polarTransform Documentation

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CHAPTER 1

Getting Started

1.1 Introduction

polarTransform is a Python package for converting images between the polar and Cartesian domain. It contains many features such as specifying the start/stop radius and angle, interpolation order (bicubic, linear, nearest, etc), and much more.

1.2 License

polarTransform has an MIT-based license.

1.3 Installing

1.3.1 Prerequisites

- Python 3
- Dependencies:
 - numpy
 - scipy
 - scikit-image

1.3.2 Installing polarTransform

polarTransform is currently available on PyPi. The simplest way to install alone is using pip at a command line:

pip install polarTransform

which installs the latest release. To install the latest code from the repository (usually stable, but may have undocumented changes or bugs):

pip install git+https://github.com/addisonElliott/polarTransform.git

For developers, you can clone the pydicom repository and run the setup.py file. Use the following commands to get a copy from GitHub and install all dependencies:

```
git clone pip install git+https://github.com/addisonElliott/polarTransform.git
cd polarTransform
pip install .
```

or, for the last line, instead use:

pip install -e .

to install in 'develop' or 'editable' mode, where changes can be made to the local working code and Python will use the updated polarTransform code.

1.4 Test and coverage

Run the following command in the base directory to run the tests:

```
python -m unittest discover -v polarTransform/tests
```

1.5 Using polarTransform

Once installed, the package can be imported at a Python command line or used in your own Python program with import polarTransform. See the *User Guide* for more details of how to use the package.

1.6 Support

Bugs can be submitted through the issue tracker. Pull requests are welcome too!

1.7 Next Steps

To start learning how to use polarTransform, see the User Guide.

CHAPTER 2

User Guide

convertToPolarImage and *convertToCartesianImage* are the two primary functions that make up this package. The two functions are opposites of one another, reversing the action that the other function does.

As the names suggest, the two functions convert an image from the cartesian or polar domain to the other domain with a given set of parameters. The power of these functions is that the user can specify the resulting image resolution, interpolation order, initial and final radii or angles and much much more. See the *Reference Guide* for more information on the specific parameters that are supported.

Since there are quite a few parameters that can be specified for the conversion functions, the class ImageTransform is created and returned from the convertToPolarImage or convertToCartesianImage functions (along with the converted image) that contains the arguments specified. The benefit of this class is that if one wants to convert the image back to another domain or convert points on either image to/from the other domain, they can simply call the functions within the ImageTransform class without specifying all of the arguments again.

2.1 Example 1

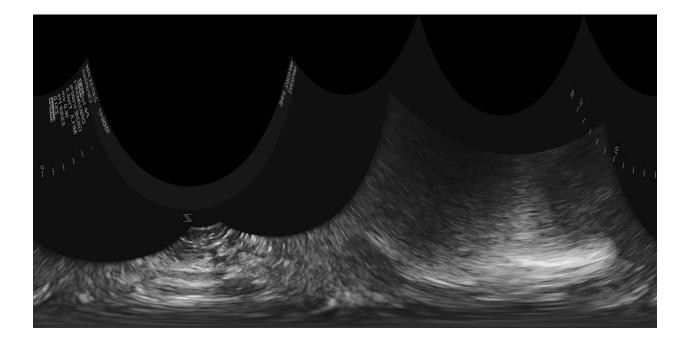
Let us take a B-mode echocardiogram and convert it to the polar domain. This is essentially reversing the scan conversion done internally by the ultrasound machine.

Here is the B-mode image:



```
import polarTransform
import matplotlib.pyplot as plt
import imageio
cartesianImage = imageio.imread('IMAGE_PATH_HERE')
polarImage, ptSettings = polarTransform.convertToPolarImage(cartesianImage, ______
___center=[401, 365])
plt.imshow(polarImage, origin='lower')
```

Resulting polar domain image:



