
hdbscan Documentation

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The hdbscan library is a suite of tools to use unsupervised learning to find clusters, or dense regions, of a dataset. The primary algorithm is HDBSCAN* as proposed by Campello, Moulavi, and Sander. The library provides a high performance implementation of this algorithm, along with tools for analysing the resulting clustering.

Basic Usage of HDBSCAN* for Clustering

We have some data, and we want to cluster it. How exactly do we do that, and what do the results look like? If you are very familiar with sklearn and its API, particularly for clustering, then you can probably skip this tutorial – `hdbscan` implements exactly this API, so you can use it just as you would any other sklearn clustering algorithm. If, on the other hand, you aren't that familiar with sklearn, fear not, and read on. Let's start with the simplest case first – we have data in a nice tidy dataframe format.

The Simple Case

Let's generate some data with, say 2000 samples, and 10 features. We can put it in a dataframe for a nice clean table view of it.

```
blobs, labels = make_blobs(n_samples=2000, n_features=10)
```

```
pd.DataFrame(blobs).head()
```

So now we need to import the `hdbscan` library.

```
import hdbscan
```

Now, to cluster we need to generate a clustering object.

```
clusterer = hdbscan.HDBSCAN()
```

We can then use this clustering object and fit it to the data we have. This will return the clusterer object back to you – just in case you want to do some method chaining.

```
clusterer.fit(blobs)
```

```
HDBSCAN(algorithm='best', alpha=1.0, approx_min_span_tree=True,
        gen_min_span_tree=False, leaf_size=40, memory=Memory(cachedir=None),
        metric='euclidean', min_cluster_size=5, min_samples=None, p=None)
```

At this point we are actually done! We've done the clustering! But where are the results? How do I get the clusters? The clusterer object knows, and stores the result in an attribute `labels_`.

```
clusterer.labels_
```

```
array([2, 2, 2, ..., 2, 2, 0])
```

So it is an array of integers. What are we to make of that? It is an array with an integer for each data sample. Samples that are in the same cluster get assigned the same number. The cluster labels are 0 up numbers. We can thus determine the number of clusters found by checking what the largest cluster label is.

```
clusterer.labels_.max()
```

```
2
```

So we have a total of three clusters, with labels 0, 1, and 2. Importantly HDBSCAN is noise aware – it has a notion of data samples that are not assigned to any cluster. This is handled by assigning these samples the label -1. But wait, there's more. The `hdbscan` library implements soft clustering, where each data point is assigned a cluster membership score ranging from 0.0 to 1.0. A score of 0.0 represents a sample that is not in the cluster at all (all noise points will get this score) while a score of 1.0 represents a sample that is at the heart of the cluster (note that this is not the spatial centroid notion of core). You can access these scores via the `probabilities_` attribute.

```
clusterer.probabilities_
```

```
array([ 0.83890858,  1.          ,  0.72629904, ...,  0.79456452,
        0.65311137,  0.76382928])
```

What about different metrics?

That is all well and good, but even data that is embedded in a vector space may not want to consider distances between data points to be pure Euclidean distance. What can we do in that case? We are still in good shape, since `hdbscan` supports a wide variety of metrics, which you can set when creating the clusterer object. For example we can do the following:

```
clusterer = hdbscan.HDBSCAN(metric='manhattan')
clusterer.fit(blobs)
clusterer.labels_
```

```
array([1, 1, 1, ..., 1, 1, 0])
```

What metrics are supported? Because we simply steal metric computations from `sklearn` we get a large number of metrics readily available.

```
hdbscan.dist_metrics.METRIC_MAPPING
```

```
{'braycurtis': hdbscan.dist_metrics.BrayCurtisDistance,
 'canberra': hdbscan.dist_metrics.CanberraDistance,
 'chebyshev': hdbscan.dist_metrics.ChebyshevDistance,
 'cityblock': hdbscan.dist_metrics.ManhattanDistance,
```



```
'dice': hdbscan.dist_metrics.DiceDistance,
'euclidean': hdbscan.dist_metrics.EuclideanDistance,
'hamming': hdbscan.dist_metrics.HammingDistance,
'haversine': hdbscan.dist_metrics.HaversineDistance,
'infinity': hdbscan.dist_metrics.ChebyshevDistance,
'jaccard': hdbscan.dist_metrics.JaccardDistance,
'kulsinski': hdbscan.dist_metrics.KulsinskiDistance,
'l1': hdbscan.dist_metrics.ManhattanDistance,
'l2': hdbscan.dist_metrics.EuclideanDistance,
'mahalanobis': hdbscan.dist_metrics.MahalanobisDistance,
'manhattan': hdbscan.dist_metrics.ManhattanDistance,
'matching': hdbscan.dist_metrics.MatchingDistance,
'minkowski': hdbscan.dist_metrics.MinkowskiDistance,
'p': hdbscan.dist_metrics.MinkowskiDistance,
'pyfunc': hdbscan.dist_metrics.PyFuncDistance,
'rogerstanimoto': hdbscan.dist_metrics.RogersTanimotoDistance,
'russellrao': hdbscan.dist_metrics.RussellRaoDistance,
'seuclidean': hdbscan.dist_metrics.SEuclideanDistance,
'sokalmichener': hdbscan.dist_metrics.SokalMichenerDistance,
'sokalsneath': hdbscan.dist_metrics.SokalSneathDistance,
'wminkowski': hdbscan.dist_metrics.WMinkowskiDistance}
```

Distance matrices

What if you don't have a nice set of points in a vector space, but only have a pairwise distance matrix providing the distance between each pair of points? This is a common situation. Perhaps you have a complex custom distance measure; perhaps you have strings and are using Levenstein distance, etc. Again, this is all fine as hdbscan supports a special metric called `precomputed`. If you create the clusterer with the metric set to `precomputed` then the clusterer will assume that, rather than being handed a vector of points in a vector space, it is receiving an all pairs distance matrix.

```
distance_matrix = pairwise_distances(blobs)
clusterer = hdbscan.HDBSCAN(metric='precomputed')
clusterer.fit(distance_matrix)
clusterer.labels_
```

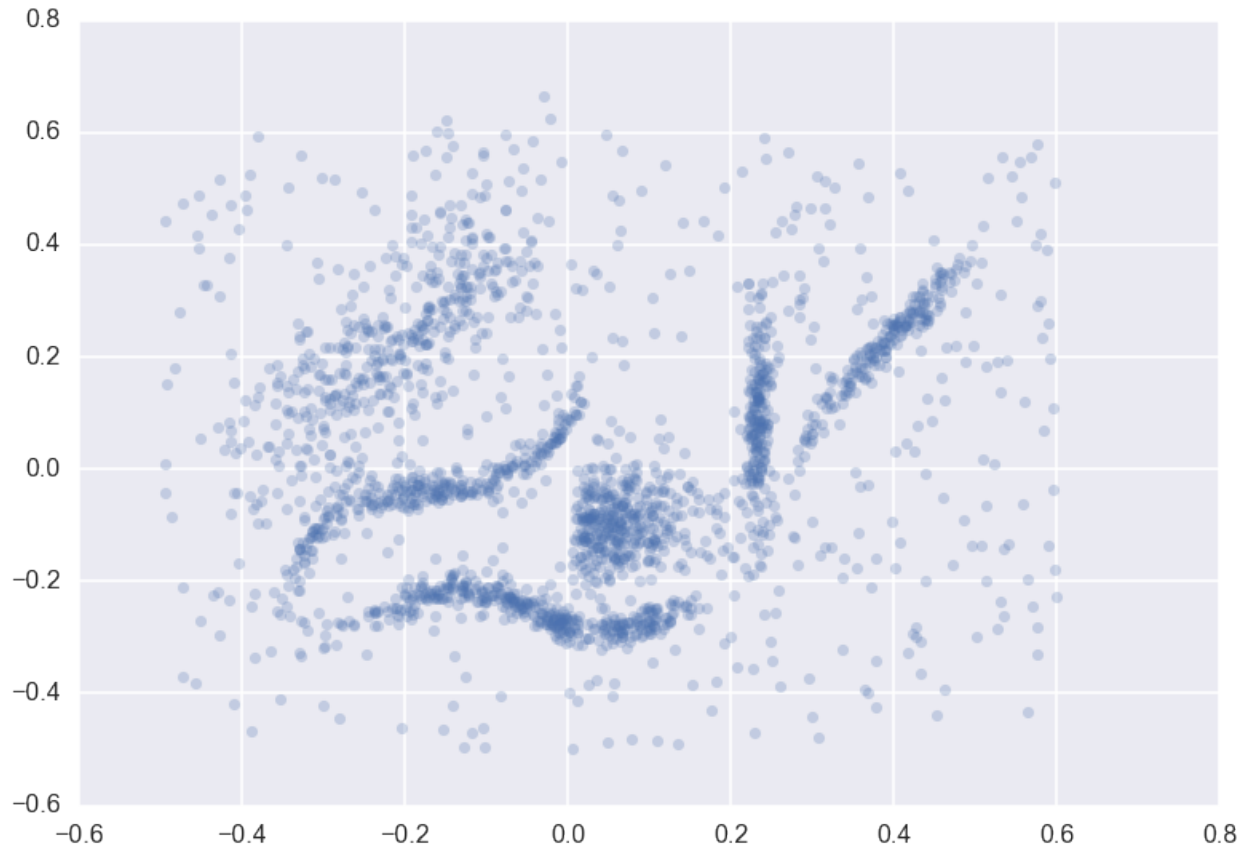
```
array([1, 1, 1, ..., 1, 1, 2])
```

Note that this result only appears different due to a different labelling order for the clusters.

Getting More Information About a Clustering

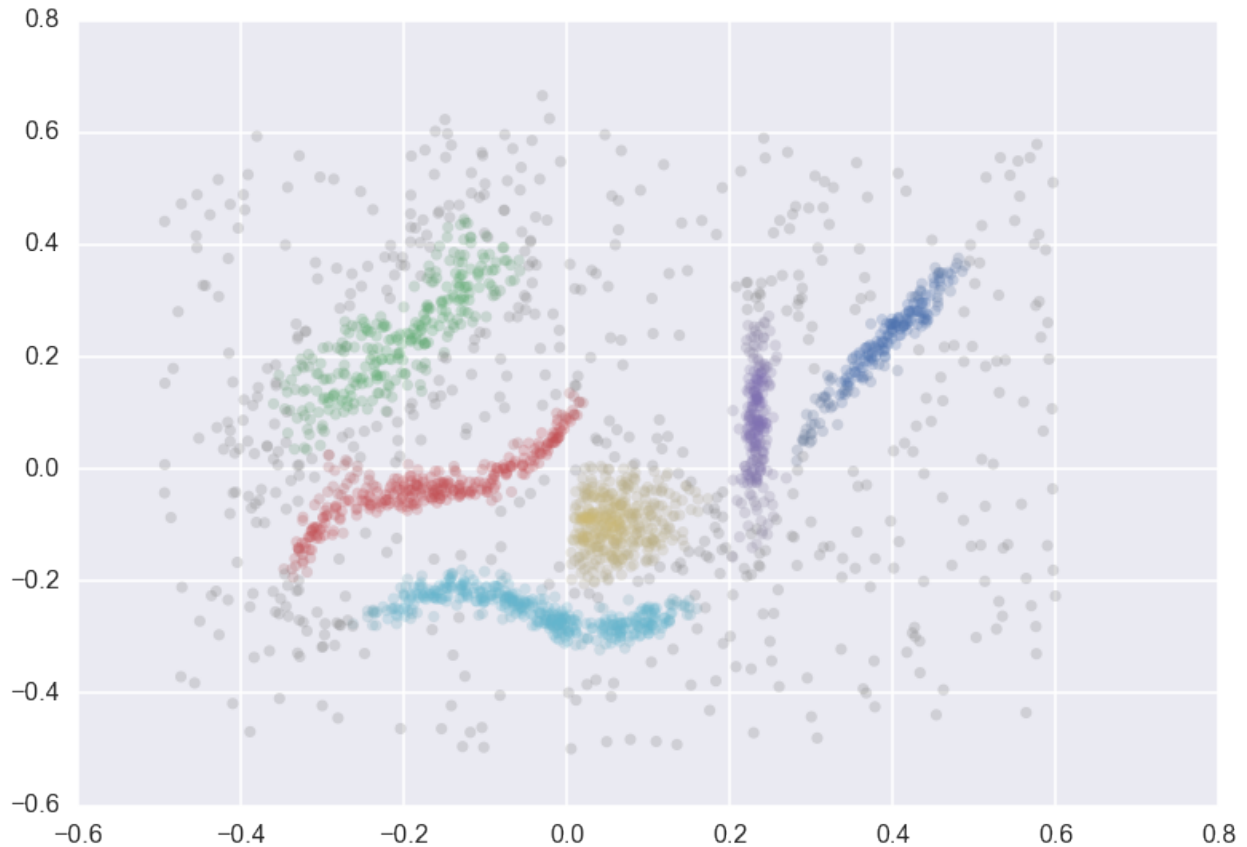
Once you have the basics of clustering sorted you may want to dig a little deeper than just the cluster labels returned to you. Fortunately the hdbscan library provides you with the facilities to do this. During processing HDBSCAN* builds a hierarchy of potential clusters, from which it extracts the flat clustering returned. It can be informative to look at that hierarchy, and potentially make use of the extra information contained therein.

Suppose we have a dataset for clustering



We can cluster the data as normal, and visualize the labels with different colors (and even the cluster membership strengths as levels of saturation)

```
clusterer = hdbscan.HDBSCAN(min_cluster_size=15).fit(data)
color_palette = sns.color_palette('deep', 8)
cluster_colors = [color_palette[x] if x >= 0
                  else (0.5, 0.5, 0.5)
                  for x in clusterer.labels_]
cluster_member_colors = [sns.desaturate(x, p) for x, p in
                        zip(cluster_colors, clusterer.probabilities_)]
plt.scatter(*data.T, s=50, linewidth=0, c=cluster_member_colors, alpha=0.25)
```



Condensed Trees

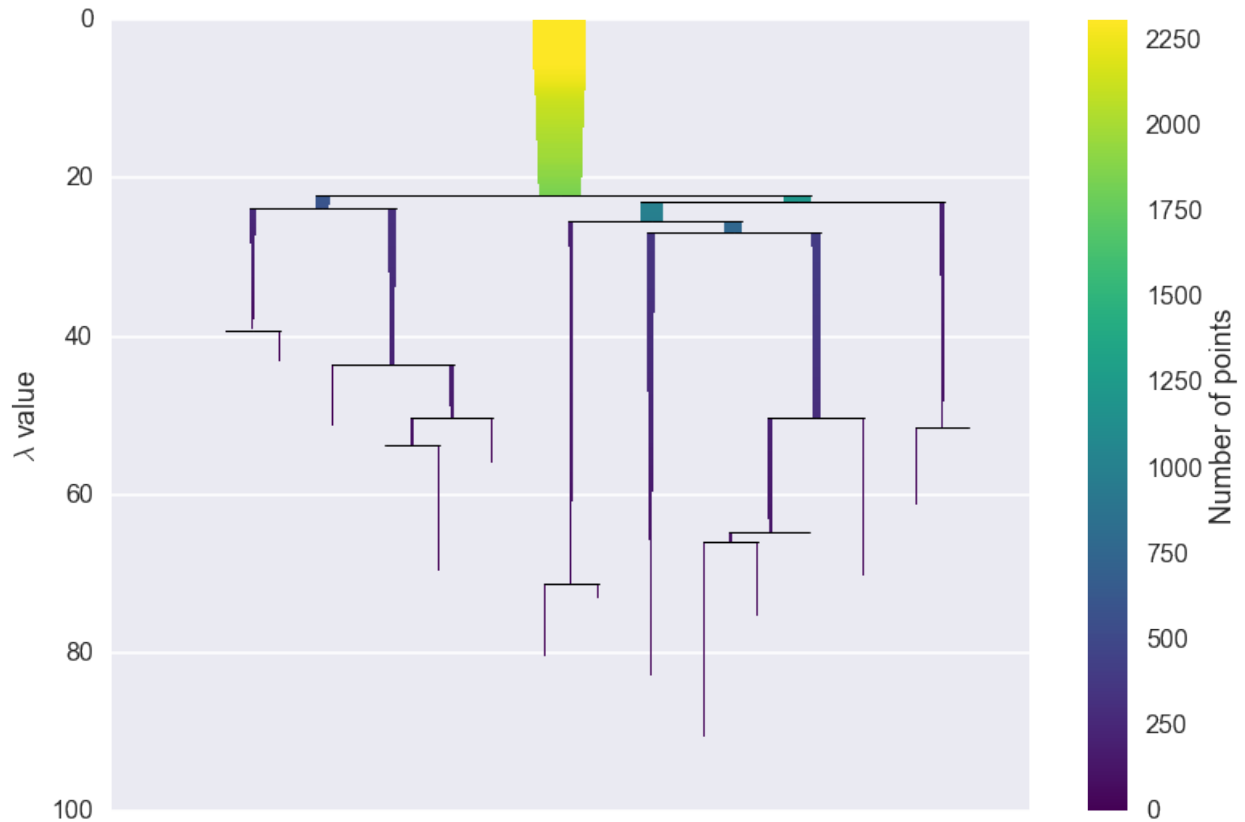
The question now is what does the cluster hierarchy look like – which clusters are near each other, or could perhaps be merged, and which are far apart. We can access the basic hierarchy via the `condensed_tree_` attribute of the clusterer object.

```
clusterer.condensed_tree_
```

```
<hdbscan.plots.CondensedTree at 0x10ea23a20>
```

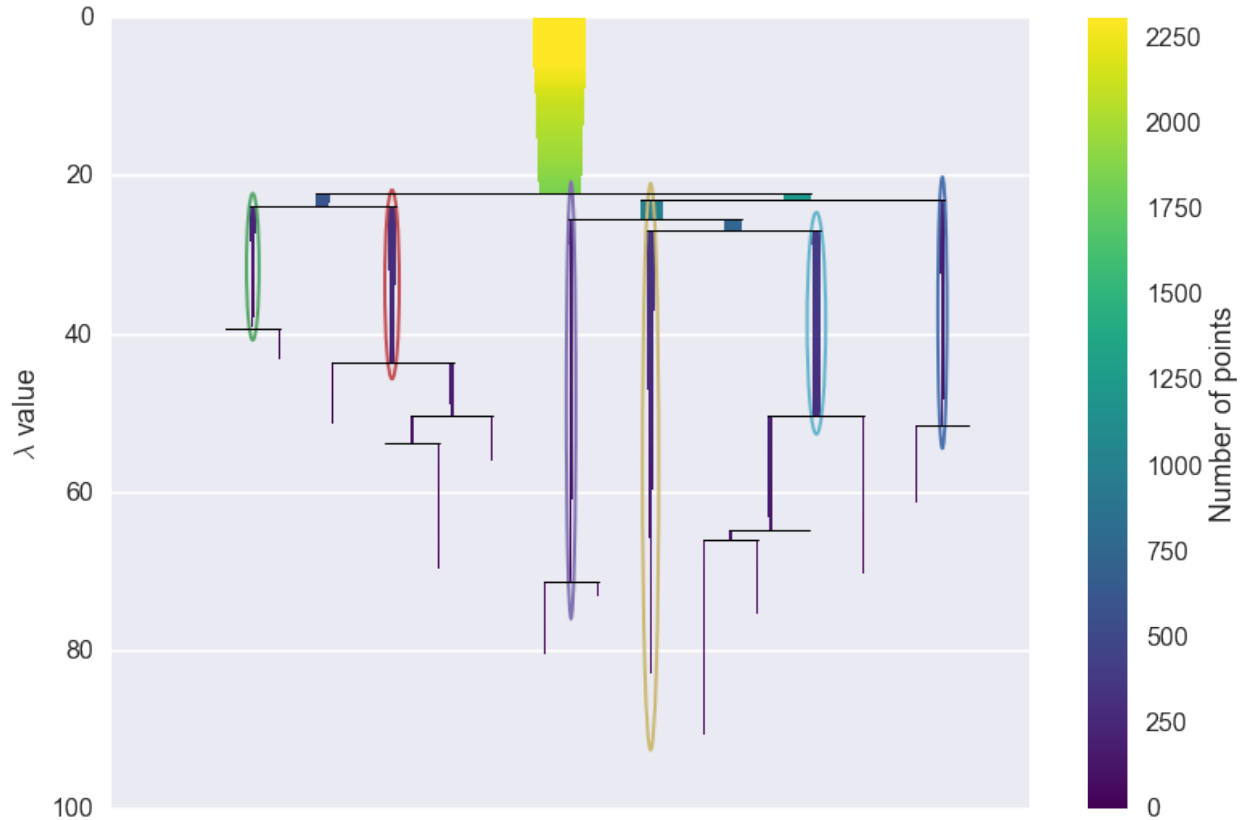
This merely gives us a *CondensedTree* object. If we want to visualize the hierarchy we can call the `plot()` method:

```
clusterer.condensed_tree_.plot()
```



We can now see the hierarchy as a dendrogram, the width (and color) of each branch representing the number of points in the cluster at that level. If we wish to know which branches were selected by the HDBSCAN* algorithm we can pass `select_clusters=True`. You can even pass a selection palette to color the selections according to the cluster labelling.

```
clusterer.condensed_tree_.plot(select_clusters=True,  
                               selection_palette=sns.color_palette('deep', 8))
```



From this we can see, for example, that the yellow cluster, at the center of the plot, forms early (breaking off from the pale blue and purple clusters) and persists for a long time. By comparison the green cluster, which also forming early, quickly breaks apart and then vanishes altogether (shattering into clusters all smaller than the `min_cluster_size` of 15).

You can also see that the pale blue cluster breaks apart into several subclusters that in turn persist for quite some time – so there is some interesting substructure to the pale blue cluster that is not present, for example, in the dark blue cluster.

If this was a simple visual analysis of the condensed tree can tell you a lot more about the structure of your data. This is not all we can do with condensed trees however. For larger and more complex datasets the tree itself may be very complex, and it may be desirable to run more interesting analytics over the tree itself. This can be achieved via several converter methods: `to_networkx()`, `to_pandas()`, and `to_numpy()`.

First we'll consider `to_networkx()`

```
clusterer.condensed_tree_.to_networkx()
```

```
<networkx.classes.digraph.DiGraph at 0x11d8023c8>
```

As you can see we get a networkx directed graph, which we can then use all the regular networkx tools and analytics on. The graph is richer than the visual plot above may lead you to believe however:

```
g = clusterer.condensed_tree_.to_networkx()
g.number_of_nodes()
```

```
2338
```

The graph actually contains nodes for all the points falling out of clusters as well as the clusters themselves. Each

node has an associated `size` attribute, and each edge has a `weight` of the `lambda` value at which that edge forms. This allows for much more interesting analyses.

Next we have the `to_pandas()` method, which returns a panda dataframe where each row corresponds to an edge of the networkx graph:

```
clusterer.condensed_tree_.to_pandas().head()
```

Here the `parent` denotes the id of the parent cluster, the `child` the id of the child cluster (or, if the child is a single data point rather than a cluster, the index in the dataset of that point), the `lambda_val` provides the `lambda` value at which the edge forms, and the `child_size` provides the number of points in the child cluster. As you can see the start of the dataframe has singleton points falling out of the root cluster, with each `child_size` equal to 1.

If you want just the clusters, rather than all the individual points as well, simply select the rows of the dataframe with `child_size` greater than 1.

```
tree = clusterer.condensed_tree_.to_pandas()
cluster_tree = tree[tree.child_size > 1]
```

Finally we have the `to_numpy()` function, which returns a numpy record array:

```
clusterer.condensed_tree_.to_numpy()
```

```
array([(2309, 2048, 5.016525967983049, 1),
      (2309, 2006, 5.076503128308643, 1),
      (2309, 2024, 5.279133057912248, 1), ...,
      (2318, 1105, 86.5507370650292, 1), (2318, 965, 86.5507370650292, 1),
      (2318, 954, 86.5507370650292, 1)],
      dtype=[('parent', '<i8'), ('child', '<i8'), ('lambda_val', '<f8'), ('child_size', '<i8')])
```

This is equivalent to the pandas dataframe, but is in pure numpy and hence has no pandas dependencies if you do not wish to use pandas.

Single Linkage Trees

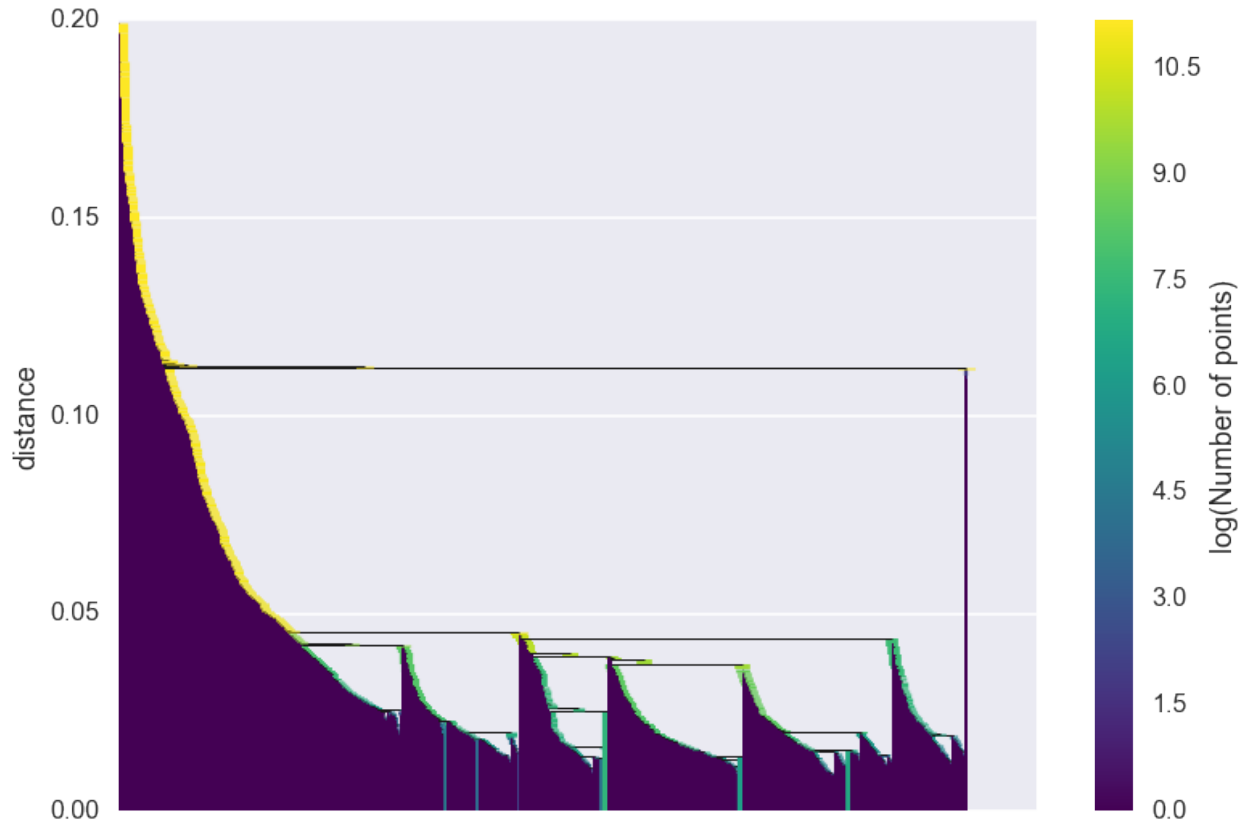
We have still more data at our disposal however. As noted in the [How HDBSCAN Works](#) section, prior to providing a condensed tree the algorithm builds a complete dendrogram. We have access to this too via the `single_linkage_tree_` attribute of the clusterer.

```
clusterer.single_linkage_tree_
```

```
<hdbscan.plots.SingleLinkageTree at 0x121d4b128>
```

Again we have an object which we can then query for relevant information. The most basic approach is the `plot()` method, just like the condensed tree.

```
clusterer.single_linkage_tree_.plot()
```



As you can see we gain a lot from condensing the tree in terms of better presenting and summarising the data. There is a lot less to be gained from visual inspection of a plot like this (and it only gets worse for larger datasets). The plot function support most of the same functionality as the dendrogram plotting from `scipy.cluster.hierarchy`, so you can view various truncations of the tree if necessary. In practice, however, you are more likely to be interested in access the raw data for further analysis. Again we have `to_networkx()`, `to_pandas()` and `to_numpy()`. This time the `to_networkx()` provides a direct networkx version of what you see above. The numpy and pandas results conform to the single linkage hierarchy format of `scipy.cluster.hierarchy`, and can be passed to routines there if necessary.

If you wish to know what the clusters are at a given fixed level of the single linkage tree you can use the `get_clusters()` method to extract a vector of cluster labels. The method takes a cut value of the level at which to cut the tree, and a `minimum_cluster_size` to determine noise points (any cluster smaller than the `minimum_cluster_size`).

```
clusterer.single_linkage_tree_.get_clusters(0.023, min_cluster_size=2)
```

```
array([ 0, -1,  0, ..., -1, -1,  0])
```

In this way it is possible to extract the DBSCAN clustering that would result for any given epsilon value, all from one run of hdbscan.

Parameter Selection for HDBSCAN*

While the HDBSCAN class has a large number of parameters that can be set on initialization, in practice there are a very small number of parameters that have significant practical effect on clustering. We will consider those major parameters, and consider how one may go about choosing them effectively.

Selecting `min_cluster_size`

The primary parameter to effect the resulting clustering is `min_cluster_size`. Ideally this is a relatively intuitive parameter to select – set it to the smallest size grouping that you wish to consider a cluster. It can have slightly non-obvious effects however. Let’s consider the digits dataset from sklearn. We can project the data into two dimensions to visualize it via t-SNE.

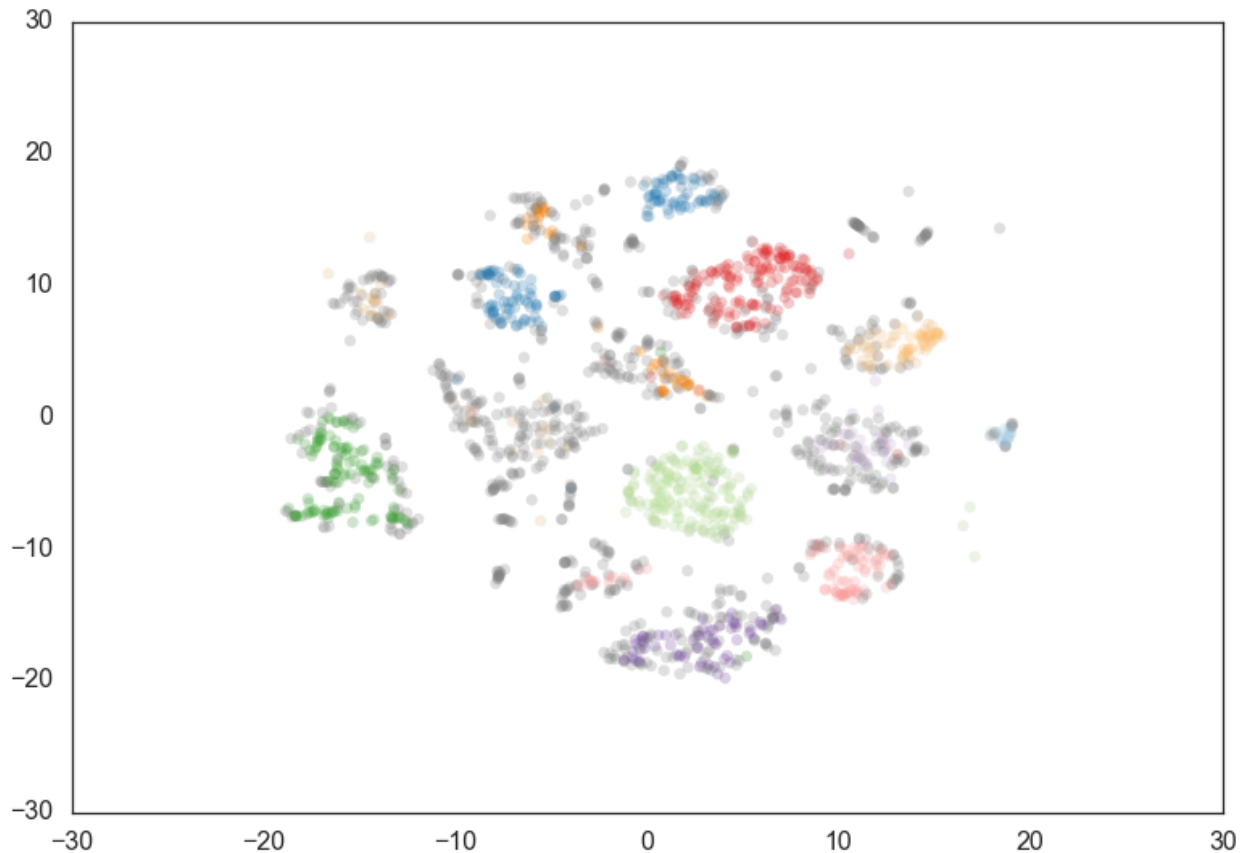
```
digits = datasets.load_digits()
data = digits.data
projection = TSNE().fit_transform(data)
plt.scatter(*projection.T, **plot_kws)
```



If we cluster this data in the full 64 dimensional space with HDBSCAN* we can see some effects from varying the `min_cluster_size`.

