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# **lattice\_mc Documentation**

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## lattice\_mc: A Python Lattice-Gas Monte Carlo Module

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[PyPI version](#) [Build Status](#) [DOI](#) [JOSS status](#) [Documentation Status](#)

`lattice_mc` is Python module for performing (kinetic) lattice-gas Monte Carlo (LGMC) simulations of ionic transport in solid electrolytes.

In solid electrolytes, ionic motion is typically effected by a series of discrete “jumps” where ions move between adjacent lattice sites [1]. For dilute mobile ions, ionic trajectories are random walks, and simple analytical expressions exists that relate macroscopic transport coefficients, i.e. diffusion coefficients and ionic conductivities, to the microscopic jump frequency of individual ions [2,3]. Practical solid electrolytes have high mobile ion concentrations, with significant interparticle interactions producing deviations from the dilute limit random walk behaviour. In general, the *quantitative* effect of interparticle interactions cannot be determined analytically. As an alternative, numerical simulations, such as lattice-gas Monte Carlo methods, can be used to directly calculate these relationships. Lattice-gas Monte Carlo methods are particularly suited to studying how varying properties across broad classes of materials give quantitative differences in macroscopic ionic transport, and can be used to understand the different transport properties of materials with, for example, different crystal structures or mobile ion stoichiometries.

`lattice_mc` has been written to allow materials scientists and solid-state chemists model how the microscopic physics of solid electrolytes (crystal structure, stoichiometry, interaction models) determine macroscopic transport behaviour (diffusion and ionic conduction), with the goal of understand the factors that make different materials more or less useful for specific applications (e.g. Li-ion batteries or fuel cells).

The code allows the programmatic construction of simple lattices (presently implemented are square, honeycomb, and cubic lattices). Lattices with arbitrary geometries can be constructed from a file format that defines the lattice sites and their connectivity, allowing models based on crystallographic data. The algorithms used and interaction models are described in more detail in Ref. [4]. Calculated properties include tracer and “jump” diffusion coefficients; where the latter is proportional to the mobility (and hence the conductivity for charged particles) [5]; and tracer (single particle) and collective correlation factors,  $f$  and  $fI$  [6]. The simplest interaction model is for “non-interacting” particles, where the only restriction is volume exclusion (two particles cannot simultaneously occupy a single site) [7]. Additional interaction models include nearest-neighbour repulsion and on-site energies for inequivalent sites. Simulations are performed using an efficient rejection-free Monte Carlo scheme [8].

## 1.1 Installation

```
pip install lattice_mc
```

Or download the latest release from [GitHub](#)

```
https://github.com/bjmorgan/lattice_mc/archive/1.0.0.tar.gz
```

Then install

```
cd lattice_mc
python setup.py install
```

Or you can clone the latest development version:

```
git clone git@github.com:bjmorgan/lattice_mc.git
```

and install the same way.

```
cd lattice_mc
python setup.py install
```

Alternatively, you can install the latest build using `pip`, direct from [GitHub](#), e.g.

```
pip3 install git+https://github.com/bjmorgan/lattice_mc.git
```

## 1.2 Documentation

Full documentation and examples are contained in a [Jupyter notebook](#) at `examples/lattice_mc_example.ipynb`. The example notebook is also hosted on [GitHub](#).

## 1.3 Tests

Automated testing of the latest build happens [here](#).

Manual tests can be run using

```
python3 -m unittest discover
```

The code has been tested with Python versions 3.5 and above.

## 1.4 References

1. C. R. A. Catlow, Sol. Stat. Ionics 8, 89 (1983).
2. R. E. Howard and A. B. Lidiard, Rep. Prog. Phys. 27, 161 (1964).
3. J. H. Harding, Defects and Transport in Ionic Solids, in Ionic Solids at High Temperatures ed. A. M. Stoneham, World Scientific (1989).
4. B. J. Morgan, arXiv: 1707.00491

5. A. Van der Ven et al. *Acc. Chem. Res.* 46, 1216 (2013).
6. G. E. Murch *Sol. Stat. Ionics* 7, 177 (1982).
7. R. Kutner *Phys. Lett.* 81A, 239 (1981).
8. A. F. Voter, *Introduction to the Kinetic Monte Carlo Method*, in *Radiation Effects in Solids*, ed. K. E. Sica et al., Springer (2007).
9. Morgan and Madden, *J. Phys. Condens. Matter* 24, 275303 (2012).
10. G. E. Murch & R. J. Thorn, *Phil. Mag.* 36 529 (1977).





