
Test Documentation

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Test

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E-Cell System is a software platform for modeling, simulation and analysis of complex, heterogeneous and multi-scale systems like the cell.

E-Cell4 is a free and open-source software licensed under the GNU General Public License version 2. The source code is available on [GitHub](#).

Please refer to <https://github.com/ecell/ecell4> for information about **installation instructions**.

1.1 Brief Tour of E-Cell4 Simulations

First of all, you have to load the E-Cell4 library:

```
[1]: %matplotlib inline
      from ecell4 import *
```

1.1.1 Quick Demo

There are three fundamental components consisting of E-Cell System version 4, which are `Model`, `World`, and `Simulator`. These components describe concepts in simulation.

- `Model` describes a problem to simulate as its name suggests.
- `World` describes a state, e.g. an initial state and a state at a time-point.
- `Simulator` describes a solver.

`Model` is independent from solvers. Every solver can share a single `Model` instance. Each solver algorithm has a corresponding pair of `World` and `Simulator` (these pairs are capsulized into `Factory` class). `World` is not necessarily needed to be bound to `Model` and `Simulator`, but `Simulator` needs both `Model` and `World`.

Before running a simulation, you have to make a `Model`. E-Cell4 supports multiple ways to build a `Model` (See **2. How to Build a Model** *local ipynb* [readthedocs](#)). Here, we explain the simplest way using the `with` statement with `reaction_rules`:

```
[2]: with reaction_rules():
      A + B > C | 0.01 # equivalent to create_binding_reaction_rule
      C > A + B | 0.3  # equivalent to create_unbinding_reaction_rule

m1 = get_model()
print(m1)

<ecell4.core.NetworkModel object at 0x000002C0F32444B0>
```

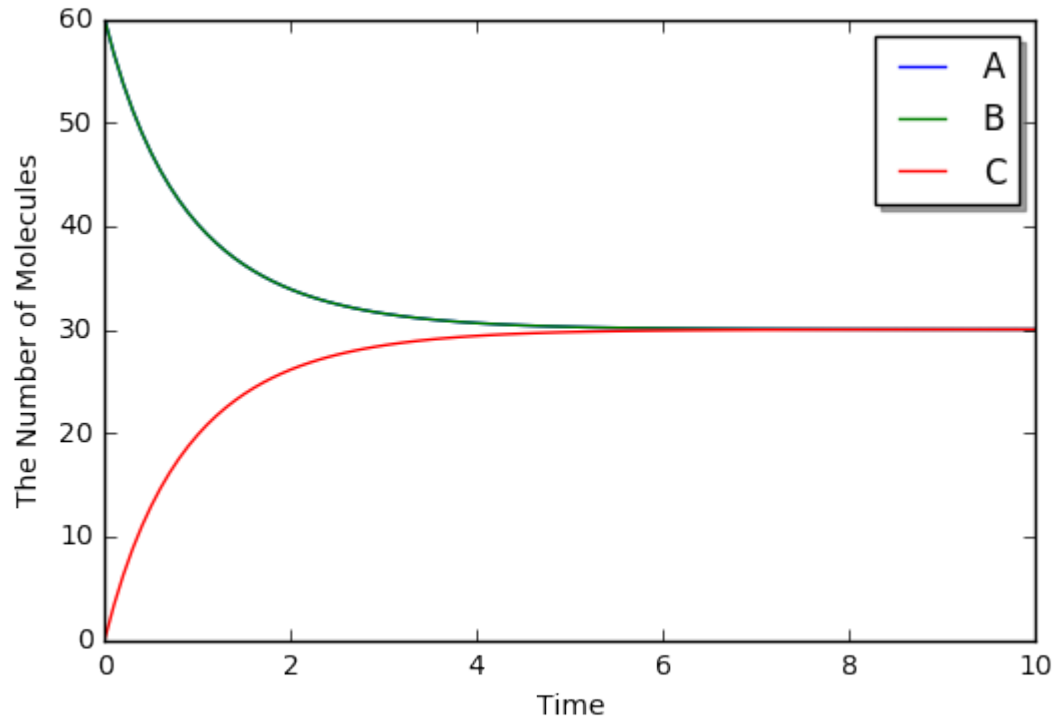
Please remember to write parentheses `()` after `reaction_rules`. Here, a `Model` with two `ReactionRules` named `m1` was built. Lines in the `with` block describe `ReactionRules`, a binding and unbinding reaction respectively. A kinetic rate for the mass action reaction is defined after a separator `|`, i.e. `0.01` or `0.3`. In the form of ordinary differential equations, this model can be described as:

$$[A]' = [B]' = -[C] = -0.01[A][B] + 0.3[C]$$

For more compact description, `A + B == C | (0.01, 0.3)` is also acceptable.

