.8481163539,
'p_b': -1800000.327593055,
'p_c': -1800000.107596966,
'q_a': -871778.0011666914,
'q_b': -871778.8157972179,
'q_c': -871778.399022273}]]

In [ ]:
In [ ]:
In [3]: import numpy as np
        from pydgrid.pydgrid import grid
```

5.2 3 bus 4 wire system with transformer

5.2.1 Data

```
In [13]: data = {
    "buses": [
        {"bus": "B1", "pos_x": 0, "pos_y": 0, "units": "m", "U_kv": 20.0},
        {"bus": "B2", "pos_x": 10, "pos_y": 0, "units": "m", "U_kv": 0.4},
        {"bus": "B3", "pos_x": 100, "pos_y": 0, "units": "m", "U_kv": 0.4}
    ],
    "grid_formers": [
        {"bus": "B1",
         "bus_nodes": [1, 2, 3], "deg": [0, -120, -240],
         "kV": [11.547, 11.547, 11.547]}
    ],
    "transformers": [
        {"bus_j": "B1", "bus_k": "B2", "S_n_kVA": 1000.0, "U_j_kv": 20, "U_k_kv": 0.4,
         "R_cc_pu": 0.01, "X_cc_pu": 0.04, "connection": "Dyn11", "conductance": 0.001, "reactance": 0.001, "series_resistance": 0.001, "series_reactance": 0.001, "shunt_resistance": 0.001, "shunt_reactance": 0.001, "angle_deg": 0, "angle_radian": 0, "status": 1}
    ]
}
```

```
        ],
    "lines": [
        {"bus_j": "B2", "bus_k": "B3", "code": "lv_cu_150", "m": 100.0},
        ],
    "loads": [{"bus": "B3" , "kVA": 300.0/3, "pf": 0.85,"type":"3P+N"},  
      {"bus": "B3" , "kVA": 300.0/3, "pf": 0.85,"type":"1P+N", 'bus_nodes':[1,4]}],
    "shunts": [
        {"bus": "B2" , "R": 0.001, "X": 0.0, "bus_nodes": [4,0]}
        ],
    "line_codes":  
      {"lv_cu_150": { "Rph":0.167, "Xph":0.08, "Rn":0.167, "Xn": 0.08}
       }
    }
```

5.2.2 Execute power flow

```
In [14]: grid_1 = grid()  
grid_1.read(data) # Load data  
  
grid_1(pf) # solve power flow
```

5.2.3 Graph with obtained results

```
In [15]: from pydgrid.plot_bokeh import plot_results  
plot_results(grid_1)
```

Data type cannot be displayed: application/vnd.bokehjs_exec.v0+json, application/javascript

```
Out[15]: Figure(id='1309', ...)  
In [ ]:  
In [ ]:  
  
In [1]: import numpy as np  
import time  
from pydgrid.pydgrid import grid  
from pydgrid.pf import pf_eval,time_serie  
from bokeh.io import output_notebook, show  
from bokeh.plotting import figure  
from bokeh.models import ColumnDataSource, HoverTool  
from bokeh.io import push_notebook  
from bokeh.resources import INLINE  
output_notebook(INLINE)
```

Data type cannot be displayed: application/vnd.bokehjs_load.v0+json, application/javascript

5.3 907 bus 3 wire system with transformer

5.3.1 Execute power flow

```
In [2]: sys1 = grid()
        sys1.read('n1_f1.json')    # Load data
        sys1.read_load_shapes('n1_f1_load_shapes.json')
        sys1.pf_solver = 2
        sys1.pf()    # solve power flow

        sys1.get_v()      # post process voltages
        sys1.get_i()      # post process currents
```

5.3.2 Graph with obtained results

```
In [7]: sys1.s_radio_scale =0.5
        sys1.s_radio_min =5
        sys1.s_radio_max =100
        sys1.snapshot(60*60*12)
        sys1.pf()
        sys1.get_v()      # post process voltages
        sys1.get_i()      # post process currents
        sys1.bokeh_tools()

p_grid = figure(width=900, height=800,
                 title='3 bus 4 wire system with transformer')