## CHAPTER 2

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### Blocked Lattices

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It is possible to construct a simulation lattice where there are no possible jumps; such a lattice is classified as “blocked”. To test for this, a `Lattice` object can be queried using the `is_blocked()` method:

```
>>> simulation.lattice.is_blocked()
True
```

If a simulation with a blocked lattice is run, a `BlockedLatticeError` exception is raised:

```
Traceback (most recent call last):
...
self.lattice.jump()
File "/Users/bjm42/source/lattice_mc/lattice_mc/lattice.py", line 228, in jump
    raise BlockedLatticeError('No moves are possible in this lattice')
lattice_mc.error.BlockedLatticeError: No moves are possible in this lattice
```



## 3.1 lattice\_mc package

### 3.1.1 Submodules

#### 3.1.2 lattice\_mc.atom module

**class** lattice\_mc.atom.**Atom**(*initial\_site*)

Bases: object

Atoms are distinguishable particles, each occupying a specific lattice site.

**atom\_number** = 0

**dr\_squared**()

$|dr|^2$ , where  $dr$  is the total displacement vector for this *Atom*.

**Parameters** **None** –

**Returns**  $|dr|^2$ .

**Return type** dr\_squared (float)

**reset**()

Reinitialise the stored displacements, number of hops, and list of sites visited for this *Atom*.

**Parameters** **None** –

**Returns** None

**site**

Get or set *self.site* for this *Atom*.

### 3.1.3 lattice\_mc.cluster module

**class** lattice\_mc.cluster.Cluster(*sites*)

Bases: object

Clusters are sets of sites.

**is\_neighbouring** (*other\_cluster*)

logical check whether the neighbour list for cluster A includes any sites in cluster B

**Parameters** **other\_cluster** (*Cluster*) – the other cluster we are testing for neighbour connectivity

**Returns** True if the other cluster neighbours this cluster.

**Return type** (Bool)

**is\_periodically\_contiguous** ()

logical check whether a cluster connects with itself across the simulation periodic boundary conditions.

**Parameters** **none** –

**Returns** ( Bool, Bool, Bool ): Contiguity along the x, y, and z coordinate axes

**merge** (*other\_cluster*)

Combine two clusters into a single cluster.

**Parameters** **other\_cluster** (*Cluster*) – The second cluster to combine.

**Returns** The combination of both clusters.

**Return type** (*Cluster*)

**remove\_sites\_from\_neighbours** (*remove\_labels*)

Removes sites from the set of neighbouring sites if these have labels in remove\_labels.

**Parameters** **Remove\_labels** (*List*) or (*Str*) – List of Site labels to be removed from the cluster neighbour set.

**Returns** None

**sites\_at\_edges** ()

Finds the six sites with the maximum and minimum coordinates along x, y, and z.

**Parameters** **None** –

**Returns** In the order [ +x, -x, +y, -y, +z, -z ]

**Return type** (List(List))

**size** ()

Number of sites in this cluster.

**Parameters** **None** –

**Returns** The number of sites in this cluster.

**Return type** (Int)

### 3.1.4 lattice\_mc.global\_vars module

### 3.1.5 lattice\_mc.init\_lattice module

`lattice_mc.init_lattice.cubic_lattice(a, b, c, spacing)`

Generate a cubic lattice.

**Parameters**

- **a** (*Int*) – Number of lattice repeat units along x.
- **b** (*Int*) – Number of lattice repeat units along y.
- **c** (*Int*) – Number of lattice repeat units along z.
- **spacing** (*Float*) – Distance between lattice sites.