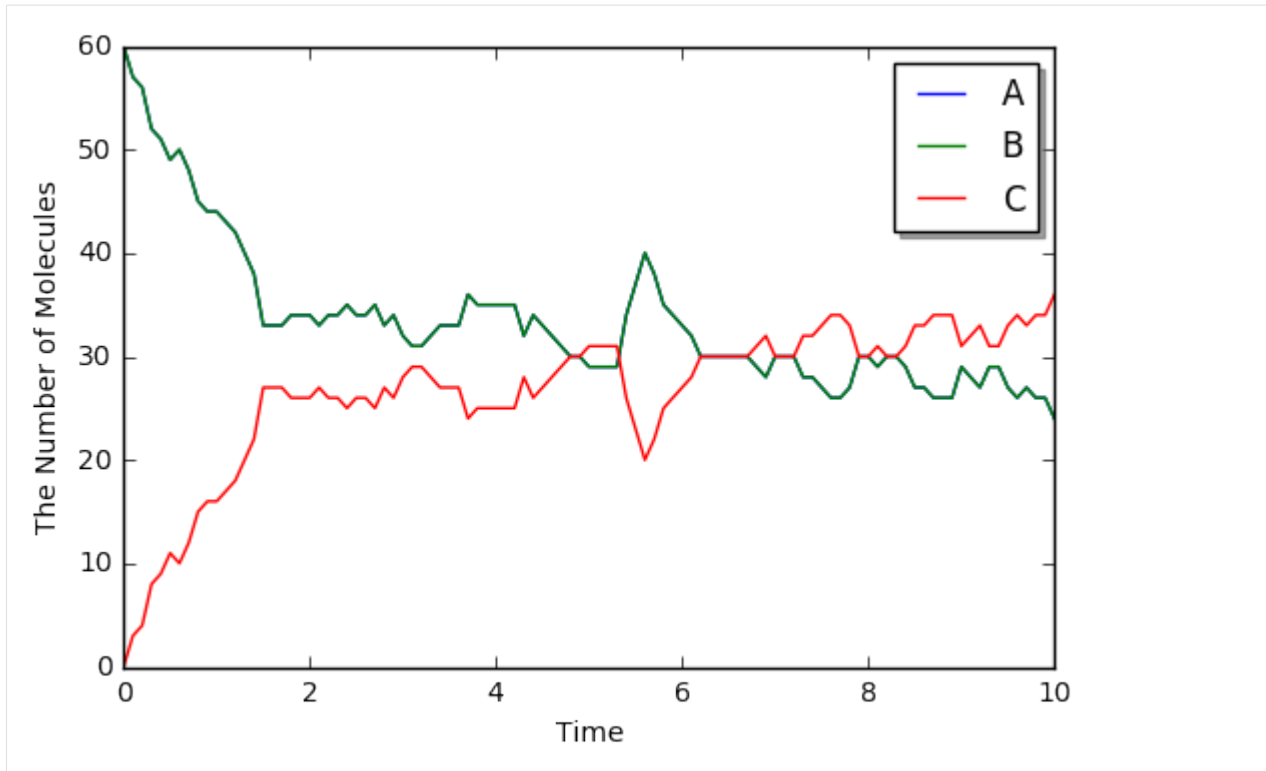
E-Cell4 has a simple interface for running simulation on a given model, called `run_simulation`. This enables for you to run simulations without instantiate `World` and `Simulator` by yourself. To solve this model, you have to give a volume, an initial value for each `Species` and duration of time:

```
[3]: run_simulation(10.0, model=m1, y0={'A': 60, 'B': 60}, volume=1.0)
```



To switch simulation algorithm, you only need to give the type of solver (`ode` is used as a default) as follows:

```
[4]: run_simulation(10.0, model=m1, y0={'A': 60, 'B': 60}, solver='gillespie')
```

1.1.2 1.2. Spatial Simulation and Visualization

E-Cell4 now supports multiple spatial simulation algorithms, `egfrd`, `spatiocyte` and `meso`. In addition to the model used in non-spatial solvers (`ode` and `gillespie`), these spatial solvers need extra information about each species, i.e. a diffusion coefficient and radius.