# lines:
source = ColumnDataSource(sys1.line_data)
lin = p_grid.multi_line(source=source, xs='x_s', ys='y_s', color="red", alpha=0.5, line_width=2)

# buses:
source = ColumnDataSource(sys1.bus_data)
cr = p_grid.circle(source=source, x='x', y='y', size='s_radio', color="s_color", alpha=0.5)

p_grid.add_tools(HoverTool(renderers=[lin], tooltips=sys1.line_tooltip))
p_grid.add_tools(HoverTool(renderers=[cr], tooltips=sys1.bus_tooltip))

def update_grid(t_h=0.0):
    sys1.snapshot(60*60*t_h)

    sys1.get_v()
    sys1.get_i()
    sys1.bokeh_tools()

    source.data = sys1.bus_data
    push_notebook()

#p_grid = gridplot([[p], [p_2]])
show(p_grid, notebook_handle=True)
```

Data type cannot be displayed: application/vnd.bokehjs_exec.v0+json, application/javascript

```
Out[7]: <bokeh.io.notebook.CommsHandle at 0x7fe010a07208>
In [8]: from ipywidgets import interact
         interact(update_grid, t_h=(0, 24, 0.01), continuous_update=False)
interactive(children=(FloatSlider(value=0.0, description='t_h', max=24.0, step=0.01), Output()), _dom_classes=['bk-root'])
Out[8]: <function __main__.update_grid(t_h=0.0)>
```

5.3.3 Interaction

```
In [5]: p = figure(width=600, height=300,
                  title='Voltage vs load powers',
                  y_range = [0.95,1.01], #x_range = [50,-300],
                  x_axis_label='Distance (m)',
                  y_axis_label='Voltage (V)')
source = ColumnDataSource(sys1.bus_data)
#cr = p1.circle(source=source, x='y', y='v_an_pu', size=15, color="red", alpha=0.5)
p.circle(source=source, x='x', y='v_an_pu', size=15, color="red", alpha=0.5)
p.circle(source=source, x='x', y='v_bn_pu', size=15, color="green", alpha=0.5)
p.circle(source=source, x='x', y='v_cn_pu', size=15, color="blue", alpha=0.5)

#p1.circle(source=source, x='y', y='v_bn_pu', size=15, color="green", alpha=0.5)
#p.circle(source=source, x='y', y='v_cn', size=15, color="blue", alpha=0.5)
#p.line([-300, 50], [231*1.05, 231*1.05], color='red', line_width=5)
#p.line([-300, 50], [231*0.90, 231*0.90], color='blue', line_width=5)
#p.add_tools(HoverTool(renderers=[cr], tooltips=sys1.bus_tooltip))

def update(t_h=0.0):
    sys1.snapshot(60*60*t_h)

    sys1.get_v()
    sys1.get_i()
    sys1.bokeh_tools()

    source.data = sys1.bus_data
    push_notebook()

#p_grid = gridplot([[p], [p_2]])
show(p, notebook_handle=True)
```

Data type cannot be displayed: application/vnd.bokehjs_exec.v0+json, application/javascript

```
Out[5]: <bokeh.io.notebook.CommsHandle at 0x7fe01c26fda0>
In [6]: from ipywidgets import interact
         interact(update, t_h=(0, 24, 0.01))
A Jupyter Widget
Out[6]: <function __main__.update>
In []:
In []:
```

```
In [11]: import numpy as np
        from pydgrid.pydgrid import grid
```

5.4 CIGRE LV European System

```
In [14]: grid_1 = grid()
        grid_1.read('cigre_europe_residential.json')    # Load data
        grid_1.pf()
```

5.4.1 Graph with obtained results

```
In [15]: from pydgrid.plot_bokeh import plot_results
        plot_results(grid_1)
```

Data type cannot be displayed: application/vnd.bokehjs_load.v0+json, application/javascript

Data type cannot be displayed: application/vnd.bokehjs_exec.v0+json, application/javascript