**Returns** The new lattice

**Return type** (*Lattice*)

`lattice_mc.init_lattice.honeycomb_lattice(a, b, spacing, alternating_sites=False)`

Generate a honeycomb lattice.

**Parameters**

- **a** (*Int*) – Number of lattice repeat units along x.
- **b** (*Int*) – Number of lattice repeat units along y.
- **spacing** (*Float*) – Distance between lattice sites.
- **alternating\_sites** (*Bool, optional*) – Label alternating sites with ‘A’ and ‘B’. Defaults to False.

**Returns** The new lattice

**Return type** (*Lattice*)

#### Notes

The returned lattice is 3D periodic, but all sites and edges lie in the xy plane.

`lattice_mc.init_lattice.lattice_from_sites_file(site_file, cell_lengths)`

Generate a lattice from a sites file.

**Parameters**

- **site\_file** (*Str*) – Filename for the file containing the site information.
- **cell\_lengths** (*List (Float, Float, Float)*) – A list containing the [ x, y, z ] cell lengths.

**Returns** The new lattice

**Return type** (*Lattice*)

#### Notes

The site information file format is:

<number\_of\_sites> (*Int*).

Followed by blocks of data separated by double linebreaks; one block per site.

site: <site number> (Int).  
centre: <x> <y> <z> (Float,Float,Float).  
neighbours: <list of site numbers of neighbouring sites> (List[Int]).  
label: <site group label> (Str).  
energy: <site occupation energy> (Float).

The energy is optional, and will be set to 0.0 if not included.

Line order within each block is not meaningful.

British and American English spellings for centre|center and neighbour|neighbor are accepted.

An example file can be found in the examples directory.

`lattice_mc.init_lattice.square_lattice(a, b, spacing)`

Generate a square lattice.

**Parameters**

- **a** (Int) – Number of lattice repeat units along x.
- **b** (Int) – Number of lattice repeat units along y.
- **spacing** (Float) – Distance between lattice sites.

**Returns** The new lattice

**Return type** (*Lattice*)

**Notes**

The returned lattice is 3D periodic, but all sites and edges lie in the xy plane.

### 3.1.6 lattice\_mc.jump module

`class lattice_mc.jump.Jump(initial_site, final_site, nearest_neighbour_energy=False, coordination_number_energy=False, jump_lookup_table=None)`

Bases: object

**boltzmann\_factor()**

Boltzmann probability factor for accepting this jump, following the Metropolis algorithm.

**Parameters** None –

**Returns** Metropolis relative probability of accepting this jump.

**Return type** (Float)

**coordination\_number\_delta\_E()**

Coordination-number dependent energy contribution to the change in system energy if this jump were accepted.

**Parameters** None –

**Returns** delta E (coordination-number)

**Return type** (Float)

**delta\_E()**

The change in system energy if this jump were accepted.

**Parameters** None –

**Returns** delta E

**Return type** (Float)

**dr** (*cell\_lengths*)

Particle displacement vector for this jump

**Parameters** **cell\_lengths** (*np.array(x, y, z)*) – Cell lengths for the orthogonal simulation cell.

**Returns** (*np.array(x,y,z)*): dr

**nearest\_neighbour\_delta\_E** ()

Nearest-neighbour interaction contribution to the change in system energy if this jump were accepted.

**Parameters** **None** –

**Returns** delta E (nearest-neighbour)

**Return type** (Float)

**rate** ()

Average rate for this jump. Calculated as (*v\_0 \* P\_jump*).

**Parameters** **None** –

**Returns** The average rate for this jump.

**Return type** (Float)

**relative\_probability**

**relative\_probability\_from\_lookup\_table** (*jump\_lookup\_table*)

Relative probability of accepting this jump from a lookup-table.