The `with` statement with `species_attributes` is available to describe these properties:

```
[5]: with species_attributes():
      A | B | C | {'radius': '0.005', 'D': '1'} # 'D' is for the diffusion coefficient

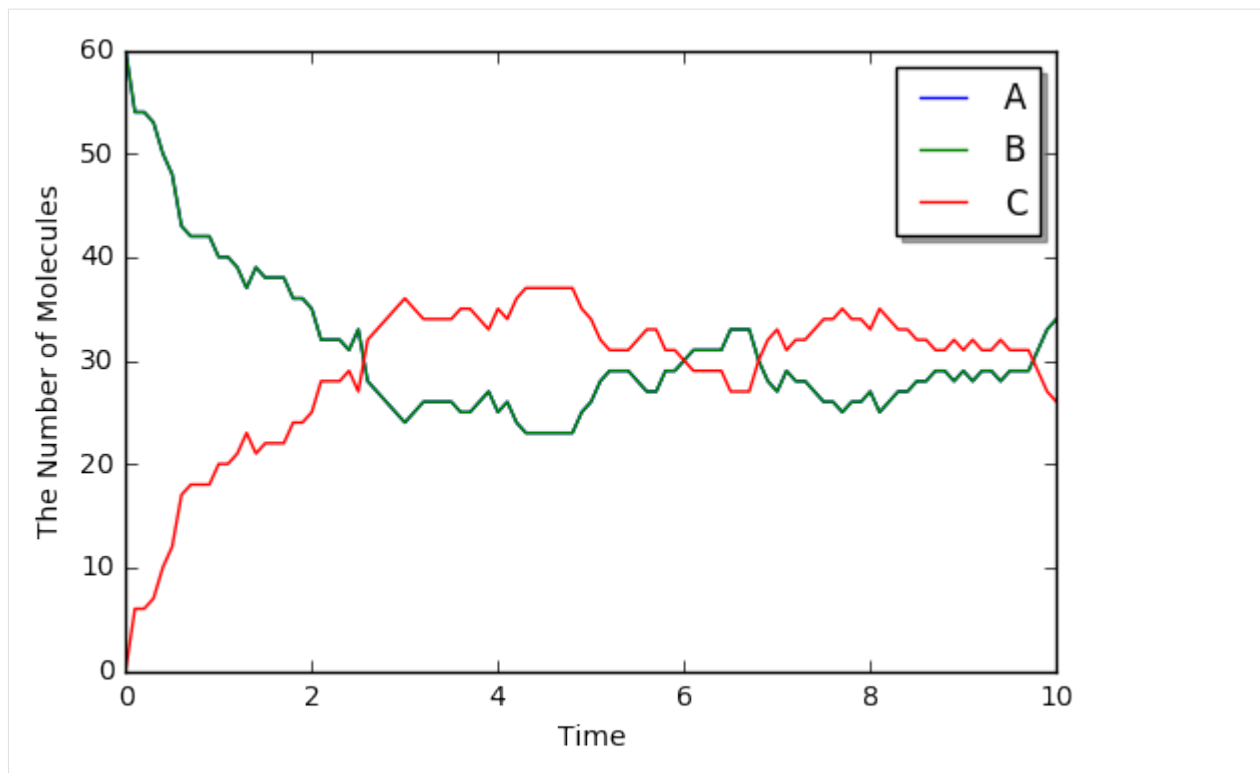
      with reaction_rules():
          A + B == C | (0.01, 0.3)

      m2 = get_model()
```

Even though the properties indicate a floating number, each attribute must be given as a string.

Now you can run a spatial simulation in the same way as above (in the case of `egfrd`, the time it takes to finish the simulation will be longer):

```
[6]: run_simulation(10.0, model=m2, y0={'A': 60, 'B': 60}, solver='meso')
```



Structure (e.g. membrane, cytoplasm and nucleus) is only supported by `spatiocyte` and `meso` for now. For the simulation, location that each species belongs to must be specified in its attribute.

```
[7]: with species_attributes():
      A | {'D': '1', 'location': 'S'} # 'S' is a name of the structure

m3 = get_model() # with no reactions
```

E-Cell4 supports primitive shapes as a structure like `Sphere`:

```
[8]: sphere = Sphere(Real3(0.5, 0.5, 0.5), 0.48) # a center position and radius
```