2.2 Example 2

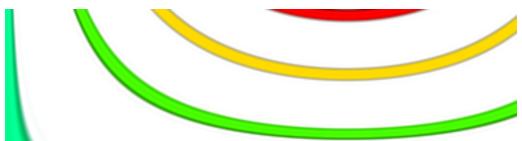


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```
cartesianImage = ptSettings.convertToCartesianImage(polarImage)
plt.figure()
plt.figure()
plt.figure()
plt.imshow(cartesianImage, origin='lower')
```

Resulting polar domain image:



Converting back to the cartesian image results in:



CHAPTER 3

Reference Guide

3.1 Table of Contents

polarTransform.convertToCartesianImage(ifagee)rt polar image to cartesian image.		
polarTransform.convertToPolarImage(image[Convert cartesian image to polar image.		
])		
polarTransform.getCartesianPointsImage(.Convert list of polar points from image to cartesian im-		
	age points based on transform metadata	
polarTransform.getPolarPointsImage(points,Convert list of cartesian points from image to polar im-		
)	age points based on transform metadata	
<pre>polarTransform.ImageTransform(center,)</pre>	Class to store settings when converting between carte-	
	sian and polar domain	

3.2 polarTransform Module

```
polarTransform.convertToCartesianImage (image, center=None, initialRadius=None, finalRa-
dius=None, initialAngle=None, finalAngle=None,
imageSize=None, order=3, border='constant',
borderVal=0.0, useMultiThreading=False, set-
tings=None)
```

Convert polar image to cartesian image.

Using a polar image, this function creates a cartesian image. This function is versatile because it can automatically calculate an appropriate cartesian image size and center given the polar image. In addition, parameters for converting to the polar domain are necessary for the conversion back to the cartesian domain.

Parameters

image [(N, M) or (N, M, P) numpy.ndarray] Polar image to convert to cartesian domain

Note: For a 3D array, polar transformation is applied separately across each 2D slice

Note: If an alpha band (4th channel of image is present), then it will be converted. Typically, this is unwanted, so the recommended solution is to transform the first 3 channels and set the 4th channel to fully on.

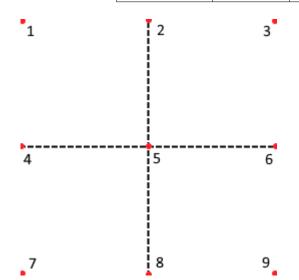
center [str or (2,) list, tuple or numpy.ndarray of int, optional] Specifies the center in the cartesian image to use as the origin in polar domain. The center in the cartesian domain will be (0, 0) in the polar domain.

If center is not set, then it will default to middle-middle. If the image size is None, the center is calculated after the image size is determined.

For relative positioning within the image, center can be one of the string values in the table below. The quadrant column contains the visible quadrants for the given center. initialAngle and finalAngle must contain at least one of the quadrants, otherwise an error will be thrown because the resulting cartesian image is blank. An example cartesian image is given below with annotations to what the center will be given a center string.

		C
Value	Quadrant	Location in image
top-left	IV	1
top-middle	III, IV	2
top-right	III	3
middle-left	I, IV	4
middle-middle	I, II, III, IV	5
middle-right	II, III	6
bottom-left	Ι	7
bottom-middle	I, II	8
bottom-right	II	9

Table 2: Valid center strings



initialRadius [int, optional] Starting radius in pixels from the center of the cartesian image in the polar image

The polar image begins at this radius, i.e. the first row of the polar image corresponds to this starting radius.

If initialRadius is not set, then it will default to 0.

finalRadius [int, optional] Final radius in pixels from the center of the cartesian image in the polar image

The polar image ends at this radius, i.e. the last row of the polar image corresponds to this ending radius.

Note: The polar image does **not** include this radius. It includes all radii starting from initial to final radii **excluding** the final radius. Rather, it will stop one step size before the final radius. Assuming the radial resolution (see radiusSize) is small enough, this should not matter.

If finalRadius is not set, then it will default to the maximum radius which is the size of the radial (1st) dimension of the polar image.

initialAngle [float, optional] Starting angle in radians in the polar image

The polar image begins at this angle, i.e. the first column of the polar image corresponds to this starting angle.

Radian angle is with respect to the x-axis and rotates counter-clockwise. The angle should be in the range of 0 to 2π .

If initialAngle is not set, then it will default to 0.0.

finalAngle [float, optional] Final angle in radians in the polar image

The polar image ends at this angle, i.e. the last column of the polar image corresponds to this ending angle.

Note: The polar image does **not** include this angle. It includes all angles starting from initial to final angle **excluding** the final angle. Rather, it stops one step size before the final angle. Assuming the angular resolution (see angleSize) is small enough, this should not matter.

Radian angle is with respect to the x-axis and rotates counter-clockwise. The angle should be in the range of 0 to 2π .

If finalAngle is not set, then it will default to 2π .

imageSize [(2,) list, tuple or numpy.ndarray of int, optional] Desired size of cartesian image where 1st dimension is number of rows and 2nd dimension is number of columns

If imageSize is not set, then it defaults to the size required to fit the entire polar image on a cartesian image.