**Parameters** **jump\_lookup\_table** (*LookupTable*) – the lookup table to be used for this jump.

**Returns** relative probability of accepting this jump.

**Return type** (Float)

### 3.1.7 lattice\_mc.lattice module

**class** `lattice_mc.lattice.Lattice` (*sites, cell\_lengths*)

Bases: `object`

Lattice class

**connected\_site\_pairs** ()

Returns a dictionary of all connections between pair of sites (by site label). e.g. for a linear lattice A-B-C will return:

```
{ 'A' : [ 'B' ], 'B' : [ 'A', 'C' ], 'C' : [ 'B' ] }
```

**Parameters** **None** –

**Returns** A dictionary of neighbouring site types in the lattice.

**Return type** `site_connections` (`Dict{Str List[Str]}`)

**connected\_sites** (*site\_labels=None*)

Searches the lattice to find sets of sites that are contiguously neighbouring. Mutually exclusive sets of contiguous sites are returned as Cluster objects.

**Parameters** ( (*site\_labels*) – obj:(List(Str)|Set(Str)|Str), optional): Labels for sites to be considered in the search. This can be a list:

```
[ 'A', 'B' ]
```

a set:

```
( 'A', 'B' )
```

or a string:

```
'A'.
```

**Returns** List of Cluster objects for groups of contiguous sites.

**Return type** (List(*Cluster*))

**detached\_sites** (*site\_labels=None*)

Returns all sites in the lattice (optionally from the set of sites with specific labels) that are not part of a percolating network. This is determined from clusters of connected sites that do not wrap round to themselves through a periodic boundary.

**Parameters** *site\_labels* (*String* or *List(String)*) – Labels of sites to be considered.

**Returns** List of sites not in a periodic percolating network.

**Return type** (List(*Site*))

**enforce\_periodic\_boundary\_conditions** ()

Ensure that all lattice sites are within the central periodic image of the simulation cell. Sites that are outside the central simulation cell are mapped back into this cell.

**Parameters** *None* –

**Returns** *None*

**initialise\_site\_lookup\_table** ()

Create a lookup table allowing sites in this lattice to be queried using *self.site\_lookup[n]* where *n* is the identifying site number.

**Parameters** *None* –

**Returns** *None*

**is\_blocked** ()

Check whether there are any possible jumps.

**Parameters** *None* –

**Returns** True if there are no possible jumps. Otherwise returns False.

**Return type** (Bool)

**jump** ()

Select a jump at random from all potential jumps, then update the lattice state.

**Parameters** *None* –

**Returns** *None*



**max\_site\_coordination\_numbers()**

Returns a dictionary of the maximum coordination number for each site label. e.g.:

```
{ 'A' : 4, 'B' : 4 }
```

**Parameters** none –

**Returns**

**Int**): dictionary of maximum coordination number for each site label.

**Return type** max\_coordination\_numbers (Dict(Str

**occupied\_site\_numbers()**

List of site id numbers for all sites that are occupied.

**Parameters** None –

**Returns** List of site id numbers for occupied sites.

**Return type** List(Int)

**occupied\_sites()**

The set of sites occupied by atoms.

**Parameters** None –

**Returns** List of sites that are occupied.

**Return type** List(*Site*)

**populate\_sites(number\_of\_atoms, selected\_sites=None)**

Populate the lattice sites with a specific number of atoms.

**Parameters**

- **number\_of\_atoms** (*Int*) – The number of atoms to populate the lattice sites with.
- (*(selected\_sites)* – obj:List, optional): List of site labels if only some sites are to be occupied. Defaults to None.

**Returns** None

**potential\_jumps()**

All nearest-neighbour jumps not blocked by volume exclusion (i.e. from occupied to neighbouring unoccupied sites).

**Parameters** None –

**Returns** List of possible jumps.

**Return type** (List(*Jump*))

**reset()**

Reset all time-dependent counters for this lattice and its constituent sites

**Parameters** None –

**Returns** None

**select\_sites(site\_labels)**

Selects sites in the lattice with specified labels.

**Parameters** **site\_labels** (*List (Str) | Set (Str) | Str*) – Labels of sites to select. This can be a List [ 'A', 'B' ], a Set ( 'A', 'B' ), or a String 'A'.

**Returns** List of sites with labels given by *site\_labels*.

**Return type** (List(*Site*))

**set\_cn\_energies** (*cn\_energies*)

Set the coordination number dependent energies for this lattice.