E-Cell4 provides various kinds of `Observers` which log the state during a simulation. In the following two observers are declared to record the position of the molecule. `FixedIntervalTrajectoryObserver` logs a trajectory of a molecule, and `FixedIntervalHDF5Observer` saves `World` to a HDF5 file at the given time interval:

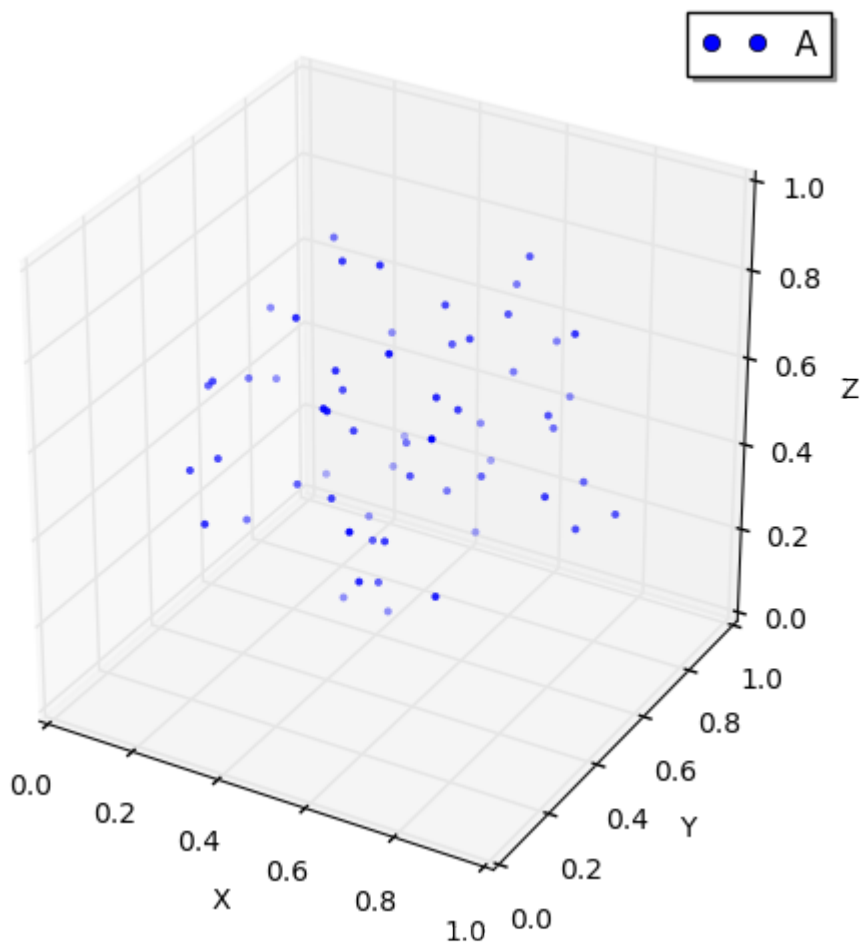
```
[9]: obs1 = FixedIntervalTrajectoryObserver(1e-3)
      obs2 = FixedIntervalHDF5Observer(0.1, 'test%02d.h5')
```

`run_simulation` can accept structures and observers as arguments `structure` and `observers` (see also `help(run_simulation)`):

```
[10]: run_simulation(1.0, model=m3, y0={'A': 60}, structures={'S': sphere},
                    solver='spatiocyte', observers=(obs1, obs2), return_type=None)
```