```
Out[15]: Figure(id='1310', ...)
```

5.4.2 Analysis using Pandas

```
In [16]: import pandas as pd
In [17]: df = pd.DataFrame()
        df['nodes'] = sys1.nodes
        df['I_node_m'] = np.abs(sys1.I_node)
        df['V_node_m'] = np.abs(sys1.V_node)
        #df['phi'] = np.angle(sys1.I_node, deg=True) - np.angle(sys1.V_node, deg=True)
        s = np.conjugate(sys1.I_node)*sys1.V_node
        df['p_kW'] = s.real/1000
        df['q_kVA'] = s.imag/1000

        df
```

```
Out[17]:   nodes      I_node_m      V_node_m      p_kW      q_kVA
0     R0.1    12.279686  11547.000000  133.228235  48.534983
1     R0.2    12.194776  11547.000000  132.224879  48.424213
2     R0.3    12.219433  11547.000000  132.822486  47.610666
3     R1.1    294.305597  226.183736 -63.206394 -20.883865
4     R1.2    294.318022  226.377454 -63.338571 -20.673117
5     R1.3    294.268246  227.024469 -63.455017 -20.892937
6     R1.4     0.129777    0.488038 -0.000018 -0.000061
7    R11.1    22.619924  221.082177 -4.751117 -1.560611
8    R11.2    22.542696  221.818706 -4.749990 -1.562532
9    R11.3    22.431808  222.842141 -4.748898 -1.560605
10   R11.4     0.111885    0.056907  0.000006 -0.000001
11   R15.1    82.678522  210.089330 -16.512848 -5.388732
12   R15.2    82.063130  211.381109 -16.463661 -5.463720
13   R15.3    81.216693  212.814945 -16.424028 -5.384451
14   R15.4     0.869274    0.627272  0.000537 -0.000093
15   R16.1    85.643246  214.560691 -17.470587 -5.695963
```

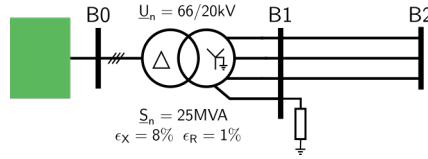
```
16  R16.2    84.972116   215.951166  -17.414043  -5.785090
17  R16.3    84.050216   217.432385  -17.366033  -5.692562
18  R16.4    0.947507    0.712773   0.000663  -0.000129
19  R17.1    55.050752   212.626217  -11.132419  -3.616867
20  R17.2    54.506010   214.317220  -11.080836  -3.697878
21  R17.3    53.767616   216.004660  -11.037499  -3.613848
22  R17.4    0.762900    1.009420   0.000755  -0.000153
23  R18.1    74.293759   211.633036  -14.954995  -4.853998
24  R18.2    73.514087   213.405120  -14.879548  -4.972049
25  R18.3    72.461012   215.150835  -14.816623  -4.849461
26  R18.4    1.089448    1.091264   0.001165  -0.000237
27  R2.1     0.000000    223.960103  0.000000  -0.000000
28  R2.2     0.000000    224.415535  -0.000000  0.000000
29  R2.3     0.000000    225.243290  0.000000  0.000000
...
45  R6.3     0.000000    219.425766  0.000000  0.000000
46  R6.4     0.000000    0.634712   0.000000  -0.000000
47  R7.1     0.000000    215.787875  0.000000  -0.000000
48  R7.2     0.000000    217.212013  -0.000000  0.000000
49  R7.3     0.000000    218.710282  0.000000  0.000000
50  R7.4     0.000000    0.741778   0.000000  -0.000000
51  R8.1     0.000000    214.889967  0.000000  -0.000000
52  R8.2     0.000000    216.422120  -0.000000  0.000000
53  R8.3     0.000000    217.994913  0.000000  0.000000
54  R8.4     0.000000    0.848844   0.000000  -0.000000
55  R9.1     0.000000    213.992505  0.000000  -0.000000
56  R9.2     0.000000    215.631806  -0.000000  0.000000
57  R9.3     0.000000    217.279749  0.000000  0.000000
58  R9.4     0.000000    0.956068   0.000000  -0.000000
59  R10.1    0.000000   213.476942  0.000000  -0.000000
60  R10.2    0.000000   215.178180  -0.000000  0.000000
61  R10.3    0.000000   216.869265  0.000000  0.000000
62  R10.4    0.000000   1.017707   0.000000  -0.000000
63  R12.1    0.000000   217.273533  0.000000  -0.000000
64  R12.2    0.000000   218.317615  -0.000000  0.000000
65  R12.3    0.000000   219.559931  0.000000  0.000000
66  R12.4    0.000000   0.367154   0.000000  -0.000000
67  R13.1    0.000000   214.877482  0.000000  -0.000000
68  R13.2    0.000000   216.004358  -0.000000  0.000000
69  R13.3    0.000000   217.310579  0.000000  0.000000
70  R13.4    0.000000   0.453609   0.000000  -0.000000
71  R14.1    0.000000   212.482806  0.000000  -0.000000
72  R14.2    0.000000   213.692088  -0.000000  0.000000
73  R14.3    0.000000   215.062258  0.000000  0.000000
74  R14.4    0.000000   0.540432   0.000000  -0.000000
```