**Parameters** (**Dict** (**Str** (*cn\_energies*) – Dict(Int:Float))) : Dictionary of dictionaries specifying the coordination number dependent energies for each site type. e.g.:

```
{ 'A' : { 0 : 0.0, 1 : 1.0, 2 : 2.0 }, 'B' : { 0 : 0.0, 1 : 2.0 } }
```

**Returns** None

**set\_nn\_energy** (*delta\_E*)

Set the lattice nearest-neighbour energy.

**Parameters** **delta\_E** (*Float*) – The nearest-neighbour energy E<sub>nn</sub>.

**Returns** None

**set\_site\_energies** (*energies*)

Set the energies for every site in the lattice according to the site labels.

**Parameters** (**Dict** (**Str** (*energies*) – Float): Dictionary of energies for each site label, e.g.:

```
{ 'A' : 1.0, 'B', 0.0 }
```

**Returns** None

**site\_coordination\_numbers** ()

Returns a dictionary of the coordination numbers for each site label. e.g.:

```
{ 'A' : { 4 }, 'B' : { 2, 4 } }
```

**Parameters** none –

**Returns**

**Set**(Int)): dictionary of coordination numbers for each site label.

**Return type** coordination\_numbers (Dict(Str

**site\_occupation\_statistics** ()

Average site occupation for each site type

**Parameters** None –

**Returns**

Float)): Dictionary of occupation statistics, e.g.:

```
{ 'A' : 2.5, 'B' : 25.3 }
```

**Return type** (Dict(Str

**site\_specific\_coordination\_numbers** ()

Returns a dictionary of coordination numbers for each site type.

**Parameters** None –

**Returns**

List(Int)): Dictionary of coordination numbers for each site type, e.g.:

```
{ 'A' : [ 2, 4 ], 'B' : [ 2 ] }
```

**Return type** `(Dict(Str`

**site\_with\_id** (*number*)

Select the site with a specific id number.

**Parameters** **number** (*Int*) – The identifying number for a specific site.

**Returns** The site with id number equal to *number*

**Return type** (*Site*)

**transmute\_sites** (*old\_site\_label, new\_site\_label, n\_sites\_to\_change*)

Selects a random subset of sites with a specific label and gives them a different label.

**Parameters**

- **old\_site\_label** (*String or List(String)*) – Site label(s) of the sites to be modified..
- **new\_site\_label** (*String*) – Site label to be applied to the modified sites.
- **n\_sites\_to\_change** (*Int*) – Number of sites to modify.

**Returns** None

**update** (*jump*)

Update the lattice state by accepting a specific jump

**Parameters** **jump** (*Jump*) – The jump that has been accepted.

**Returns** None.

**update\_site\_occupation\_times** (*delta\_t*)

Increase the time occupied for all occupied sites by delta t

**Parameters** **delta\_t** (*Float*) – Timestep.

**Returns** None

**vacant\_site\_numbers** ()

List of site id numbers for all sites that are vacant.

**Parameters** None –

**Returns** List of site id numbers for vacant sites.

**Return type** `List(Int)`

**vacant\_sites** ()

The set of sites not occupied by atoms.

**Parameters** None –

**Returns** List of sites that are vacant.

**Return type** `List(Site)`

### 3.1.8 lattice\_mc.lattice\_site module

**class** `lattice_mc.lattice_site.Site` (*number, coordinates, neighbours, energy, label, cn\_energies=None*)

Bases: `object`

Site class

**cn\_occupation\_energy** (*delta\_occupation=None*)

The coordination-number dependent energy for this site.

**Parameters** ( (*delta\_occupation*) – obj:Dict(Str:Int), optional): A dictionary of a change in (site-type specific) coordination number, e.g. { ‘A’ : 1, ‘B’ : -1 }. If this is not None, the coordination-number dependent energy is calculated including these changes in neighbour-site occupations. Defaults to None

**Returns** The coordination-number dependent energy for this site.

**Return type** (Float)

**index** = 0

**nn\_occupation** ()

The number of occupied nearest-neighbour sites.