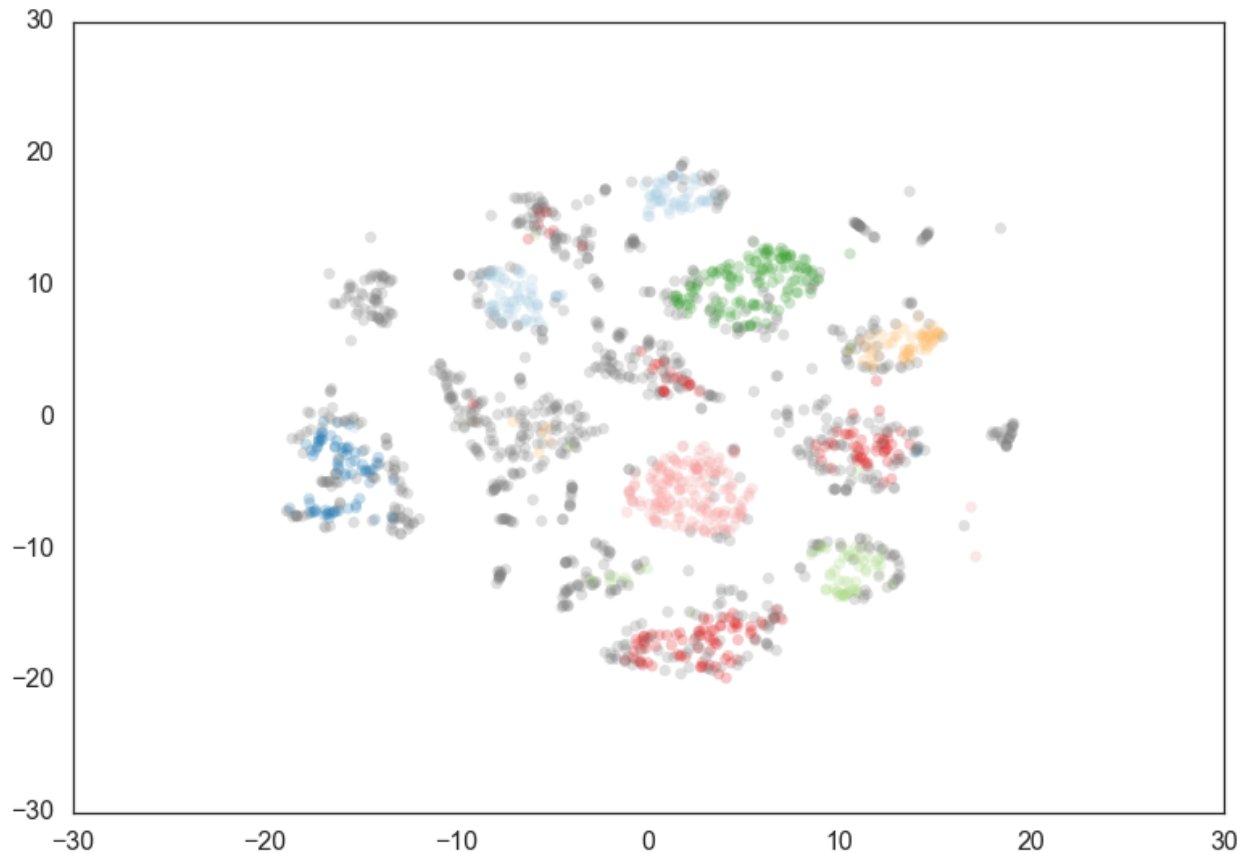
We start with a `min_cluster_size` of 15.

```
clusterer = hdbscan.HDBSCAN(min_cluster_size=15).fit(data)
color_palette = sns.color_palette('Paired', 12)
cluster_colors = [color_palette[x] if x >= 0
                  else (0.5, 0.5, 0.5)
                  for x in clusterer.labels_]
cluster_member_colors = [sns.desaturate(x, p) for x, p in
                        zip(cluster_colors, clusterer.probabilities_)]
plt.scatter(*projection.T, s=50, linewidth=0, c=cluster_member_colors, alpha=0.25)
```

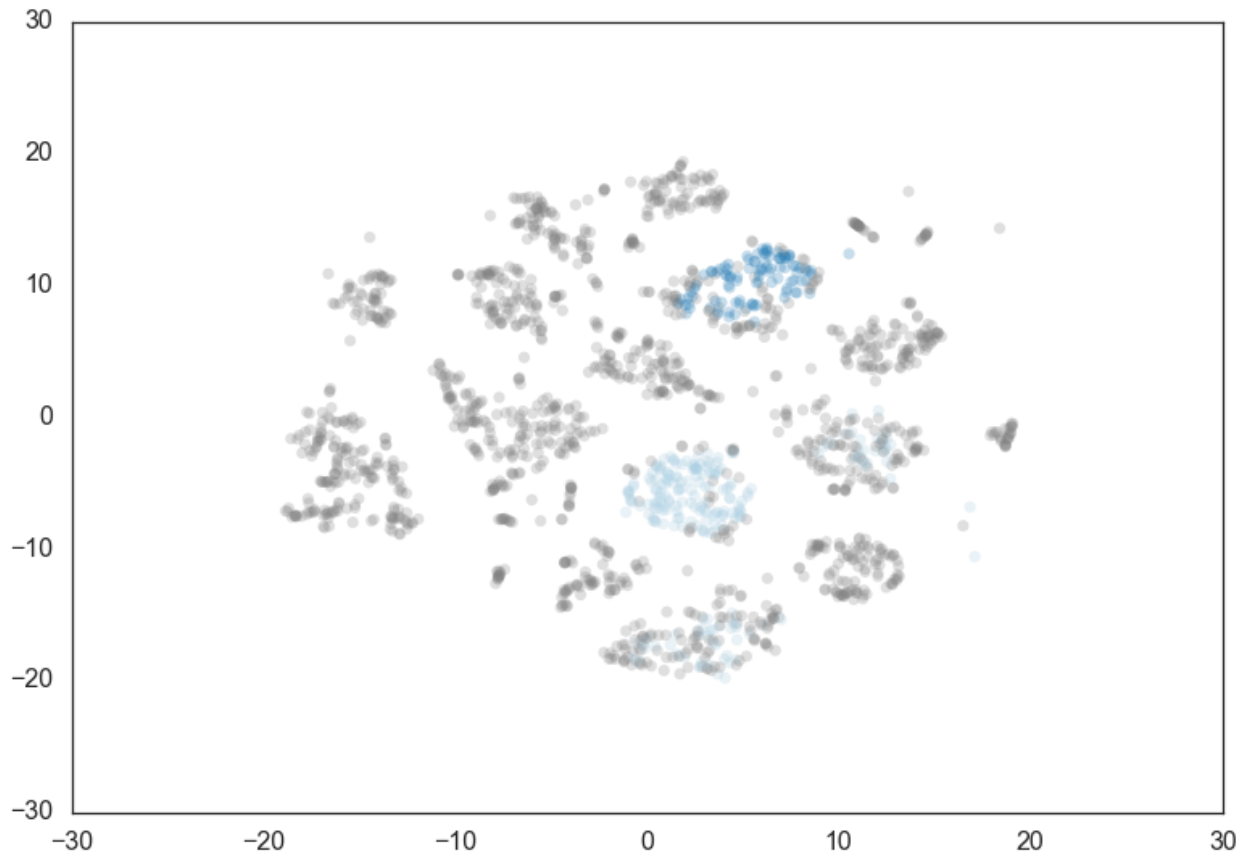
Increasing the `min_cluster_size` to 30 reduces the number of clusters, merging some together. This is a result of HDBSCAN* reoptimizing which flat clustering provides greater stability under a slightly different notion of what constitutes a cluster.

```
clusterer = hdbscan.HDBSCAN(min_cluster_size=30).fit(data)
color_palette = sns.color_palette('Paired', 12)
cluster_colors = [color_palette[x] if x >= 0
                  else (0.5, 0.5, 0.5)
                  for x in clusterer.labels_]
cluster_member_colors = [sns.desaturate(x, p) for x, p in
                        zip(cluster_colors, clusterer.probabilities_)]
plt.scatter(*projection.T, s=50, linewidth=0, c=cluster_member_colors, alpha=0.25)
```

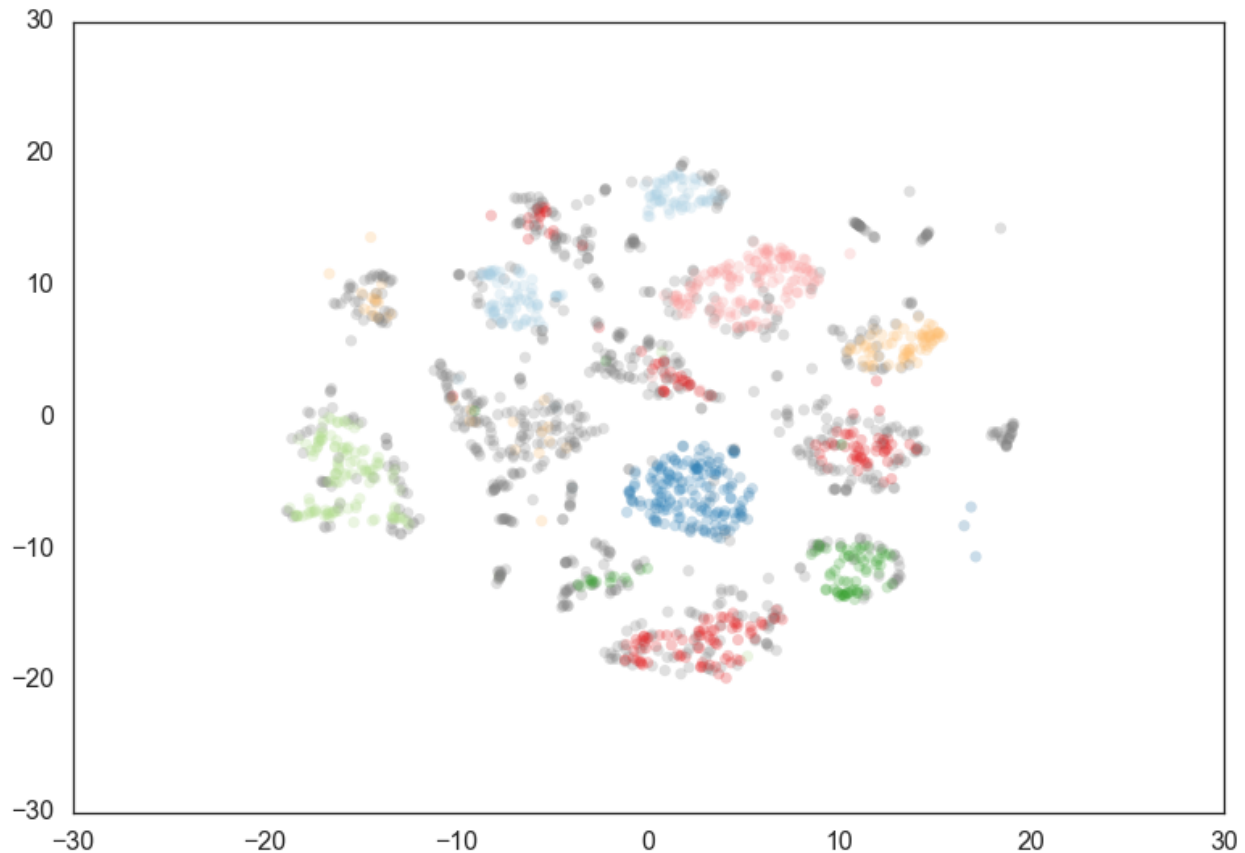


Doubling the `min_cluster_size` again to 60 gives us just two clusters – the really core clusters. This is somewhat as expected, but surely some of the other clusters that we had previously had more than 60 members? Why are they being considered noise? The answer is that HDBSCAN* has a second parameter `min_samples`. The implementation defaults this value (if it is unspecified) to whatever `min_cluster_size` is set to. We can recover some of our original clusters by explicitly providing `min_samples` at the original value of 15.

```
clusterer = hdbscan.HDBSCAN(min_cluster_size=60).fit(data)
color_palette = sns.color_palette('Paired', 12)
cluster_colors = [color_palette[x] if x >= 0
                  else (0.5, 0.5, 0.5)
                  for x in clusterer.labels_]
cluster_member_colors = [sns.desaturate(x, p) for x, p in
                        zip(cluster_colors, clusterer.probabilities_)]
plt.scatter(*projection.T, s=50, linewidth=0, c=cluster_member_colors, alpha=0.25)
```



```
clusterer = hdbscan.HDBSCAN(min_cluster_size=60, min_samples=15).fit(data)
color_palette = sns.color_palette('Paired', 12)
cluster_colors = [color_palette[x] if x >= 0
                  else (0.5, 0.5, 0.5)
                  for x in clusterer.labels_]
cluster_member_colors = [sns.desaturate(x, p) for x, p in
                        zip(cluster_colors, clusterer.probabilities_)]
plt.scatter(*projection.T, s=50, linewidth=0, c=cluster_member_colors, alpha=0.25)
```



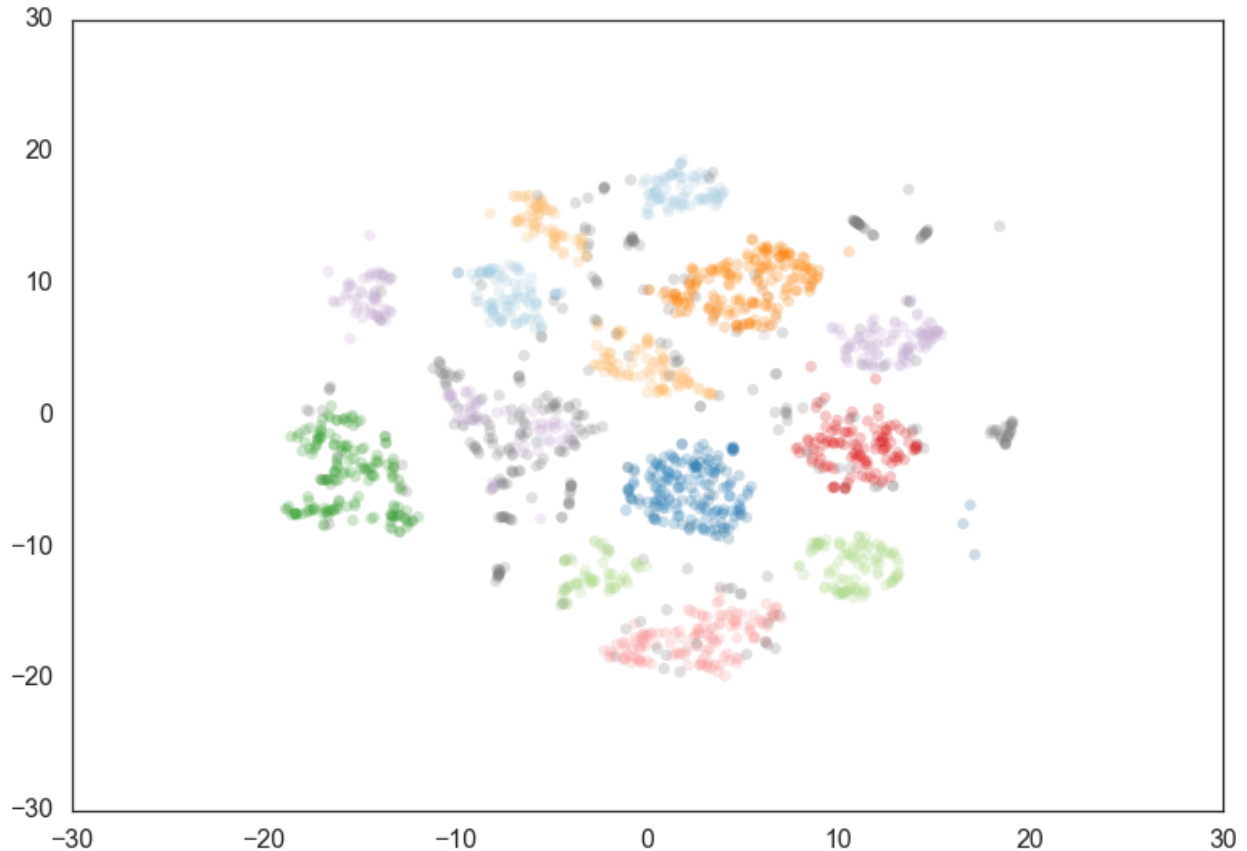
As you can see this results in us recovering something much closer to our original clustering, only now with some of the smaller clusters pruned out. Thus `min_cluster_size` does behave more closely to our intuitions, but only if we fix `min_samples`. If you wish to explore different `min_cluster_size` settings with a fixed `min_samples` value, especially for larger dataset sizes, you can cache the hard computation, and recompute only the relatively cheap flat cluster extraction using the `memory` parameter, which makes use of `joblib`

Selecting `min_samples`

Since we have seen that `min_samples` clearly has a dramatic effect on clustering, the question becomes: how do we select this parameter? The simplest intuition for what `min_samples` does is provide a measure of how conservative you want your clustering to be. The larger the value of `min_samples` you provide, the more conservative the clustering – more points will be declared as noise, and clusters will be restricted to progressively more dense areas. We can see this in practice by leaving the `min_cluster_size` at 60, but reducing `min_samples` to 1.

```
clusterer = hdbscan.HDBSCAN(min_cluster_size=60, min_samples=1).fit(data)
color_palette = sns.color_palette('Paired', 12)
cluster_colors = [color_palette[x] if x >= 0
                  else (0.5, 0.5, 0.5)
                  for x in clusterer.labels_]
cluster_member_colors = [sns.desaturate(x, p) for x, p in
                        zip(cluster_colors, clusterer.probabilities_)]
plt.scatter(*projection.T, s=50, linewidth=0, c=cluster_member_colors, alpha=0.25)
```

```
<matplotlib.collections.PathCollection at 0x120978438>
```

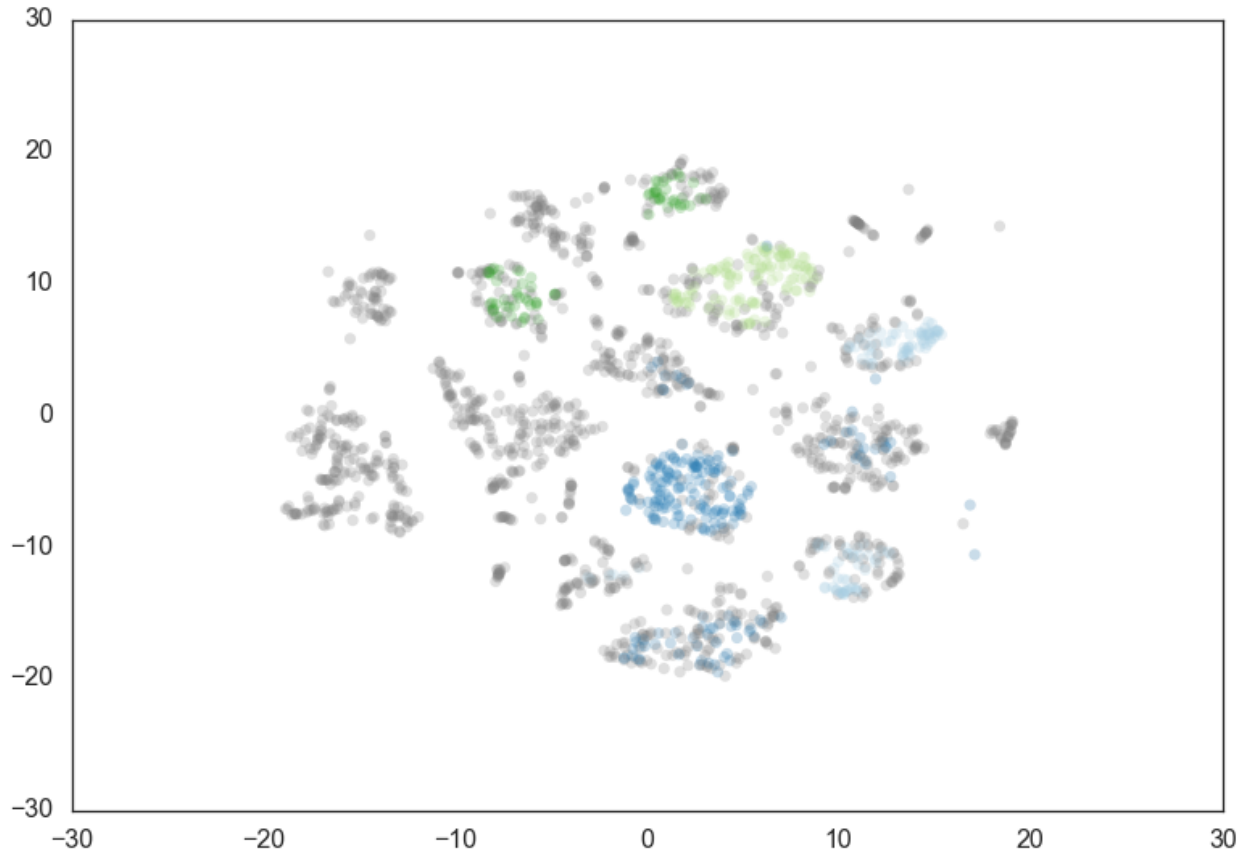


Now most points are clustered, and there are much fewer noise points. Steadily increasing `min_samples` will, as we saw in the examples above, make the clustering progressively more conservative, culminating in the example above where `min_samples` was set to 60 and we had only two clusters with most points declared as noise.

Selecting `alpha`

A further parameter that effects the resulting clustering is `alpha`. In practice it is best not to mess with this parameter – ultimately it is part of the `RobustSingleLinkage` code, but flows naturally into `HDBSCAN*`. If, for some reason, `min_samples` is not providing you what you need, stop, rethink things, and try again with `min_samples`. If you still need to play with another parameter (and you shouldn't), then you can try setting `alpha`. The `alpha` parameter provides a slightly different approach to determining how conservative the clustering is. By default `alpha` is set to 1.0. Increasing `alpha` will make the clustering more conservative, but on a much tighter scale, as we can see by setting `alpha` to 1.3.

```
clusterer = hdbscan.HDBSCAN(min_cluster_size=60, min_samples=15, alpha=1.3).fit(data)
color_palette = sns.color_palette('Paired', 12)
cluster_colors = [color_palette[x] if x >= 0
                  else (0.5, 0.5, 0.5)
                  for x in clusterer.labels_]
cluster_member_colors = [sns.desaturate(x, p) for x, p in
                        zip(cluster_colors, clusterer.probabilities_)]
plt.scatter(*projection.T, s=50, linewidth=0, c=cluster_member_colors, alpha=0.25)
```

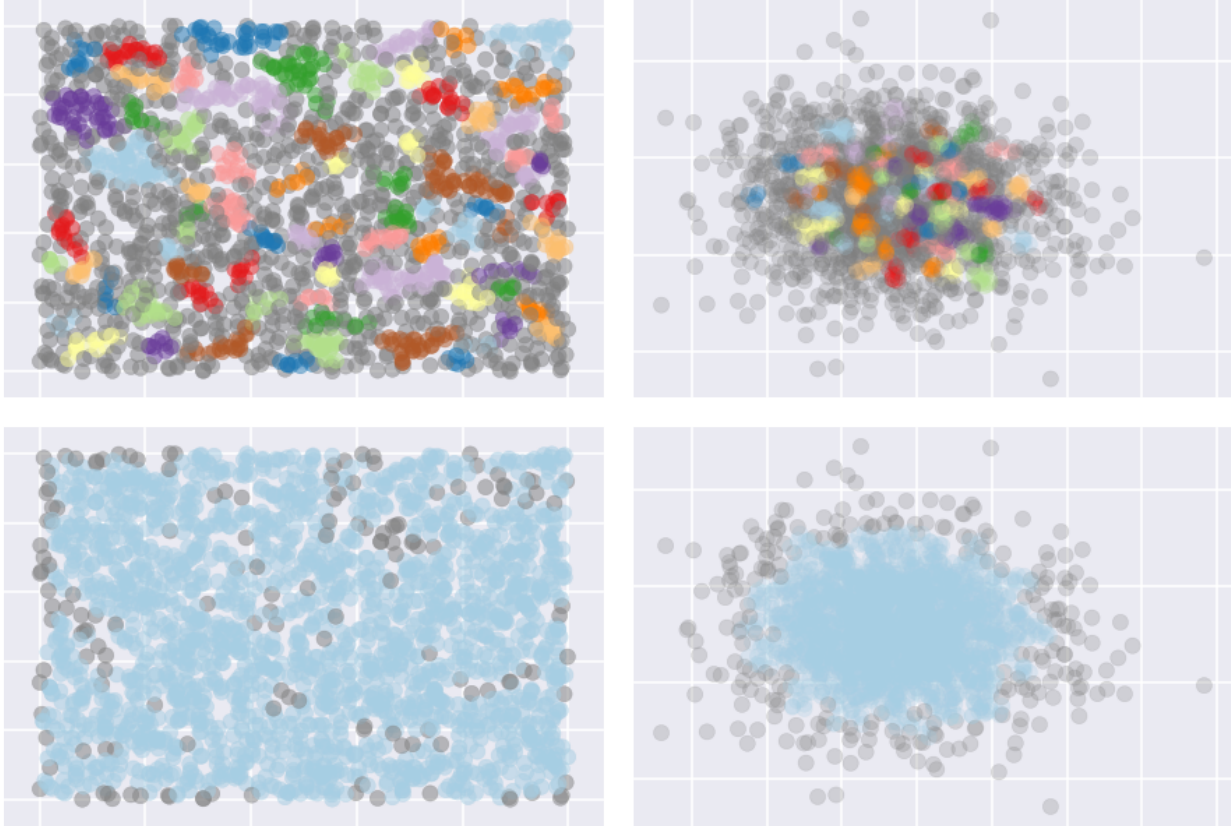


Leaf clustering

HDBSCAN supports an extra parameter `cluster_selection_method` to determine how it selects flat clusters from the cluster tree hierarchy. The default method is 'eom' for Excess of Mass, the algorithm described in [How HDBSCAN Works](#). This is not always the most desirable approach to cluster selection. If you are more interested in having small homogeneous clusters then you may find Excess of Mass has a tendency to pick one or two large clusters and then a number of small extra clusters. In this situation you may be tempted to recluster just the data in the single large cluster. Instead, a better option is to select 'leaf' as a cluster selection method. This will select leaf nodes from the tree, producing many small homogeneous clusters. Note that you can still get variable density clusters via this method, and it is also still possible to get large clusters, but there will be a tendency to produce a more fine grained clustering than Excess of Mass can provide.

Allowing a single cluster

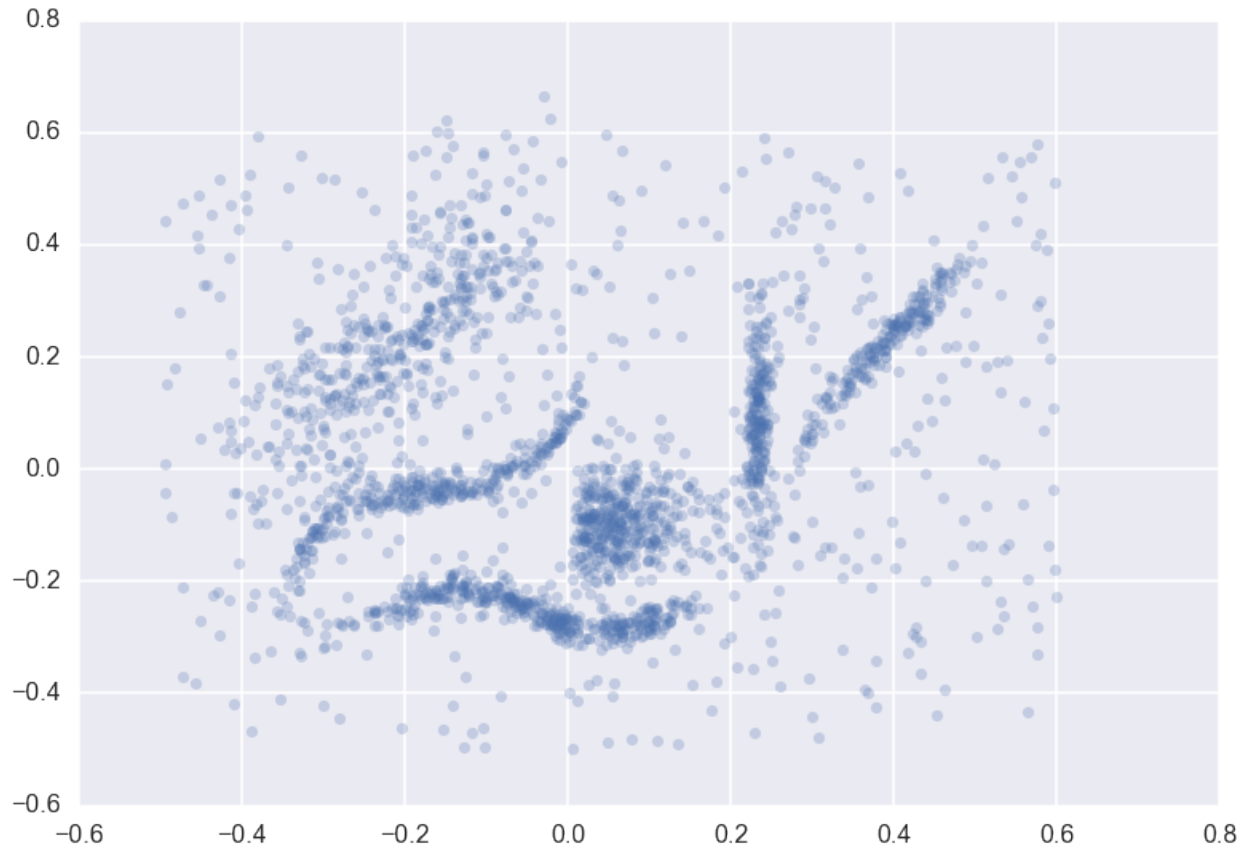
In contrast, if you are getting lots of small clusters, but believe there should be some larger scale structure (or the possibility of no structure), consider the `allow_single_cluster` option. By default HDBSCAN* does not allow a single cluster to be returned – this is due to how the Excess of Mass algorithm works, and a bias towards the root cluster that may occur. You can override this behaviour and see what clustering would look like if you allow a single cluster to be returned. This can alleviate issue caused by there only being a single large cluster, or by data that is essentially just noise. For example, the image below shows the effects of setting `allow_single_cluster=True` in the bottom row, compared to the top row which used default settings.



Outlier Detection

The hdbscan library supports the GLOSH outlier detection algorithm, and does so within the HDBSCAN clustering class. The GLOSH outlier detection algorithm is related to older outlier detection methods such as [LOF](#) and [LOCI](#). It is a fast and flexible outlier detection system, and supports a notion of local outliers. This means that it can detect outliers that may be noticeably different from points in its local region (for example points not on a local submanifold) but that are not necessarily outliers globally. So how do we find outliers? We proceed identically to the basic use of HDBSCAN*. We start with some data, and fit it with an HDBSCAN object.

```
plt.scatter(*data.T, s=50, linewidth=0, c='b', alpha=0.25)
```



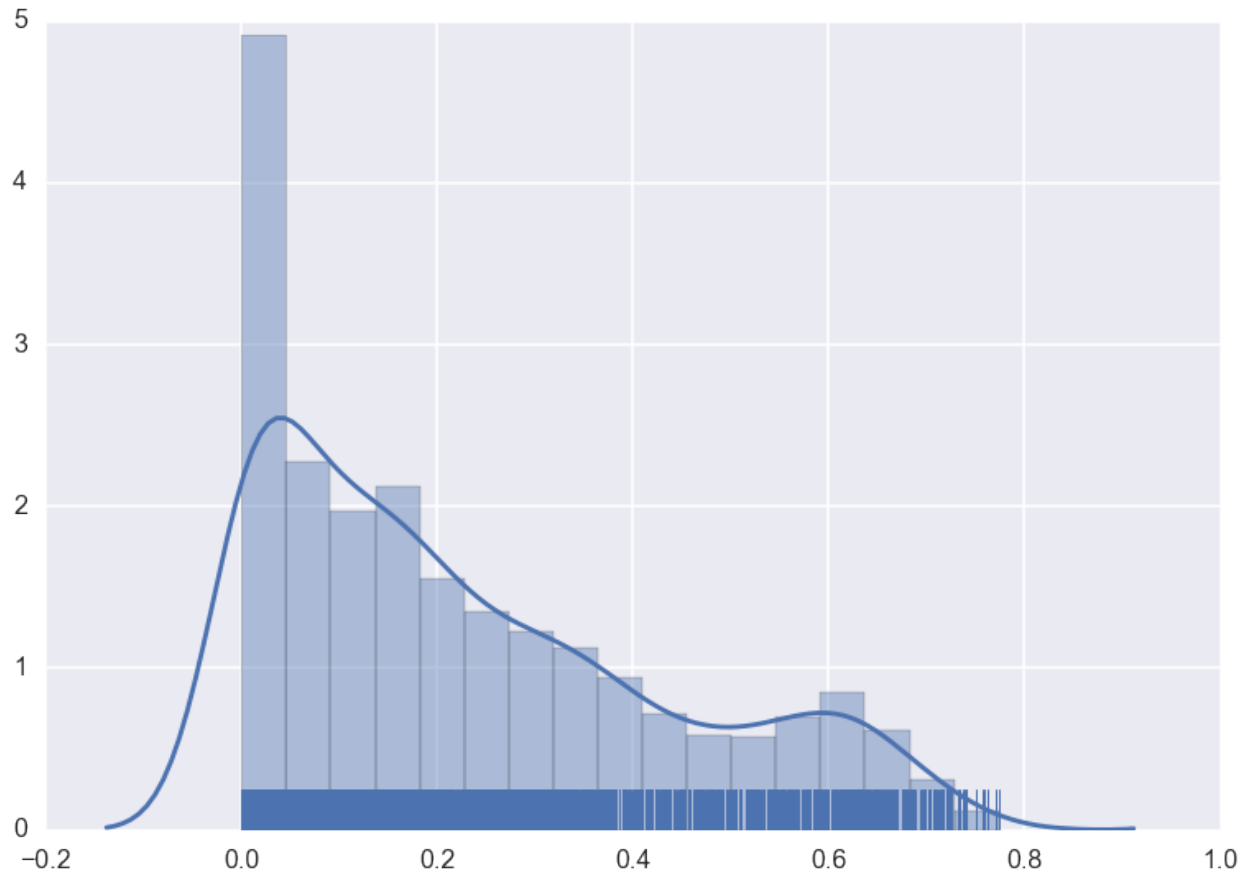
```
clusterer = hdbscan.HDBSCAN(min_cluster_size=15).fit(data)
```

The `clusterer` object now has an attribute (computed when first accessed) called `outlier_scores_`. This provides a numpy array with a value for each sample in the original dataset that was fit with the `clusterer`. The higher the score, the more likely the point is to be an outlier. In practice it is often best to look at the distributions of outlier scores.

```
clusterer.outlier_scores_
```

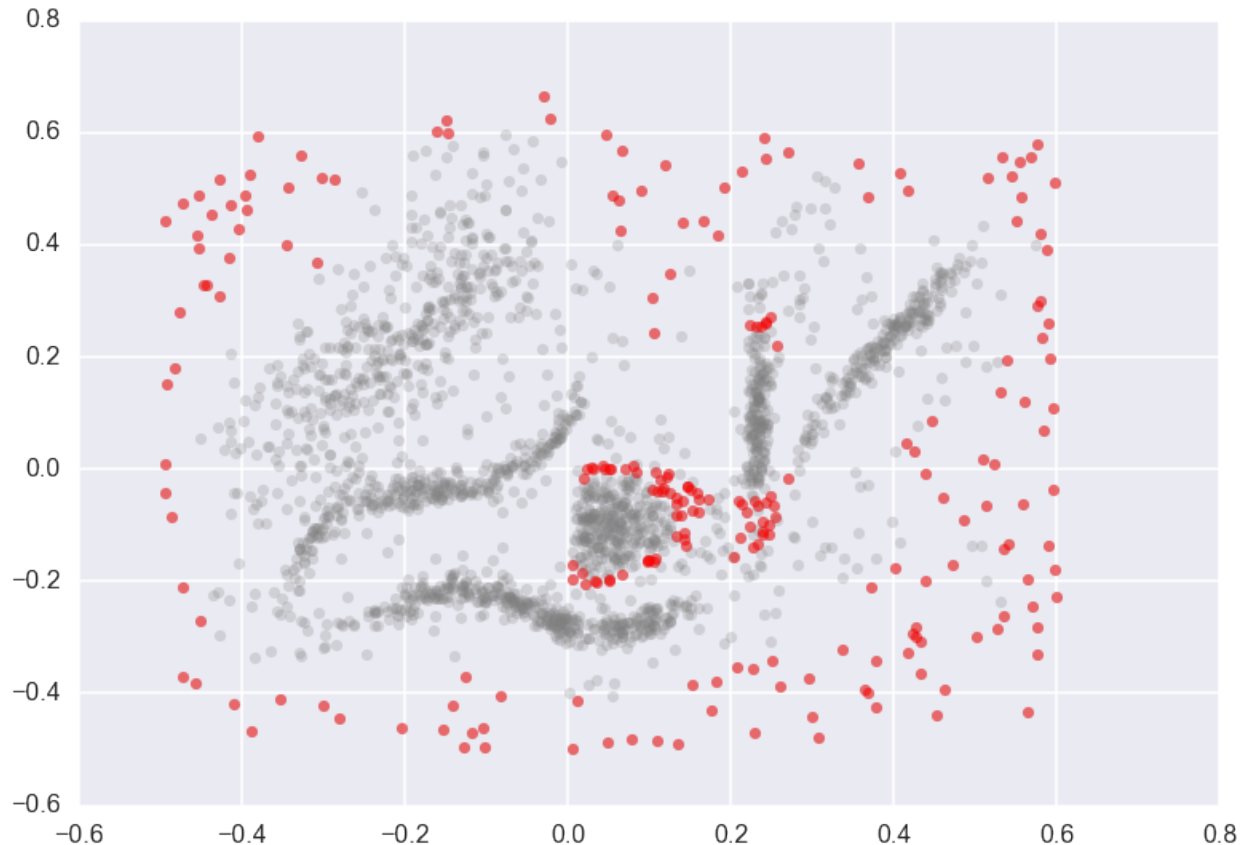
```
array([ 0.14791852,  0.14116731,  0.09171929, ...,  0.62050534,  
        0.56749298,  0.20681685])
```

```
sns.distplot(clusterer.outlier_scores_[np.isfinite(clusterer.outlier_scores_)],  
             rug=True)
```

We can pull off upper quantiles to detect outliers, which we can then plot.

```
threshold = pd.Series(clusterer.outlier_scores_).quantile(0.9)
outliers = np.where(clusterer.outlier_scores_ > threshold)[0]
plt.scatter(*data.T, s=50, linewidth=0, c='gray', alpha=0.25)
plt.scatter(*data[outliers].T, s=50, linewidth=0, c='red', alpha=0.5)
```



Note that not only are the outlying border points highlighted as outliers, but points at the edge of the central ball like cluster, and just below the vertical band cluster, are also designated as outliers. This is because those two clusters are extremely dense, and the points at the edge of this cluster are close enough to the cluster that they should be part of it, but far enough from the being core parts of the cluster that they are extremely unlikely and hence anomalous.

Predicting clusters for new points

Often it is useful to train a model once on a large amount of data, and then query the model repeatedly with small amounts of new data. This is hard for HDBSCAN* as it is a transductive method – new data points can (and should!) be able to alter the underlying clustering. That is, given new information it might make sense to create a new cluster, split an existing cluster, or merge two previously separate clusters. If the actual clusters (and hence their labels) change with each new data point it becomes impossible to compare the cluster assignments between such queries.

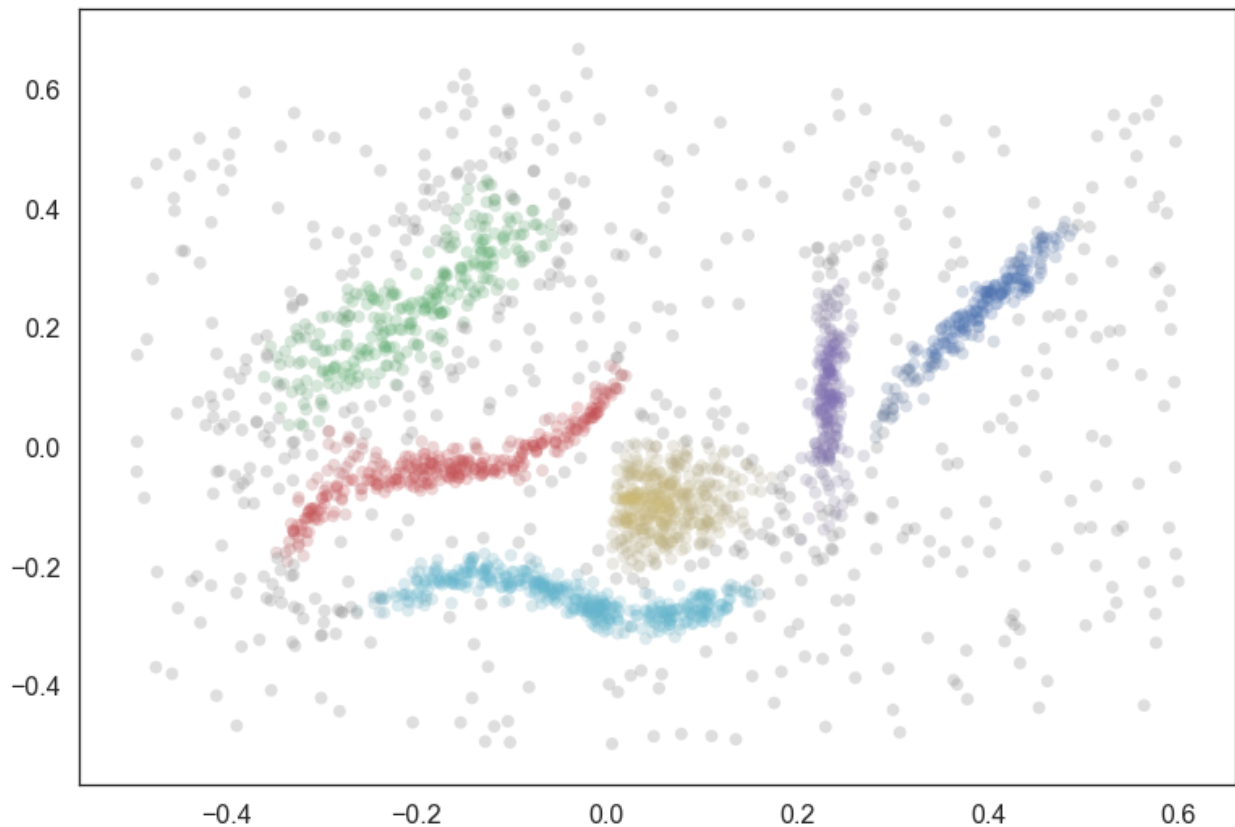
We can accommodate this by effectively holding a clustering fixed (after a potentially expensive training run) and then asking: *if we do not change the existing clusters* which cluster would HDBSCAN* assign a new data point to. In practice this amounts to determining where in the condensed tree the new data point would fall (see [How HDBSCAN Works](#)) assuming we do not change the condensed tree. This allows for a very inexpensive operation to compute a predicted cluster for the new data point.