```
[75 rows x 5 columns]
```

```
In [ ]:
```

5.5 Short circuits in MV line

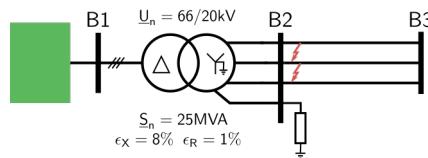
```
In [12]: import numpy as np
from pydgrid import grid
from pydgrid.plot_bokeh import plot_results
```



5.5.1 System

```
In [2]: data = {
    "transformers": [
        {"bus_j": "B0", "bus_k": "B1", "S_n_kVA": 250000.0, "U_j_kv": 66.0, "U_k_kv": 20.0,
         "R_cc_pu": 0.01, "X_cc_pu": 0.08, "connection": "Dyn1",
         "conductors_1": 3, "conductors_2": 4}
    ],
    "lines": [
        {"bus_j": "B1", "bus_k": "B2", "code": "mv_al_120", "m": 200.0}
    ],
    "buses": [
        {"bus": "B0", "pos_x": 0, "pos_y": 0, "units": "m", "U_kv": 66.0},
        {"bus": "B1", "pos_x": 30, "pos_y": 0, "units": "m", "U_kv": 20.0},
        {"bus": "B2", "pos_x": 200, "pos_y": 0, "units": "m", "U_kv": 20.0}
    ],
    "grid_formers": [
        {"bus": "B0",
         "bus_nodes": [1, 2, 3], "deg": [0, -120, -240],
         "kv": [38.105, 38.105, 38.105]}
    ],
    "grid_feeders": [{"bus": "B2", "bus_nodes": [1, 2, 3],
                      "kw": [0, 0, 0], "kvar": [0, 0, 0],
                      "ka": [0, 0, 0], "phi_deg": [30, 30, 30]}]
    ],
    "line_codes": {
        "mv_al_50": {"R1": 0.8, "X1": 0.148, "R0": 0.8, "X0": 0.148},
        "mv_al_95": {"R1": 0.403, "X1": 0.129, "R0": 0.403, "X0": 0.129},
        "mv_al_120": {"R1": 0.321, "X1": 0.123, "R0": 0.321, "X0": 0.321},
        "mv_al_185": {"R1": 0.209, "X1": 0.113, "R0": 0.209, "X0": 0.209},
        "mv_al_300": {"R1": 0.128, "X1": 0.105, "R0": 0.128, "X0": 0.128}
    },
    "shunts": [
        {"bus": "B1", "R": 1e12, "X": 0.0, "bus_nodes": [1, 0]},
        {"bus": "B1", "R": 1e-8, "X": 0.0, "bus_nodes": [1, 2]}, # applied fault
        {"bus": "B1", "R": 1e-8, "X": 0.0, "bus_nodes": [2, 3]}, # applied fault
    ]
}
```

5.5.2 Three phase short circuit

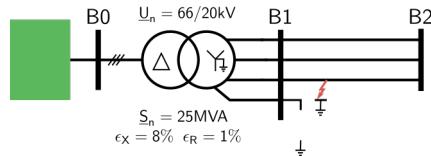