**Parameters** None –

**Returns** The number of occupied nearest-neighbour sites.

**Return type** (Int)

**set\_cn\_occupation\_energies** (*cn\_energies*)

Set the coordination-number dependent energies for this site.

**Parameters** (Dict (Int (*cn\_energies*) – Float)): Dictionary of coordination number dependent site energies, e.g. { 0 : 0.0, 1 : 0.5 }.

**Returns** None

**site\_specific\_neighbours** ()

Returns the number of neighbouring sites, classified by site type.

**Parameters** None –

**Returns** Int)): Dictionary of neighboring sites, classified by site label, e.g. { ‘A’ : 1, ‘B’ : 1 }.

**Return type** (Dict(Str

**site\_specific\_nn\_occupation** ()

Returns the number of occupied nearest neighbour sites, classified by site type.

**Parameters** None –

**Returns** Int)): Dictionary of nearest-neighbour occupied site numbers, classified by site label, e.g. { ‘A’ : 2, ‘B’ : 1 }.

**Return type** (Dict(Str

### 3.1.9 lattice\_mc.lookup\_table module

**class** lattice\_mc.lookup\_table.LookupTable (*lattice, hamiltonian*)

Bases: object

LookupTable class

**generate\_nearest\_neighbour\_lookup\_table** ()

Construct a look-up table of relative jump probabilities for a nearest-neighbour interaction Hamiltonian.

**Parameters** None. –

**Returns** None.

**relative\_probability** (*l1, l2, c1, c2*)

The relative probability for a jump between two sites with specific site types and coordination numbers.

**Parameters**

- **l1** (*Str*) – Site label for the initial site.
- **l2** (*Str*) – Site label for the final site.
- **c1** (*Int*) – Coordination number for the initial site.
- **c2** (*Int*) – Coordination number for the final site.

**Returns** The relative probability of this jump occurring.

**Return type** (Float)

`lattice_mc.lookup_table.metropolis` (*delta\_E*)

Boltzmann probability factor for an event with an energy change *delta\_E*, following the Metropolis algorithm.

**Parameters** **delta\_E** (*Float*) – The change in energy.

**Returns** Metropolis relative probability for this event.

**Return type** (Float)

### 3.1.10 lattice\_mc.options module

**class** `lattice_mc.options.Options`

Bases: `object`

Object for storing options for setting up and running a simulation.

**read\_lattice\_from\_file** (*filename*)

Set the filename for the sites file used to define the simulation lattice.

**Parameters** **filename** (*Str*) – The filename for the sites file.

**Returns** None

**set\_cn\_energies** (*cn\_energies*)

Set the coordination-number dependent energies.

**Parameters** (**Dict** (**Str** (*cn\_energies*) – **Dict**(**Int**:**Float**))) : Dict of Dicts specifying the coordination-number dependent energies for each site type. e.g. { 'A' : { 0 : 0.0, 1 : 1.0 }, 'B' : { 0 : 0.0, 1 : 2.0 } }

**Returns** None

**set\_cn\_energy\_scaling** (*cn\_energy\_scaling*)

Set a scaling factor for the coordination-number dependent energies.

**Parameters** **cn\_energy\_scaling** (*Float*) – Coordination-number dependent energy scaling.

**Returns** None

**set\_lattice\_cell\_lengths** (*cell\_lengths*)

Set the lattice cell lengths for a simulation.

**Parameters** **cell\_lengths** (*np.array(x, y, z)*) – Lattice cell lengths.

**Returns** None

**set\_nn\_energy\_scaling** (*energy\_scaling*)

Set a scaling factor for the nearest-neighbour interaction energy.

**Parameters** `energy_scaling` (*Float*) – Nearest-neighbour energy scaling.

**Returns** None

**set\_number\_of\_atoms** (*number\_of\_atoms*)

Set the number of atoms present in the simulation.

**Parameters** `number_of_atoms` (*int*) – The number of atoms.

**Returns** None

**set\_number\_of\_equilibration\_jumps** (*number\_of\_equilibration\_jumps*)

Set the number of equilibration jumps for a simulation.