This has been implemented in `hdbscan` as the `approximate_predict()` function. We'll look at how this works below.

As usual we begin with our test synthetic data set, and cluster it with HDBSCAN. The primary point to note here, however, is the use of the `prediction_data=True` keyword argument. This ensures that HDBSCAN does a little extra computation when fitting the model that can dramatically speed up the prediction queries later.

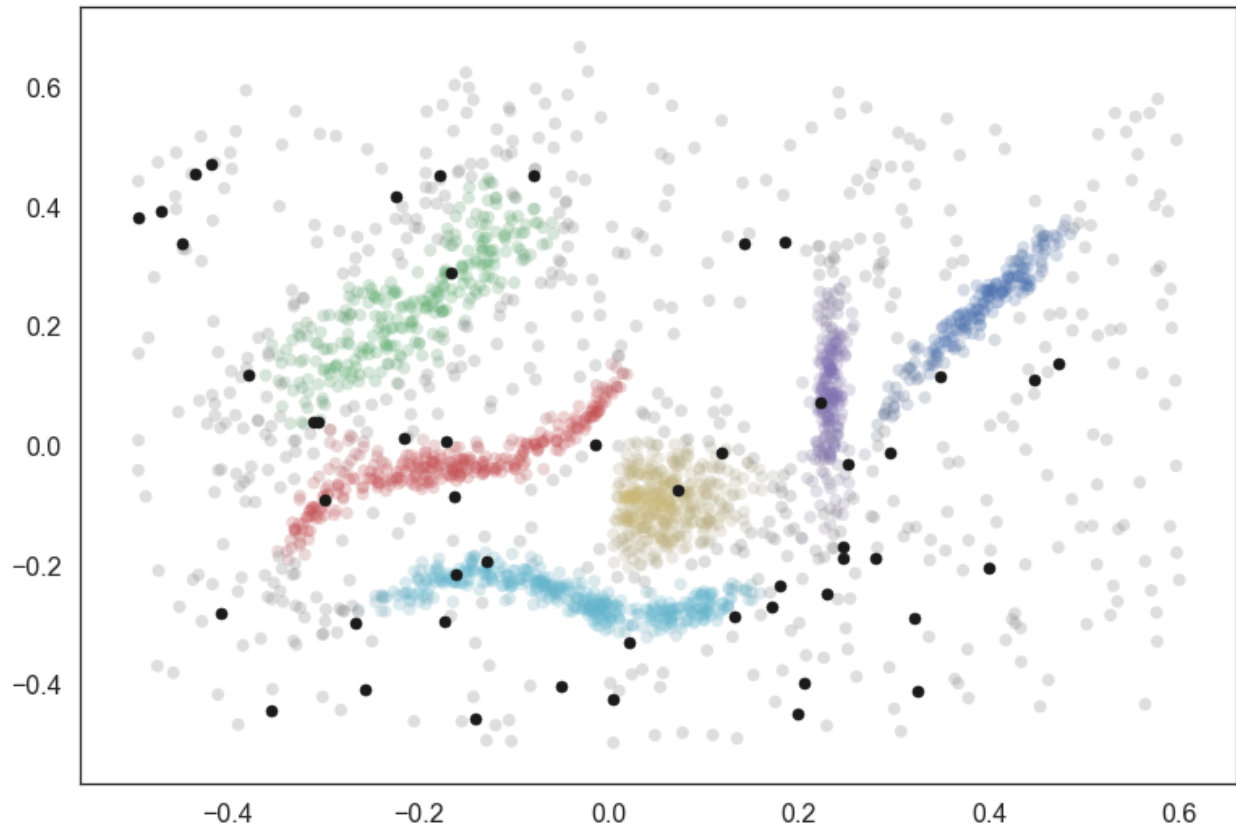
You can also get an HDBSCAN object to create this data after the fact via the `generate_prediction_data()` method.

```
data = np.load('clusterable_data.npy')
clusterer = hdbscan.HDBSCAN(min_cluster_size=15, prediction_data=True).fit(data)
pal = sns.color_palette('deep', 8)
colors = [sns.desaturate(pal[col], sat) for col, sat in zip(clusterer.labels_,
                                                           clusterer.probabilities_)]
plt.scatter(data.T[0], data.T[1], c=colors, **plot_kwds);
```



Now to make things a little more interesting let's generate 50 new data points scattered across the data. We can plot them in black to see where they happen to fall.

```
test_points = np.random.random(size=(50, 2)) - 0.5
colors = [sns.desaturate(pal[col], sat) for col, sat in zip(clusterer.labels_,
                                                           clusterer.probabilities_)]
plt.scatter(data.T[0], data.T[1], c=colors, **plot_kwds);
plt.scatter(*test_points.T, c='k', s=50)
```



We can use the predict API on this data, calling `approximate_predict()` with the HDBSCAN object, and the numpy array of new points. Note that `approximate_predict()` takes an *array* of new points. If you have a single point be sure to wrap it in a list.

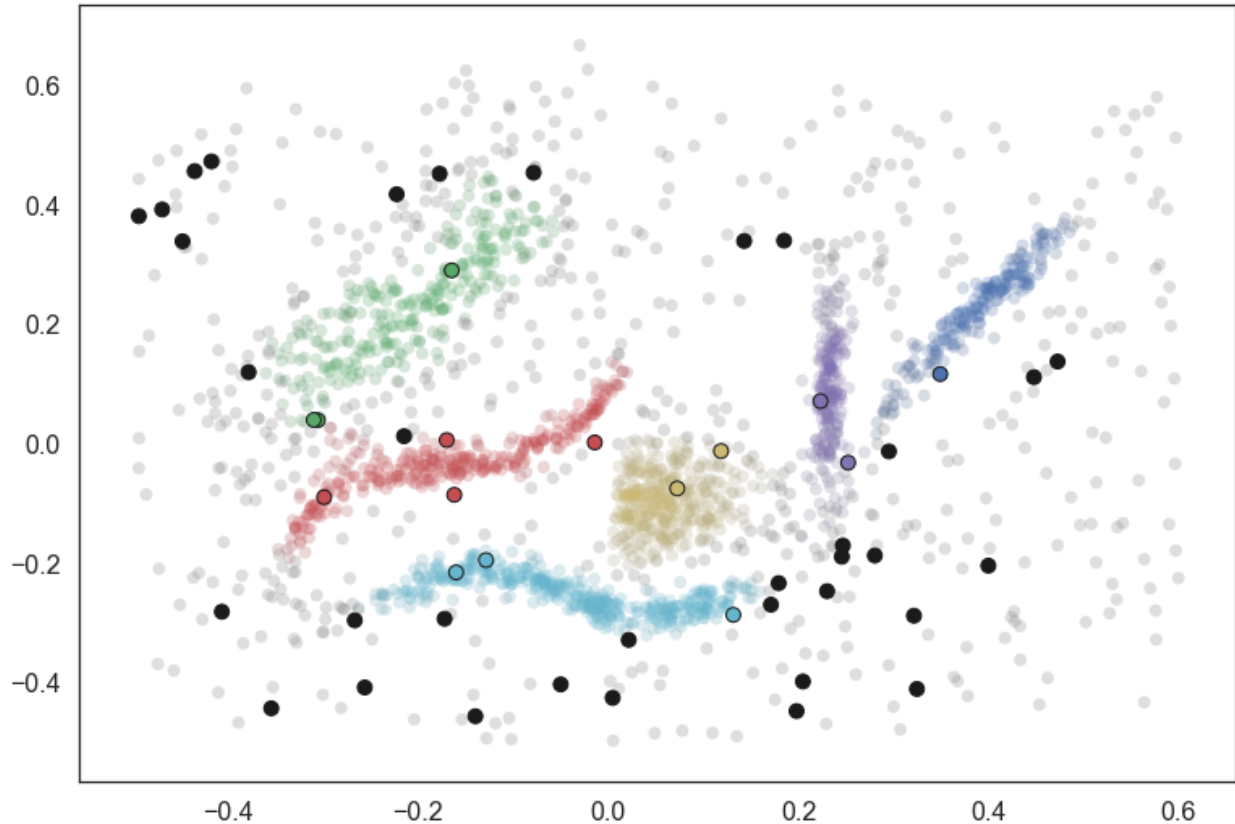
```
test_labels, strengths = hdbscan.approximate_predict(clusterer, test_points)
test_labels
```

```
array([ 2, -1, -1, -1, -1, -1,  1,  5, -1, -1,  5, -1, -1, -1, -1,  4, -1,
       -1, -1, -1, -1,  4, -1, -1, -1, -1,  2, -1, -1,  1, -1, -1, -1,  0,
       -1,  2, -1, -1,  3, -1, -1,  1, -1, -1, -1, -1, -1,  5,  3,  2])
```

The result is a set of labels as you can see. Many of the points are classified as noise, but several are also assigned to clusters. This is a very fast operation, even with large datasets, as long as the HDBSCAN object has the prediction data generated beforehand.

We can also visualize how this worked, coloring the new data points by the cluster to which they were assigned. I have added a black border around the points so they don't get lost inside the clusters they fall into.

```
colors = [sns.desaturate(pal[col], sat) for col, sat in zip(clusterer.labels_,
                                                           clusterer.probabilities_)]
test_colors = [pal[col] if col >= 0 else (0.1, 0.1, 0.1) for col in test_labels]
plt.scatter(data.T[0], data.T[1], c=colors, **plot_kwds);
plt.scatter(*test_points.T, c=test_colors, s=80, linewidths=1, edgecolors='k')
```



It is as simple as that. So now you can get started using HDBSCAN as a streaming clustering service – just be sure to cache your data and retrain your model periodically to avoid drift!

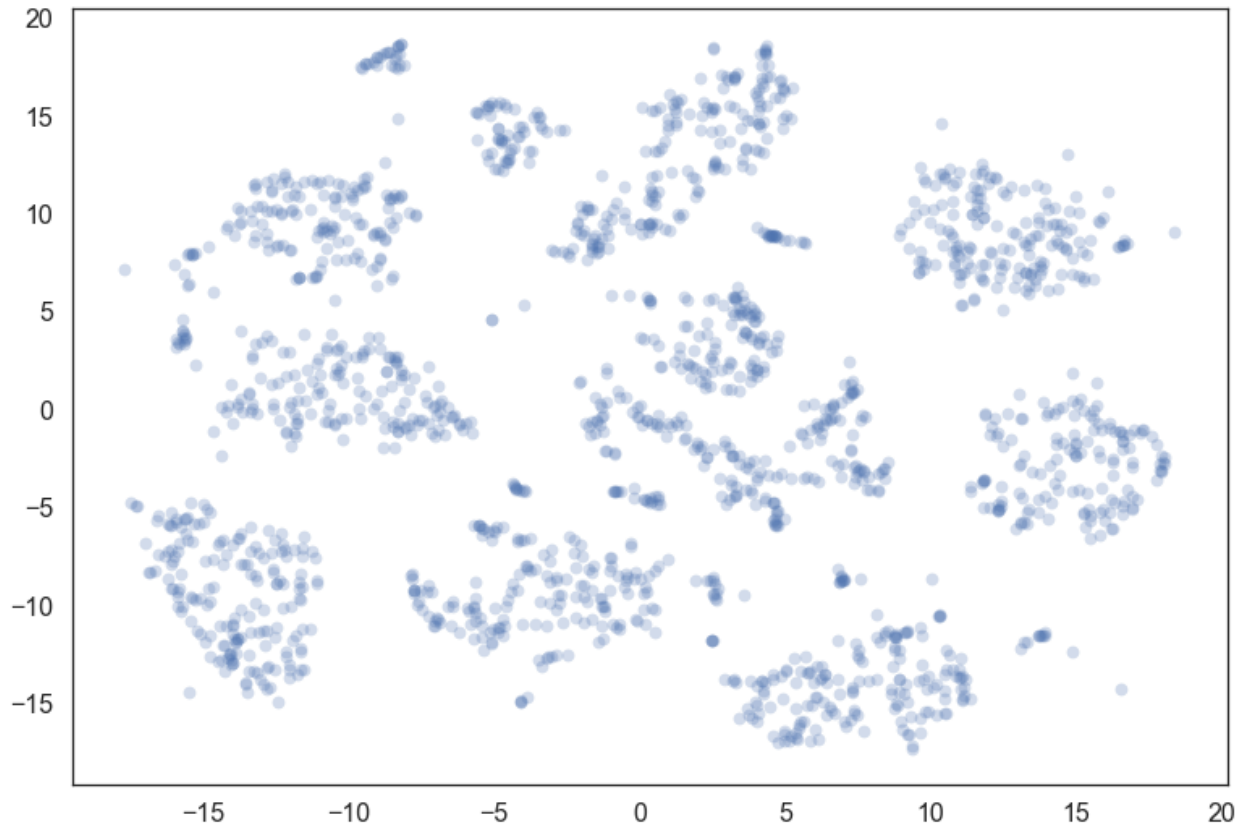
Soft Clustering for HDBSCAN*

Soft clustering is a new (and still somewhat experimental) feature of the hdbscan library. It takes advantage of the fact that the condensed tree is a kind of smoothed density function over data points, and the notion of exemplars for clusters. If you want to better understand how soft clustering works please refer to [How Soft Clustering for HDBSCAN Works](#).

Let's consider the digits dataset from sklearn. We can project the data into two dimensions to visualize it via t-SNE.

```
from sklearn import datasets
from sklearn.manifold import TSNE
import matplotlib.pyplot as plt
import seaborn as sns
import numpy as np
```

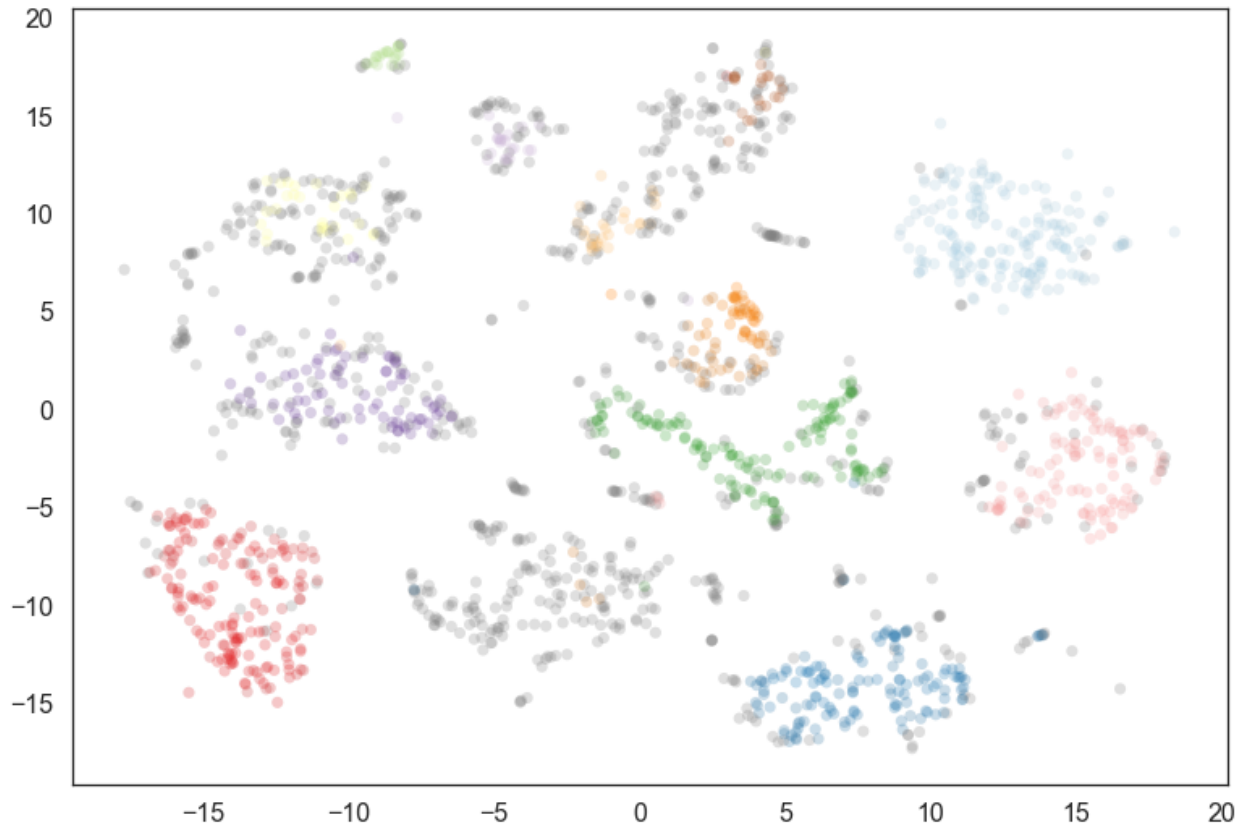
```
digits = datasets.load_digits()
data = digits.data
projection = TSNE().fit_transform(data)
plt.scatter(*projection.T, **plot_kwds)
```



Now we import `hdbscan` and then cluster in the full 64 dimensional space. It is important to note that, if we wish to use the soft clustering we should use the `prediction_data=True` option for `HDBSCAN`. This will ensure we generate the extra data required that will allow soft clustering to work.

```
import hdbscan
```

```
clusterer = hdbscan.HDBSCAN(min_cluster_size=10, prediction_data=True).fit(data)
color_palette = sns.color_palette('Paired', 12)
cluster_colors = [color_palette[x] if x >= 0
                  else (0.5, 0.5, 0.5)
                  for x in clusterer.labels_]
cluster_member_colors = [sns.desaturate(x, p) for x, p in
                        zip(cluster_colors, clusterer.probabilities_)]
plt.scatter(*projection.T, s=50, linewidth=0, c=cluster_member_colors, alpha=0.25)
```

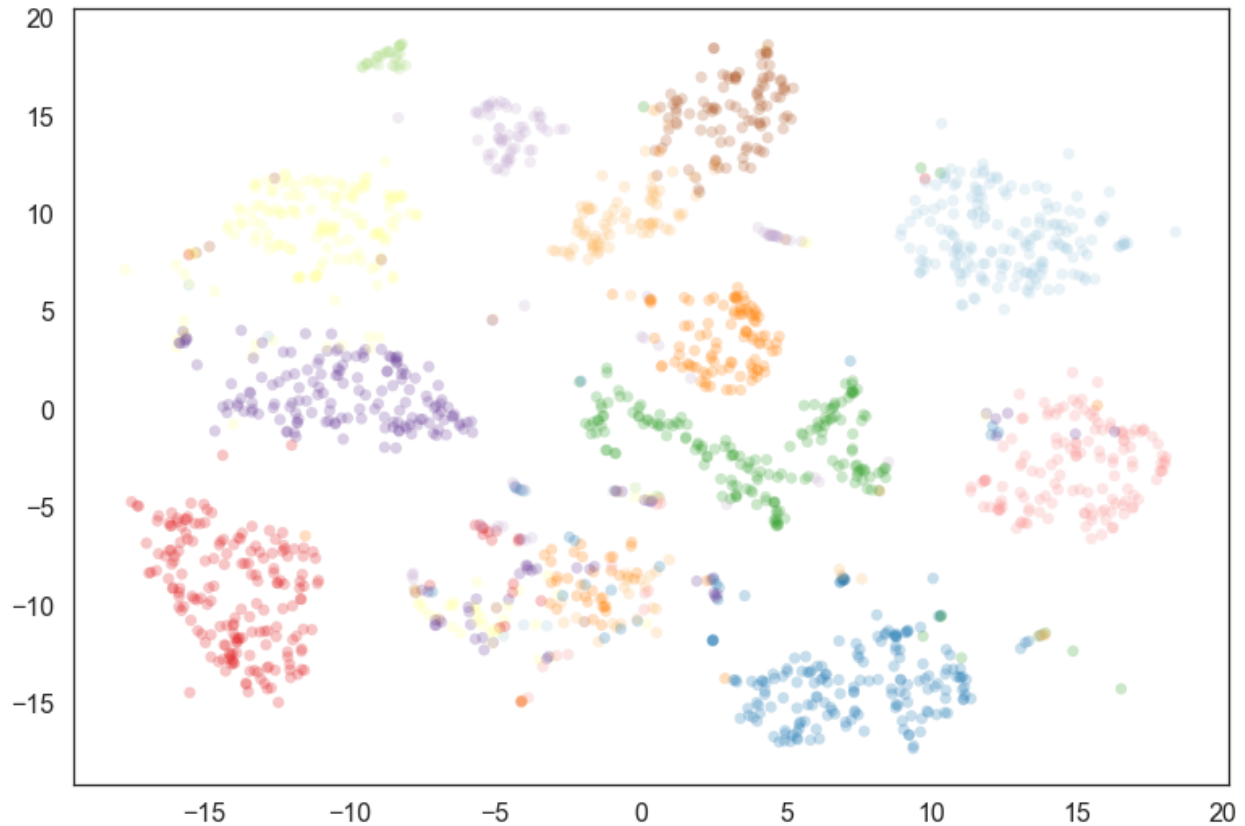


Certainly a number of clusters were found, but the data is fairly noisy in 64 dimensions, so there are a number of points that have been classified as noise. We can generate a soft clustering to get more information about some of these noise points.

To generate a soft clustering for all the points in the original dataset we use the `all_points_membership_vectors()` function which takes a clusterer object. If we wanted to get soft cluster membership values for a set of new unseen points we could use `membership_vector()` instead.

The return value is a two-dimensional numpy array. Each point of the input data is assigned a vector of probabilities of being in a cluster. For a first pass we can visualize the data looking at what the *most likely* cluster was, by coloring according to the `argmax` of the probability vector (i.e. the cluster for which a given point has the highest probability of being in).

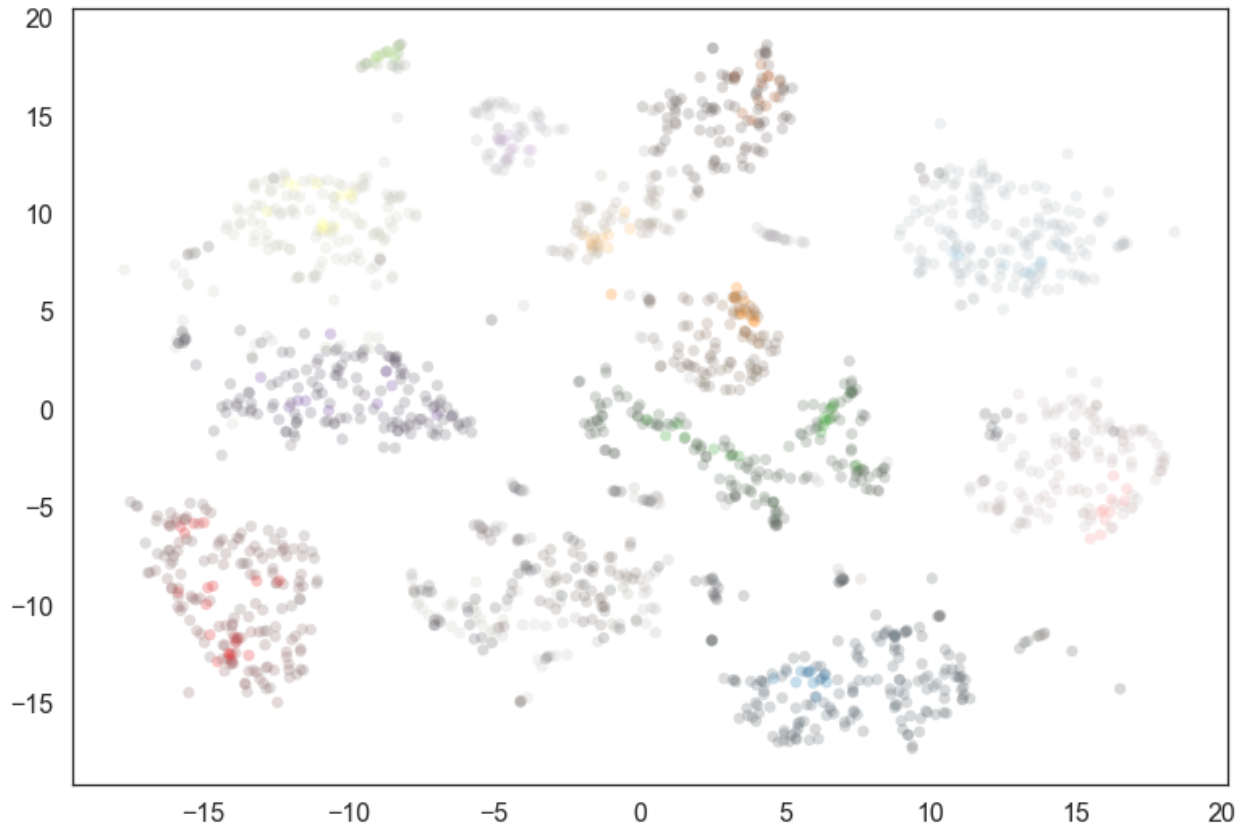
```
soft_clusters = hdbscan.all_points_membership_vectors(clusterer)
color_palette = sns.color_palette('Paired', 12)
cluster_colors = [color_palette[np.argmax(x)]
                  for x in soft_clusters]
plt.scatter(*projection.T, s=50, linewidth=0, c=cluster_colors, alpha=0.25)
```



This fills out the clusters nicely – we see that there were many noise points that are most likely to belong to the clusters we would expect; we can also see where things have gotten confused in the middle, and there is a mix of cluster assignments.

We are still only using part of the information however; we can desaturate according to the actual probability value for the most likely cluster.

```
color_palette = sns.color_palette('Paired', 12)
cluster_colors = [sns.desaturate(color_palette[np.argmax(x)], np.max(x))
                  for x in soft_clusters]
plt.scatter(*projection.T, s=50, linewidth=0, c=cluster_colors, alpha=0.25)
```

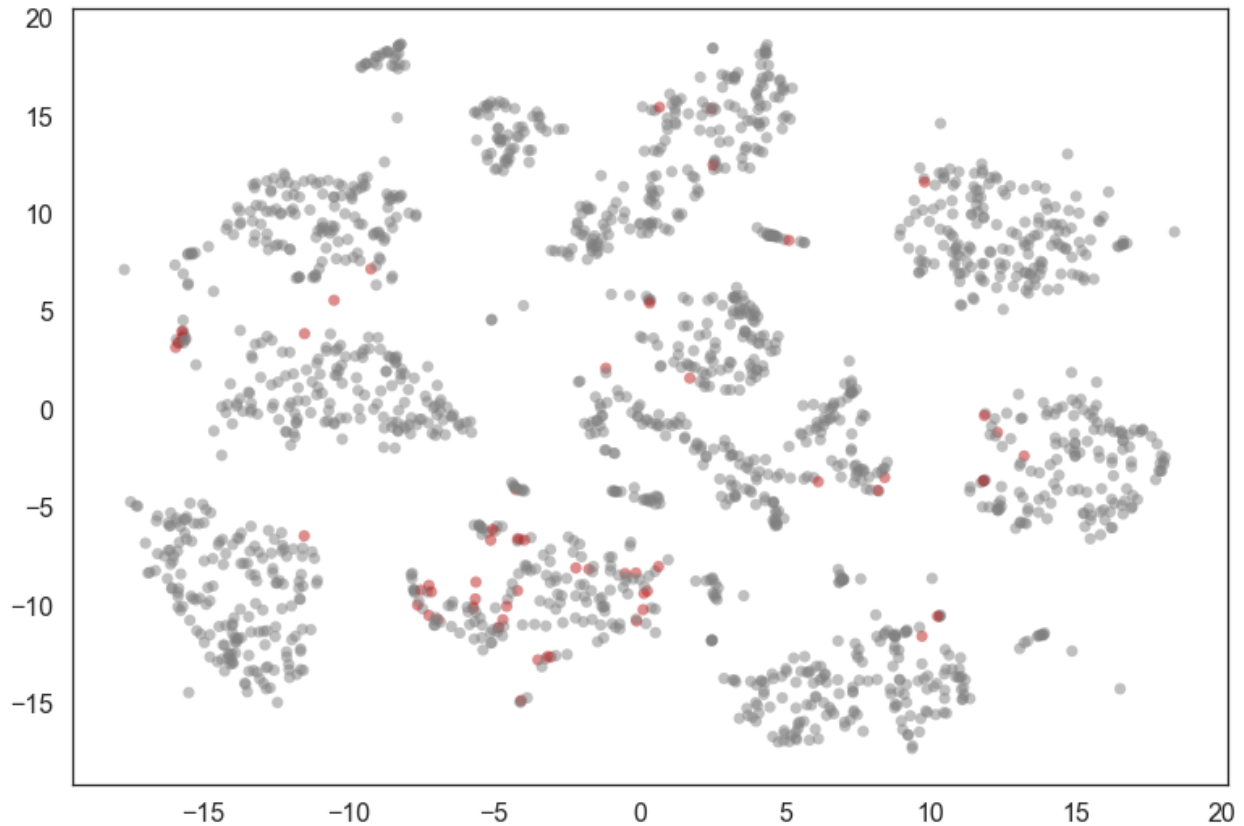
We see that many points actually have a low probability of being in the cluster – indeed the soft clustering applies *within* a cluster, so only the very cores of each cluster have high probabilities. In practice desaturating is a fairly string treatment; visually a lot will look gray. We could apply a function and put a lower limit on the desaturation that meets better with human visual perception, but that is left as an exercise for the reader.

Instead we’ll explore what else we can learn about the data from these cluster membership probabilities. An interesting question is which points have high likelihoods for *two* clusters (and low likelihoods for the other clusters).

```
def top_two_probs_diff(probs):
    sorted_probs = np.sort(probs)
    return sorted_probs[-1] - sorted_probs[-2]

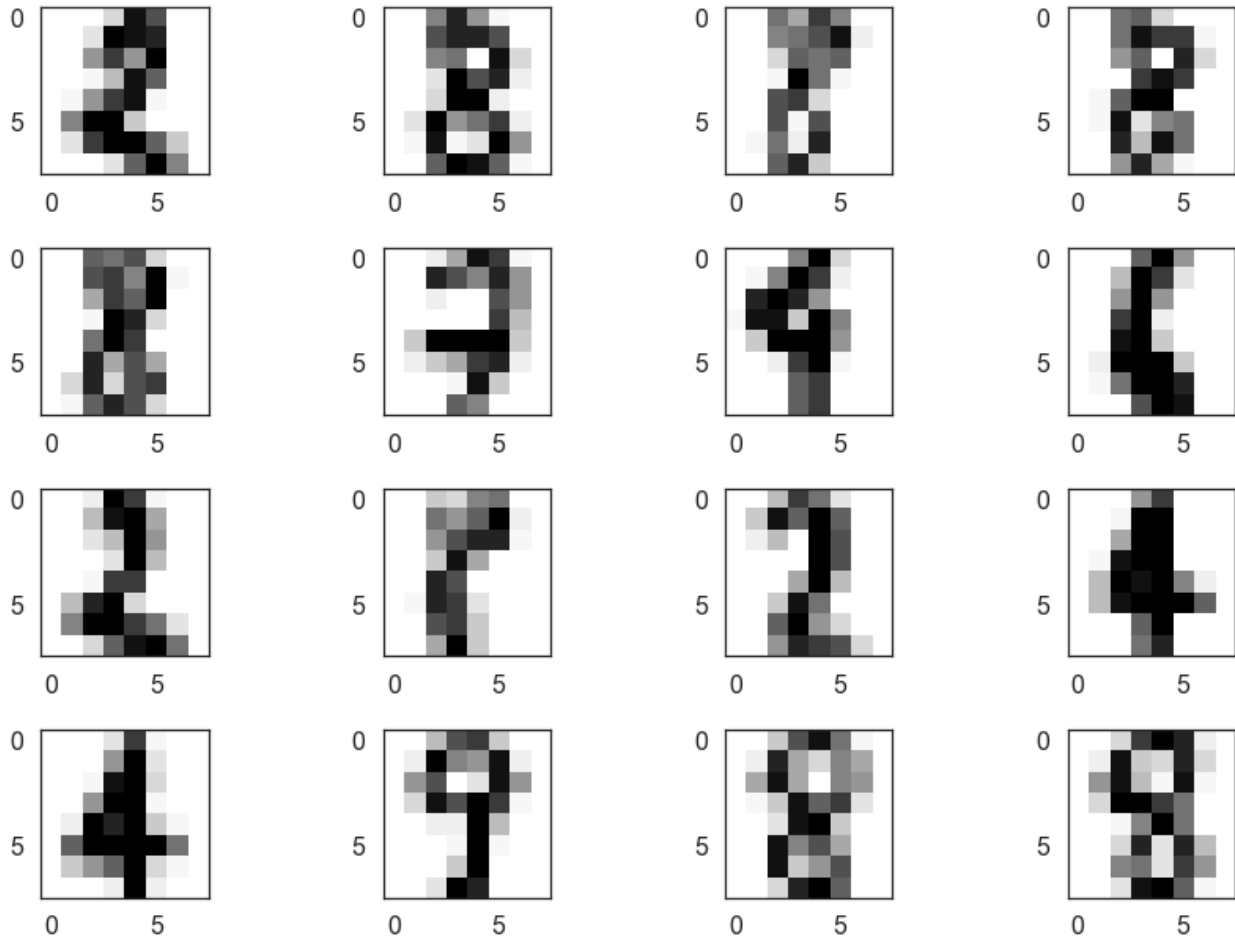
# Compute the differences between the top two probabilities
diffs = np.array([top_two_probs_diff(x) for x in soft_clusters])
# Select out the indices that have a small difference, and a larger total probability
mixed_points = np.where((diffs < 0.001) & (np.sum(soft_clusters, axis=1) > 0.5))[0]
```

```
colors = [(0.75, 0.1, 0.1) if x in mixed_points
          else (0.5, 0.5, 0.5) for x in range(data.shape[0])]
plt.scatter(*projection.T, s=50, linewidth=0, c=colors, alpha=0.5)
```



We can look at a few of these and see that many are, indeed, hard to classify (even for humans). It also seems that 8 was not assigned a cluster and is seen as a mixture of other clusters.

```
fig = plt.figure()
for i, image in enumerate(digits.images[mixed_points][:16]):
    ax = fig.add_subplot(4,4,i+1)
    ax.imshow(image)
plt.tight_layout()
```



There is, of course, a lot more analysis that can be done from here, but hopefully this provides sufficient introduction to what can be achieved with soft clustering.

Frequently Asked Questions

Here we attempt to address some common questions, directing the user to some helpful answers.

Q: Most of data is classified as noise; why?

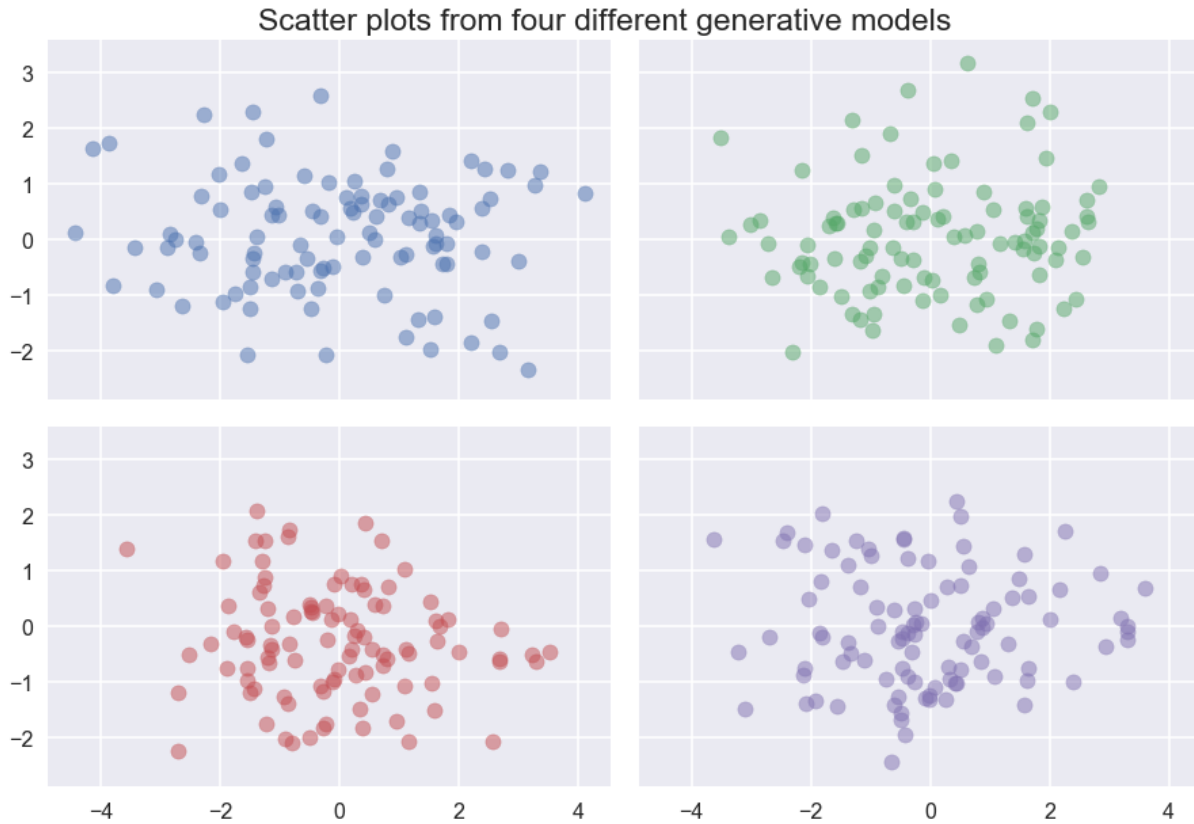
The amount of data classified as noise is controlled by the `min_samples` parameter. By default, if not otherwise set, this value is set to the same value as `min_cluster_size`. You can set it independently if you wish by specifying it separately. The lower the value, the less noise you'll get, but there are limits, and it is possible that you simply have noisy data. See `_min_samples_label` for more details.