```
In [3]: grid_1 = grid()
grid_1.read(data) # Load data
```

```
grid_1.pf() # solve power flow
p=plot_results(grid_1)
```

Data type cannot be displayed: application/vnd.bokehjs_exec.v0+json, application/javascript

5.5.3 Phase ground fault (isolated neutral)

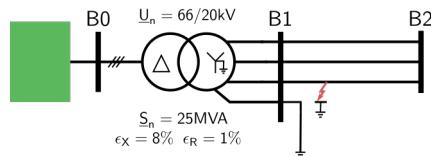


```
In [4]: data['shunts'] = [
    {"bus": "B1" , "R": 1e12, "X": 0.0, "bus_nodes": [1,0]},
    {"bus": "B1" , "R": 1e-8, "X": 0.0, "bus_nodes": [1,0]}, # applied fault
]

In [5]: grid_ph_g = grid()
grid_ph_g.read(data) # Load data
grid_ph_g.pf() # solve power flow
p=plot_results(grid_ph_g)
```

Data type cannot be displayed: application/vnd.bokehjs_exec.v0+json, application/javascript

5.5.4 Phase ground fault (grounded neutral)



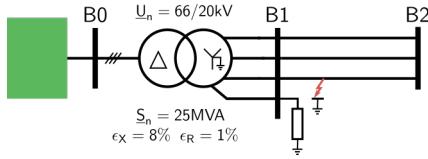
```
In [6]: data['shunts'] = [
    {"bus": "B1" , "R": 1e-12, "X": 0.0, "bus_nodes": [4,0]},
    {"bus": "B1" , "R": 1e-12, "X": 0.0, "bus_nodes": [1,0]}, # applied fault
]

In [7]: grid_ph_n = grid()
grid_ph_n.read(data) # Load data
grid_ph_n.pf() # solve power flow
p=plot_results(grid_ph_n)
```

Data type cannot be displayed: application/vnd.bokehjs_exec.v0+json, application/javascript

5.5.5 Phase ground fault (grounded neutral with impedance)

```
In [10]: data['shunts'] = [
    {"bus": "B1" , "R": 12.0, "X": 0.0, "bus_nodes": [4,0]},
```



```

        {"bus": "B1" , "R": 1e-12, "X": 0.0, "bus_nodes": [1,0]}, # applied fault
    ]

In [11]: grid_ph_n = grid()
grid_ph_n.read(data) # Load data
grid_ph_n.pf() # solve power flow
p=plot_results(grid_ph_n)

```

Data type cannot be displayed: application/vnd.bokehjs_exec.v0+json, application/javascript

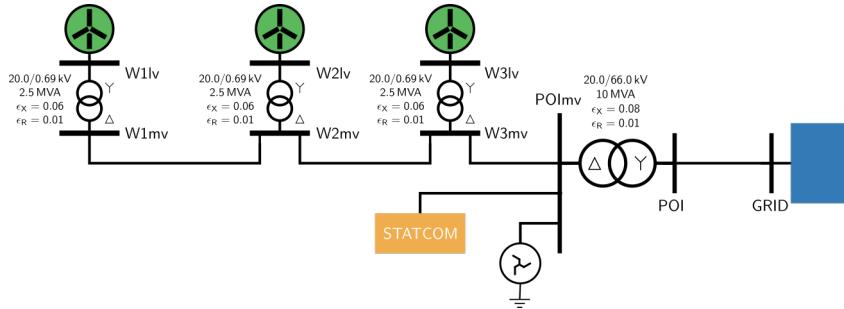
Run this notebook in binder:

5.6 Wind farm

```

In [207]: import numpy as np
          from pydgrid import grid
          from pydgrid.plot_bokeh import plot_results

```



5.6.1 System