order [int (0-5), optional] The order of the spline interpolation, default is 3. The order has to be in the range 0-5.

The following orders have special names:

- 0 nearest neighbor
- 1 bilinear
- 3 bicubic
- **border** [{'constant', 'nearest', 'wrap', 'reflect'}, optional] Polar points outside the cartesian image boundaries are filled according to the given mode.

Default is 'constant'

The following table describes the mode and expected output when seeking past the boundaries. The input column is the 1D input array whilst the extended columns on either side of the input array correspond to the expected values for the given mode if one extends past the boundaries.

Mode	Ext.	Input	Ext.
mirror	432	12345678	765
reflect	321	12345678	876
nearest	111	12345678	888
constant	000	12345678	000
wrap	678	12345678	123

Table 3: Valid border modes and expected output

Refer to scipy.ndimage.map_coordinates() for more details on this argument.

borderVal [same datatype as image, optional] Value used for polar points outside the cartesian image boundaries if border = 'constant'.

Default is 0.0

useMultiThreading [bool, optional] Whether to use multithreading when applying transformation for 3D images. This considerably speeds up the execution time for large images but adds overhead for smaller 3D images.

Default is False

settings [*ImageTransform*, optional] Contains metadata for conversion between polar and cartesian image.

Settings contains many of the arguments in *convertToPolarImage()* and *convertToCartesianImage()* and provides an easy way of passing these parameters along without having to specify them all again.

Warning: Cleaner and more succint to use ImageTransform. convertToCartesianImage()

If settings is not specified, then the other arguments are used in this function and the defaults will be calculated if necessary. If settings is given, then the values from settings will be used.

Returns

- **cartesianImage** [(N, M) or (N, M, P) numpy.ndarray] Cartesian image (3D cartesian image if 3D input image is given)
- **settings** [*ImageTransform*] Contains metadata for conversion between polar and cartesian image.

Settings contains many of the arguments in *convertToPolarImage()* and *convertToCartesianImage()* and provides an easy way of passing these parameters along without having to specify them all again.

polarTransform.convertToPolarImage (image, center=None, initialRadius=None, finalRadius=None, initialAngle=None, finalAngle=None, radiusSize=None, angleSize=None, order=3, border='constant', borderVal=0.0, useMultiThreading=False, settings=None)

Convert cartesian image to polar image.

Using a cartesian image, this function creates a polar domain image where the first dimension is radius and second dimension is the angle. This function is versatile because it allows different starting and stopping radii and angles to extract the polar region you are interested in.

Note: Traditionally images are loaded such that the origin is in the upper-left hand corner. In these cases the initialAngle and finalAngle will rotate clockwise from the x-axis. For simplicitly, it is recommended to flip the image along first dimension before passing to this function.

Parameters

image [(N, M) or (N, M, P) numpy.ndarray] Cartesian image to convert to polar domain

Note: For a 3D array, polar transformation is applied separately across each 2D slice

Note: If an alpha band (4th channel of image is present), then it will be converted. Typically, this is unwanted, so the recommended solution is to transform the first 3 channels and set the 4th channel to fully on.

center [(2,) list, tuple or numpy.ndarray of int, optional] Specifies the center in the cartesian image to use as the origin in polar domain. The center in the cartesian domain will be (0, 0) in the polar domain.

The center is structured as (x, y) where the first item is the x-coordinate and second item is the y-coordinate.

If center is not set, then it will default to round (image.shape[::-1] / 2).

initialRadius [int, optional] Starting radius in pixels from the center of the cartesian image that will appear in the polar image

The polar image will begin at this radius, i.e. the first row of the polar image will correspond to this starting radius.

If initialRadius is not set, then it will default to 0.

finalRadius [int, optional] Final radius in pixels from the center of the cartesian image that will appear in the polar image

The polar image will end at this radius, i.e. the last row of the polar image will correspond to this ending radius.

Note: The polar image will **not** include this radius. It will include all radii starting from initial to final radii **excluding** the final radius. Rather, it will stop one step size before the final radius. Assuming the radial resolution (see radiusSize) is small enough, this should not matter.

If finalRadius is not set, then it will default to the maximum radius of the cartesian image. Using the furthest corner from the center, the finalRadius can be calculated as:

$$finalRadius = \sqrt{((X_{max} - X_{center})^2 + (Y_{max} - Y_{center})^2)}$$

initialAngle [float, optional] Starting angle in radians that will appear in the polar image

The polar image will begin at this angle, i.e. the first column of the polar image will correspond to this starting angle.