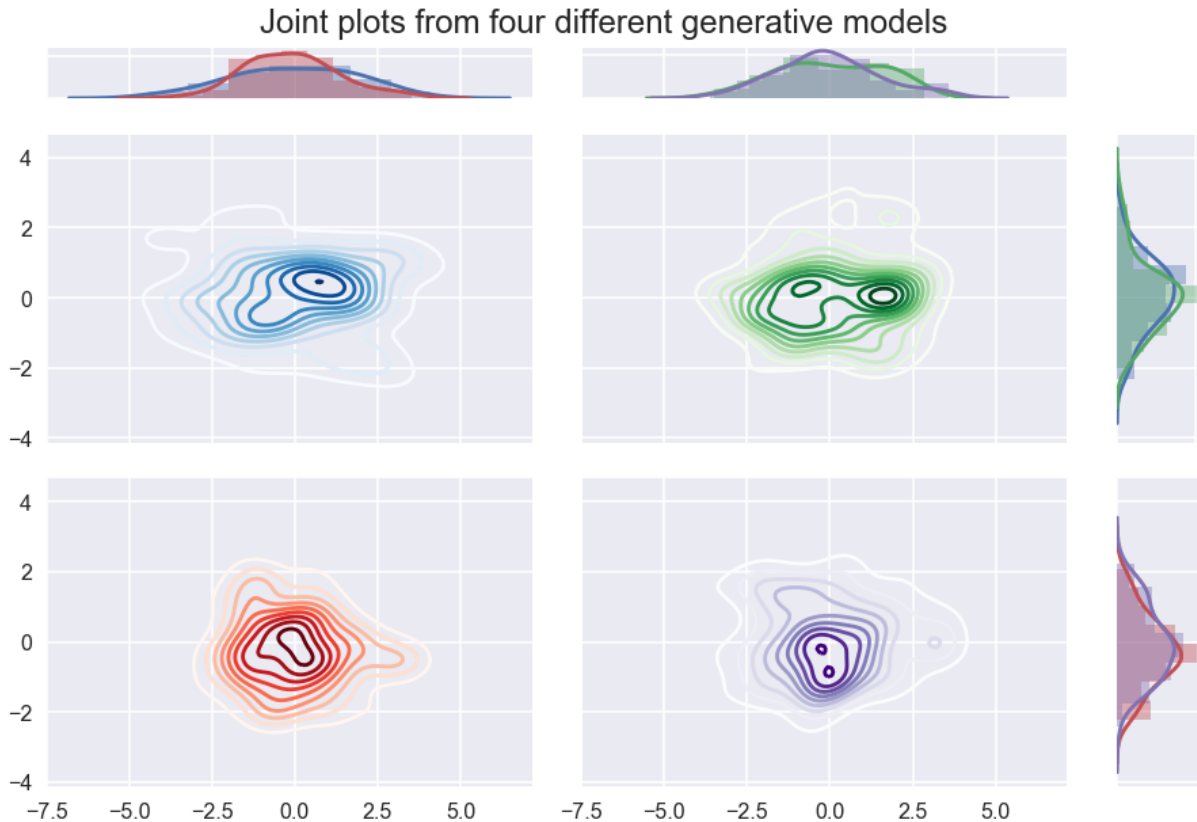
Q: I mostly just get one large cluster; I want smaller clusters.

If you are getting a single large cluster and a few small outlying clusters that means your data is essentially a large glob with some small outlying clusters – there may be structure to the glob, but compared to how well separated those other small clusters are, it doesn't really show up. You may, however, want to get at that more fine grained structure. You can do that, and what you are looking for is leaf clustering `_leaf_cluster_label`.

Q: HDBSCAN is failing to separate the clusters I think it should.

Density based clustering relies on having enough data to separate dense areas . In higher dimensional spaces this becomes more difficult, and hence requires more data. Quite possibly there is not enough data to make your clusters clearly separable. Consider the following plots:





Four different generative models, when sampled, produce results that are hard to easily differentiate. The blue dataset is sampled from a mixture of three standard Gaussians centered at $(-2, 0)$, $(0, 0)$ and $(2, 0)$; the green dataset is sampled from a mixture of two standard Gaussians centered at $(-1, 0)$ and $(1, 0)$; the red data is sampled from a multivariate Gaussian with covariance $\begin{bmatrix} 2 & 0 \\ 0 & 1 \end{bmatrix}$; the purple data is a single standard Gaussian with uniform background noise.

Despite the generate model having clearly different “clusters”, without more data we simply cannot differentiate between these models, and hence no density based clustering will manage cluster these according to the model.

Q: I want to predict the cluster of a new unseen point. How do I do this?

This is possible via the function `approximate_predict()`. Note that you either need to set `prediction_data=True` on initialization of your clusterer object, or run the `generate_prediction_data` method after fitting. With that done you can run `approximate_predict()` with the model and any new data points you wish to predict. Note that this differs from re-running HDBSCAN with the new points added since no new clusters will be considered – instead the new points will be labelled according to the clusters already labelled by the model.

Q: Haversine metric is not clustering my Lat-Lon data correctly.

The Haversine metric as implemented supports coordinates in radians. That means you’ll need to convert your latitude and longitude data into radians before passing it in to HDBSCAN.

Background on Clustering with HDBSCAN

How HDBSCAN Works

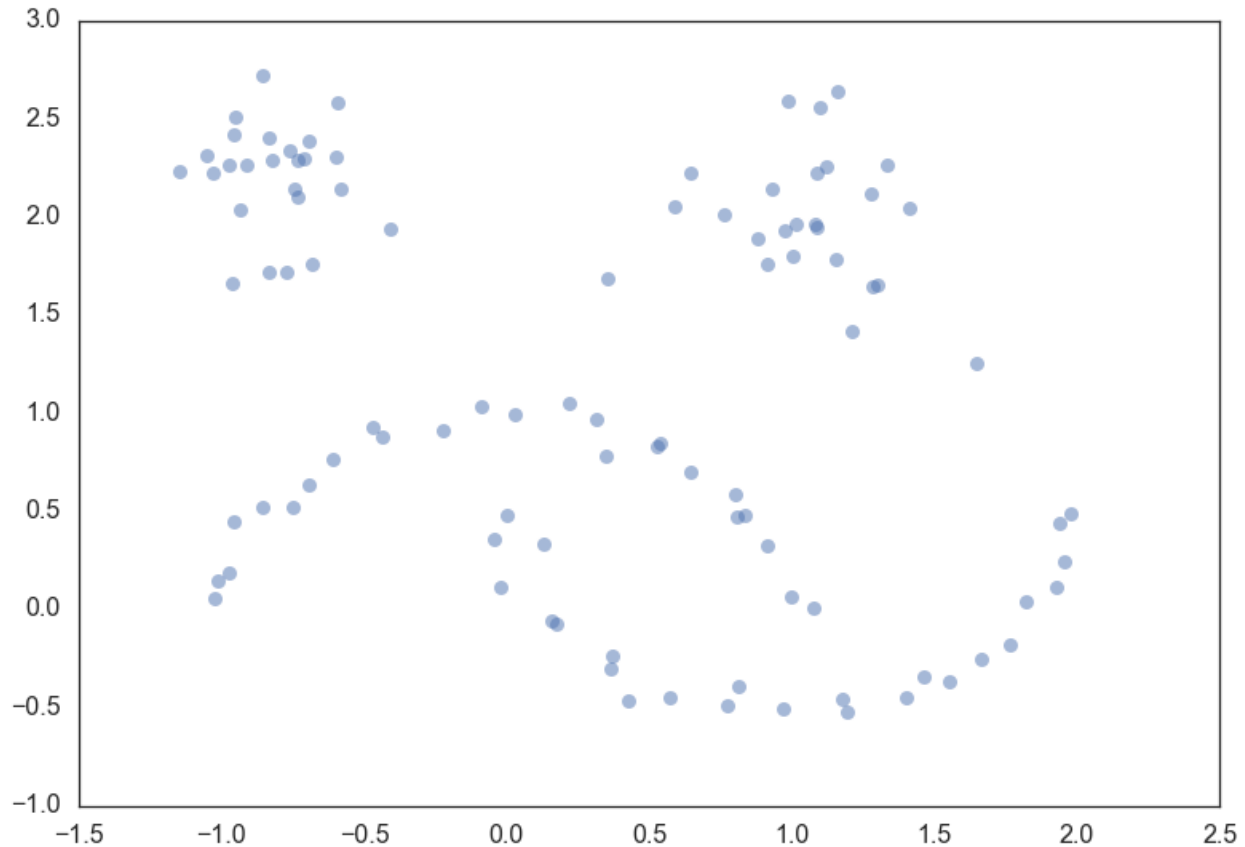
HDBSCAN is a clustering algorithm developed by [Campello, Moulavi, and Sander](#). It extends DBSCAN by converting it into a hierarchical clustering algorithm, and then using a technique to extract a flat clustering based in the stability of clusters. The goal of this notebook is to give you an overview of how the algorithm works and the motivations behind it. In contrast to the HDBSCAN paper I'm going to describe it without reference to DBSCAN. Instead I'm going to explain how I like to think about the algorithm, which aligns more closely with [Robust Single Linkage with flat cluster extraction](#) on top of it.

Before we get started we'll load up most of the libraries we'll need in the background, and set up our plotting (because I believe the best way to understand what is going on is to actually see it working in pictures).

```
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns
import sklearn.datasets as data
%matplotlib inline
sns.set_context('poster')
sns.set_style('white')
sns.set_color_codes()
plot_kwds = {'alpha' : 0.5, 's' : 80, 'linewidths':0}
```

The next thing we'll need is some data. To make for an illustrative example we'll need the data size to be fairly small so we can see what is going on. It will also be useful to have several clusters, preferably of different kinds. Fortunately sklearn has facilities for generating sample clustering data so I'll make use of that and make a dataset of one hundred data points.

```
moons, _ = data.make_moons(n_samples=50, noise=0.05)
blobs, _ = data.make_blobs(n_samples=50, centers=[(-0.75,2.25), (1.0, 2.0)], cluster_
    ↪std=0.25)
test_data = np.vstack([moons, blobs])
plt.scatter(test_data.T[0], test_data.T[1], color='b', **plot_kwds)
```



Now, the best way to explain HDBSCAN is actually just use it and then go through the steps that occurred along the way teasing out what is happening at each step. So let's load up the [hdbscan library](#) and get to work.

```
import hdbscan
```

```
clusterer = hdbscan.HDBSCAN(min_cluster_size=5, gen_min_span_tree=True)
clusterer.fit(test_data)
```

```
HDBSCAN(algorithm='best', alpha=1.0, approx_min_span_tree=True,
        gen_min_span_tree=True, leaf_size=40, memory=Memory(cachedir=None),
        metric='euclidean', min_cluster_size=5, min_samples=None, p=None)
```

So now that we have clustered the data – what actually happened? We can break it out into a series of steps

1. Transform the space according to the density/sparsity.
2. Build the minimum spanning tree of the distance weighted graph.
3. Construct a cluster hierarchy of connected components.
4. Condense the cluster hierarchy based on minimum cluster size.
5. Extract the stable clusters from the condensed tree.

Transform the space

To find clusters we want to find the islands of higher density amid a sea of sparser noise – and the assumption of noise is important: real data is messy and has outliers, corrupt data, and noise. The core of the clustering algorithm is single

linkage clustering, and it can be quite sensitive to noise: a single noise data point in the wrong place can act as a bridge between islands, gluing them together. Obviously we want our algorithm to be robust against noise so we need to find a way to help ‘lower the sea level’ before running a single linkage algorithm.

How can we characterize ‘sea’ and ‘land’ without doing a clustering? As long as we can get an estimate of density we can consider lower density points as the ‘sea’. The goal here is not to perfectly distinguish ‘sea’ from ‘land’ – this is an initial step in clustering, not the output – just to make our clustering core a little more robust to noise. So given an identification of ‘sea’ we want to lower the sea level. For practical purposes that means making ‘sea’ points more distant from each other and from the ‘land’.

That’s just the intuition however. How does it work in practice? We need a very inexpensive estimate of density, and the simplest is the distance to the k th nearest neighbor. If we have the distance matrix for our data (which we will need imminently anyway) we can simply read that off; alternatively if our metric is supported (and dimension is low) this is the sort of query that [kd-trees](#) are good for. Let’s formalise this and (following the DBSCAN, LOF, and HDBSCAN literature) call it the **core distance** defined for parameter k for a point x and denote as $\text{core}_k(x)$. Now we need a way to spread apart points with low density (correspondingly high core distance). The simple way to do this is to define a new distance metric between points which we will call (again following the literature) the **mutual reachability distance**. We define mutual reachability distance as follows:

$$d_{\text{mreach}-k}(a, b) = \max\{\text{core}_k(a), \text{core}_k(b), d(a, b)\}$$

where $d(a, b)$ is the original metric distance between a and b . Under this metric dense points (with low core distance) remain the same distance from each other but sparser points are pushed away to be at least their core distance away from any other point. This effectively ‘lowers the sea level’ spreading sparse ‘sea’ points out, while leaving ‘land’ untouched. The caveat here is that obviously this is dependent upon the choice of k ; larger k values interpret more points as being in the ‘sea’. All of this is a little easier to understand with a picture, so let’s use a k value of five. Then for a given point we can draw a circle for the core distance as the circle that touches the sixth nearest neighbor (counting the point itself), like so:

Pick another point and we can do the same thing, this time with a different set of neighbors (one of them even being the first point we picked out).

And we can do that a third time for good measure, with another set of six nearest neighbors and another circle with slightly different radius again.

Now if we want to know the mutual reachability distance between the blue and green points we can start by drawing in an arrow giving the distance between green and blue:

This passes through the blue circle, but not the green circle – the core distance for green is larger than the distance between blue and green. Thus we need to mark the mutual reachability distance between blue and green as larger – equal to the radius of the green circle (easiest to picture if we base one end at the green point).

On the other hand the mutual reachability distance from red to green is simply distance from red to green since that distance is greater than either core distance (i.e. the distance arrow passes through both circles).

In general there is [underlying theory](#) to demonstrate that mutual reachability distance as a transform works well in allowing single linkage clustering to more closely approximate the hierarchy of level sets of whatever true density distribution our points were sampled from.

Build the minimum spanning tree

Now that we have a new mutual reachability metric on the data we want start finding the islands on dense data. Of course dense areas are relative, and different islands may have different densities. Conceptually what we will do is the following: consider the data as a weighted graph with the data points as vertices and an edge between any two points with weight equal to the mutual reachability distance of those points.

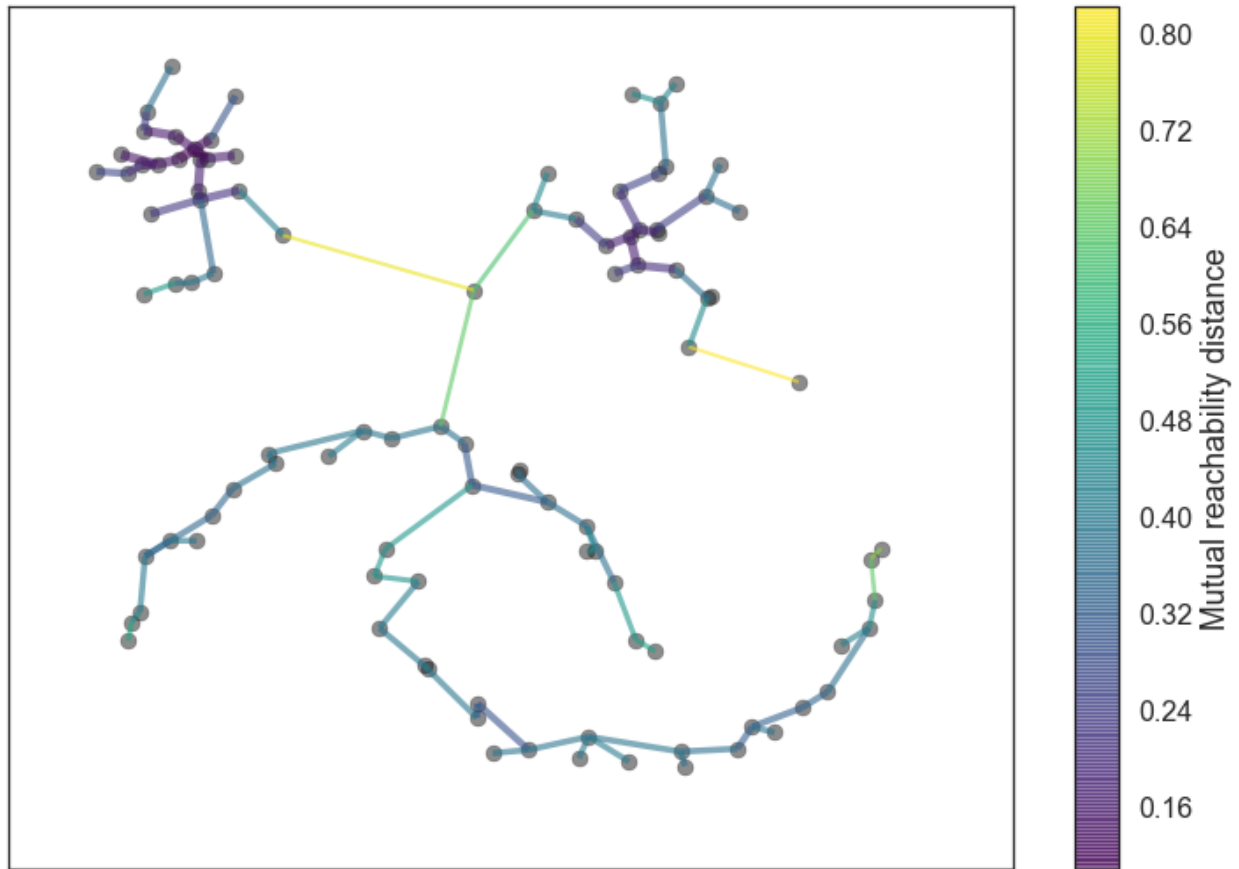
Now consider a threshold value, starting high, and steadily being lowered. Drop any edges with weight above that threshold. As we drop edges we will start to disconnect the graph into connected components. Eventually we will have a hierarchy of connected components (from completely connected to completely disconnected) at varying threshold levels.

In practice this is very expensive: there are n^2 edges and we don't want to have to run a connected components algorithm that many times. The right thing to do is to find a minimal set of edges such that dropping any edge from the set causes a disconnection of components. But we need more, we need this set to be such that there is no lower weight edge that could connect the components. Fortunately graph theory furnishes us with just such a thing: the minimum spanning tree of the graph.

We can build the minimum spanning tree very efficiently via [Prim's algorithm](#) – we build the tree one edge at a time, always adding the lowest weight edge that connects the current tree to a vertex not yet in the tree. You can see the tree HDBSCAN constructed below; note that this is the minimum spanning tree for *mutual reachability distance* which is different from the pure distance in the graph. In this case we had a k value of 5.

In the case that the data lives in a metric space we can use even faster methods, such as Dual Tree Boruvka to build the minimal spanning tree.

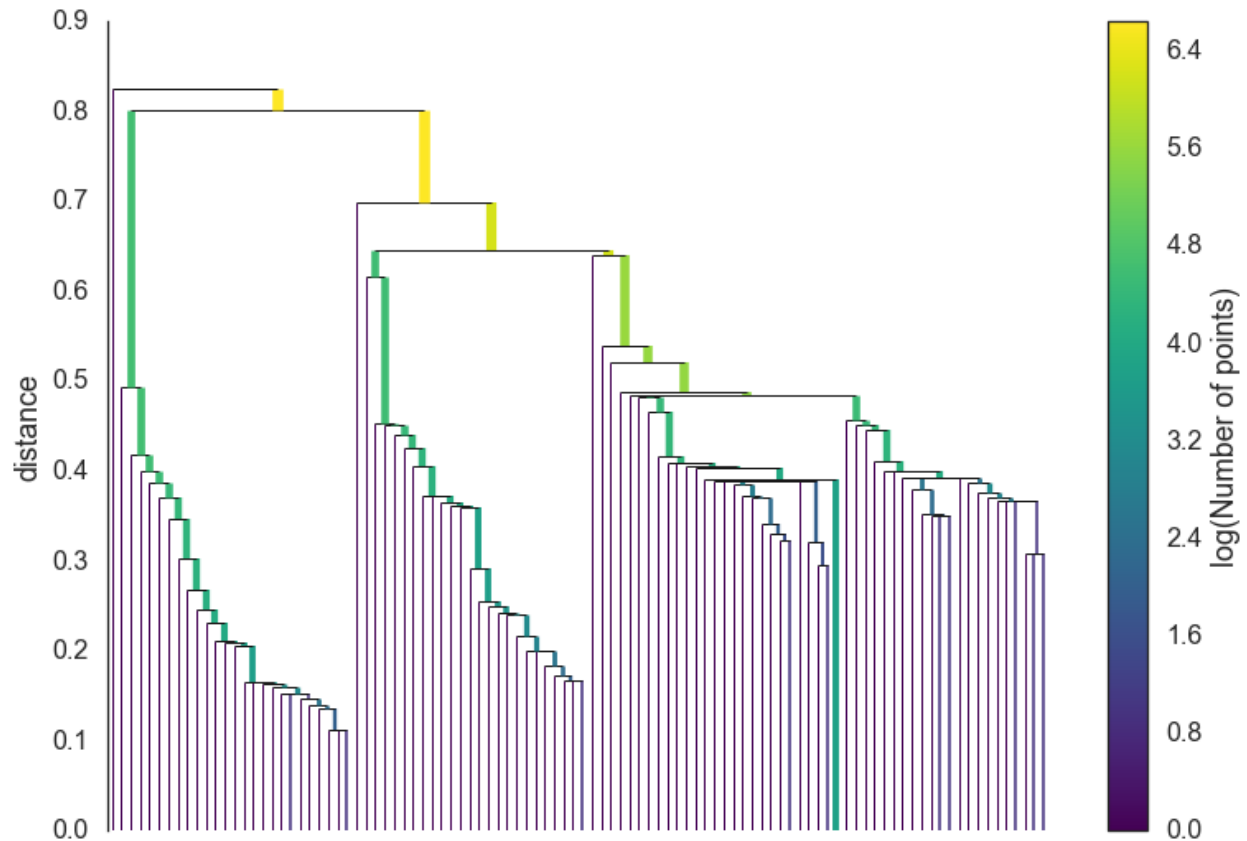
```
clusterer.minimum_spanning_tree_.plot(edge_cmap='viridis',
                                       edge_alpha=0.6,
                                       node_size=80,
                                       edge_linewidth=2)
```



Build the cluster hierarchy

Given the minimal spanning tree, the next step is to convert that into the hierarchy of connected components. This is most easily done in the reverse order: sort the edges of the tree by distance (in increasing order) and then iterate through, creating a new merged cluster for each edge. The only difficult part here is to identify the two clusters each edge will join together, but this is easy enough via a [union-find](#) data structure. We can view the result as a dendrogram as we see below:

```
clusterer.single_linkage_tree_.plot(cmap='viridis', colorbar=True)
```



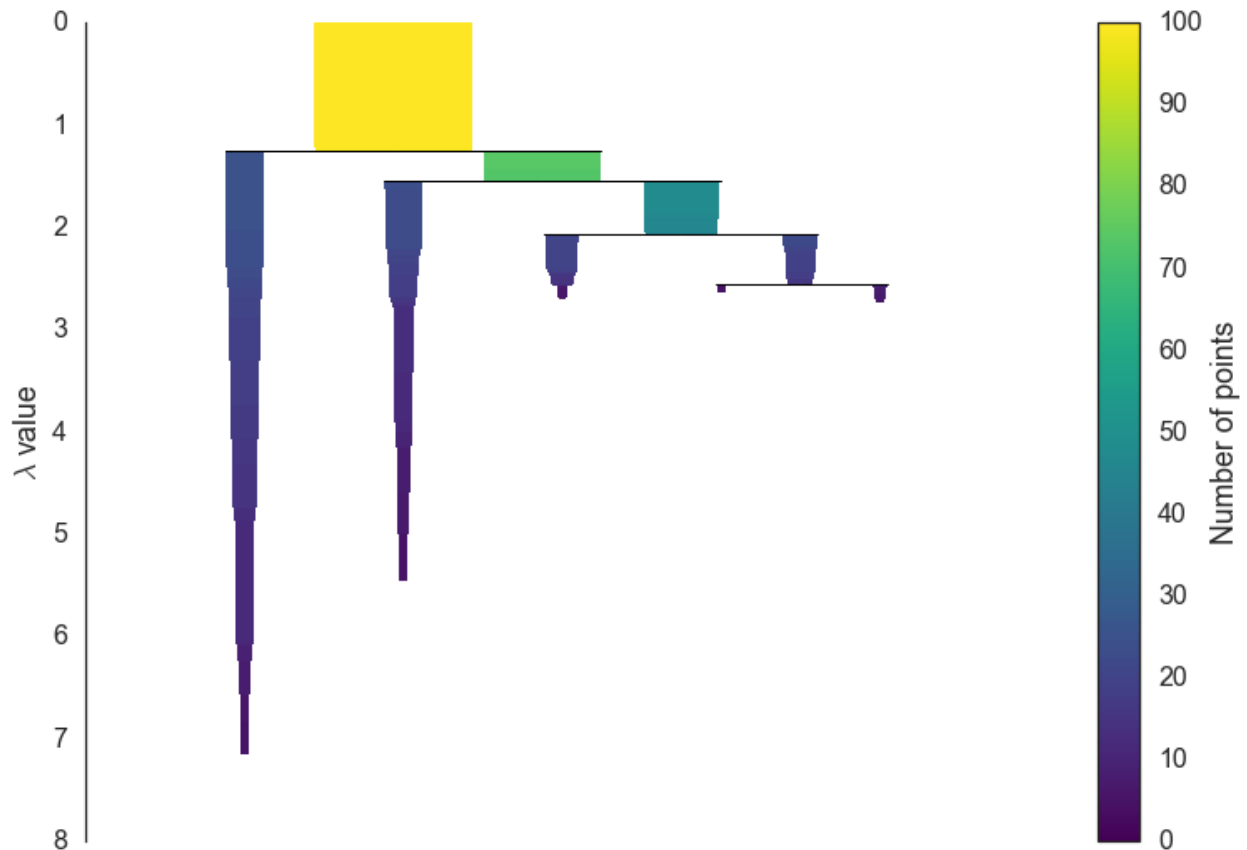
This brings us to the point where robust single linkage stops. We want more though; a cluster hierarchy is good, but we really want a set of flat clusters. We could do that by drawing a horizontal line through the above diagram and selecting the clusters that it cuts through. This is in practice what **DBSCAN** effectively does (declaring any singleton clusters at the cut level as noise). The question is, how do we know where to draw that line? DBSCAN simply leaves that as a (very unintuitive) parameter. Worse, we really want to deal with variable density clusters and any choice of cut line is a choice of mutual reachability distance to cut at, and hence a single fixed density level. Ideally we want to be able to cut the tree at different places to select our clusters. This is where the next steps of HDBSCAN begin and create the difference from robust single linkage.

Condense the cluster tree

The first step in cluster extraction is condensing down the large and complicated cluster hierarchy into a smaller tree with a little more data attached to each node. As you can see in the hierarchy above it is often the case that a cluster split is one or two points splitting off from a cluster; and that is the key point – rather than seeing it as a cluster splitting into two new clusters we want to view it as a single persistent cluster that is ‘losing points’. To make this concrete we need a notion of **minimum cluster size** which we take as a parameter to HDBSCAN. Once we have a value for minimum cluster size we can now walk through the hierarchy and at each split ask if one of the new clusters created by the split has fewer points than the minimum cluster size. If it is the case that we have fewer points than the minimum cluster size we declare it to be ‘points falling out of a cluster’ and have the larger cluster retain the cluster identity of the parent, marking down which points ‘fell out of the cluster’ and at what distance value that happened. If on the other hand the split is into two clusters each at least as large as the minimum cluster size then we consider that a true cluster split and let that split persist in the tree. After walking through the whole hierarchy and doing this we end up with a much smaller tree with a small number of nodes, each of which has data about how the size of the cluster at that node decreases over varying distance. We can visualize this as a dendrogram similar to the one above – again we can have the width of the line represent the number of points in the cluster. This time, however, that width varies over the

length of the line as points fall out of the cluster. For our data using a minimum cluster size of 5 the result looks like this:

```
clusterer.condensed_tree_.plot()
```



This is much easier to look at and deal with, particularly in as simple a clustering problem as our current test dataset. However we still need to pick out clusters to use as a flat clustering. Looking at the plot above should give you some ideas about how one might go about doing this.

Extract the clusters

Intuitively we want to choose clusters that persist and have a longer lifetime; short lived clusters are ultimately probably merely artifacts of the single linkage approach. Looking at the previous plot we could say that we want to choose those clusters that have the greatest area of ink in the plot. To make a flat clustering we will need to add a further requirement that, if you select a cluster, then you cannot select any cluster that is a descendant of it. And in fact that intuitive notion of what should be done is exactly what HDBSCAN does. Of course we need to formalise things to make it a concrete algorithm.

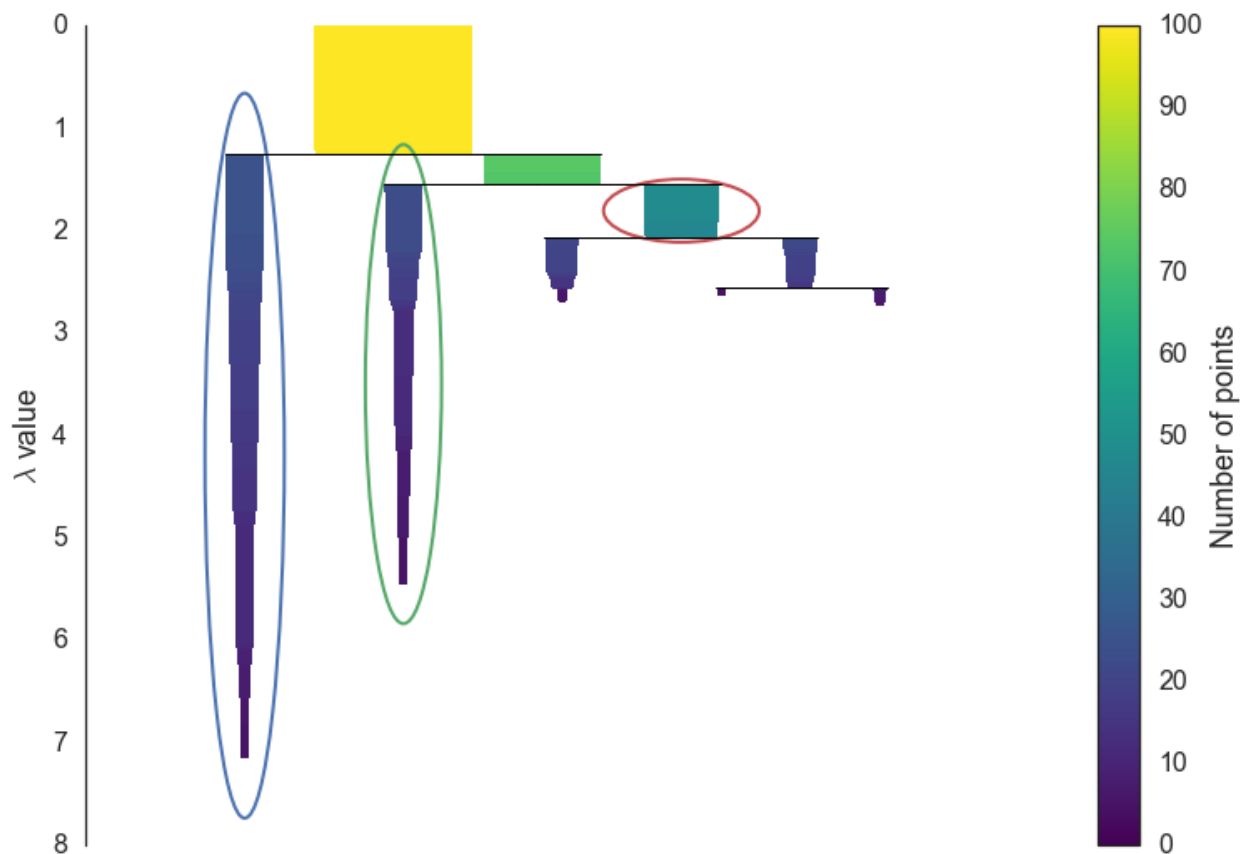
First we need a different measure than distance to consider the persistence of clusters; instead we will use $\lambda = \frac{1}{\text{distance}}$. For a given cluster we can then define values λ_{birth} and λ_{death} to be the lambda value when the cluster split off and became its own cluster, and the lambda value (if any) when the cluster split into smaller clusters respectively. In turn, for a given cluster, for each point p in that cluster we can define the value λ_p as the lambda value at which that point ‘fell out of the cluster’ which is a value somewhere between λ_{birth} and λ_{death} since the point either falls out of the cluster at some point in the cluster’s lifetime, or leaves the cluster when the cluster splits into two smaller clusters. Now, for each cluster compute the **stability** to as

$$\sum_{p \in \text{cluster}} (\lambda_p - \lambda_{\text{birth}}).$$

Declare all leaf nodes to be selected clusters. Now work up through the tree (the reverse topological sort order). If the sum of the stabilities of the child clusters is greater than the stability of the cluster then we set the cluster stability to be the sum of the child stabilities. If, on the other hand, the cluster's stability is greater than the sum of its children then we declare the cluster to be a selected cluster, and unselect all its descendants. Once we reach the root node we call the current set of selected clusters our flat clustering and return that.

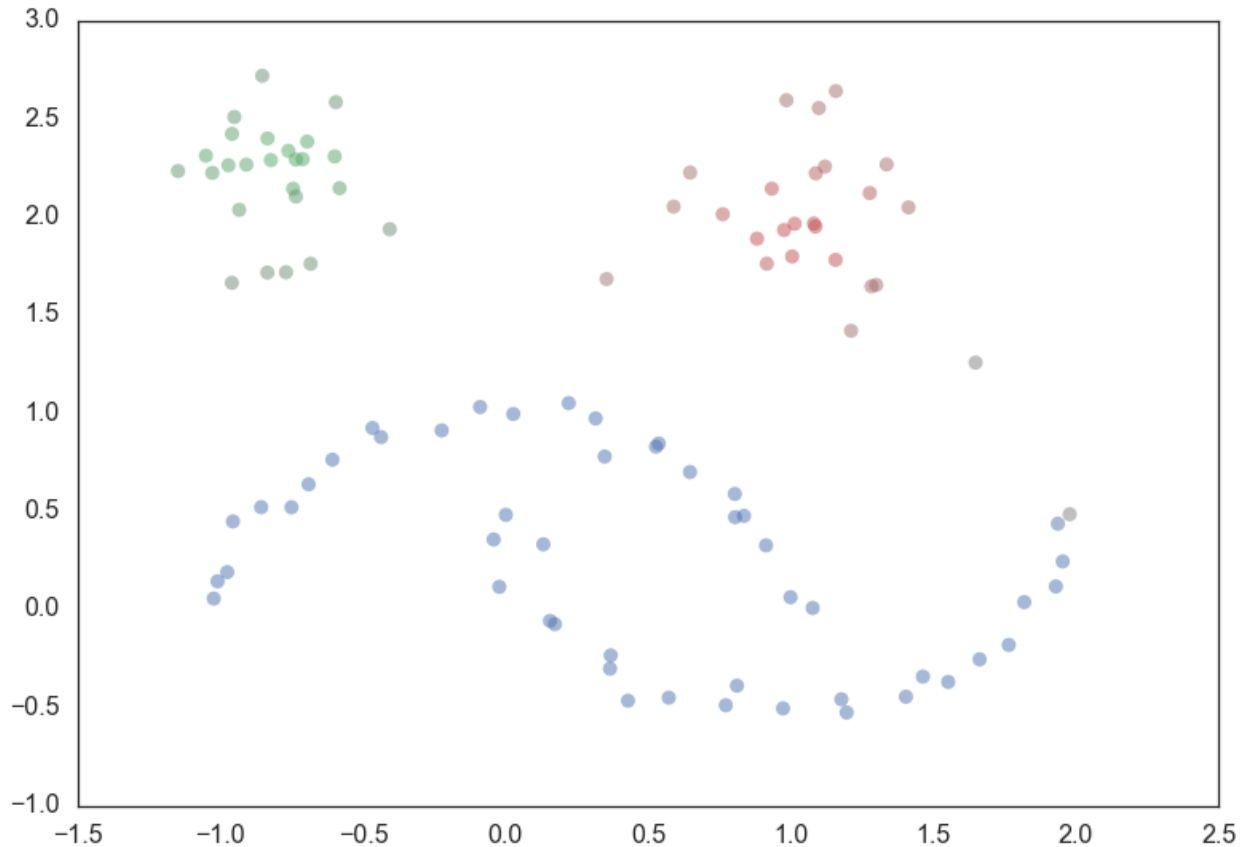
Okay, that was wordy and complicated, but it really is simply performing our 'select the clusters in the plot with the largest total ink area' subject to descendant constraints that we explained earlier. We can select the clusters in the condensed tree dendrogram via this algorithm, and you get what you expect:

```
clusterer.condensed_tree_.plot(select_clusters=True, selection_palette=sns.color_
    ↪palette())
```



Now that we have the clusters it is a simple enough matter to turn that into cluster labelling as per the sklearn API. Any point not in a selected cluster is simply a noise point (and assigned the label -1). We can do a little more though: for each cluster we have the λ_p for each point p in that cluster; If we simply normalize those values (so they range from zero to one) then we have a measure of the strength of cluster membership for each point in the cluster. The hdbscan library returns this as a `probabilities_` attribute of the clusterer object. Thus, with labels and membership strengths in hand we can make the standard plot, choosing a color for points based on cluster label, and desaturating that color according the strength of membership (and make unclustered points pure gray).

```
palette = sns.color_palette()
cluster_colors = [sns.desaturate(palette[col], sat)
    if col >= 0 else (0.5, 0.5, 0.5) for col, sat in
    zip(clusterer.labels_, clusterer.probabilities_)]
plt.scatter(test_data.T[0], test_data.T[1], c=cluster_colors, **plot_kwds)
```



And that is how HDBSCAN works. It may seem somewhat complicated – there are a fair number of moving parts to the algorithm – but ultimately each part is actually very straightforward and can be optimized well. Hopefully with a better understanding both of the intuitions and some of the implementation details of HDBSCAN you will feel motivated to [try it out](#). The library continues to develop, and will provide a base for new ideas including a near parameterless Persistent Density Clustering algorithm, and a new semi-supervised clustering algorithm.