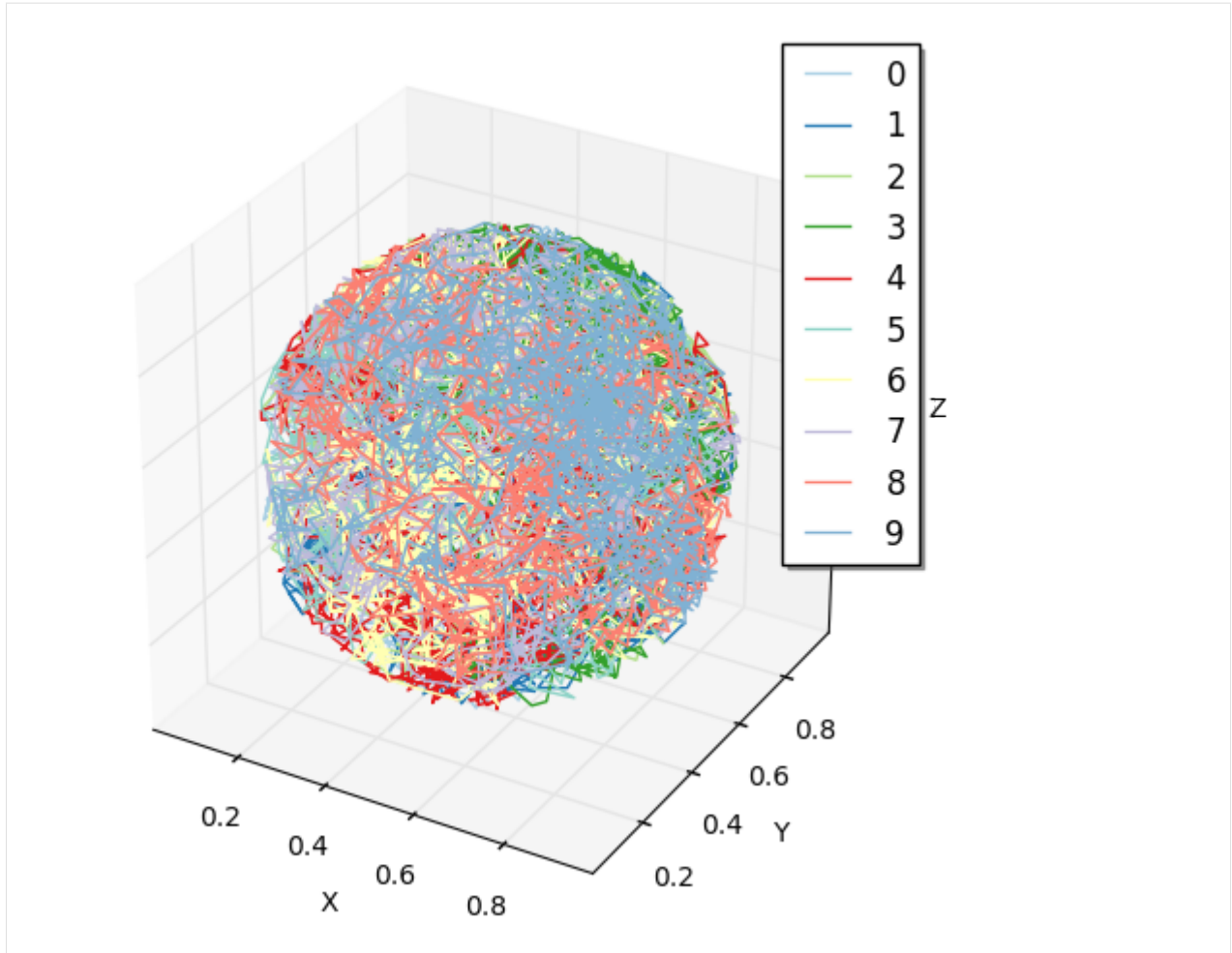
E-Cell4 has a function to visualize the world which is also capable of interactive visualization named `viz.plot_world`. `viz.plot_world` plots positions of molecules in 3D. In addition, by using `load_world`, you can easily restore the state of `World` from a HDF5 file:

```
[11]: # viz.plot_world(load_world('test00.h5'), species_list=['A'])  
viz.plot_world(load_world('test00.h5'), species_list=['A'], interactive=True)
```



Also, for `FixedIntervalTrajectoryObserver`, `viz.plot_trajectory` generates a plot of the trajectory. (Again, it is possible to generate interactive plots.):

```
[12]: # viz.plot_trajectory(obs1)  
viz.plot_trajectory(obs1, interactive=True)
```



For more details, see [5. How to Log and Visualize Simulations](#) [local](#) [ipynb](#) [readthedocs](#).

1.2 2. How to Build a Model

Model is composed of a set of `Species` and `ReactionRules`.

- `Species` describes a molecule entitie (e.g. a type or state of a protein) in the model. `Species` also has its attributes like the size.
- `ReactionRule` describes the interactions between `Species` (e.g. binding and unbinding).

```
[1]: %matplotlib inline
from eccl14 import *
```

1.2.1 2.1. Species

`Species` can be generated by giving its name:

```
[2]: sp1 = Species("A")
print(sp1.serial())
```

A

There are some naming conventions for the name of `Species`. This naming convention requires careful use of special symbols (e.g. parenthesis `()`, dot `.`, underbar `_`), numbers and blank.