Radian angle is with respect to the x-axis and rotates counter-clockwise. The angle should be in the range of 0 to 2π .

If initial Angle is not set, then it will default to 0.0.

finalAngle [float, optional] Final angle in radians that will appear in the polar image

The polar image will end at this angle, i.e. the last column of the polar image will correspond to this ending angle.

Note: The polar image will not include this angle. It will include all angle starting from initial to final angle excluding the final angle. Rather, it will stop one step size before the final angle. Assuming the angular resolution (see angleSize) is small enough, this should not matter.

Radian angle is with respect to the x-axis and rotates counter-clockwise. The angle should be in the range of 0 to 2π .

If finalAngle is not set, then it will default to 2π .

radiusSize [int, optional] Size of polar image for radial (1st) dimension

This in effect determines the resolution of the radial dimension of the polar image based on the initialRadius and finalRadius. Resolution can be calculated using equation below in radial px per cartesian px:

$$radialResolution = \frac{radiusSize}{finalRadius - initialRadius}$$

If radiusSize is not set, then it will default to the minimum size necessary to ensure that image information is not lost in the transformation. The minimum resolution necessary can be found by finding the smallest change in radius from two connected pixels in the cartesian image. Through experimentation, there is a surprisingly close relationship between the maximum difference from width or height of the cartesian image to the center times two.

The radiusSize is calculated based on this relationship and is proportional to the initialRadius and finalRadius given.

angleSize [int, optional] Size of polar image for angular (2nd) dimension

This in effect determines the resolution of the angular dimension of the polar image based on the initialAngle and finalAngle. Resolution can be calculated using equation below in angular px per cartesian px:

$$angularResolution = \frac{angleSize}{finalAngle - initialAngle}$$

If angleSize is not set, then it will default to the minimum size necessary to ensure that image information is not lost in the transformation. The minimum resolution necessary can be found by finding the smallest change in angle from two connected pixels in the cartesian image.

For a cartesian image with either dimension greater than 500px, the angleSize is set to be **two** times larger than the largest dimension proportional to initialAngle and finalAngle. Otherwise, for a cartesian image with both dimensions less than

500px, the angleSize is set to be four times larger the largest dimension proportional to initialAngle and finalAngle.

Note: The above logic **estimates** the necessary angleSize to reduce image information loss. No algorithm currently exists for determining the required angleSize.

order [int (0-5), optional] The order of the spline interpolation, default is 3. The order has to be in the range 0-5.

The following orders have special names:

- 0 nearest neighbor
- 1 bilinear
- 3 bicubic
- **border** [{'constant', 'nearest', 'wrap', 'reflect'}, optional] Polar points outside the cartesian image boundaries are filled according to the given mode.

Default is 'constant'

The following table describes the mode and expected output when seeking past the boundaries. The input column is the 1D input array whilst the extended columns on either side of the input array correspond to the expected values for the given mode if one extends past the boundaries.

Mode	Ext.	Input	Ext.
mirror	432	12345678	765
reflect	321	12345678	876
nearest	111	12345678	888
constant	000	12345678	000
wrap	678	12345678	123

Table 4: Valid border modes and expected output

Refer to scipy.ndimage.map_coordinates() for more details on this argument.

borderVal [same datatype as image, optional] Value used for polar points outside the cartesian image boundaries if border = 'constant'.

Default is 0.0

useMultiThreading [bool, optional] Whether to use multithreading when applying transformation for 3D images. This considerably speeds up the execution time for large images but adds overhead for smaller 3D images.

Default is False

settings [*ImageTransform*, optional] Contains metadata for conversion between polar and cartesian image.

Settings contains many of the arguments in *convertToPolarImage()* and *convertToCartesianImage()* and provides an easy way of passing these parameters along without having to specify them all again.

Warning: Cleaner and more succint to use ImageTransform. convertToPolarImage()

If settings is not specified, then the other arguments are used in this function and the defaults will be calculated if necessary. If settings is given, then the values from settings will be used.

Returns

- **polarImage** [(N, M) or (N, M, P) numpy.ndarray] Polar image where first dimension is radii and second dimension is angle (3D polar image if 3D input image is given)
- **settings** [*ImageTransform*] Contains metadata for conversion between polar and cartesian image.

Settings contains many of the arguments in *convertToPolarImage()* and *convertToCartesianImage()* and provides an easy way of passing these parameters along without having to specify them all again.