**Parameters** `number_of_equilibration_jumps` (*Int*) – The number of equilibration jumps.

**Returns** None

**set\_number\_of\_jumps** (*number\_of\_jumps*)

Set the on-site energies for each site type.

**Parameters** (**Dict** (**Str** (*site\_energies*) – *Float*)): On-site energies for each site type label. e.g. { 'A' : 1.0, 'B', -1.0 }

**Returns** None

**set\_site\_energies** (*site\_energies*)

Set the on-site energies for each site type.

**Parameters** (**Dict** (**Str** (*site\_energies*) – *Float*)): On-site energies for each site type label. e.g. { 'A' : 1.0, 'B', -1.0 }

**Returns** None

### 3.1.11 lattice\_mc.simulation module

**class** `lattice_mc.simulation.Simulation`

Bases: `object`

Simulation class

**average\_site\_occupations**

Average site occupation numbers.

**Parameters** None –

**Returns**

**Float**)): Average site occupation numbers for each site label, e.g. { 'A' : 12.4, 'B' : 231.2 }

**Return type** (**Dict**(**Str**

**collective\_correlation**

Returns the collective correlation factor, `f_I`

**Parameters** None –

**Returns** The collective correlation factor, `f_I`.

**Return type** (*Float*)

**collective\_diffusion\_coefficient**

Returns the collective or “jump” diffusion coefficient, `D_J`.

**Parameters** **None** –

**Returns** The collective diffusion coefficient,  $D_J$ .

**Return type** (Float)

**collective\_diffusion\_coefficient\_per\_atom**

The collective diffusion coefficient per atom.  $D_J / n_{\text{atoms}}$ .

**Parameters** **None** –

**Returns** The collective diffusion coefficient per atom,  $D_J / n_{\text{atoms}}$ .

**Return type** (Float)

**define\_lattice\_from\_file** (*filename*, *cell\_lengths*)

**Set up the simulation lattice from a file containing site data.** Uses `init_lattice.lattice_from_sites_file`, which defines the site file spec.

**Parameters**

- **filename** (*Str*) – sites file filename.
- **cell\_lengths** (*List* (*x*, *y*, *z*)) – cell lengths for the simulation cell.

**Returns** None

**is\_initialised** ()

Check whether the simulation has been initialised.

**Parameters** **None** –

**Returns** None

**old\_collective\_correlation**

Returns the collective correlation factor,  $f_I$

**Parameters** **None** –

**Returns** The collective correlation factor,  $f_I$ .

**Return type** (Float)

## Notes

This function assumes that the jump distance between sites has been normalised to  $a=1$ . If the jumps distance is not equal to 1 then the value returned by this function should be divided by  $a^2$ . Even better, use `self.collective_correlation`

**old\_tracer\_correlation**

Deprecated tracer correlation factor for this simulation.

**Parameters** **None** –

**Returns** The tracer correlation factor,  $f$ .

**Return type** (Float)

## Notes

This function assumes that the jump distance between sites has been normalised to  $a=1$ . If the jump distance is not equal to 1 then the value returned by this function should be divided by  $a^2$ . Even better, use *self.tracer\_correlation*.

**reset** ()

Reset all counters for this simulation.

**Parameters** None –

**Returns** None

**run** (*for\_time=None*)

Run the simulation.

**Parameters** ( (*for\_time*) – obj:Float, optional): If *for\_time* is set, then run the simulation until a set amount of time has passed. Otherwise, run the simulation for a set number of jumps. Defaults to None.

**Returns** None

**set\_cn\_energies** (*cn\_energies*)

Set the coordination-number dependent energies for this simulation.

**Parameters** (**Dict** (**Str** (*cn\_energies*) – Dict(Int:Float))) : Dict of Dicts specifying the coordination-number dependent energies. e.g. { 'A' : { 0 : 0.0, 1: 0.5 }, 'B' : { 0 : -0.5, 1 : -2.0 } }

**Returns** None

**set\_nn\_energy** (*nn\_energy*)

Set the nearest-neighbour energy for this simulation.