Comparing Python Clustering Algorithms

There are a lot of clustering algorithms to choose from. The standard `sklearn` clustering suite has thirteen different clustering classes alone. So what clustering algorithms should you be using? As with every question in data science and machine learning it depends on your data. A number of those thirteen classes in `sklearn` are specialised for certain tasks (such as co-clustering and bi-clustering, or clustering features instead data points). Obviously an algorithm specializing in text clustering is going to be the right choice for clustering text data, and other algorithms specialize in other specific kinds of data. Thus, if you know enough about your data, you can narrow down on the clustering algorithm that best suits that kind of data, or the sorts of important properties your data has, or the sorts of clustering you need done. All well and good, but what if you don't know much about your data? If, for example, you are 'just looking' and doing some exploratory data analysis (EDA) it is not so easy to choose a specialized algorithm. So, what algorithm is good for exploratory data analysis?

Some rules for EDA clustering

To start, let's lay down some ground rules of what we need a good EDA clustering algorithm to do, then we can set about seeing how the algorithms available stack up.

- **Don't be wrong!:** If you are doing EDA you are trying to learn and gain intuitions about your data. In that case it is far better to get no result at all than a result that is wrong. Bad results lead to false intuitions which in turn send you down completely the wrong path. Not only do you not understand your data, you *misunderstand* your data. This means a good EDA clustering algorithm needs to be conservative in its clustering; it should be willing to not assign points to clusters; it should not group points together unless they really are in a cluster; this is true of far fewer algorithms than you might think.
- **Intuitive Parameters:** All clustering algorithms have parameters; you need some knobs to turn to adjust things. The question is: how do you pick settings for those parameters? If you know little about your data it can be hard to determine what value or setting a parameter should have. This means parameters need to be intuitive enough that you can hopefully set them without having to know a lot about your data.
- **Stable Clusters:** If you run the algorithm twice with a different random initialization, you should expect to get roughly the same clusters back. If you are sampling your data, taking a different random sample shouldn't radically change the resulting cluster structure (unless your sampling has problems). If you vary the clustering algorithm parameters you want the clustering to change in a somewhat stable predictable fashion.
- **Performance:** Data sets are only getting bigger. You can sub-sample (but see *stability*), but ultimately you need a clustering algorithm that can scale to large data sizes. A clustering algorithm isn't much use if you can only use it if you take such a small sub-sample that it is no longer representative of the data at large!

There are other nice to have features like soft clusters, or overlapping clusters, but the above desiderata is enough to get started with because, oddly enough, very few clustering algorithms can satisfy them all!

Getting set up

If we are going to compare clustering algorithms we'll need a few things; first some libraries to load and cluster the data, and second some visualisation tools so we can look at the results of clustering.

```
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns
import sklearn.cluster as cluster
import time
%matplotlib inline
sns.set_context('poster')
sns.set_color_codes()
plot_kwds = {'alpha' : 0.25, 's' : 80, 'linewidths':0}
```

Next we need some data. In order to make this more interesting I've constructed an artificial dataset that will give clustering algorithms a challenge – some non-globular clusters, some noise etc.; the sorts of things we expect to crop up in messy real-world data. So that we can actually visualize clusterings the dataset is two dimensional; this is not something we expect from real-world data where you generally can't just visualize and see what is going on.

```
data = np.load('clusterable_data.npy')
```

So let's have a look at the data and see what we have.

```
plt.scatter(data.T[0], data.T[1], c='b', **plot_kwds)
frame = plt.gca()
frame.axes.get_xaxis().set_visible(False)
frame.axes.get_yaxis().set_visible(False)
```




It's messy, but there are certainly some clusters that you can pick out by eye; determining the exact boundaries of those clusters is harder of course, but we can hope that our clustering algorithms will find at least some of those clusters. So, on to testing ...

Testing Clustering Algorithms

To start let's set up a little utility function to do the clustering and plot the results for us. We can time the clustering algorithm while we're at it and add that to the plot since we do care about performance.

```
def plot_clusters(data, algorithm, args, kwds):
    start_time = time.time()
    labels = algorithm(*args, **kwds).fit_predict(data)
    end_time = time.time()
    palette = sns.color_palette('deep', np.unique(labels).max() + 1)
    colors = [palette[x] if x >= 0 else (0.0, 0.0, 0.0) for x in labels]
    plt.scatter(data.T[0], data.T[1], c=colors, **plot_kwds)
    frame = plt.gca()
    frame.axes.get_xaxis().set_visible(False)
    frame.axes.get_yaxis().set_visible(False)
    plt.title('Clusters found by {}'.format(str(algorithm.__name__)), fontsize=24)
    plt.text(-0.5, 0.7, 'Clustering took {:.2f} s'.format(end_time - start_time),
    ↪ fontsize=14)
```

Before we try doing the clustering, there are some things to keep in mind as we look at the results.

- In real use cases we *can't* look at the data and realise points are not really in a cluster; we have to take the clustering algorithm at its word.

- This is a small dataset, so poor performance here bodes very badly.

On to the clustering algorithms.

K-Means

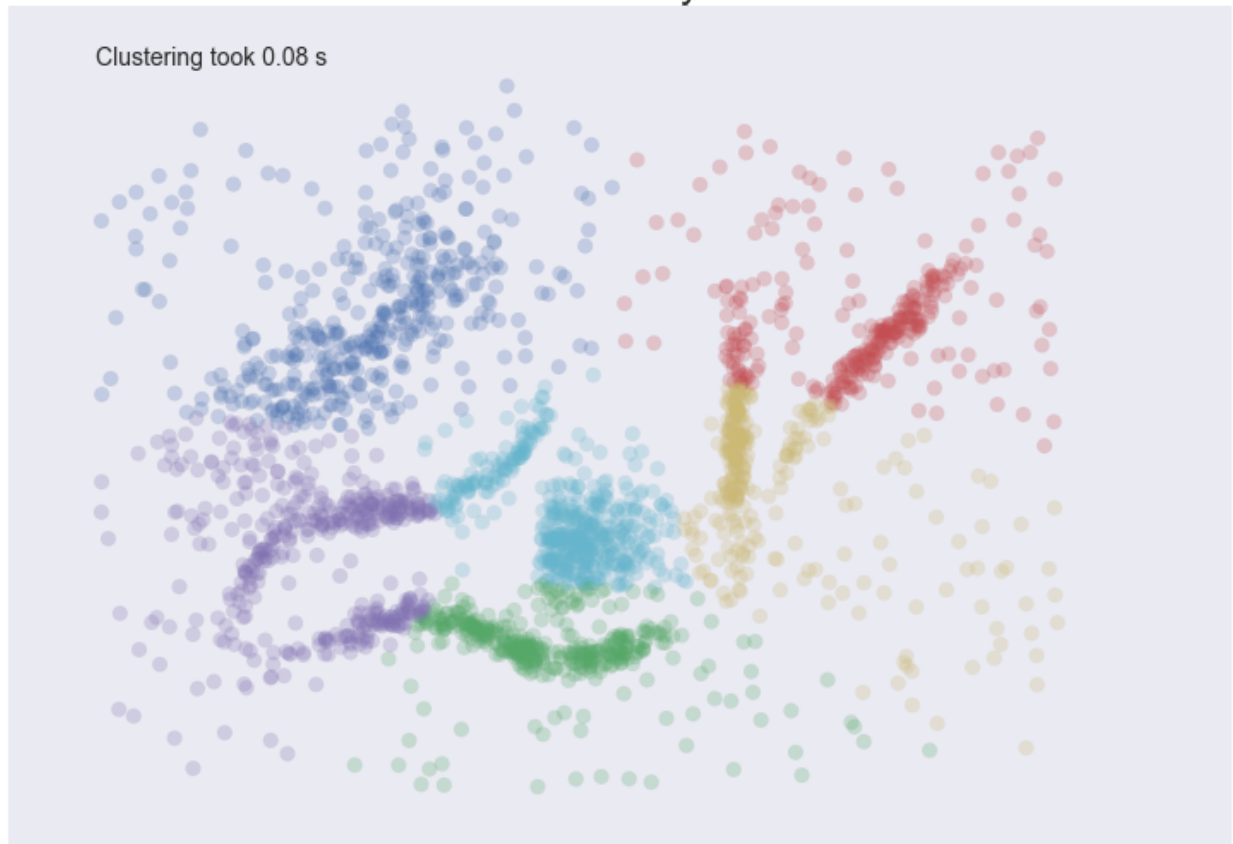
K-Means is the ‘go-to’ clustering algorithm for many simply because it is fast, easy to understand, and available everywhere (there’s an implementation in almost any statistical or machine learning tool you care to use). K-Means has a few problems however. The first is that it isn’t a clustering algorithm, it is a partitioning algorithm. That is to say K-means doesn’t ‘find clusters’ it partitions your dataset into as many (assumed to be globular) chunks as you ask for by attempting to minimize intra-partition distances. That leads to the second problem: you need to specify exactly how many clusters you expect. If you know a lot about your data then that is something you might expect to know. If, on the other hand, you are simply exploring a new dataset then ‘number of clusters’ is a hard parameter to have any good intuition for. The usually proposed solution is to run K-Means for many different ‘number of clusters’ values and score each clustering with some ‘cluster goodness’ measure (usually a variation on intra-cluster vs inter-cluster distances) and attempt to find an ‘elbow’. If you’ve ever done this in practice you know that finding said elbow is usually not so easy, nor does it necessarily correlate as well with the actual ‘natural’ number of clusters as you might like. Finally K-Means is also dependent upon initialization; give it multiple different random starts and you can get multiple different clusterings. This does not engender much confidence in any individual clustering that may result.

So, in summary, here’s how K-Means seems to stack up against our desiderata: * **Don’t be wrong!:** K-means is going to throw points into clusters whether they belong or not; it also assumes you clusters are globular. K-Means scores very poorly on this point. * **Intuitive parameters:** If you have a good intuition for how many clusters the dataset your exploring has then great, otherwise you might have a problem. * **Stability:** Hopefully the clustering is stable for your data. Best to have many runs and check though. * **Performance:** This is K-Means big win. It’s a simple algorithm and with the right tricks and optimizations can be made exceptionally efficient. There are few algorithms that can compete with K-Means for performance. If you have truly huge data then K-Means might be your only option.

But enough opinion, how does K-Means perform on our test dataset? Let’s have look. We’ll be generous and use our knowledge that there are six natural clusters and give that to K-Means.

```
plot_clusters(data, cluster.KMeans, (), {'n_clusters':6})
```

Clusters found by KMeans



We see some interesting results. First, the assumption of perfectly globular clusters means that the natural clusters have been spliced and clumped into various more globular shapes. Worse, the noise points get lumped into clusters as well: in some cases, due to where relative cluster centers ended up, points very distant from a cluster get lumped in. Having noise pollute your clusters like this is particularly bad in an EDA world since they can easily mislead your intuition and understanding of the data. On a more positive note we completed clustering very quickly indeed, so at least we can be wrong quickly.

Affinity Propagation

Affinity Propagation is a newer clustering algorithm that uses a graph based approach to let points ‘vote’ on their preferred ‘exemplar’. The end result is a set of cluster ‘exemplars’ from which we derive clusters by essentially doing what K-Means does and assigning each point to the cluster of it’s nearest exemplar. Affinity Propagation has some advantages over K-Means. First of all the graph based exemplar voting means that the user doesn’t need to specify the number of clusters. Second, due to how the algorithm works under the hood with the graph representation it allows for non-metric dissimilarities (i.e. we can have dissimilarities that don’t obey the triangle inequality, or aren’t symmetric). This second point is important if you are ever working with data isn’t naturally embedded in a metric space of some kind; few clustering algorithms support, for example, non-symmetric dissimilarities. Finally Affinity Propagation does, at least, have better stability over runs (but not over parameter ranges!).

The weak points of Affinity Propagation are similar to K-Means. Since it partitions the data just like K-Means we expect to see the same sorts of problems, particularly with noisy data. While Affinity Propagation eliminates the need to specify the number of clusters, it has ‘preference’ and ‘damping’ parameters. Picking these parameters well can be difficult. The implementation in `sklearn` default preference to the median dissimilarity. This tends to result in a very large number of clusters. A better value is something smaller (or negative) but data dependent. Finally Affinity

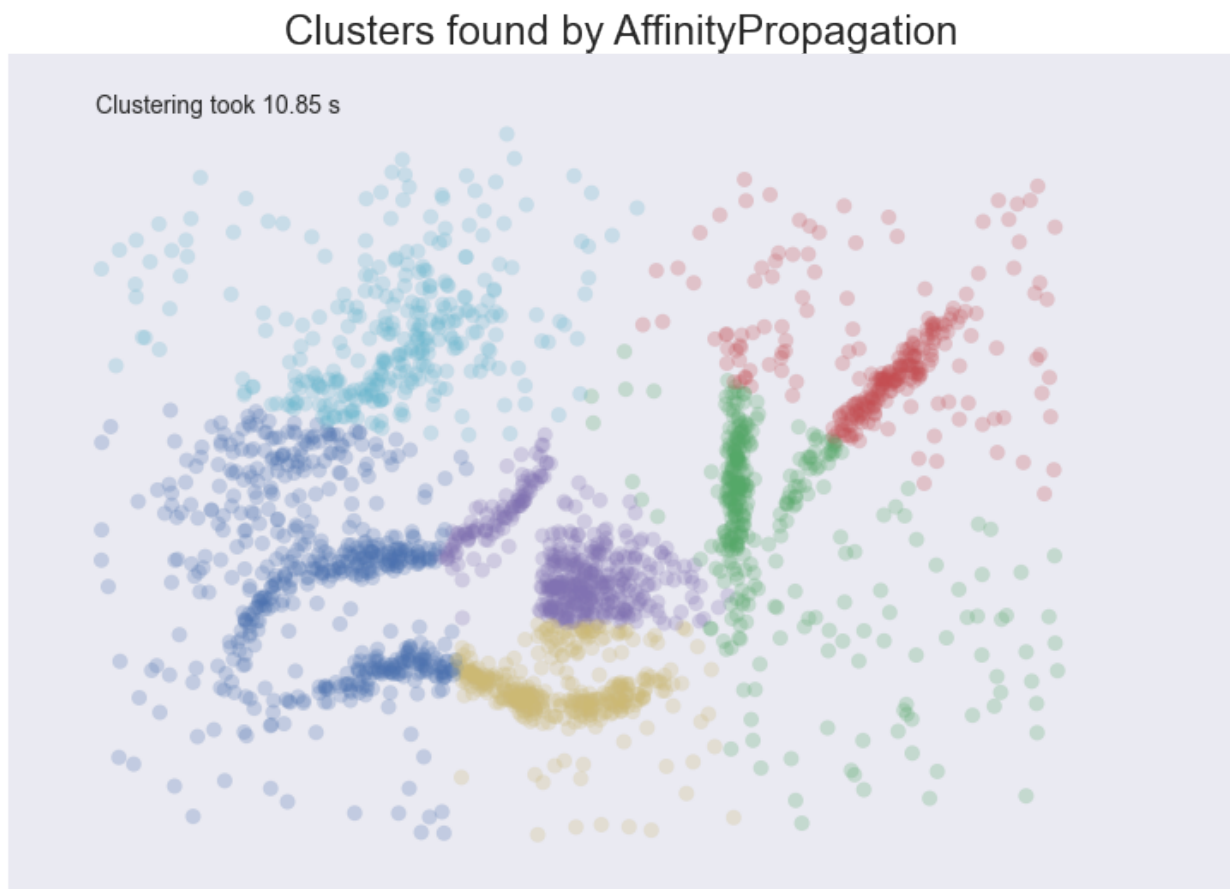
Propagation is *slow*; since it supports non-metric dissimilarities it can't take any of the shortcuts available to other algorithms, and the basic operations are expensive as data size grows.

So, in summary, over our desiderata we have:

- **Don't be wrong:** The same issues as K-Means; Affinity Propagation is going to throw points into clusters whether they belong or not; it also assumes you clusters are globular.
- **Intuitive Parameters:** It can be easier to guess at preference and damping than number of clusters, but since Affinity Propagation is quite sensitive to preference values it can be fiddly to get "right". This isn't really that much of an improvement over K-Means.
- **Stability:** Affinity Propagation is deterministic over runs.
- **Performance:** Affinity Propagation tends to be very slow. In practice running it on large datasets is essentially impossible without a carefully crafted and optimized implementation (i.e. not the default one available in `sklearn`).

And how does it look in practice on our chosen dataset? I've tried to select a preference and damping value that gives a reasonable number of clusters (in this case six) but feel free to play with the parameters yourself and see if you can come up with a better clustering.

```
plot_clusters(data, cluster.AffinityPropagation, (), {'preference':-5.0, 'damping':0.  
→95})
```



The result is eerily similar to K-Means and has all the same problems. The globular clusters have lumped together splined parts of various 'natural' clusters. The noise points have been assigned to clusters regardless of being significant outliers. In other words, we'll have a very poor intuitive understanding of our data based on these 'clusters'. Worse

still it took us several seconds to arrive at this unenlightening conclusion.

Mean Shift

Mean shift is another option if you don't want to have to specify the number of clusters. It is centroid based, like K-Means and affinity propagation, but can return clusters instead of a partition. The underlying idea of the Mean Shift algorithm is that there exists some probability density function from which the data is drawn, and tries to place centroids of clusters at the maxima of that density function. It approximates this via kernel density estimation techniques, and the key parameter is then the bandwidth of the kernel used. This is easier to guess than the number of clusters, but may require some staring at, say, the distributions of pairwise distances between data points to choose successfully. The other issue (at least with the sklearn implementation) is that it is fairly slow despite potentially having good scaling!

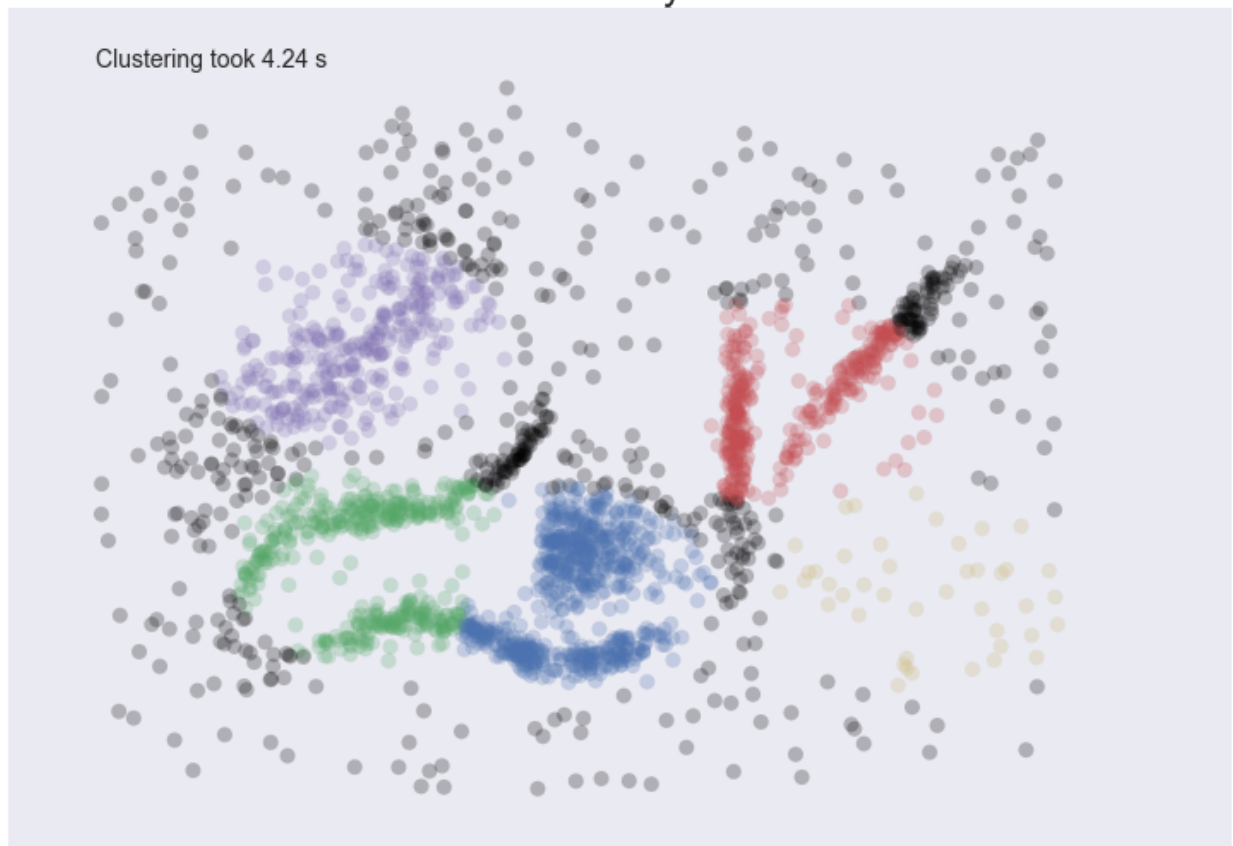
How does Mean Shift fare against our criteria? In principle promising, but in practice ...

- **Don't be wrong!:** Mean Shift doesn't cluster every point, but it still aims for globular clusters, and in practice it can return less than ideal results (see below for example). Without visual validation it can be hard to know how wrong it may be.
- **Intuitive parameters:** Mean Shift has more intuitive and meaningful parameters; this is certainly a strength.
- **Stability:** Mean Shift results can vary a lot as you vary the bandwidth parameter (which can make selection more difficult than it first appears. It also has a random initialisation, which means stability under runs can vary (if you reseed the random start).
- **Performance:** While Mean Shift has good scalability in principle (using ball trees) in practice the sklearn implementation is slow; this is a serious weak point for Mean Shift.

Let's see how it works on some actual data. I spent a while trying to find a good bandwidth value that resulted in a reasonable clustering. The choice below is about the best I found.

```
plot_clusters(data, cluster.MeanShift, (0.175,), {'cluster_all':False})
```

Clusters found by MeanShift



We at least aren't polluting our clusters with as much noise, but we certainly have dense regions left as noise and clusters that run across and split what seem like natural clusters. There is also the outlying yellow cluster group that doesn't make a lot of sense. Thus while Mean Shift had good promise, and is certainly better than K-Means, it's still short of our desiderata. Worse still it took over 4 seconds to cluster this small dataset!

Spectral Clustering

Spectral clustering can best be thought of as a graph clustering. For spatial data one can think of inducing a graph based on the distances between points (potentially a k-NN graph, or even a dense graph). From there spectral clustering will look at the eigenvectors of the Laplacian of the graph to attempt to find a good (low dimensional) embedding of the graph into Euclidean space. This is essentially a kind of manifold learning, finding a transformation of our original space so as to better represent manifold distances for some manifold that the data is assumed to lie on. Once we have the transformed space a standard clustering algorithm is run; with `sklearn` the default is K-Means. That means that the key for spectral clustering is the transformation of the space. Presuming we can better respect the manifold we'll get a better clustering – we need worry less about K-Means globular clusters as they are merely globular on the transformed space and not the original space. We unfortunately retain some of K-Means weaknesses: we still partition the data instead of clustering it; we have the hard to guess 'number of clusters' parameter; we have stability issues inherited from K-Means. Worse, if we operate on the dense graph of the distance matrix we have a very expensive initial step and sacrifice performance.

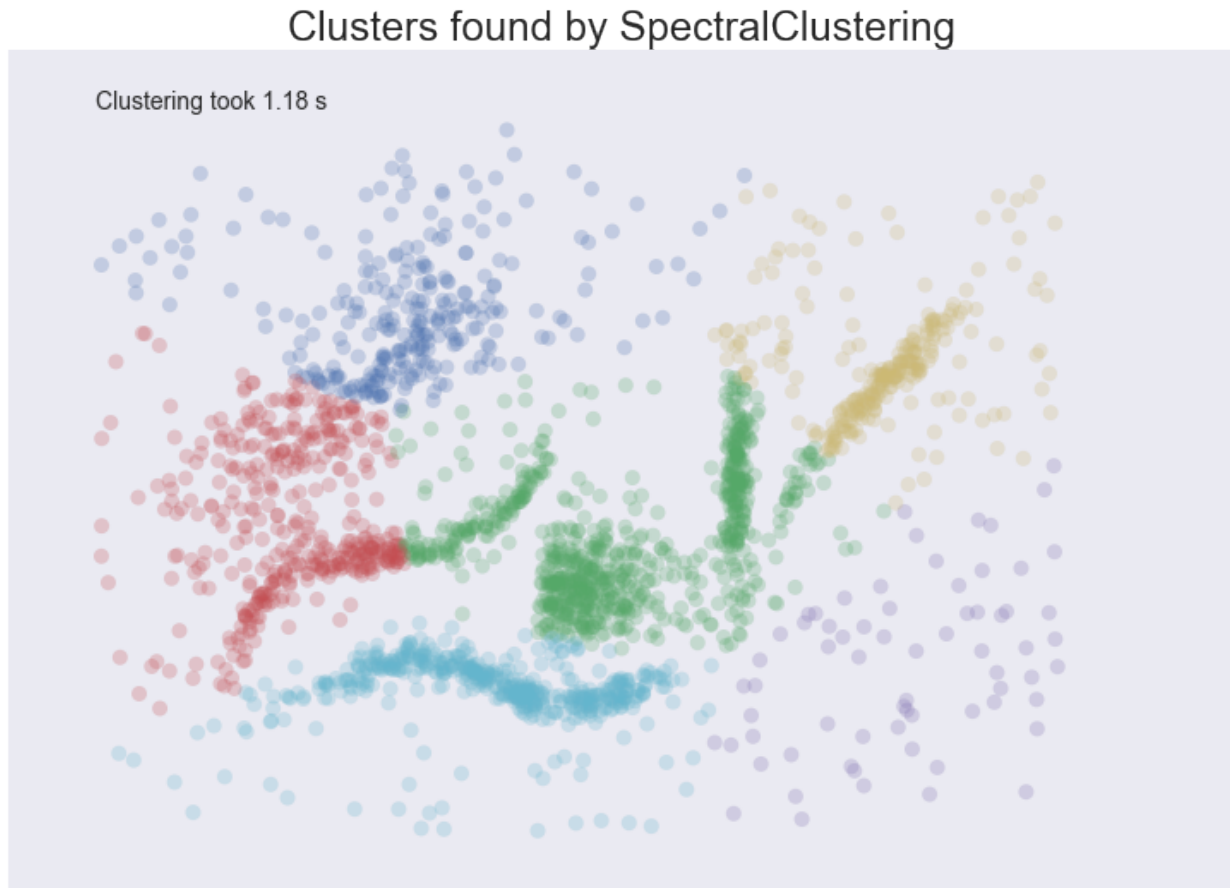
So, in summary:

- **Don't be wrong!:** We are less wrong, in that we don't have a purely globular cluster assumption; we do still have partitioning and hence are polluting clusters with noise, messing with our understanding of the clusters and hence the data.

- **Intuitive parameters:** We are no better than K-Means here; we have to know the correct number of clusters, or hope to guess by clustering over a range of parameter values and finding some way to pick the ‘right one’.
- **Stability:** Slightly more stable than K-Means due to the transformation, but we still suffer from those issues.
- **Performance:** For spatial data we don’t have a sparse graph (unless we prep one ourselves) so the result is a somewhat slower algorithm.

Let’s have a look at how it operates on our test dataset. Again, we’ll be generous and give it the six clusters to look for.

```
plot_clusters(data, cluster.SpectralClustering, (), {'n_clusters':6})
```



Spectral clustering performed *better* on the long thin clusters, but still ended up cutting some of them strangely and dumping parts of them in with other clusters. We also still have the issue of noise points polluting our clusters, so again our intuitions are going to be led astray. Performance was a distinct improvement of Affinity Propagation however. Over all we are doing better, but are still a long way from achieving our desiderata.

Agglomerative Clustering

Agglomerative clustering is really a suite of algorithms all based on the same idea. The fundamental idea is that you start with each point in it’s own cluster and then, for each cluster, use some criterion to choose another cluster to merge with. Do this repeatedly until you have only one cluster and you get a hierarchy, or binary tree, of clusters branching down to the last layer which has a leaf for each point in the dataset. The most basic version of this, single linkage, chooses the closest cluster to merge, and hence the tree can be ranked by distance as to when clusters merged/split. More complex variations use things like mean distance between clusters, or distance between cluster

centroids etc. to determine which cluster to merge. Once you have a cluster hierarchy you can choose a level or cut (according to some criteria) and take the clusters at that level of the tree. For `sklearn` we usually choose a cut based on a ‘number of clusters’ parameter passed in.

The advantage of this approach is that clusters can grow ‘following the underlying manifold’ rather than being presumed to be globular. You can also inspect the dendrogram of clusters and get more information about how clusters break down. On the other hand, if you want a flat set of clusters you need to choose a cut of the dendrogram, and that can be hard to determine. You can take the `sklearn` approach and specify a number of clusters, but as we’ve already discussed that isn’t a particularly intuitive parameter when you’re doing EDA. You can look at the dendrogram and try to pick a natural cut, but this is similar to finding the ‘elbow’ across varying k values for K-Means: in principle it’s fine, and the textbook examples always make it look easy, but in practice on messy real world data the ‘obvious’ choice is often far from obvious. We are also still partitioning rather than clustering the data, so we still have that persistent issue of noise polluting our clusters. Fortunately performance can be pretty good; the `sklearn` implementation is fairly slow, but `fastcluster` <<https://pypi.python.org/pypi/fastcluster>>__ provides high performance agglomerative clustering if that’s what you need.

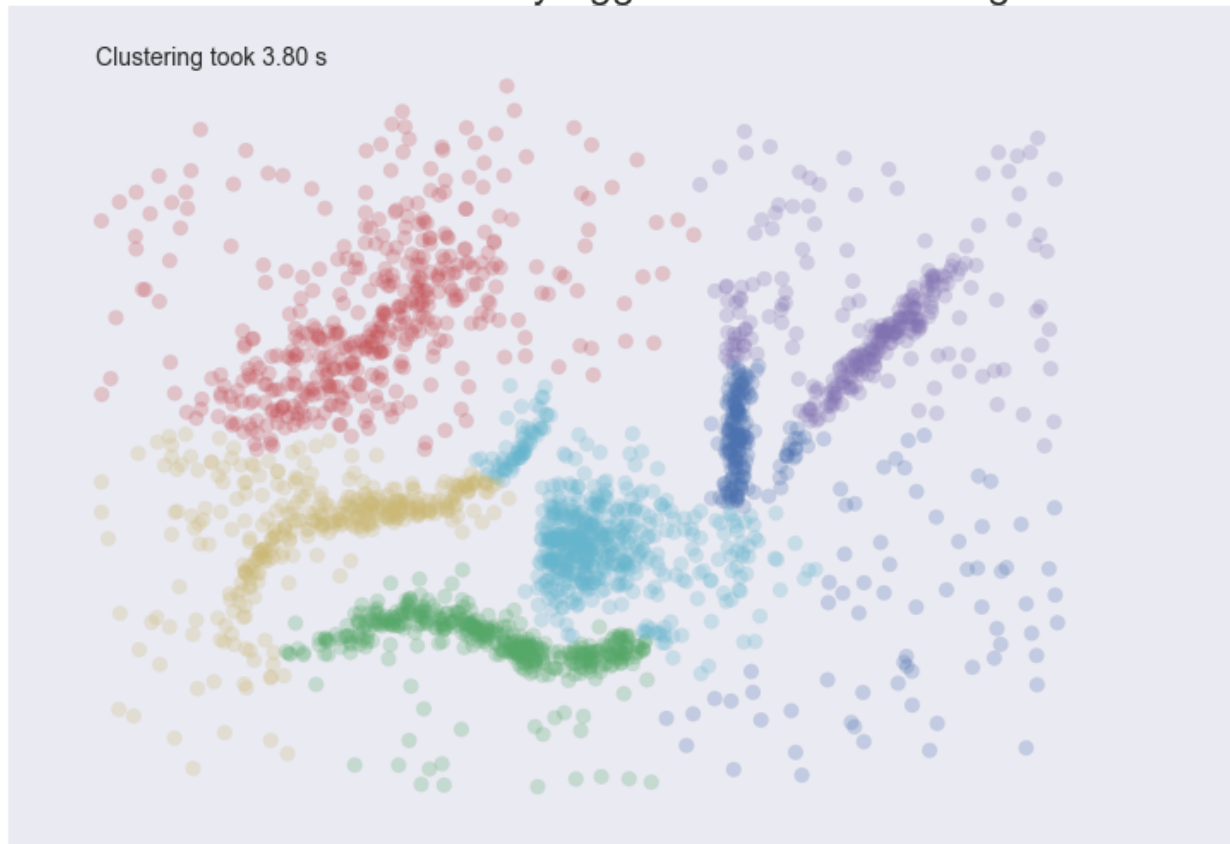
So, in summary:

- **Don’t be wrong!:** We have gotten rid of the globular assumption, but we are still assuming that all the data belongs in clusters with no noise.
- **Intuitive parameters:** Similar to K-Means we are stuck choosing the number of clusters (not easy in EDA), or trying to discern some natural parameter value from a plot that may or may not have any obvious natural choices.
- **Stability:** Agglomerative clustering is stable across runs and the dendrogram shows how it varies over parameter choices (in a reasonably stable way), so stability is a strong point.
- **Performance:** Performance can be good if you get the right implementation.

So, let’s see it clustering data. I chose to provide the correct number of clusters (six) and use Ward as the linkage/merge method. This is a more robust method than say single linkage, but it does tend toward more globular clusters.

```
plot_clusters(data, cluster.AgglomerativeClustering, (), {'n_clusters':6, 'linkage':  
↪ 'ward'})
```


Clusters found by AgglomerativeClustering



Similar to the spectral clustering we have handled the long thin clusters much better than K-Means or Affinity Propagation. We in fact improved on spectral clustering a bit on that front. We do still have clusters that contain parts of several different natural clusters, but those ‘mis-clustering’ are smaller. We also still have all the noise points polluting our clusters. The end result is probably the best clustering we’ve seen so far, but given the mis-clustering and noise issues we are still not going to get as good an intuition for the data as we might reasonably hope for.

DBSCAN

DBSCAN is a density based algorithm – it assumes clusters for dense regions. It is also the first actual clustering algorithm we’ve looked at: it doesn’t require that every point be assigned to a cluster and hence doesn’t partition the data, but instead extracts the ‘dense’ clusters and leaves sparse background classified as ‘noise’. In practice DBSCAN is related to agglomerative clustering. As a first step DBSCAN transforms the space according to the density of the data: points in dense regions are left alone, while points in sparse regions are moved further away. Applying single linkage clustering to the transformed space results in a dendrogram, which we cut according to a distance parameter (called epsilon or `eps` in many implementations) to get clusters. Importantly any singleton clusters at that cut level are deemed to be ‘noise’ and left unclustered. This provides several advantages: we get the manifold following behaviour of agglomerative clustering, and we get actual clustering as opposed to partitioning. Better yet, since we can frame the algorithm in terms of local region queries we can use various tricks such as kdtrees to get exceptionally good performance and scale to dataset sizes that are otherwise unapproachable with algorithms other than K-Means. There are some catches however. Obviously epsilon can be hard to pick; you can do some data analysis and get a good guess, but the algorithm can be quite sensitive to the choice of the parameter. The density based transformation depends on another parameter (`min_samples` in `sklearn`). Finally the combination of `min_samples` and `eps` amounts to a choice of density and the clustering only finds clusters at or above that density; if your data has variable density clusters then DBSCAN is either going to miss them, split them up, or lump some of them together depending on your

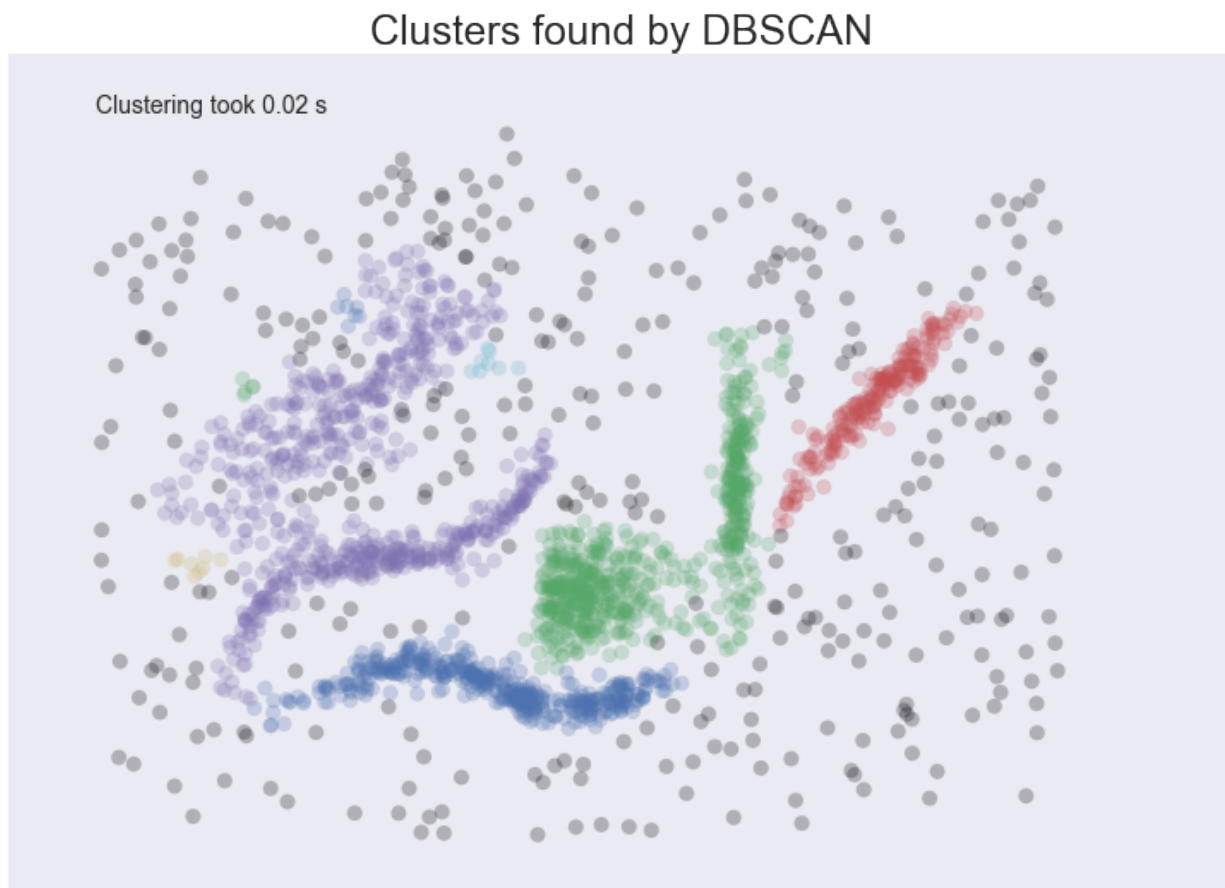
parameter choices.