```
class polarTransform.ImageTransform(center, initialRadius, finalRadius, initialAngle, finalAn-gle, cartesianImageSize, polarImageSize)
```

Class to store settings when converting between cartesian and polar domain

convertToCartesianImage (*image*, *order=3*, *border='constant'*, *borderVal=0.0*, *useMultiThread-ing=False*)

Convert polar image to cartesian image.

Using a polar image, this function creates a cartesian image. This function is versatile because it can automatically calculate an appropriate cartesian image size and center given the polar image. In addition, parameters for converting to the polar domain are necessary for the conversion back to the cartesian domain.

Parameters

image [(N, M) or (N, M, P) numpy.ndarray] Polar image to convert to cartesian domain

Note: For a 3D array, polar transformation is applied separately across each 2D slice

Note: If an alpha band (4th channel of image is present), then it will be converted. Typically, this is unwanted, so the recommended solution is to transform the first 3 channels and set the 4th channel to fully on.

order [int (0-5), optional] The order of the spline interpolation, default is 3. The order has to be in the range 0-5.

The following orders have special names:

- 0 nearest neighbor
- 1 bilinear
- 3 bicubic
- **border** [{'constant', 'nearest', 'wrap', 'reflect'}, optional] Polar points outside the cartesian image boundaries are filled according to the given mode.

Default is 'constant'

The following table describes the mode and expected output when seeking past the boundaries. The input column is the 1D input array whilst the extended columns on either side of the input array correspond to the expected values for the given mode if one extends past the boundaries.

		-	-
Mode	Ext.	Input	Ext.
mirror	432	12345678	765
reflect	321	12345678	876
nearest	111	12345678	888
constant	000	12345678	000
wrap	678	12345678	123

Table 5: Valid border modes and expected output

Refer to scipy.ndimage.map_coordinates() for more details on this argument.

borderVal [same datatype as image, optional] Value used for polar points outside the cartesian image boundaries if border = 'constant'.

Default is 0.0

useMultiThreading [bool, optional] Whether to use multithreading when applying transformation for 3D images. This considerably speeds up the execution time for large images but adds overhead for smaller 3D images.

Default is False

Returns

cartesianImage [(N, M) or (N, M, P) numpy.ndarray] Cartesian image (3D cartesian image if 3D input image is given)

See also:

```
convertToCartesianImage()
```

convertToPolarImage (*image*, *order=3*, *border='constant'*, *borderVal=0.0*, *useMultiThread-ing=False*)

Convert cartesian image to polar image.

Using a cartesian image, this function creates a polar domain image where the first dimension is radius and second dimension is the angle. This function is versatile because it allows different starting and stopping radii and angles to extract the polar region you are interested in.

Note: Traditionally images are loaded such that the origin is in the upper-left hand corner. In these cases the initialAngle and finalAngle will rotate clockwise from the x-axis. For simplicitly, it is recommended to flip the image along first dimension before passing to this function.

Parameters

image [(N, M) or (N, M, P) numpy.ndarray] Cartesian image to convert to polar domain

Note: For a 3D array, polar transformation is applied separately across each 2D slice

Note: If an alpha band (4th channel of image is present), then it will be converted. Typically, this is unwanted, so the recommended solution is to transform the first 3 channels and set the 4th channel to fully on.

order [int (0-5), optional] The order of the spline interpolation, default is 3. The order has to be in the range 0-5.

The following orders have special names:

- 0 nearest neighbor
- 1 bilinear
- 3 bicubic

border [{'constant', 'nearest', 'wrap', 'reflect'}, optional] Polar points outside the cartesian image boundaries are filled according to the given mode.

Default is 'constant'

The following table describes the mode and expected output when seeking past the boundaries. The input column is the 1D input array whilst the extended columns on either side of the input array correspond to the expected values for the given mode if one extends past the boundaries.

Mode	Ext.	Input	Ext.
mirror	432	12345678	765
reflect	321	12345678	876
nearest	111	12345678	888
constant	000	12345678	000
wrap	678	12345678	123

Table 6: Valid border modes and expected output

Refer to scipy.ndimage.map_coordinates() for more details on this argument.

borderVal [same datatype as image, optional] Value used for polar points outside the cartesian image boundaries if border = 'constant'.

Default is 0.0

Returns

polarImage [(N, M) or (N, M, P) numpy.ndarray] Polar image where first dimension is radii and second dimension is angle (3D polar image if 3D input image is given)

getCartesianPointsImage (points)

Convert list of polar points from image to cartesian image points based on transform metadata

Note: This does **not** convert from polar to cartesian points, but rather converts pixels from polar image to pixels from cartesian image using *ImageTransform*.

The returned points are not rounded to the nearest point. User must do that by hand if desired.

Parameters

points [(N, 2) or (2,) numpy.ndarray] List of polar points to convert to cartesian domain

First column is r and second column is theta

Returns

cartesianPoints [(N, 2) or (2,) numpy.ndarray] Corresponding cartesian points from polar points using *ImageTransform*

See also:

getCartesianPointsImage(),getCartesianPoints(),getCartesianPoints2()

getPolarPointsImage (points)

Convert list of cartesian points from image to polar image points based on transform metadata

Note: This does **not** convert from cartesian to polar points, but rather converts pixels from cartesian image to pixels from polar image using *ImageTransform*.

The returned points are not rounded to the nearest point. User must do that by hand if desired.

Parameters

points [(N, 2) or (2,) numpy.ndarray] List of cartesian points to convert to polar domain

First column is x and second column is y

Returns

polarPoints [(N, 2) or (2,) numpy.ndarray] Corresponding polar points from cartesian points using *ImageTransform*

See also:

getPolarPointsImage(), getPolarPoints(), getPolarPoints2()

polarTransform.getCartesianPointsImage (points, settings)

Convert list of polar points from image to cartesian image points based on transform metadata

Warning: Cleaner and more succinct to use ImageTransform.getCartesianPointsImage()

Note: This does **not** convert from polar to cartesian points, but rather converts pixels from polar image to pixels from cartesian image using *ImageTransform*.

The returned points are not rounded to the nearest point. User must do that by hand if desired.

Parameters

points [(N, 2) or (2,) numpy.ndarray] List of polar points to convert to cartesian domain

First column is r and second column is theta

settings [ImageTransform] Contains metadata for conversion from polar to cartesian domain

Settings contains many of the arguments in *convertToPolarImage()* and *convertToCartesianImage()* and provides an easy way of passing these parameters along without having to specify them all again.

Returns

cartesianPoints [(N, 2) or (2,) numpy.ndarray] Corresponding cartesian points from polar points using settings

See also:

```
ImageTransform.getCartesianPointsImage(), getCartesianPoints(),
getCartesianPoints2()
```

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