```

In [210]: p_gen = 2000.0 # kW
          q_gen = 0         # kvar

          p_statcom = 0.0   # kW
          q_statcom = 0.0    # kvar

          data = {
                  "lines": [
                      {"bus_j": "W1mv", "bus_k": "W2mv", "code": "mv_al_300", "m": 500},
                      {"bus_j": "W2mv", "bus_k": "W3mv", "code": "mv_al_300", "m": 500},
                      {"bus_j": "W3mv", "bus_k": "POImv", "code": "mv_al_300", "m": 500},
                      {"bus_j": "POI", "bus_k": "GRID", "code": "hv_line", "m": 50.0e3},
                  ],
                  "buses": [

```

```

{
    "bus": "W11v", "pos_x": -1500.0, "pos_y": 200.0, "units": "m", "U_kv": 0.69},
    {"bus": "W21v", "pos_x": -1000.0, "pos_y": 200.0, "units": "m", "U_kv": 0.69},
    {"bus": "W31v", "pos_x": -500.0, "pos_y": 200.0, "units": "m", "U_kv": 0.69},
    {"bus": "W1mv", "pos_x": -1500.0, "pos_y": 180.0, "units": "m", "U_kv": 20.0},
    {"bus": "W2mv", "pos_x": -1000.0, "pos_y": 180.0, "units": "m", "U_kv": 20.0},
    {"bus": "W3mv", "pos_x": -500.0, "pos_y": 180.0, "units": "m", "U_kv": 20.0},
    {"bus": "POImv", "pos_x": 0.0, "pos_y": 0.0, "units": "m", "U_kv": 20.0},
    {"bus": "POI", "pos_x": 100.0, "pos_y": 0.0, "units": "m", "U_kv": 66.0},
    {"bus": "GRID", "pos_x": 500.0, "pos_y": 0.0, "units": "m", "U_kv": 66.0}
],
"transformers": [
    {"bus_j": "POImv", "bus_k": "POI", "S_n_kVA": 10000.0, "U_1_kv": 20.0,
     "R_cc_pu": 0.01, "X_cc_pu": 0.08, "connection": "Dyg11_3w", "conductors": 3},
    {"bus_j": "W1mv", "bus_k": "W11v", "S_n_kVA": 2500.0, "U_1_kv": 20,
     "R_cc_pu": 0.01, "X_cc_pu": 0.06, "connection": "Dyg11_3w", "conductors": 3},
    {"bus_j": "W2mv", "bus_k": "W21v", "S_n_kVA": 2500.0, "U_1_kv": 20,
     "R_cc_pu": 0.01, "X_cc_pu": 0.06, "connection": "Dyg11_3w", "conductors": 3},
    {"bus_j": "W3mv", "bus_k": "W31v", "S_n_kVA": 2500.0, "U_1_kv": 20,
     "R_cc_pu": 0.01, "X_cc_pu": 0.06, "connection": "Dyg11_3w", "conductors": 3}
],
"grid_formers": [
    {"bus": "GRID", "bus_nodes": [1, 2, 3], "kv": [38.105, 38.105, 38.105], "deg": [30, 150, 270.0]}
]
],
"grid_feeders": [
    {"bus": "W11v", "bus_nodes": [1, 2, 3], "kW": p_gen, "kvar": q_gen},
    {"bus": "W21v", "bus_nodes": [1, 2, 3], "kW": p_gen, "kvar": q_gen},
    {"bus": "W31v", "bus_nodes": [1, 2, 3], "kW": p_gen, "kvar": q_gen},
    {"bus": "POImv", "bus_nodes": [1, 2, 3], "kW": p_statcom, "kvar": q_statcom}
],
"groundings": [
    {"bus": "POImv", "R_gnd": 32.0, "X_gnd": 0.0, "conductors": 3}
],
"line_codes": [
    {
        "mv_al_150": {"R1": 0.262, "X1": 0.118, "C_1_muF": 0.250},
        "mv_al_185": {"R1": 0.209, "X1": 0.113, "C_1_muF": 0.281},
        "mv_al_240": {"R1": 0.161, "X1": 0.109, "C_1_muF": 0.301},
        "mv_al_300": {"R1": 0.128, "X1": 0.105, "C_1_muF": 0.340},
        "hv_line": {"R1": 0.219, "X1": 0.365, "R0": 0.219, "X0": 0.365}
    }
}
}