So, in summary:

- **Don't be wrong!:** Clusters don't need to be globular, and won't have noise lumped in; varying density clusters may cause problems, but that is more in the form of insufficient detail rather than explicitly wrong. DBSCAN is the first clustering algorithm we've looked at that actually meets the 'Don't be wrong!' requirement.
- **Intuitive parameters:** Epsilon is a distance value, so you can survey the distribution of distances in your dataset to attempt to get an idea of where it should lie. In practice, however, this isn't an especially intuitive parameter, nor is it easy to get right.
- **Stability:** DBSCAN is stable across runs (and to some extent subsampling if you re-parameterize well); stability over varying epsilon and min samples is not so good.
- **Performance:** This is DBSCAN's other great strength; few clustering algorithms can tackle datasets as large as DBSCAN can.

So how does it cluster our test dataset? I played with a few epsilon values until I got something reasonable, but there was little science to this – getting the parameters right can be hard.

```
plot_clusters(data, cluster.DBSCAN, (), {'eps':0.025})
```



This is a pretty decent clustering; we've lumped natural clusters together a couple of times, but at least we didn't carve them up to do so. We also picked up a few tiny clusters in amongst the large sparse cluster. These problems are artifacts of not handling variable density clusters – to get the sparser clusters to cluster we end up lumping some of the denser clusters with them; in the meantime the very sparse cluster is still broken up into several clusters. All in all we're finally doing a decent job, but there's still plenty of room for improvement.

HDBSCAN

HDBSCAN is a recent algorithm developed by some of the same people who write the original DBSCAN paper. Their goal was to allow varying density clusters. The algorithm starts off much the same as DBSCAN: we transform the space according to density, exactly as DBSCAN does, and perform single linkage clustering on the transformed space. Instead of taking an epsilon value as a cut level for the dendrogram however, a different approach is taken: the dendrogram is condensed by viewing splits that result in a small number of points splitting off as points ‘falling out of a cluster’. This results in a smaller tree with fewer clusters that ‘lose points’. That tree can then be used to select the most stable or persistent clusters. This process allows the tree to be cut at varying height, picking our varying density clusters based on cluster stability. The immediate advantage of this is that we can have varying density clusters; the second benefit is that we have eliminated the epsilon parameter as we no longer need it to choose a cut of the dendrogram. Instead we have a new parameter `min_cluster_size` which is used to determine whether points are ‘falling out of a cluster’ or splitting to form two new clusters. This trades an unintuitive parameter for one that is not so hard to choose for EDA (what is the minimum size cluster I am willing to care about?).

So, in summary:

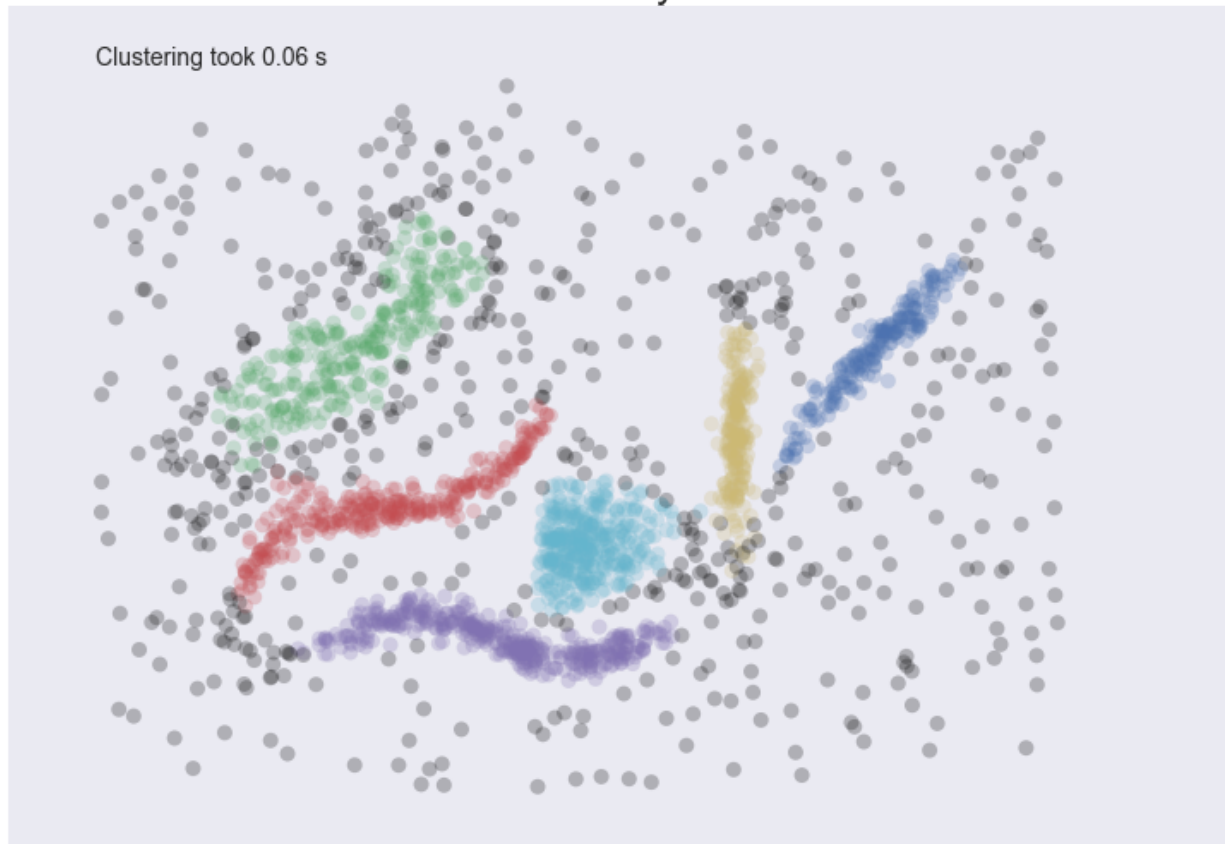
- **Don’t be wrong!:** We inherited all the benefits of DBSCAN and removed the varying density clusters issue. HDBSCAN is easily the strongest option on the ‘Don’t be wrong!’ front.
- **Intuitive parameters:** Choosing a minimum cluster size is very reasonable. The only remaining parameter is `min_samples` inherited from DBSCAN for the density based space transformation. Sadly `min_samples` is not that intuitive; HDBSCAN is not that sensitive to it and we can choose some sensible defaults, but this remains the biggest weakness of the algorithm.
- **Stability:** HDBSCAN is stable over runs and subsampling (since the variable density clustering will still cluster sparser subsampled clusters with the same parameter choices), and has good stability over parameter choices.
- **Performance:** When implemented well HDBSCAN can be very efficient. The current implementation has similar performance to `fastcluster`’s agglomerative clustering (and will use `fastcluster` if it is available), but we expect future implementations that take advantage of newer data structure such as cover trees to scale significantly better.

How does HDBSCAN perform on our test dataset? Unfortunately HDBSCAN is not part of `sklearn`. Fortunately we can just import the [hdbscan library](#) and use it as if it were part of `sklearn`.

```
import hdbscan
```

```
plot_clusters(data, hdbscan.HDBSCAN, (), {'min_cluster_size':15})
```

Clusters found by HDBSCAN



I think the picture speaks for itself.

Benchmarking Performance and Scaling of Python Clustering Algorithms

There are a host of different clustering algorithms and implementations thereof for Python. The performance and scaling can depend as much on the implementation as the underlying algorithm. Obviously a well written implementation in C or C++ will beat a naive implementation on pure Python, but there is more to it than just that. The internals and data structures used can have a large impact on performance, and can even significantly change asymptotic performance. All of this means that, given some amount of data that you want to cluster your options as to algorithm and implementation maybe significantly constrained. I'm both lazy, and prefer empirical results for this sort of thing, so rather than analyzing the implementations and deriving asymptotic performance numbers for various implementations I'm just going to run everything and see what happens.

To begin with we need to get together all the clustering implementations, along with some plotting libraries so we can see what is going on once we've got data. Obviously this is not an exhaustive collection of clustering implementations, so if I've left off your favourite I apologise, but one has to draw a line somewhere.

The implementations being test are:

- [Sklearn](#) (which implements several algorithms):
- K-Means clustering
- DBSCAN clustering

- Agglomerative clustering
- Spectral clustering
- Affinity Propagation
- `Scipy` (which provides basic algorithms):
- K-Means clustering
- Agglomerative clustering
- `Fastcluster` (which provides very fast agglomerative clustering in C++)
- `DeBaCl` (Density Based Clustering; similar to a mix of DBSCAN and Agglomerative)
- `HDBSCAN` (A robust hierarchical version of DBSCAN)

Obviously a major factor in performance will be the algorithm itself. Some algorithms are simply slower – often, but not always, because they are doing more work to provide a better clustering.

```
import hdbscan
import debacl
import fastcluster
import sklearn.cluster
import scipy.cluster
import sklearn.datasets
import numpy as np
import pandas as pd
import time
import matplotlib.pyplot as plt
import seaborn as sns
%matplotlib inline
sns.set_context('poster')
sns.set_palette('Paired', 10)
sns.set_color_codes()
```

Now we need some benchmarking code at various dataset sizes. Because some clustering algorithms have performance that can vary quite a lot depending on the exact nature of the dataset we'll also need to run several times on randomly generated datasets of each size so as to get a better idea of the average case performance.

We also need to generalise over algorithms which don't necessarily all have the same API. We can resolve that by taking a clustering function, argument tuple and keywords dictionary to let us do semi-arbitrary calls (fortunately all the algorithms do at least take the dataset to cluster as the first parameter).

Finally some algorithms scale poorly, and I don't want to spend forever doing clustering of random datasets so we'll cap the maximum time an algorithm can use; once it has taken longer than max time we'll just abort there and leave the remaining entries in our dataset by samples matrix unfilled.

In the end this all amounts to a fairly straightforward set of nested loops (over dataset sizes and number of samples) with calls to sklearn to generate mock data and the clustering function inside a timer. Add in some early abort and we're done.

```
def benchmark_algorithm(dataset_sizes, cluster_function, function_args, function_kwds,
                        dataset_dimension=10, dataset_n_clusters=10, max_time=45,
                        sample_size=2):

    # Initialize the result with NaNs so that any unfilled entries
    # will be considered NULL when we convert to a pandas dataframe at the end
    result = np.nan * np.ones((len(dataset_sizes), sample_size))
    for index, size in enumerate(dataset_sizes):
        for s in range(sample_size):
```

```

# Use sklearn's make_blobs to generate a random dataset with specified size
# dimension and number of clusters
data, labels = sklearn.datasets.make_blobs(n_samples=size,
                                           n_features=dataset_dimension,
                                           centers=dataset_n_clusters)

# Start the clustering with a timer
start_time = time.time()
cluster_function(data, *function_args, **function_kwds)
time_taken = time.time() - start_time

# If we are taking more than max_time then abort -- we don't
# want to spend excessive time on slow algorithms
if time_taken > max_time:
    result[index, s] = time_taken
    return pd.DataFrame(np.vstack([dataset_sizes.repeat(sample_size),
                                   result.flatten()]).T, columns=['x', 'y',
    ↪'])
else:
    result[index, s] = time_taken

# Return the result as a dataframe for easier handling with seaborn afterwards
return pd.DataFrame(np.vstack([dataset_sizes.repeat(sample_size),
                                result.flatten()]).T, columns=['x', 'y'])

```

Comparison of all ten implementations

Now we need a range of dataset sizes to test out our algorithm. Since the scaling performance is wildly different over the ten implementations we're going to look at it will be beneficial to have a number of very small dataset sizes, and increasing spacing as we get larger, spanning out to 32000 datapoints to cluster (to begin with). Numpy provides convenient ways to get this done via `arange` and vector multiplication. We'll start with step sizes of 500, then shift to steps of 1000 past 3000 datapoints, and finally steps of 2000 past 6000 datapoints.

```

dataset_sizes = np.hstack([np.arange(1, 6) * 500, np.arange(3, 7) * 1000, np.arange(4,
    ↪17) * 2000])

```

Now it is just a matter of running all the clustering algorithms via our benchmark function to collect up all the requisite data. This could be prettier, rolled up into functions appropriately, but sometimes brute force is good enough. More importantly (for me) since this can take a significant amount of compute time, I wanted to be able to comment out algorithms that were slow or I was uninterested in easily. Which brings me to a warning for you the reader and potential user of the notebook: this next step is very expensive. We are running ten different clustering algorithms multiple times each on twenty two different dataset sizes – and some of the clustering algorithms are slow (we are capping out at forty five seconds per run). That means that the next cell can take an hour or more to run. That doesn't mean "Don't try this at home" (I actually encourage you to try this out yourself and play with dataset parameters and clustering parameters) but it does mean you should be patient if you're going to!

```

k_means = sklearn.cluster.KMeans(10)
k_means_data = benchmark_algorithm(dataset_sizes, k_means.fit, (), {})

dbscan = sklearn.cluster.DBSCAN(eps=1.25)
dbscan_data = benchmark_algorithm(dataset_sizes, dbscan.fit, (), {})

scipy_k_means_data = benchmark_algorithm(dataset_sizes,
                                         scipy.cluster.vq.kmeans, (10,), {})

```

```

scipy_single_data = benchmark_algorithm(dataset_sizes,
                                       scipy.cluster.hierarchy.single, (), {})

fastclust_data = benchmark_algorithm(dataset_sizes,
                                    fastcluster.linkage_vector, (), {})

hdbscan_ = hdbscan.HDBSCAN()
hdbscan_data = benchmark_algorithm(dataset_sizes, hdbscan_.fit, (), {})

debacl_data = benchmark_algorithm(dataset_sizes,
                                  debacl.geom_tree.geomTree, (5, 5), {'verbose':False}
↳)

agglomerative = sklearn.cluster.AgglomerativeClustering(10)
agg_data = benchmark_algorithm(dataset_sizes,
                              agglomerative.fit, (), {}, sample_size=4)

spectral = sklearn.cluster.SpectralClustering(10)
spectral_data = benchmark_algorithm(dataset_sizes,
                                    spectral.fit, (), {}, sample_size=6)

affinity_prop = sklearn.cluster.AffinityPropagation()
ap_data = benchmark_algorithm(dataset_sizes,
                              affinity_prop.fit, (), {}, sample_size=3)

```

Now we need to plot the results so we can see what is going on. The catch is that we have several datapoints for each dataset size and ultimately we would like to try and fit a curve through all of it to get the general scaling trend. Fortunately [seaborn](#) comes to the rescue here by providing `regplot` which plots a regression through a dataset, supports higher order regression (we should probably use order two as most algorithms are effectively quadratic) and handles multiple datapoints for each x-value cleanly (using the `x_estimator` keyword to put a point at the mean and draw an error bar to cover the range of data).

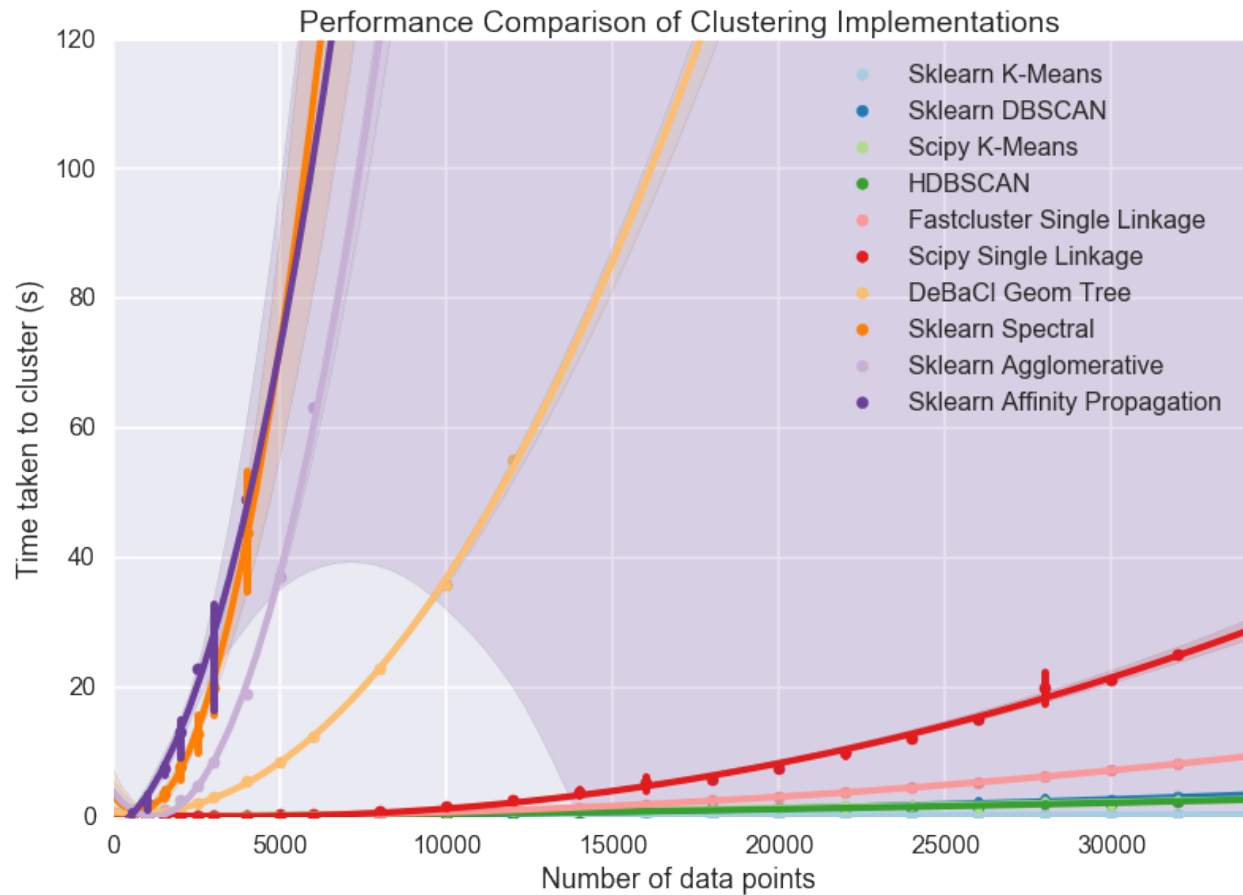
```

sns.regplot(x='x', y='y', data=k_means_data, order=2,
           label='Sklearn K-Means', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=dbscan_data, order=2,
           label='Sklearn DBSCAN', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=scipy_k_means_data, order=2,
           label='Scipy K-Means', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=hdbscan_data, order=2,
           label='HDBSCAN', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=fastclust_data, order=2,
           label='Fastcluster Single Linkage', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=scipy_single_data, order=2,
           label='Scipy Single Linkage', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=debacl_data, order=2,
           label='DeBaCl Geom Tree', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=spectral_data, order=2,
           label='Sklearn Spectral', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=agg_data, order=2,
           label='Sklearn Agglomerative', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=ap_data, order=2,
           label='Sklearn Affinity Propagation', x_estimator=np.mean)
plt.gca().axis([0, 34000, 0, 120])
plt.gca().set_xlabel('Number of data points')
plt.gca().set_ylabel('Time taken to cluster (s)')
plt.title('Performance Comparison of Clustering Implementations')
plt.legend()

```



```
<matplotlib.legend.Legend at 0x1125dee50>
```



A few features stand out. First of all there appear to be essentially two classes of implementation, with DeBaCl being an odd case that falls in the middle. The fast implementations tend to be implementations of single linkage agglomerative clustering, K-means, and DBSCAN. The slow cases are largely from sklearn and include agglomerative clustering (in this case using Ward instead of single linkage).

For practical purposes this means that if you have much more than 10000 datapoints your clustering options are significantly constrained: sklearn spectral, agglomerative and affinity propagation are going to take far too long. DeBaCl may still be an option, but given that the hdbscan library provides “robust single linkage clustering” equivalent to what DeBaCl is doing (and with effectively the same runtime as hdbscan as it is a subset of that algorithm) it is probably not the best choice for large dataset sizes.

So let’s drop out those slow algorithms so we can scale out a little further and get a closer look at the various algorithms that managed 32000 points in under thirty seconds. There is almost undoubtedly more to learn as we get ever larger dataset sizes.

Comparison of fast implementations

Let’s compare the six fastest implementations now. We can scale out a little further as well; based on the curves above it looks like we should be able to comfortably get to 60000 data points without taking much more than a minute per run. We can also note that most of these implementations weren’t that noisy so we can get away with a single run per dataset size.


```

large_dataset_sizes = np.arange(1,16) * 4000

hdbscan_boruvka = hdbscan.HDBSCAN(algorithm='boruvka_kdtree')
large_hdbscan_boruvka_data = benchmark_algorithm(large_dataset_sizes,
                                                hdbscan_boruvka.fit, (), {},
                                                max_time=90, sample_size=1)

k_means = sklearn.cluster.KMeans(10)
large_k_means_data = benchmark_algorithm(large_dataset_sizes,
                                        k_means.fit, (), {},
                                        max_time=90, sample_size=1)

dbscan = sklearn.cluster.DBSCAN(eps=1.25, min_samples=5)
large_dbscan_data = benchmark_algorithm(large_dataset_sizes,
                                       dbscan.fit, (), {},
                                       max_time=90, sample_size=1)

large_fastclust_data = benchmark_algorithm(large_dataset_sizes,
                                          fastcluster.linkage_vector, (), {},
                                          max_time=90, sample_size=1)

large_scipy_k_means_data = benchmark_algorithm(large_dataset_sizes,
                                              scipy.cluster.vq.kmeans, (10,), {},
                                              max_time=90, sample_size=1)

large_scipy_single_data = benchmark_algorithm(large_dataset_sizes,
                                             scipy.cluster.hierarchy.single, (), {},
                                             max_time=90, sample_size=1)

```

Again we can use seaborn to do curve fitting and plotting, exactly as before.

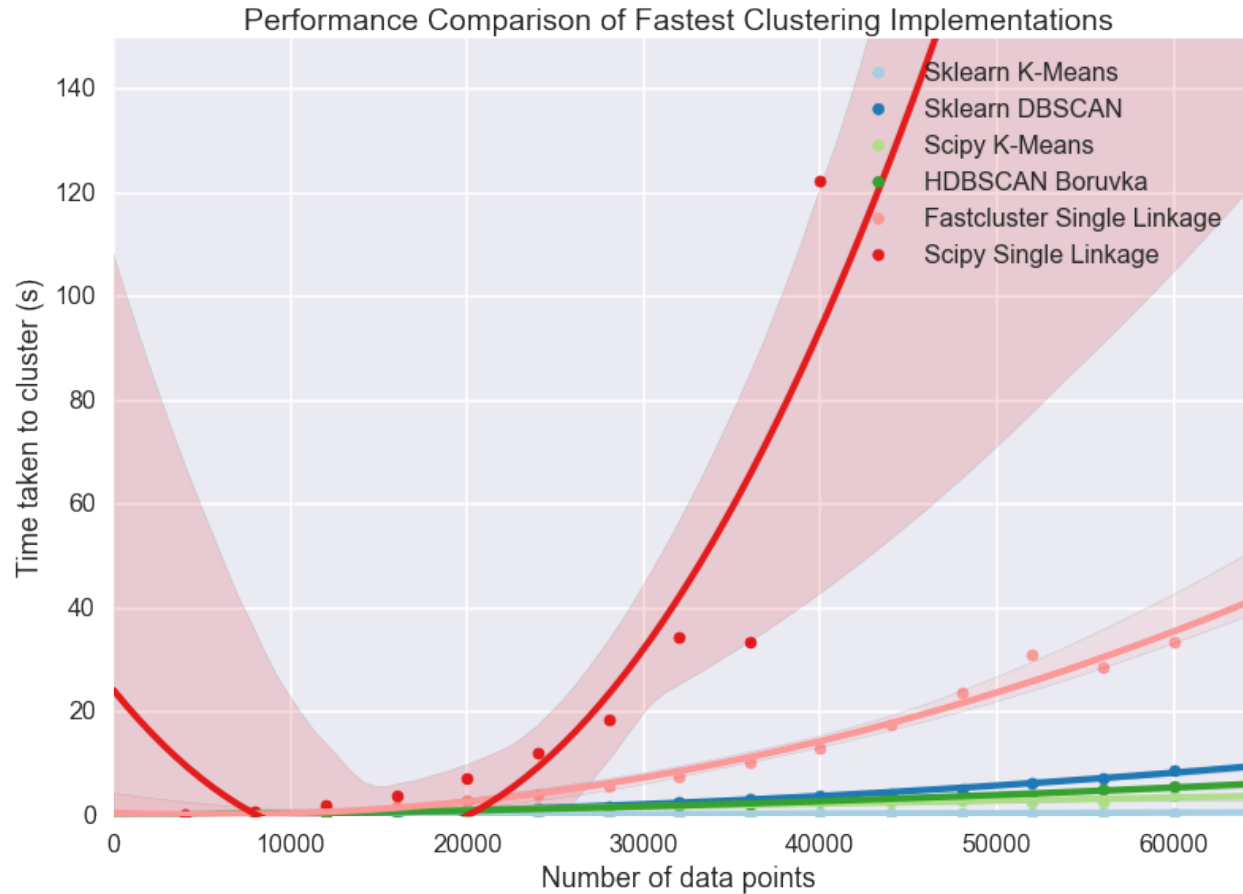
```

sns.regplot(x='x', y='y', data=large_k_means_data, order=2,
            label='Sklearn K-Means', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=large_dbscan_data, order=2,
            label='Sklearn DBSCAN', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=large_scipy_k_means_data, order=2,
            label='Scipy K-Means', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=large_hdbscan_boruvka_data, order=2,
            label='HDBSCAN Boruvka', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=large_fastclust_data, order=2,
            label='Fastcluster Single Linkage', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=large_scipy_single_data, order=2,
            label='Scipy Single Linkage', x_estimator=np.mean)

plt.gca().axis([0, 64000, 0, 150])
plt.gca().set_xlabel('Number of data points')
plt.gca().set_ylabel('Time taken to cluster (s)')
plt.title('Performance Comparison of Fastest Clustering Implementations')
plt.legend()

```

```
<matplotlib.legend.Legend at 0x116038bd0>
```



Clearly something has gone woefully wrong with the curve fitting for the scipy single linkage implementation, but what exactly? If we look at the raw data we can see.

```
large_scipy_single_data.tail(10)
```

It seems that at around 44000 points we hit a wall and the runtimes spiked. A hint is that I'm running this on a laptop with 8GB of RAM. Both single linkage algorithms use `scipy.spatial.pdist` to compute pairwise distances between points, which returns an array of shape $(n(n-1)/2, 1)$ of doubles. A quick computation shows that that array of distances is quite large once we have 44000 points:

```
size_of_array = 44000 * (44000 - 1) / 2          # from pdist documentation
bytes_in_array = size_of_array * 8                # Since doubles use 8 bytes
gigabytes_used = bytes_in_array / (1024.0 ** 3)   # divide out to get the number of GB
gigabytes_used
```

```
7.211998105049133
```

If we assume that my laptop is keeping much other than that distance array in RAM then clearly we are going to spend time paging out the distance array to disk and back and hence we will see the runtimes increase dramatically as we become disk IO bound. If we just leave off the last element we can get a better idea of the curve, but keep in mind that the scipy single linkage implementation does not scale past a limit set by your available RAM.

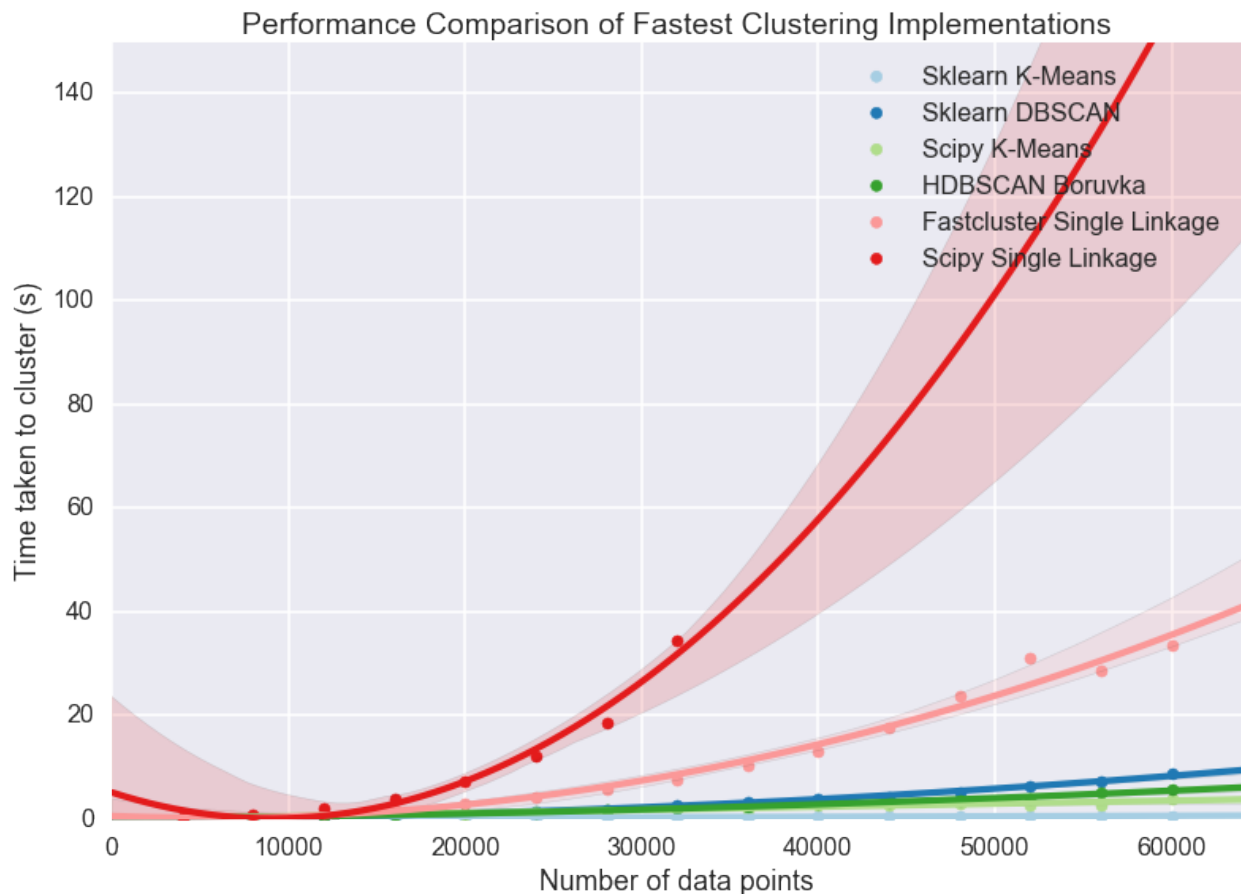
```
sns.regplot(x='x', y='y', data=large_k_means_data, order=2,
            label='Sklearn K-Means', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=large_dbscan_data, order=2,
            label='Sklearn DBSCAN', x_estimator=np.mean)
```

```
sns.regplot(x='x', y='y', data=large_scipy_k_means_data, order=2,
            label='Scipy K-Means', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=large_hdbscan_boruvka_data, order=2,
            label='HDBSCAN Boruvka', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=large_fastclust_data, order=2,
            label='Fastcluster Single Linkage', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=large_scipy_single_data[:8], order=2,
            label='Scipy Single Linkage', x_estimator=np.mean)

plt.gca().axis([0, 64000, 0, 150])
plt.gca().set_xlabel('Number of data points')
plt.gca().set_ylabel('Time taken to cluster (s)')
plt.title('Performance Comparison of Fastest Clustering Implementations')
plt.legend()
```

```
/Users/leland/.conda/envs/hdbscan_dev/lib/python2.7/site-packages/numpy/lib/
↳ polynomial.py:595: RankWarning: Polyfit may be poorly conditioned
    warnings.warn(msg, RankWarning)
```

```
<matplotlib.legend.Legend at 0x118843210>
```



If we're looking for scaling we can write off the scipy single linkage implementation – if even we didn't hit the RAM limit the $O(n^2)$ scaling is going to quickly catch up with us. Fastcluster has the same asymptotic scaling, but is heavily optimized to being the constant down much lower – at this point it is still keeping close to the faster algorithms. It's asymptotics will still catch up with it eventually however.

In practice this is going to mean that for larger datasets you are going to be very constrained in what algorithms you can apply: if you get enough datapoints only K-Means, DBSCAN, and HDBSCAN will be left. This is somewhat disappointing, particularly as **K-Means is not a particularly good clustering algorithm**, particularly for exploratory data analysis.

With this in mind it is worth looking at how these last several implementations perform at much larger sizes, to see, for example, when fastcluster starts to have its asymptotic complexity start to pull it away.

Comparison of high performance implementations

At this point we can scale out to 200000 datapoints easily enough, so let's push things at least that far so we can start to really see scaling effects.

```
huge_dataset_sizes = np.arange(1,11) * 20000

k_means = sklearn.cluster.KMeans(10)
huge_k_means_data = benchmark_algorithm(huge_dataset_sizes,
                                       k_means.fit, (), {},
                                       max_time=120, sample_size=2, dataset_
↳dimension=10)

dbscan = sklearn.cluster.DBSCAN(eps=1.5)
huge_dbscan_data = benchmark_algorithm(huge_dataset_sizes,
                                       dbscan.fit, (), {},
                                       max_time=120, sample_size=2, dataset_
↳dimension=10)

huge_scipy_k_means_data = benchmark_algorithm(huge_dataset_sizes,
                                             scipy.cluster.vq.kmeans, (10,), {},
                                             max_time=120, sample_size=2, dataset_
↳dimension=10)

hdbscan_boruvka = hdbscan.HDBSCAN(algorithm='boruvka_kdtree')
huge_hdbscan_data = benchmark_algorithm(huge_dataset_sizes,
                                       hdbscan_boruvka.fit, (), {},
                                       max_time=240, sample_size=4, dataset_
↳dimension=10)

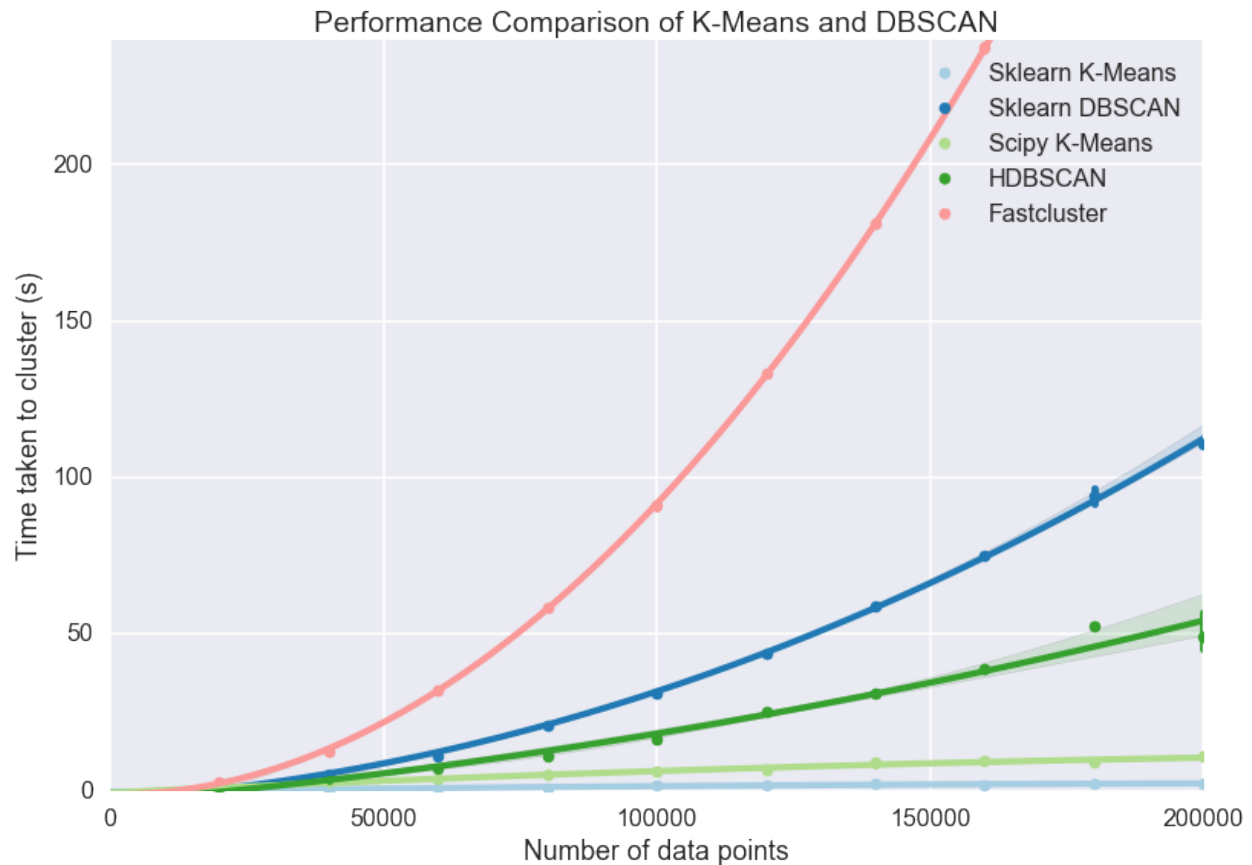
huge_fastcluster_data = benchmark_algorithm(huge_dataset_sizes,
                                           fastcluster.linkage_vector, (), {},
                                           max_time=240, sample_size=2, dataset_
↳dimension=10)
```

```
sns.regplot(x='x', y='y', data=huge_k_means_data, order=2,
            label='Sklearn K-Means', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=huge_dbscan_data, order=2,
            label='Sklearn DBSCAN', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=huge_scipy_k_means_data, order=2,
            label='Scipy K-Means', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=huge_hdbscan_data, order=2,
            label='HDBSCAN', x_estimator=np.mean)
sns.regplot(x='x', y='y', data=huge_fastcluster_data, order=2,
            label='Fastcluster', x_estimator=np.mean)

plt.gca().axis([0, 200000, 0, 240])
plt.gca().set_xlabel('Number of data points')
```

```
plt.gca().set_ylabel('Time taken to cluster (s)')
plt.title('Performance Comparison of K-Means and DBSCAN')
plt.legend()
```

```
<matplotlib.legend.Legend at 0x11d2aff50>
```



Now the some differences become clear. The asymptotic complexity starts to kick in with fastcluster failing to keep up. In turn HDBSCAN and DBSCAN, while having sub- $O(n^2)$ complexity, can't achieve $O(n \log(n))$ at this dataset dimension, and start to curve upward precipitously. Finally it demonstrates again how much of a difference implementation can make: the sklearn implementation of K-Means is far better than the scipy implementation. Since HDBSCAN clustering is a lot better than K-Means (unless you have good reasons to assume that the clusters partition your data and are all drawn from Gaussian distributions) and the scaling is still pretty good I would suggest that unless you have a truly stupendous amount of data you wish to cluster then the HDBSCAN implementation is a good choice.