**Parameters** **nn\_energy** (*Float*) – nearest-neighbour energy.

**Returns** None

**set\_number\_of\_atoms** (*n*, *selected\_sites=None*)

Set the number of atoms for the simulation, and populate the simulation lattice.

**Parameters**

- **n** (*Int*) – Number of atoms for this simulation.
- ( (*selected\_sites*) – obj:(List|Set|String), optional): Selects a subset of site types to be populated with atoms. Defaults to None.

**Returns** None

**set\_number\_of\_equilibration\_jumps** (*n*)

Set the number of equilibration jumps for this simulation.

**Parameters** **n** (*Int*) – number of equilibration jumps

**Returns** None

**set\_number\_of\_jumps** (*n*)

Set the number of jumps for this simulation.

**Parameters** **n** (*Int*) – number of jumps

**Returns** None

**set\_site\_energies** (*site\_energies*)

Set the on-site energies for this simulation.



**Parameters** **Dict (Str (site\_energies) – Float)**: Dict of energies for each site type.  
e.g. { 'A' : 0.0., 'B' : 1.0 }

**Returns** None

**setup\_lookup\_table** (*hamiltonian='nearest-neighbour'*)

Create a jump-probability look-up table corresponding to the appropriate Hamiltonian.

**Parameters** **hamiltonian** (*Str, optional*) – String specifying the simulation Hamiltonian. valid values are 'nearest-neighbour' (default) and 'coordination\_number'.

**Returns** None

**tracer\_correlation**

Tracer correlation factor, f.

**Parameters** **None** –

**Returns** The tracer correlation factor, f.

**Return type** (Float)

**tracer\_diffusion\_coefficient**

Tracer diffusion coefficient, D\*.

**Parameters** **None** –

**Returns** The tracer diffusion coefficient, D\*.

**Return type** (Float)

### 3.1.12 lattice\_mc.species module

**class** lattice\_mc.species.**Species** (*atoms*)

Bases: object

Species class.

Contains methods that operate on sets of Atom objects

**collective\_correlation** ()

Collective correlation factor, f\_I, for these atoms.

**Parameters** **None** –

**Returns** The collective correlation factor, f\_I, for these atoms.

**Return type** (Float)

**collective\_dr\_squared** ()

Squared sum of total displacements for these atoms.

**Parameters** **None** –

**Returns** The square of the summed total displacements for these atoms.

**Return type** (Float)

**occupations** (*site\_label*)

Number of these atoms occupying a specific site type.

**Parameters** **site\_label** (*Str*) – Label for the site type being considered.

**Returns** Number of atoms occupying sites of type *site\_label*.

**Return type** (Int)

**sites\_occupied()**

Returns a list of sites occupied by these atoms.

**Parameters** *None* –

**Returns** List of sites occupied by these atoms.

**Return type** (List)

**sum\_dr\_squared()**

Sum of squared total displacements for these atoms.

**Parameters** *None* –

**Returns** The sum of squared total displacements for these atoms.

**Return type** (Float)

**summed\_dr2()**

Sum of squared individual displacements for these atoms.

**Parameters** *None* –

**Returns** The sum of squared individual displacements for these atoms.

**Return type** (Float)

**tracer\_correlation()**

Tracer correlation factor, *f*, for these atoms.

**Parameters** *None* –

**Returns** The tracer correlation factor, *f*, for these atoms.

**Return type** (Float)

### 3.1.13 lattice\_mc.transitions module

**class** `lattice_mc.transitions.Transitions` (*jumps*)

Bases: `object`

Transitions class

Contains methods that operate on sets of Jumps.

**cumulative\_probabilities()**

Cumulative sum of the relative probabilities for all possible jumps.

**Parameters** *None* –

**Returns** Cumulative sum of relative jump probabilities.

**Return type** (`np.array`)

**random()**

Select a jump at random with appropriate relative probabilities.

**Parameters** *None* –

**Returns** The randomly selected Jump.

**Return type** (*Jump*)

**time\_to\_jump()**

The timestep until the next jump.

**Parameters** *None* –

**Returns** The timestep until the next jump.

**Return type** (Float)

### 3.1.14 Module contents



## CHAPTER 4

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