In [211]: grid_1 = grid()
grid_1.read(data) # Load data
grid_1(pf) # solve power flow
p=plot_results(grid_1)

```

Data type cannot be displayed: application/vnd.bokehjs_exec.v0+json, application/javascript

```

In [214]: mon = grid_1.monitor(bus_from='POI', bus_to='GRID')
mon.P

```

```
Out[214]: 5910895.785662318
```

```
In [215]: mon.Q
```

```
Out[215]: -490329.45241958584
```

5.6.2 Short circuits

Three phase at MV side POI

```
In [4]: data['shunts'] = [ # three phase fault to ground
    {"bus": "POImv", "R": 1.0e-8, "X": 0.0, "bus_nodes": [1, 2]},
    {"bus": "POImv", "R": 1.0e-8, "X": 0.0, "bus_nodes": [2, 3]},
    {"bus": "POImv", "R": 1.0e-8, "X": 0.0, "bus_nodes": [3, 0]},
]

# powers to zero:
data['grid_feeders'] = [{"bus": "W1lv", "bus_nodes": [1, 2, 3], "kW": 0, "kvar": 0},
    {"bus": "W2lv", "bus_nodes": [1, 2, 3], "kW": 0, "kvar": 0},
    {"bus": "W3lv", "bus_nodes": [1, 2, 3], "kW": 0, "kvar": 0},
    {"bus": "POImv", "bus_nodes": [1, 2, 3], "kW": 0, "kvar": 0}] # STATCOM

grid_1 = grid()
grid_1.read(data)
grid_1.pf()

p=plot_results(grid_1)
```

Data type cannot be displayed: application/vnd.bokehjs_exec.v0+json, application/javascript

```
In [ ]: I_cc = grid_1.transformers[0]['i_1a_m']
print('Three phase short circuit current at POImv = {:.2f} kA'.format(I_cc/1000))

Three phase short circuit current at POImv = 2.28 kA
```

Phase-ground W1mv bus

```
In [ ]: data['shunts'] = [
    {"bus": "W1mv", "R": 1.0e-8, "X": 0.0, "bus_nodes": [1, 0]},
]
grid_1 = grid()
grid_1.read(data) # Load data
grid_1.pf()

p=plot_results(grid_1)
```

Data type cannot be displayed: application/vnd.bokehjs_exec.v0+json, application/javascript

```
In [ ]: I_cc = grid_1.transformers[0]['i_1a_m']
print('Phase-ground short circuit current at W1mv = {:.2f} kA'.format(I_cc/1000))

Phase-ground short circuit current at W1mv = 0.62 kA
```

Get POI voltage with generators reactive powers

```
In [ ]: from scipy import optimize as opt
```

```

data['shunts'] = []

V_ref = 1.0
p_gen = 2.0e3
q_gen = 0

data['grid_feeders'][0]['kW'] = p_gen
data['grid_feeders'][1]['kW'] = p_gen
data['grid_feeders'][2]['kW'] = p_gen

grid_1 = grid()
grid_1.read(data) # Load data
grid_1.pf()

def residual(x):

    q_gen = x
    data['grid_feeders'][0]['kvar'] = q_gen
    data['grid_feeders'][1]['kvar'] = q_gen
    data['grid_feeders'][2]['kvar'] = q_gen
    grid_1.read(data) # Load data
    grid_1.pf() # solve power flow

    V = abs(grid_1.res['POI'].v_ag)/66.0e3*np.sqrt(3)

    return V_ref - V

res = sopt.bisect(residual,-3000.0,3000.0)
res

p=plot_results(grid_1)

```

Data type cannot be displayed: application/vnd.bokehjs_exec.v0+json, application/javascript

Optimization with reactive powers (without STATCOM)