But should I get a coffee?

So we know which implementations scale and which don't; a more useful thing to know in practice is, given a dataset, what can I run interactively? What can I run while I go and grab some coffee? How about a run over lunch? What if I'm willing to wait until I get in tomorrow morning? Each of these represent significant breaks in productivity – once you aren't working interactively anymore your productivity drops measurably, and so on.

We can build a table for this. To start we'll need to be able to approximate how long a given clustering implementation will take to run. Fortunately we already gathered a lot of that data; if we load up the `statsmodels` package we can fit the data (with a quadratic or $n \log n$ fit depending on the implementation; DBSCAN and HDBSCAN get caught here, since while they are under $O(n^2)$ scaling, they don't have an easily described model, so I'll model them as n^2

for now) and use the resulting model to make our predictions. Obviously this has some caveats: if you fill your RAM with a distance matrix your runtime isn't going to fit the curve.

I've hand built a `time_samples` list to give a reasonable set of potential data sizes that are nice and human readable. After that we just need a function to fit and build the curves.

```
import statsmodels.formula.api as sm

time_samples = [1000, 2000, 5000, 10000, 25000, 50000, 75000, 100000, 250000, 500000,
↳750000,
                1000000, 2500000, 5000000, 10000000, 50000000, 100000000, 500000000,
↳1000000000]

def get_timing_series(data, quadratic=True):
    if quadratic:
        data['x_squared'] = data.x**2
        model = sm.ols('y ~ x + x_squared', data=data).fit()
        predictions = [model.params.dot([1.0, i, i**2]) for i in time_samples]
        return pd.Series(predictions, index=pd.Index(time_samples))
    else: # assume n log(n)
        data['xlogx'] = data.x * np.log(data.x)
        model = sm.ols('y ~ x + xlogx', data=data).fit()
        predictions = [model.params.dot([1.0, i, i*np.log(i)]) for i in time_samples]
        return pd.Series(predictions, index=pd.Index(time_samples))
```

Now we run that for each of our pre-existing datasets to extrapolate out predicted performance on the relevant dataset sizes. A little pandas wrangling later and we've produced a table of roughly how large a dataset you can tackle in each time frame with each implementation. I had to leave out the scipy KMeans timings because the noise in timing results caused the model to be unrealistic at larger data sizes. Note how the $O(n \log n)$ algorithms utterly dominate here. In the meantime, for medium sizes data sets you can still get quite a lot done with HDBSCAN.

```
ap_timings = get_timing_series(ap_data)
spectral_timings = get_timing_series(spectral_data)
agg_timings = get_timing_series(agg_data)
debacl_timings = get_timing_series(debacl_data)
fastclust_timings = get_timing_series(large_fastclust_data.ix[:10,:].copy())
scipy_single_timings = get_timing_series(large_scipy_single_data.ix[:10,:].copy())
hdbscan_boruvka = get_timing_series(huge_hdbscan_data, quadratic=True)
#scipy_k_means_timings = get_timing_series(huge_scipy_k_means_data, quadratic=False)
dbscan_timings = get_timing_series(huge_dbscan_data, quadratic=True)
k_means_timings = get_timing_series(huge_k_means_data, quadratic=False)

timing_data = pd.concat([ap_timings, spectral_timings, agg_timings, debacl_timings,
                        scipy_single_timings, fastclust_timings, hdbscan_boruvka,
                        dbscan_timings, k_means_timings
                        ], axis=1)
timing_data.columns=['AffinityPropagation', 'Spectral', 'Agglomerative',
                    'DeBaCl', 'ScipySingleLinkage', 'Fastcluster',
                    'HDBSCAN', 'DBSCAN', 'SKLearn KMeans'
                    ]

def get_size(series, max_time):
    return series.index[series < max_time].max()

datasize_table = pd.concat([
    timing_data.apply(get_size, max_time=30),
    timing_data.apply(get_size, max_time=300),
    timing_data.apply(get_size, max_time=3600),
    timing_data.apply(get_size, max_time=8*3600)
```

```

], axis=1)
datasize_table.columns=('Interactive', 'Get Coffee', 'Over Lunch', 'Overnight')
datasize_table

```

Conclusions

Performance obviously depends on the algorithm chosen, but can also vary significantly upon the specific implementation (HDBSCAN is far better hierarchical density based clustering than DeBaCl, and sklearn has by far the best K-Means implementation). For anything beyond toy datasets, however, your algorithm options are greatly constrained. In my (obviously biased) opinion **HDBSCAN is the best algorithm for clustering**. If you need to cluster data beyond the scope that HDBSCAN can reasonably handle then the only algorithm options on the table are DBSCAN and K-Means; DBSCAN is the slower of the two, especially for very large data, but K-Means clustering can be remarkably poor – it’s a tough choice.

How Soft Clustering for HDBSCAN Works

This is a general description of how the soft clustering algorithm for HDBSCAN Works. We will implement soft clustering from scratch – not in the efficient way that the **hdbscan library** implements it, but in a way that makes it clearer what is actually going on.

What is Soft Clustering?

To start, we’ll provide a quick primer on what soft clustering is, and why you might want it in the first place. Traditional clustering assigns each point in a data set to a cluster (or to noise). This is a hard assignment; there are no mixed memberships. A point near the edge of one cluster and also close to a second cluster, is just as much “in the first cluster” as a point solidly in the center that is very distant from the second cluster. Equally, if the clustering algorithm supports noise assignments, then points are simply assigned as “noise”. We are left with no idea as to which, if any cluster, they might have just missed the cur on being in.

The remedy for this is ‘soft clustering’ or ‘fuzzy clustering’. In this approach points are not assigned cluster labels, but are instead assigned a vector of probabilities. The length of the vector is equal to the number of clusters found. The probability value at the i th entry of the vector is the probability that that point is a member of the i th cluster. This allows points to potentially be a mix of clusters. By looking at the vector a data scientist can discern how strongly a point is in a cluster, and which other clusters it is related to. Equally noise point will usually be assigned low probabilities of being in any cluster, but you can discern which clusters they are closer to, or even if they were very nearly part of a cluster. This is a much richer and more informative clustering result ... so how do we get it?

Soft Clustering for HDBSCAN

We want to produce a method of providing a soft membership vector for a given point across the selected clusters of a clustering. Ideally we want this to be interpretable as a probability of being a member of that cluster. For now we will work solely with categorizing points already in the clustered data set, but in principle this can be extended to new previously unseen points presuming we have a method to insert such points into the condensed tree (see other discussions on how to handle “prediction”). First let’s get some test data, and an associated clustering so we have some idea of what we’re working with in our test example.

```

import hdbscan
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns

```

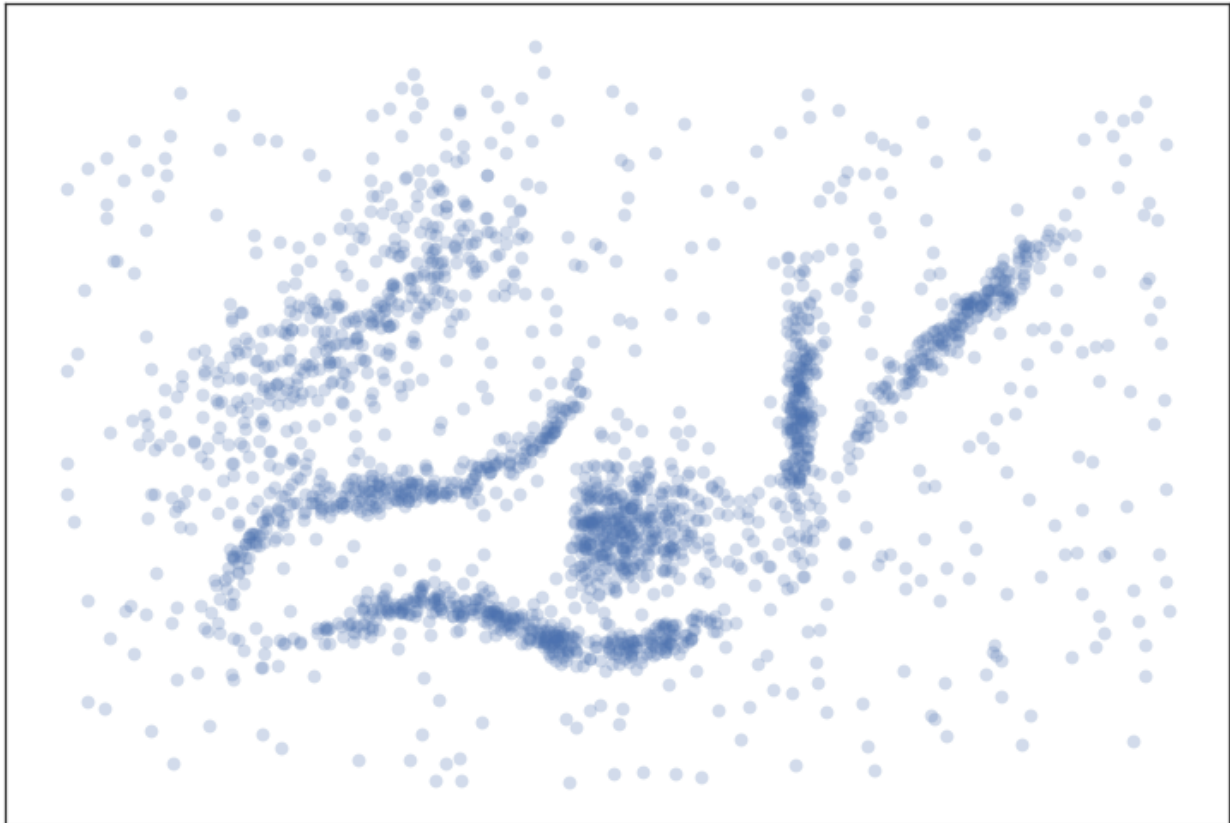
```
import pandas as pd
import matplotlib as mpl

from scipy.spatial.distance import cdist

%matplotlib inline
sns.set_context('poster')
sns.set_style('white')
sns.set_color_codes()

plot_kwds={'alpha':0.25, 's':60, 'linewidths':0}
palette = sns.color_palette('deep', 12)
```

```
data = np.load('clusterable_data.npy')
fig = plt.figure()
ax = fig.add_subplot(111)
plt.scatter(data.T[0], data.T[1], **plot_kwds)
ax.set_xticks([])
ax.set_yticks([]);
```

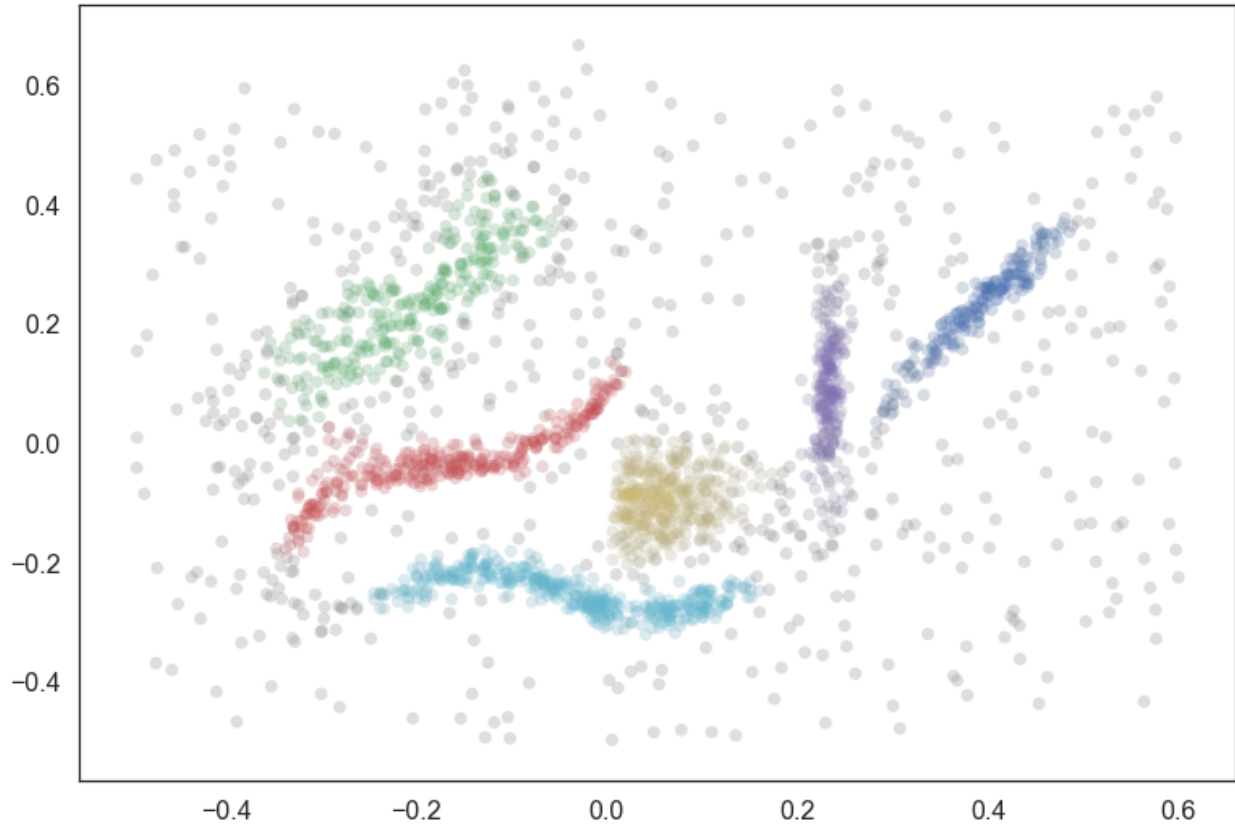


Now let's build a clusterer and fit it to this data.

```
clusterer = hdbscan.HDBSCAN(min_cluster_size=15).fit(data)
```

We can visualize the resulting clustering (using the soft cluster scores to vary the saturation so that we gain some intuition about how soft the clusters may be) to get an idea of what we are looking at:


```
pal = sns.color_palette('deep', 8)
colors = [sns.desaturate(pal[col], sat) for col, sat in zip(clusterer.labels_,
                                                           clusterer.probabilities_)]
plt.scatter(data.T[0], data.T[1], c=colors, **plot_kwds);
```



Suppose now that we have a data point and we want to get a notion of how close it is to each of the clusters. There are at least two ways we can think about this. The first approach is to take the question somewhat literally and consider the distance from the cluster. As can be seen in our example, however, clusters need not have clear centers (they may be linear, or oddly shaped); even if we get a notion of distance it may not follow the “cluster manifold distance” and hence may be somewhat less than ideal. The second way of looking at things is to consider how much of an outlier the point is relative to each cluster – using something akin to the outlier scores from GLOSH. The advantage of this approach is that it handles odd shaped clusters (even toroidal clusters) far better since it will explicitly follow the manifolds of the clusters. The down side of the outlier approach is that many points will all be equally “outlying”, particularly noise points. Our goal is to fuse these two ideas.

Distance Based Membership

First we’ll build a vector for a purely distance based vector of possible cluster membership – essentially just asking “which cluster am I closest to?”. To start this process we need some notion of exemplar point for each cluster to measure distance to. This is tricky since our clusters may have odd shapes. In practice there isn’t really any single clear exemplar for a cluster. The right solution, then, is to have a set of exemplar points for each cluster? How do we determine which points those should be? They should be the points that persist in the the cluster (and it’s children in the HDBSCAN condensed tree) for the longest range of lambda values – such points represent the “heart” of the cluster around which the ultimate cluster forms.

In practice we want to be careful and get the most persistent points in each leaf cluster beneath the cluster we are

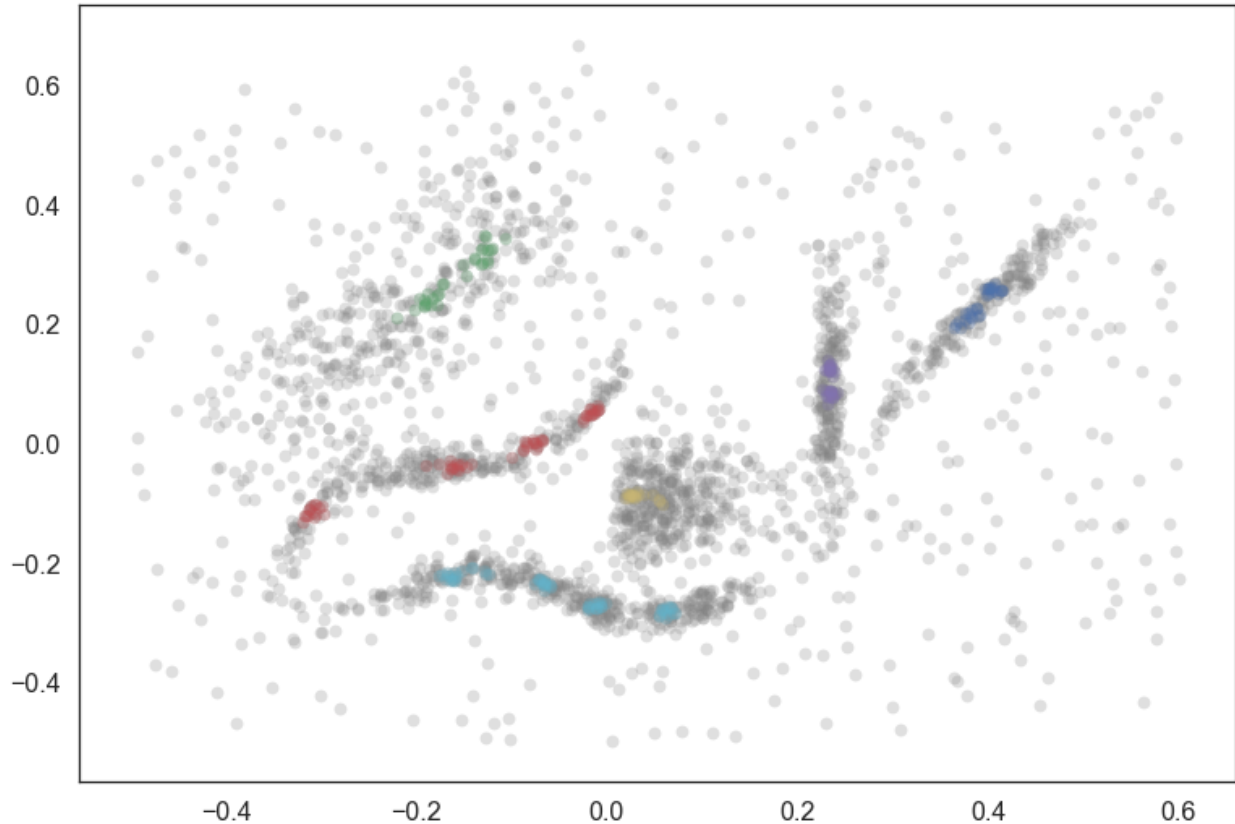
considering. This is because as a oddly shaped cluster breaks down it will split into subclusters. We don't want simply the most persistent of those subclusters, but rather representatives of each subcluster.

We can write this as a simple function to generate exemplar points. We work through the condensed tree, get the leaf clusters beneath a given cluster, and then find the points with maximum lambda value in that leaf. If we combine all those points together we get “exemplars”.

```
def exemplars(cluster_id, condensed_tree):
    raw_tree = condensed_tree._raw_tree
    # Just the cluster elements of the tree, excluding singleton points
    cluster_tree = raw_tree[raw_tree['child_size'] > 1]
    # Get the leaf cluster nodes under the cluster we are considering
    leaves = hdbscan.plots._recurse_leaf_dfs(cluster_tree, cluster_id)
    # Now collect up the last remaining points of each leaf cluster (the heart of the
    ↪leaf)
    result = np.array([])
    for leaf in leaves:
        max_lambda = raw_tree['lambda_val'][raw_tree['parent'] == leaf].max()
        points = raw_tree['child'][(raw_tree['parent'] == leaf) &
                                   (raw_tree['lambda_val'] == max_lambda)]
        result = np.hstack((result, points))
    return result.astype(np.int)
```

We can plot the exemplars so you can get a sense of what points are being pulled out as exemplars for each cluster. First we plot all the data in gray, and then plot the exemplars for each cluster over the top, following the coloring used in the plot of the clusters above.

```
tree = clusterer.condensed_tree_
plt.scatter(data.T[0], data.T[1], c='grey', **plot_kwds)
for i, c in enumerate(tree._select_clusters()):
    c_exemplars = exemplars(c, tree)
    plt.scatter(data.T[0][c_exemplars], data.T[1][c_exemplars], c=palette[i], **plot_
    ↪kwds)
```



You can see the several leaves in action here, with the red and cyan clusters having several subclusters stretched along their length.

Now to compute a cluster membership score for a point we need to simply compute the distance to each of the cluster exemplar sets and scale membership scores accordingly. In practice we work with the inverse distance (just as HDBSCAN handles things with lambda values in the tree). Whether we do a softmax or simply normalize by dividing by the sum is “to be determined” as there isn’t necessarily a clear answer. We’ll leave it as an option in the code.

```
def min_dist_to_exemplar(point, cluster_exemplars, data):
    dists = cdist([data[point]], data[cluster_exemplars.astype(np.int32)])
    return dists.min()

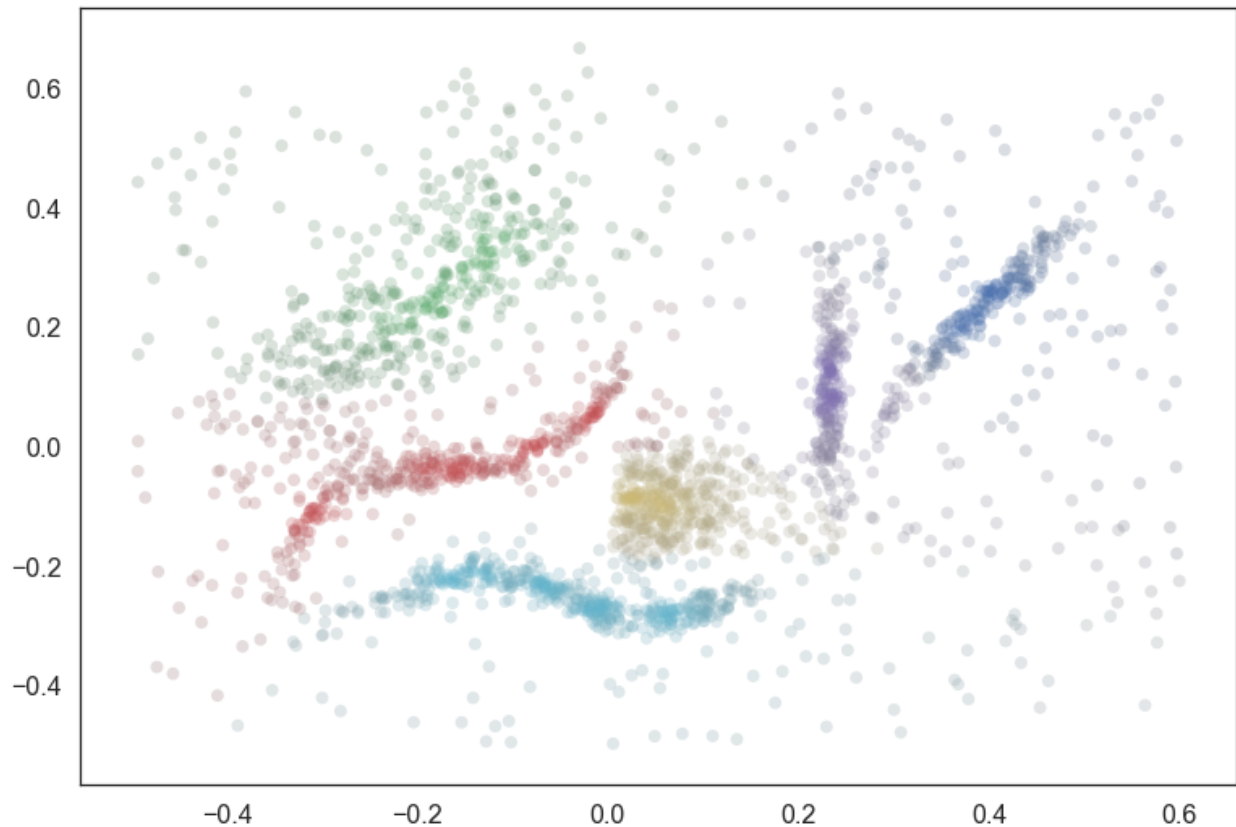
def dist_vector(point, exemplar_dict, data):
    result = {}
    for cluster in exemplar_dict:
        result[cluster] = min_dist_to_exemplar(point, exemplar_dict[cluster], data)
    return np.array(list(result.values()))

def dist_membership_vector(point, exemplar_dict, data, softmax=False):
    if softmax:
        result = np.exp(1./dist_vector(point, exemplar_dict, data))
        result[~np.isfinite(result)] = np.finfo(np.double).max
    else:
        result = 1./dist_vector(point, exemplar_dict, data)
        result[~np.isfinite(result)] = np.finfo(np.double).max
    result /= result.sum()
    return result
```

We can get some sense of what this is doing by assigning every point to a cluster via the membership vector, and

desaturating according to the strength of membership.

```
exemplar_dict = {c:exemplars(c,tree) for c in tree._select_clusters()}
colors = np.empty((data.shape[0], 3))
for x in range(data.shape[0]):
    membership_vector = dist_membership_vector(x, exemplar_dict, data)
    color = np.argmax(membership_vector)
    saturation = membership_vector[color]
    colors[x] = sns.desaturate(pal[color], saturation)
plt.scatter(data.T[0], data.T[1], c=colors, **plot_kwds);
```



As you can see this is something that is a step in the right direction, but we are not following the manifold well. For example there is spill over between the cyan and yellow clusters, the red and yellow clusters, the red and green clusters, and the purple and blue clusters in a way that is not really ideal. This is because we are using pure distance (rather than any sort of cluster/manifold/density aware distance) and latching on to whatever is closest. What we need is an approach that understands the cluster structure better – something based off the the actual structure (and lambda values therein) of the condensed tree. This is exactly the sort of approach something based on outlier scores can provide.

Outlier Based Membership

We want a notion of membership that follows the density based notions upon which the clustering is actually built. This is actually not too hard to arrange via a modification of the GLOSH algorithm for providing outlier scores. In that algorithm, given a point, we find the closest cluster in the condensed tree and then compare how long the point stayed in that cluster to the total persistence of the heart of the cluster. If we modify this to instead find the merge height of the point with a fixed cluster and then perform the same comparison of the points membership persistence with the maximum persistence of the cluster we can get a measure of how much of an outlier the point is *relative to the fixed cluster*. If we perform this calculation for each of the clusters we can get a vector of outlier scores. We can

then normalize that (again, whether by softmax, or simply divide by the sum) to get a cluster membership vector.

To start we'll need some utility functions. These are far from the most efficient way to do this (in terms of compute time) but they demonstrate what is going on more clearly.

```
def max_lambda_val(cluster, tree):
    cluster_tree = tree[tree['child_size'] > 1]
    leaves = hdbscan.plots._recurse_leaf_dfs(cluster_tree, cluster)
    max_lambda = 0.0
    for leaf in leaves:
        max_lambda = max(max_lambda,
                        tree['lambda_val'][tree['parent'] == leaf].max())
    return max_lambda

def points_in_cluster(cluster, tree):
    leaves = hdbscan.plots._recurse_leaf_dfs(tree, cluster)
    return leaves
```

Next we'll need a function to find the merge height. We'll presume we've used the above functions to precompute a dict of points for every cluster in our cluster tree.

```
def merge_height(point, cluster, tree, point_dict):
    cluster_row = tree[tree['child'] == cluster]
    cluster_height = cluster_row['lambda_val'][0]
    if point in point_dict[cluster]:
        merge_row = tree[tree['child'] == float(point)][0]
        return merge_row['lambda_val']
    else:
        while point not in point_dict[cluster]:
            parent_row = tree[tree['child'] == cluster]
            cluster = parent_row['parent'].astype(np.float64)[0]
        for row in tree[tree['parent'] == cluster]:
            child_cluster = float(row['child'])
            if child_cluster == point:
                return row['lambda_val']
            if child_cluster in point_dict and point in point_dict[child_cluster]:
                return row['lambda_val']
```

Now we can create a scoring function, providing an outlier score relative to each cluster. Now we'll assume we have a precomputed dict of maximum lambda values for each cluster, and a precomputed list of cluster_ids.

```
def per_cluster_scores(point, cluster_ids, tree, max_lambda_dict, point_dict):
    result = {}
    point_row = tree[tree['child'] == point]
    point_cluster = float(point_row[0]['parent'])
    max_lambda = max_lambda_dict[point_cluster] + 1e-8 # avoid zero lambda vals in_
    ↪odd cases

    for c in cluster_ids:
        height = merge_height(point, c, tree, point_dict)
        result[c] = (max_lambda / (max_lambda - height))
    return result
```

Finally we can write our function to provide an outlier based membership vector, leaving an option for using softmax instead of straightforward normalization.

```
def outlier_membership_vector(point, cluster_ids, tree,
                             max_lambda_dict, point_dict, softmax=True):
    if softmax:
```

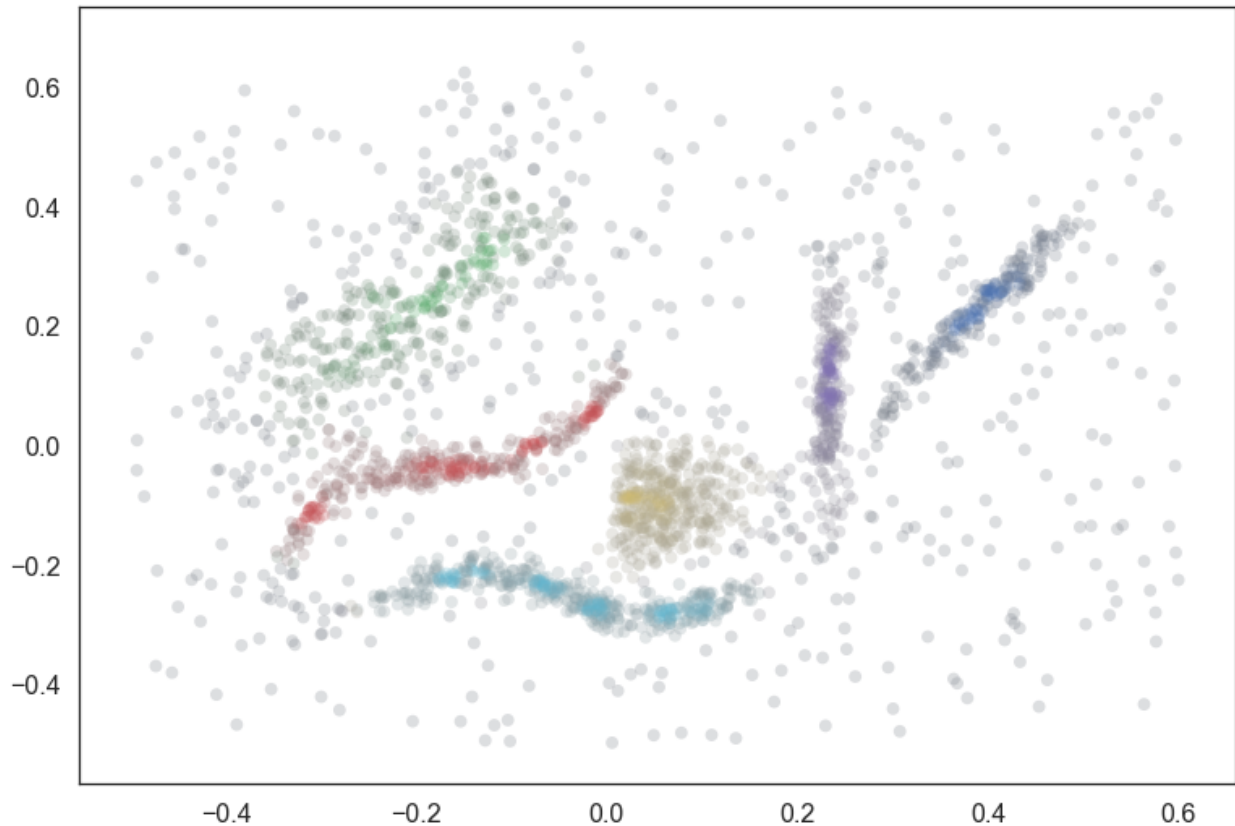
```
result = np.exp(np.array(list(per_cluster_scores(point,
                                                cluster_ids,
                                                tree,
                                                max_lambda_dict,
                                                point_dict
                                                ).values()))
result[~np.isfinite(result)] = np.finfo(np.double).max
else:
    result = np.array(list(per_cluster_scores(point,
                                                cluster_ids,
                                                tree,
                                                max_lambda_dict,
                                                point_dict
                                                ).values()))

result /= result.sum()
return result
```

We can apply the same approach as before to get a general notion of what this approach has done for us, coloring points by the most likely cluster and then desaturating according to the actual membership strength.

```
cluster_ids = tree._select_clusters()
raw_tree = tree._raw_tree
all_possible_clusters = np.arange(data.shape[0], raw_tree['parent'].max() + 1).
    ↳astype(np.float64)
max_lambda_dict = {c:max_lambda_val(c, raw_tree) for c in all_possible_clusters}
point_dict = {c:set(points_in_cluster(c, raw_tree)) for c in all_possible_clusters}
colors = np.empty((data.shape[0], 3))
for x in range(data.shape[0]):
    membership_vector = outlier_membership_vector(x, cluster_ids, raw_tree,
                                                max_lambda_dict, point_dict, False)

    color = np.argmax(membership_vector)
    saturation = membership_vector[color]
    colors[x] = sns.desaturate(pal[color], saturation)
plt.scatter(data.T[0], data.T[1], c=colors, **plot_kwds);
```



We see that we follow the clusters much better with this approach, but now everything is somewhat desaturated, and there are many points, even points quite close to one cluster (and far from others) that are pure gray. Thus while we follow the clusters well we've lost a certain amount of locality information since at certain distance scales many points join/leave a cluster at the same time, so they all get the same relative score across clusters. The ideal would be to combine the two sets of information that we have – the cluster oriented and the locality oriented. That is the middle way which we will pursue.

The Middle Way

We need a way to combine these two approaches. The first point to note is that we can view the resulting membership vectors as probability mass functions for the probability that the point is a member of each cluster. Given two observations of PMFs the natural approach is simply to combine them via Bayes' to get a new posterior distribution. This is easy enough to arrange.

```
def combined_membership_vector(point, data, tree, exemplar_dict, cluster_ids,
                              max_lambda_dict, point_dict, softmax=False):
    raw_tree = tree._raw_tree
    dist_vec = dist_membership_vector(point, exemplar_dict, data, softmax)
    outl_vec = outlier_membership_vector(point, cluster_ids, raw_tree,
                                         max_lambda_dict, point_dict, softmax)

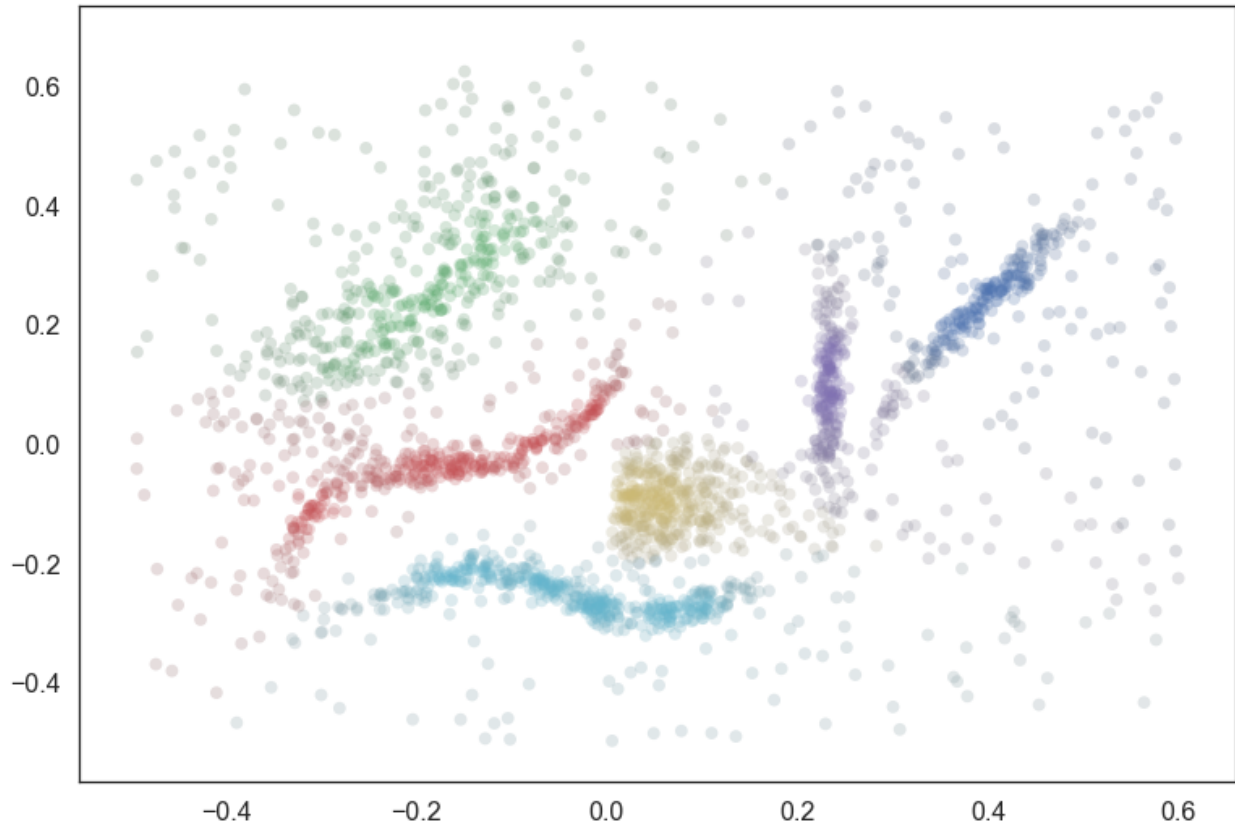
    result = dist_vec * outl_vec
    result /= result.sum()
    return result
```

Again we can have some manner of window on the results by plotting points colored and desaturated according to the most likely cluster and the probability that the point is “in” that cluster.

```

colors = np.empty((data.shape[0], 3))
for x in range(data.shape[0]):
    membership_vector = combined_membership_vector(x, data, tree, exemplar_dict,
    ↳ cluster_ids,
    max_lambda_dict, point_dict, False)
    color = np.argmax(membership_vector)
    saturation = membership_vector[color]
    colors[x] = sns.desaturate(pal[color], saturation)
plt.scatter(data.T[0], data.T[1], c=colors, **plot_kwds);

```



This looks a lot closer to what we had in mind – We have cluster membership following manifolds, and noise points near clusters taking on some shades of the appropriate hue. Our one remaining problem is related to the noise points – they are unlikely to be in any cluster, not merely a smear across the probabilities of being in any particular cluster.

Converting a Conditional Probability

What we have computed so far is a probability vector that a point is in each cluster conditional on the point being in a cluster (since the sum of the vector is one, implying that, with probability one the point is in some cluster). We wish to convert this to a vector of probabilities with no such conditional. We can convert the conditional to the joint probability easily

$$P(x \in C_i | \exists j : x \in C_j) \cdot P(\exists j : x \in C_j) = P(x \in C_i, \exists j : x \in C_j)$$

But then we just note that

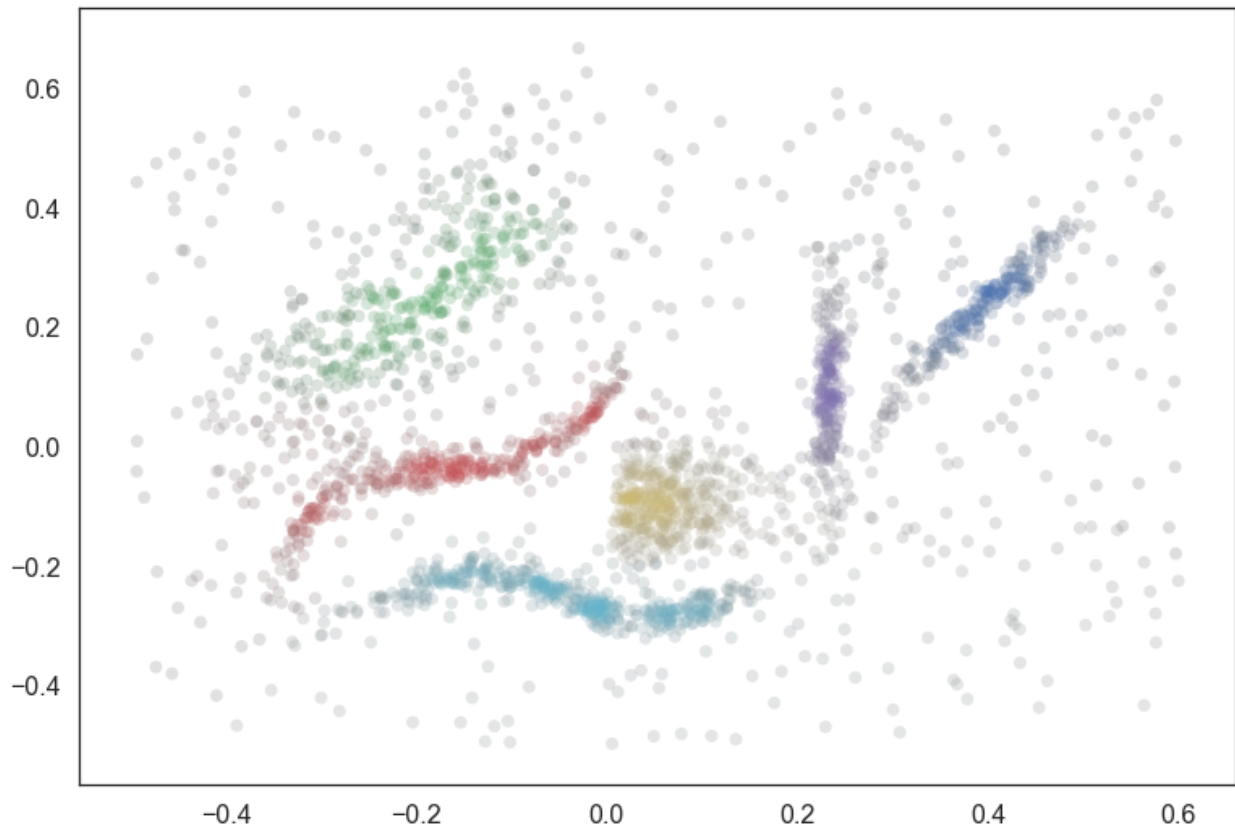
$$P(x \in C_i, \exists j : x \in C_j) = P(x \in C_i)$$

since $P(\exists j : x \in C_j) = 1$ whenever $x \in C_i$. We then only need to estimate $P(\exists j : x \in C_j)$, and we can do that by simply comparing the merge height to the nearest cluster with the maximum lambda of that cluster.

```
def prob_in_some_cluster(point, tree, cluster_ids, point_dict, max_lambda_dict):
    heights = []
    for cluster in cluster_ids:
        heights.append(merge_height(point, cluster, tree._raw_tree, point_dict))
    height = max(heights)
    nearest_cluster = cluster_ids[np.argmax(heights)]
    max_lambda = max_lambda_dict[nearest_cluster]
    return height / max_lambda
```

The result is that we merely need to multiply our combined membership vector to get a vector of probabilities of being in a cluster. We can visualize the results again.

```
colors = np.empty((data.shape[0], 3))
for x in range(data.shape[0]):
    membership_vector = combined_membership_vector(x, data, tree, exemplar_dict,
    cluster_ids,
    max_lambda_dict, point_dict, False)
    membership_vector *= prob_in_some_cluster(x, tree, cluster_ids, point_dict, max_
    lambda_dict)
    color = np.argmax(membership_vector)
    saturation = membership_vector[color]
    colors[x] = sns.desaturate(pal[color], saturation)
plt.scatter(data.T[0], data.T[1], c=colors, **plot_kws);
```



And there we have the result!

API Reference

Major classes are `HDBSCAN` and `RobustSingleLinkage`.

HDBSCAN

```
class hdbscan.hdbscan_.HDBSCAN(min_cluster_size=5, min_samples=None, metric='euclidean',
                                alpha=1.0, p=None, algorithm='best', leaf_size=40, mem-
                                ory=Memory(cachedir=None), approx_min_span_tree=True,
                                gen_min_span_tree=False, core_dist_n_jobs=4, clus-
                                ter_selection_method='eom', allow_single_cluster=False, pre-
                                diction_data=False, match_reference_implementation=False,
                                **kwargs)
```

Perform HDBSCAN clustering from vector array or distance matrix.

HDBSCAN - Hierarchical Density-Based Spatial Clustering of Applications with Noise. Performs DBSCAN over varying epsilon values and integrates the result to find a clustering that gives the best stability over epsilon. This allows HDBSCAN to find clusters of varying densities (unlike DBSCAN), and be more robust to parameter selection.

min_cluster_size [int, optional (default=5)] The minimum size of clusters; single linkage splits that contain fewer points than this will be considered points “falling out” of a cluster rather than a cluster splitting into two new clusters.

min_samples [int, optional (default=None)] The number of samples in a neighbourhood for a point to be considered a core point.

metric [string, or callable, optional (default='euclidean')] The metric to use when calculating distance between instances in a feature array. If metric is a string or callable, it must be one of the options allowed by `metrics.pairwise.pairwise_distances` for its metric parameter. If metric is “precomputed”, X is assumed to be a distance matrix and must be square.

p [int, optional (default=None)] p value to use if using the minkowski metric.

alpha [float, optional (default=1.0)] A distance scaling parameter as used in robust single linkage. See³ for more information.

algorithm [string, optional (default='best')] Exactly which algorithm to use; hdbscan has variants specialised for different characteristics of the data. By default this is set to `best` which chooses the “best” algorithm given the nature of the data. You can force other options if you believe you know better. Options are:

- `best`
- `generic`
- `prims_kdtree`
- `prims_balltree`
- `boruvka_kdtree`
- `boruvka_balltree`

leaf_size: int, optional (default=40) If using a space tree algorithm (kdtree, or balltree) the number of points in a leaf node of the tree. This does not alter the resulting clustering, but may have an effect on the runtime of the algorithm.

memory [Instance of `joblib.Memory` or string (optional)] Used to cache the output of the computation of the tree. By default, no caching is done. If a string is given, it is the path to the caching directory.

approx_min_span_tree [bool, optional (default=True)] Whether to accept an only approximate minimum spanning tree. For some algorithms this can provide a significant speedup, but the resulting clustering may be of marginally lower quality. If you are willing to sacrifice speed for correctness you may want to explore this; in general this should be left at the default `True`.

gen_min_span_tree: bool, optional (default=False) Whether to generate the minimum spanning tree with regard to mutual reachability distance for later analysis.

core_dist_n_jobs [int, optional (default=4)] Number of parallel jobs to run in core distance computations (if supported by the specific algorithm). For `core_dist_n_jobs` below -1, (`n_cpus + 1 + core_dist_n_jobs`) are used.

cluster_selection_method [string, optional (default='eom')] The method used to select clusters from the condensed tree. The standard approach for HDBSCAN* is to use an Excess of Mass algorithm to find the most persistent clusters. Alternatively you can instead select the clusters at the leaves of the tree – this provides the most fine grained and homogeneous clusters. Options are:

- `eom`
- `leaf`

allow_single_cluster [bool, optional (default=False)] By default HDBSCAN* will not produce a single cluster, setting this to `True` will override this and allow single cluster results in the case that you feel this is a valid result for your dataset.

prediction_data [boolean, optional] Whether to generate extra cached data for predicting labels or membership vectors for new unseen points later. If you wish to persist the clustering object for later re-use you probably want to set this to `True`. (default `False`)

match_reference_implementation [bool, optional (default=False)] There exist some interpretational differences between this HDBSCAN* implementation and the original authors reference implementation in Java. This can result in very minor differences in clustering results. Setting this flag to `True` will, at some performance cost, ensure that the clustering results match the reference implementation.

****kwargs** [optional] Arguments passed to the distance metric

³ Chaudhuri, K., & Dasgupta, S. (2010). Rates of convergence for the cluster tree. In *Advances in Neural Information Processing Systems* (pp. 343-351).

labels_ [ndarray, shape (n_samples,)] Cluster labels for each point in the dataset given to fit(). Noisy samples are given the label -1.

probabilities_ [ndarray, shape (n_samples,)] The strength with which each sample is a member of its assigned cluster. Noise points have probability zero; points in clusters have values assigned proportional to the degree that they persist as part of the cluster.

cluster_persistence_ [ndarray, shape (n_clusters,)] A score of how persistent each cluster is. A score of 1.0 represents a perfectly stable cluster that persists over all distance scales, while a score of 0.0 represents a perfectly ephemeral cluster. These scores can be gauge the relative coherence of the clusters output by the algorithm.

condensed_tree_ [CondensedTree object] The condensed tree produced by HDBSCAN. The object has methods for converting to pandas, networkx, and plotting.

single_linkage_tree_ [SingleLinkageTree object] The single linkage tree produced by HDBSCAN. The object has methods for converting to pandas, networkx, and plotting.

minimum_spanning_tree_ [MinimumSpanningTree object] The minimum spanning tree of the mutual reachability graph generated by HDBSCAN. Note that this is not generated by default and will only be available if `gen_min_span_tree` was set to True on object creation. Even then in some optimized cases a tree may not be generated.

outlier_scores_ [ndarray, shape (n_samples,)] Outlier scores for clustered points; the larger the score the more outlier-like the point. Useful as an outlier detection technique. Based on the GLOSH algorithm by Campello, Moulavi, Zimek and Sander.

prediction_data_ [PredictionData object] Cached data used for predicting the cluster labels of new or unseen points. Necessary only if you are using functions from `hdbscan.prediction` (see `approximate_predict()`, `membership_vector()`, and `all_points_membership_vectors()`).

exemplars_ [list] A list of exemplar points for clusters. Since HDBSCAN supports arbitrary shapes for clusters we cannot provide a single cluster exemplar per cluster. Instead a list is returned with each element of the list being a numpy array of exemplar points for a cluster – these points are the “most representative” points of the cluster.

fit (X, y=None)

Perform HDBSCAN clustering from features or distance matrix.

X [array or sparse (CSR) matrix of shape (n_samples, n_features), or array of shape (n_samples, n_samples)] A feature array, or array of distances between samples if `metric='precomputed'`.

self [object] Returns self

fit_predict (X, y=None)

Performs clustering on X and returns cluster labels.

X [array or sparse (CSR) matrix of shape (n_samples, n_features), or array of shape (n_samples, n_samples)] A feature array, or array of distances between samples if `metric='precomputed'`.

y [ndarray, shape (n_samples,)] cluster labels

generate_prediction_data ()

Create data that caches intermediate results used for predicting the label of new/unseen points. This data is only useful if you are intending to use functions from `hdbscan.prediction`.

RobustSingleLinkage

```
class hdbscan.robust_single_linkage_.RobustSingleLinkage (cut=0.4,      k=5,      al-  
                                                         pha=1.4142135623730951,  
                                                         gamma=5,      met-  
                                                         ric='euclidean',      al-  
                                                         gorithm='best',  
                                                         core_dist_n_jobs=4,  
                                                         **kwargs)
```

Perform robust single linkage clustering from a vector array or distance matrix.

Robust single linkage is a modified version of single linkage that attempts to be more robust to noise. Specifically the goal is to more accurately approximate the level set tree of the unknown probability density function from which the sample data has been drawn.

X [array or sparse (CSR) matrix of shape (n_samples, n_features), or \]

array of shape (n_samples, n_samples)

A feature array, or array of distances between samples if `metric='precomputed'`.

cut [float] The reachability distance value to cut the cluster heirarchy at to derive a flat cluster labelling.

k [int, optional (default=5)] Reachability distances will be computed with regard to the *k* nearest neighbors.

alpha [float, optional (default=np.sqrt(2))] Distance scaling for reachability distance computation. Reachability distance is computed as $\max \{ \text{core_k}(a), \text{core_k}(b), 1/\alpha d(a,b) \}$.

gamma [int, optional (default=5)] Ignore any clusters in the flat clustering with size less than gamma, and declare points in such clusters as noise points.

metric [string, or callable, optional (default='euclidean')] The metric to use when calculating distance between instances in a feature array. If metric is a string or callable, it must be one of the options allowed by `metrics.pairwise.pairwise_distances` for its metric parameter. If metric is “precomputed”, X is assumed to be a distance matrix and must be square.

algorithm [string, optional (default='best')] Exactly which algorithm to use; hdbscan has variants specialised for different characteristics of the data. By default this is set to `best` which chooses the “best” algorithm given the nature of the data. You can force other options if you believe you know better. Options are:

- `small`
- `small_kdtree`
- `large_kdtree`
- `large_kdtree_fastcluster`

core_dist_n_jobs [int, optional] Number of parallel jobs to run in core distance computations (if supported by the specific algorithm). For `core_dist_n_jobs` below -1, (`n_cpus + 1 + core_dist_n_jobs`) are used. (default 4)

labels_ [ndarray, shape (n_samples,)] Cluster labels for each point. Noisy samples are given the label -1.

cluster_hierarchy_ [SingleLinkageTree object] The single linkage tree produced during clustering. This object provides several methods for:

- Plotting
- Generating a flat clustering
- Exporting to NetworkX
- Exporting to Pandas

fit (*X*, *y=None*)

Perform robust single linkage clustering from features or distance matrix.

X [array or sparse (CSR) matrix of shape (n_samples, n_features), or array of shape (n_samples, n_samples)] A feature array, or array of distances between samples if *metric*='precomputed'.

self [object] Returns self

fit_predict (*X*, *y=None*)

Performs clustering on *X* and returns cluster labels.

X [array or sparse (CSR) matrix of shape (n_samples, n_features), or array of shape (n_samples, n_samples)] A feature array, or array of distances between samples if *metric*='precomputed'.

y [ndarray, shape (n_samples,)] cluster labels

Utilities

Other useful classes are contained in the plots module, the validity module, and the prediction module.

class `hdbscan.plots.CondensedTree` (*condensed_tree_array*, *cluster_selection_method*='eom')

The condensed tree structure, which provides a simplified or smoothed version of the [SingleLinkageTree](#).

condensed_tree_array [numpy recarray from HDBSCAN] The raw numpy rec array version of the condensed tree as produced internally by hdbscan.

cluster_selection_method [string, optional (default 'eom')] The method of selecting clusters. One of 'eom' or 'leaf'

get_plot_data (*leaf_separation*=1, *log_size*=False, *max_rectangle_per_icle*=20)

Generates data for use in plotting the 'icle plot' or dendrogram plot of the condensed tree generated by HDBSCAN.

leaf_separation [float, optional] How far apart to space the final leaves of the dendrogram. (default 1)

log_size [boolean, optional] Use log scale for the 'size' of clusters (i.e. number of points in the cluster at a given lambda value). (default False)

max_rectangles_per_icle [int, optional] To simplify the plot this method will only emit *max_rectangles_per_icle* bars per branch of the dendrogram. This ensures that we don't suffer from massive overplotting in cases with a lot of data points.

plot_data [dict]

Data associated to bars in a bar plot: *bar_centers* x coordinate centers for bars *bar_tops* heights of bars in lambda scale *bar_bottoms* y coordinate of bottoms of bars *bar_widths* widths of the bars (in x coord scale) *bar_bounds* a 4-tuple of [left, right, bottom, top]

giving the bounds on a full set of cluster bars

Data associates with cluster splits: *line_xs* x coordinates for horizontal dendrogram lines *line_ys* y coordinates for horizontal dendrogram lines

plot (*leaf_separation*=1, *cmap*='viridis', *select_clusters*=False, *label_clusters*=False, *selection_palette*=None, *axis*=None, *colorbar*=True, *log_size*=False, *max_rectangles_per_icle*=20)
Use matplotlib to plot an 'icle plot' dendrogram of the condensed tree.

Effectively this is a dendrogram where the width of each cluster bar is equal to the number of points (or log of the number of points) in the cluster at the given lambda value. Thus bars narrow as points progressively

drop out of clusters. To make the effect more apparent the bars are also colored according to the number of points (or log of the number of points).

leaf_separation [float, optional (default 1)] How far apart to space the final leaves of the dendrogram.

cmap [string or matplotlib colormap, optional (default viridis)] The matplotlib colormap to use to color the cluster bars.

select_clusters [boolean, optional (default False)] Whether to draw ovals highlighting which cluster bar represent the clusters that were selected by HDBSCAN as the final clusters.

label_clusters [boolean, optional (default False)] If select_clusters is True then this determines whether to draw text labels on the clusters.

selection_palette [list of colors, optional (default None)] If not None, and at least as long as the number of clusters, draw ovals in colors iterating through this palette. This can aid in cluster identification when plotting.

axis [matplotlib axis or None, optional (default None)] The matplotlib axis to render to. If None then a new axis will be generated. The rendered axis will be returned.

colorbar [boolean, optional (default True)] Whether to draw a matplotlib colorbar displaying the range of cluster sizes as per the colormap.

log_size [boolean, optional (default False)] Use log scale for the 'size' of clusters (i.e. number of points in the cluster at a given lambda value).

max_rectangles_per_icicle [int, optional (default 20)]

To simplify the plot this method will only emit `max_rectangles_per_icicle` bars per branch of the dendrogram. This ensures that we don't suffer from massive overplotting in cases with a lot of data points.

Returns

axis [matplotlib axis] The axis on which the 'icicle plot' has been rendered.

to_networkx()

Return a NetworkX DiGraph object representing the condensed tree.

Edge weights in the graph are the lambda values at which child nodes 'leave' the parent cluster.

Nodes have a *size* attribute attached giving the number of points that are in the cluster (or 1 if it is a singleton point) at the point of cluster creation (fewer points may be in the cluster at larger lambda values).

to_numpy()

Return a numpy structured array representation of the condensed tree.

to_pandas()

Return a pandas dataframe representation of the condensed tree.

Each row of the dataframe corresponds to an edge in the tree. The columns of the dataframe are *parent*, *child*, *lambda_val* and *child_size*.

The *parent* and *child* are the ids of the parent and child nodes in the tree. Node ids less than the number of points in the original dataset represent individual points, while ids greater than the number of points are clusters.

The *lambda_val* value is the value (1/distance) at which the *child* node leaves the cluster.

The *child_size* is the number of points in the *child* node.

class hdbscan.plots.**SingleLinkageTree** (*linkage*)

A single linkage format dendrogram tree, with plotting functionality and networkX support.

linkage [ndarray (n_samples, 4)] The numpy array that holds the tree structure. As output by `scipy.cluster.hierarchy`, `hdbscan`, or `fastcluster`.

get_clusters (*cut_distance*, *min_cluster_size*=5)

Return a flat clustering from the single linkage hierarchy.

This represents the result of selecting a cut value for robust single linkage clustering. The *min_cluster_size* allows the flat clustering to declare noise points (and cluster smaller than *min_cluster_size*).

cut_distance [float] The mutual reachability distance cut value to use to generate a flat clustering.

min_cluster_size [int, optional] Clusters smaller than this value will be called ‘noise’ and remain unclustered in the resulting flat clustering.

labels [array [n_samples]] An array of cluster labels, one per datapoint. Unclustered points are assigned the label -1.

plot (*axis*=None, *truncate_mode*=None, *p*=0, *vary_line_width*=True, *cmap*=‘viridis’, *colorbar*=True)

Plot a dendrogram of the single linkage tree.

truncate_mode [str, optional] The dendrogram can be hard to read when the original observation matrix from which the linkage is derived is large. Truncation is used to condense the dendrogram. There are several modes:

None / ‘none’ No truncation is performed (Default).

‘**lastp**’ The last *p* non-singleton formed in the linkage are the only non-leaf nodes in the linkage; they correspond to rows `Z[n-p-2:end]` in `Z`. All other non-singleton clusters are contracted into leaf nodes.

‘**level**’ / ‘**mtica**’ No more than *p* levels of the dendrogram tree are displayed. This corresponds to Mathematica(TM) behavior.

p [int, optional] The *p* parameter for *truncate_mode*.

vary_line_width [boolean, optional] Draw downward branches of the dendrogram with line thickness that varies depending on the size of the cluster.

cmap [string or matplotlib colormap, optional] The matplotlib colormap to use to color the cluster bars. A value of ‘none’ will result in black bars. (default ‘viridis’)

colorbar [boolean, optional] Whether to draw a matplotlib colorbar displaying the range of cluster sizes as per the colormap. (default True)

axis [matplotlib axis] The axis on which the dendrogram plot has been rendered.

to_networkx ()

Return a NetworkX DiGraph object representing the single linkage tree.

Edge weights in the graph are the distance values at which child nodes merge to form the parent cluster.

Nodes have a *size* attribute attached giving the number of points that are in the cluster.

to_numpy ()

Return a numpy array representation of the single linkage tree.

This representation conforms to the `scipy.cluster.hierarchy` notion of a single linkage tree, and can be used with all the associated scipy tools. Please see the scipy documentation for more details on the format.

to_pandas ()

Return a pandas dataframe representation of the single linkage tree.

Each row of the dataframe corresponds to an edge in the tree. The columns of the dataframe are *parent*, *left_child*, *right_child*, *distance* and *size*.

The *parent*, *left_child* and *right_child* are the ids of the parent and child nodes in the tree. Node ids less than the number of points in the original dataset represent individual points, while ids greater than the number of points are clusters.

The *distance* value is the at which the child nodes merge to form the parent node.

The *size* is the number of points in the *parent* node.

class `hdbscan.plots.MinimumSpanningTree` (*mst*, *data*)

plot (*axis=None*, *node_size=40*, *node_color='k'*, *node_alpha=0.8*, *edge_alpha=0.5*,
edge_cmap='viridis_r', *edge_linewidth=2*, *vary_line_width=True*, *colorbar=True*)

Plot the minimum spanning tree (as projected into 2D by t-SNE if required).

axis [matplotlib axis, optional] The axis to render the plot to

node_size [int, optional] The size of nodes in the plot (default 40).

node_color [matplotlib color spec, optional] The color to render nodes (default black).

node_alpha [float, optional] The alpha value (between 0 and 1) to render nodes with (default 0.8).

edge_cmap [matplotlib colormap, optional]

The colormap to color edges by (varying color by edge weight/distance). Can be a cmap object or a string recognised by matplotlib. (default *viridis_r*)

edge_alpha [float, optional] The alpha value (between 0 and 1) to render edges with (default 0.5).

edge_linewidth [float, optional] The linewidth to use for rendering edges (default 2).

vary_line_width [bool, optional] Edge width is proportional to (log of) the inverse of the mutual reachability distance. (default True)

colorbar [bool, optional] Whether to draw a colorbar. (default True)

axis [matplotlib axis] The axis used the render the plot.

to_networkx ()

Return a NetworkX Graph object representing the minimum spanning tree.

Edge weights in the graph are the distance between the nodes they connect.

Nodes have a *data* attribute attached giving the data vector of the associated point.

to_numpy ()

Return a numpy array of weighted edges in the minimum spanning tree

to_pandas ()

Return a Pandas dataframe of the minimum spanning tree.

Each row is an edge in the tree; the columns are *from*, *to*, and *distance* giving the two vertices of the edge which are indices into the dataset, and the distance between those datapoints.

`hdbscan.validity.all_points_core_distance` (*distance_matrix*, *d=2.0*)

Compute the all-points-core-distance for all the points of a cluster.

distance_matrix [array (cluster_size, cluster_size)] The pairwise distance matrix between points in the cluster.

d [integer] The dimension of the data set, which is used in the computation of the all-point-core-distance as per the paper.

core_distances [array (cluster_size,)] The all-points-core-distance of each point in the cluster

Moulavi, D., Jaskowiak, P.A., Campello, R.J., Zimek, A. and Sander, J., 2014. Density-Based Clustering Validation. In SDM (pp. 839-847).

```
hdbscan.validity.all_points_mutual_reachability(X, labels, cluster_id, metric='euclidean', d=None,
**kwd_args)
```

Compute the all-points-mutual-reachability distances for all the points of a cluster.

If metric is 'precomputed' then assume X is a distance matrix for the full dataset. Note that in this case you must pass in 'd' the dimension of the dataset.

X [array (n_samples, n_features) or (n_samples, n_samples)] The input data of the clustering. This can be the data, or, if metric is set to *precomputed* the pairwise distance matrix used for the clustering.

labels [array (n_samples)] The label array output by the clustering, providing an integral cluster label to each data point, with -1 for noise points.

cluster_id [integer] The cluster label for which to compute the all-points mutual-reachability (which should be done on a cluster by cluster basis).

metric [string] The metric used to compute distances for the clustering (and to be re-used in computing distances for mr distance). If set to *precomputed* then X is assumed to be the precomputed distance matrix between samples.

d [integer (or None)] The number of features (dimension) of the dataset. This need only be set in the case of metric being set to *precomputed*, where the ambient dimension of the data is unknown to the function.

****kwd_args** : Extra arguments to pass to the distance computation for other metrics, such as minkowski, Mahalanobis etc.

mutual_reachability [array (n_samples, n_samples)] The pairwise mutual reachability distances between all points in X with *label* equal to *cluster_id*.

core_distances [array (n_samples,)] The all-points-core_distance of all points in X with *label* equal to *cluster_id*.

Moulavi, D., Jaskowiak, P.A., Campello, R.J., Zimek, A. and Sander, J., 2014. Density-Based Clustering Validation. In SDM (pp. 839-847).

```
hdbscan.validity.density_separation(X, labels, cluster_id1, cluster_id2, internal_nodes1, internal_nodes2, core_distances1, core_distances2, metric='euclidean', **kwd_args)
```

Compute the density separation between two clusters. This is the minimum all-points mutual reachability distance between pairs of points, one from internal nodes of MSTs of each cluster.

X [array (n_samples, n_features) or (n_samples, n_samples)] The input data of the clustering. This can be the data, or, if metric is set to *precomputed* the pairwise distance matrix used for the clustering.

labels [array (n_samples)] The label array output by the clustering, providing an integral cluster label to each data point, with -1 for noise points.

cluster_id1 [integer] The first cluster label to compute separation between.

cluster_id2 [integer] The second cluster label to compute separation between.

internal_nodes1 [array] The vertices of the MST for *cluster_id1* that were internal vertices.

internal_nodes2 [array] The vertices of the MST for *cluster_id2* that were internal vertices.

core_distances1 [array (size of cluster_id1,)] The all-points-core_distances of all points in the cluster specified by cluster_id1.

core_distances2 [array (size of cluster_id2,)] The all-points-core_distances of all points in the cluster specified by cluster_id2.

metric [string] The metric used to compute distances for the clustering (and to be re-used in computing distances for mr distance). If set to *precomputed* then X is assumed to be the precomputed distance matrix between samples.

****kwd_args** : Extra arguments to pass to the distance computation for other metrics, such as minkowski, Mahalanobis etc.

The ‘density separation’ between the clusters specified by *cluster_id1* and *cluster_id2*.

Moulavi, D., Jaskowiak, P.A., Campello, R.J., Zimek, A. and Sander, J., 2014. Density-Based Clustering Validation. In SDM (pp. 839-847).

`hdbscan.validity.internal_minimum_spanning_tree(mr_distances)`

Compute the ‘internal’ minimum spanning tree given a matrix of mutual reachability distances. Given a minimum spanning tree the ‘internal’ graph is the subgraph induced by vertices of degree greater than one.

mr_distances [array (cluster_size, cluster_size)] The pairwise mutual reachability distances, inferred to be the edge weights of a complete graph. Since MSTs are computed per cluster this is the all-points-mutual-reachability for points within a single cluster.

internal_nodes [array] An array listing the indices of the internal nodes of the MST

internal_edges [array (?, 3)] An array of internal edges in weighted edge list format; that is an edge is an array of length three listing the two vertices forming the edge and weight of the edge.

Moulavi, D., Jaskowiak, P.A., Campello, R.J., Zimek, A. and Sander, J., 2014. Density-Based Clustering Validation. In SDM (pp. 839-847).

`hdbscan.validity.validity_index(X, labels, metric='euclidean', d=None, per_cluster_scores=False, **kwd_args)`

Compute the density based cluster validity index for the clustering specified by *labels* and for each cluster in *labels*.

X [array (n_samples, n_features) or (n_samples, n_samples)] The input data of the clustering. This can be the data, or, if metric is set to *precomputed* the pairwise distance matrix used for the clustering.

labels [array (n_samples)] The label array output by the clustering, providing an integral cluster label to each data point, with -1 for noise points.

metric [optional, string (default ‘euclidean’)] The metric used to compute distances for the clustering (and to be re-used in computing distances for mr distance). If set to *precomputed* then X is assumed to be the precomputed distance matrix between samples.

d [optional, integer (or None) (default None)] The number of features (dimension) of the dataset. This need only be set in the case of metric being set to *precomputed*, where the ambient dimension of the data is unknown to the function.

per_cluster_scores [optional, boolean (default False)] Whether to return the validity index for individual clusters. Defaults to False with the function returning a single float value for the whole clustering.

****kwd_args** : Extra arguments to pass to the distance computation for other metrics, such as minkowski, Mahalanobis etc.

validity_index [float] The density based cluster validity index for the clustering. This is a numeric value between -1 and 1, with higher values indicating a ‘better’ clustering.

per_cluster_validity_index [array (n_clusters,)] The cluster validity index of each individual cluster as an array. The overall validity index is the weighted average of these values. Only returned if *per_cluster_scores* is set to True.

Moulavi, D., Jaskowiak, P.A., Campello, R.J., Zimek, A. and Sander, J., 2014. Density-Based Clustering Validation. In SDM (pp. 839-847).

class `hdbscan.prediction.PredictionData` (*data*, *condensed_tree*, *min_samples*,
tree_type='kdtree', *metric='euclidean'*, ***kwargs*)

Extra data that allows for faster prediction if cached.

data [array (n_samples, n_features)] The original data set that was clustered

condensed_tree [CondensedTree] The condensed tree object created by a clustering

min_samples [int] The min_samples value used in clustering

tree_type [string, optional] Which type of space tree to use for core distance computation. One of:

- `kdtree`
- `balltree`

metric [string, optional] The metric used to determine distance for the clustering. This is the metric that will be used for the space tree to determine core distances etc.

****kwargs** : Any further arguments to the metric.

raw_data [array (n_samples, n_features)] The original data set that was clustered

tree [KDTree or BallTree] A space partitioning tree that can be queried for nearest neighbors.

core_distances [array (n_samples,)] The core distances for every point in the original data set.

cluster_map [dict] A dictionary mapping cluster numbers in the condensed tree to labels in the final selected clustering.

cluster_tree [structured array] A version of the condensed tree that only contains clusters, not individual points.

max_lambdas [dict] A dictionary mapping cluster numbers in the condensed tree to the maximum lambda value seen in that cluster.

`hdbscan.prediction.all_points_membership_vectors` (*clusterer*)

Predict soft cluster membership vectors for all points in the original dataset the clusterer was trained on. This function is more efficient by making use of the fact that all points are already in the condensed tree, and processing in bulk.

clusterer [HDBSCAN]

A clustering object that has been fit to the data and

either had `prediction_data=True` set, or called the `generate_prediction_data` method after the fact. This method does not work if the clusterer was trained with `metric='precomputed'`.

membership_vectors [array (n_samples, n_clusters)] The probability that point *i* of the original dataset is a member of cluster *j* is in `membership_vectors[i, j]`.

`hdbscan.predict.predict()` `hdbscan.predict.all_points_membership_vectors()`

`hdbscan.prediction.approximate_predict` (*clusterer*, *points_to_predict*)

Predict the cluster label of new points. The returned labels will be those of the original clustering found by `clusterer`, and therefore are not (necessarily) the cluster labels that would be found by clustering the original data combined with `points_to_predict`, hence the ‘approximate’ label.

If you simply wish to assign new points to an existing clustering in the ‘best’ way possible, this is the function to use. If you want to predict how `points_to_predict` would cluster with the original data under HDBSCAN the most efficient existing approach is to simply recluster with the new point(s) added to the original dataset.

clusterer [HDBSCAN] A clustering object that has been fit to the data and either had `prediction_data=True` set, or called the `generate_prediction_data` method after the fact.

points_to_predict [array, or array-like (n_samples, n_features)] The new data points to predict cluster labels for. They should have the same dimensionality as the original dataset over which clusterer was fit.

labels [array (n_samples,)] The predicted labels of the `points_to_predict`

probabilities [array (n_samples,)] The soft cluster scores for each of the `points_to_predict`

```
hdbscan.predict.membership_vector()                                hdbscan.predict.  
all_points_membership_vectors()
```

`hdbscan.predict.membership_vector(clusterer, points_to_predict)`

Predict soft cluster membership. The result produces a vector for each point in `points_to_predict` that gives a probability that the given point is a member of a cluster for each of the selected clusters of the clusterer.

clusterer [HDBSCAN] A clustering object that has been fit to the data and either had `prediction_data=True` set, or called the `generate_prediction_data` method after the fact.

points_to_predict [array, or array-like (n_samples, n_features)] The new data points to predict cluster labels for. They should have the same dimensionality as the original dataset over which clusterer was fit.

membership_vectors [array (n_samples, n_clusters)] The probability that point `i` is a member of cluster `j` is in `membership_vectors[i, j]`.

```
hdbscan.predict.predict() hdbscan.predict.all_points_membership_vectors()
```

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