```

In [ ]: V_ref = 1.0
         p_gen = 3.0e3
         q_gen = 0

         data['grid_feeders'][0]['kW'] = p_gen
         data['grid_feeders'][1]['kW'] = p_gen
         data['grid_feeders'][2]['kW'] = p_gen

         grid_1 = grid()
         grid_1.read(data) # Load data
         grid_1.pf()

def obj(x):

    data['grid_feeders'][0]['kvar'] = x[0]
    data['grid_feeders'][1]['kvar'] = x[1]
    data['grid_feeders'][2]['kvar'] = x[2]
    grid_1.read(data) # Load data

```

```

grid_1.pf() # solve power flow
mon = grid_1.monitor(bus_from='POI', bus_to='GRID')

P_loss = p_gen*3*1000 - mon.P

return P_loss

res = sopt.minimize(obj,[0,0,0], method='SLSQP')
print(res)

p=plot_results(grid_1)

fun: 192203.64692081884
jac: array([0.875, 0.875, 1.375])
message: 'Optimization terminated successfully.'
nfev: 61
nit: 8
njev: 8
status: 0
success: True
x: array([496.46556547, 496.46556547, 466.3287252 ])

```

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```

In [ ]: mon = grid_1.monitor(bus_from='POI', bus_to='GRID')
        print('POI active power = {:0.3f} MW'.format(mon.P/1e6))
        print('POI reactive power = {:0.2f} Mvar'.format(mon.Q/1e6))

POI active power = 8.808 MW
POI reactive power = 0.32 Mvar

```

Optimization with reactive powers (with STATCOM)

```

In [ ]: V_ref = 1.0
        p_gen = 3.0e3
        q_gen = 0

        data['grid_feeders'][0]['kW'] = p_gen
        data['grid_feeders'][1]['kW'] = p_gen
        data['grid_feeders'][2]['kW'] = p_gen

        grid_1 = grid()
        grid_1.read(data) # Load data
        grid_1.pf()

def obj(x):

        data['grid_feeders'][0]['kvar'] = x[0]
        data['grid_feeders'][1]['kvar'] = x[1]
        data['grid_feeders'][2]['kvar'] = x[2]
        data['grid_feeders'][3]['kvar'] = x[3]
        grid_1.read(data) # Load data
        grid_1.pf() # solve power flow
        mon = grid_1.monitor(bus_from='POI', bus_to='GRID')

```

```
P_loss = p_gen*3*1000 - mon.P

return P_loss

def const1(x):
    return 1.02-abs(grid_1.monitor(bus_from='POI', bus_to='GRID').V_a)/38.105/1000

def const2(x):
    return -(0.98-abs(grid_1.monitor(bus_from='POI', bus_to='GRID').V_a)/38.105/1000)

res = sopt.minimize(obj,[0,0,0,0], method='COBYLA',
                     constraints=[{'type':'ineq','fun':const1},{'type':'ineq','fun':const2}]
                     )
print(res)

p=plot_results(grid_1)

fun: 192924.1092131082
maxcv: 0.0
message: 'Optimization terminated successfully.'
nfev: 644
status: 1
success: True
x: array([201.34719703, 200.97303112, 200.48882721, 286.99544409])
```

Data type cannot be displayed: application/vnd.bokehjs_exec.v0+json, application/javascript

```
In [ ]: mon = grid_1.monitor(bus_from='POI', bus_to='GRID')
        print('POI active power = {:.3f} MW'.format(mon.P/1e6))
        print('POI reactive power = {:.2f} Mvar'.format(mon.Q/1e6))

POI active power = 8.807 MW
POI reactive power = -0.25 Mvar
```

Run this notebook in binder:

CHAPTER 6

Indices and tables

- genindex
- modindex
- search

Bibliography

- [T1] Dugan, R. C., & Santoso, S. (2003). An example of 3-phase transformer modeling for distribution system analysis. 2003 IEEE PES Transmission and Distribution Conference and Exposition (IEEE Cat. No.03CH37495), 3, 1028–1032. <https://doi.org/10.1109/TDC.2003.1335084>