`Species` has a set of APIs for handling its attributes:

```
[3]: sp1.set_attribute("radius", "0.005")
      sp1.set_attribute("D", "1")
      sp1.set_attribute("location", "cytoplasm")
      print(sp1.get_attribute("radius"))
      sp1.remove_attribute("radius")
      print(sp1.has_attribute("radius"))
```

```
0.005
False
```

The arguments in `set_attribute` is the name of attribute and its value. Both of them have to be string. There is a shortcut to set the attributes above at once because `radius`, `D` (a diffusion coefficient) and `location` are frequently used.

```
[4]: sp1 = Species("A", "0.005", "1", "cytoplasm") # serial, radius, D, location
```

The equality between `Species` is just evaluated based on their serial:

```
[5]: print(Species("A") == Species("B"), Species("A") == Species("A"))
```

```
False True
```

A `Species` consists of one or more `UnitSpecies`:

```
[6]: sp1 = Species()
      usp1 = UnitSpecies("C")
      print(usp1.serial())
      sp1.add_unit(usp1)
      sp1.add_unit(UnitSpecies("A"))
      sp1.add_unit(UnitSpecies("B"))
      print(sp1.serial(), len(sp1.units()))
```

```
C
C.A.B 3
```

A `Species` can be reproduced from a serial. In a serial, all `UnitSpecies` are joined with the separator, dot `.`. The order of `UnitSpecies` affects the `Species` comparison.

```
[7]: sp1 = Species("C.A.B")
      print(sp1.serial())
      print(Species("A.B.C") == Species("C.A.B"))
      print(Species("A.B.C") == Species("A.B.C"))
```

```
C.A.B
False
True
```

`UnitSpecies` can have sites. Sites consists of a name, state and bond, and are sorted automatically in `UnitSpecies`. name must be unique in a `UnitSpecies`. All the value have to be string. Do not include parenthesis, dot and blank, and not start from numbers except for bond.

```
[8]: uspl = UnitSpecies("A")
      uspl.add_site("us", "u", "")
      uspl.add_site("ps", "p", "_")
      uspl.add_site("bs", "", "_")
      print(uspl.serial())
```

```
A(bs^_,ps=p^_,us=u)
```

UnitSpecies can be also reproduced from its serial. Please be careful with the order of sites where a site with a state must be placed after sites with no state specification:

```
[9]: uspl = UnitSpecies()
      uspl.deserialize("A(bs^_, us=u, ps=p^_)")
      print(uspl.serial())
```

```
A(bs^_,ps=p^_,us=u)
```

Of course, a site of UnitSpecies is available even in Species' serial.

```
[10]: spl = Species("A(bs^1, ps=u).A(bs, ps=p^1)")
       print(spl.serial())
       print(len(spl.units()))
```

```
A(bs^1,ps=u).A(bs,ps=p^1)
2
```

The information (UnitSpecies and its site) is used for rule-based modeling. The way of rule-based modeling in E-Cell4 will be explained in **7. Introduction of Rule-based Modeling** [local ipynb](#) [readthedocs](#).

1.2.2 2.2. ReactionRule

ReactionRule consists of reactants, products and k. reactants and products are a list of Species, and k is a kinetic rate given as a floating number.

```
[11]: rr1 = ReactionRule()
      rr1.add_reactant(Species("A"))
      rr1.add_reactant(Species("B"))
      rr1.add_product(Species("C"))
      rr1.set_k(1.0)
```

Here is a binding reaction from A and B to C. In this reaction definition, you don't need to set attributes to Species. The above series of operations can be written in one line using `create_binding_reaction_rule(Species("A"), Species("B"), Species("C"), 1.0)`.

You can use `as_string` function to check ReactionRule:

```
[12]: rr1 = create_binding_reaction_rule(Species("A"), Species("B"), Species("C"), 1.0)
       print(rr1.as_string())
```

```
A+B>C|1
```

You can also provide components to the constructor:

```
[13]: rr1 = ReactionRule([Species("A"), Species("B")], [Species("C")], 1.0)
       print(rr1.as_string())
```

```
A+B>C|1
```

Basically `ReactionRule` represents a mass action reaction with the rate k . `ode` solver also supports rate laws though it's under development yet. `ode.ODERatelaw` is explained in **6. How to Solve ODEs with Rate Law Functions** [local ipynb](#) [readthedocs](#).

1.2.3 2.3. NetworkModel

You have learned how to create some `Model` components. Next let's put the components in a `Model`.

```
[14]: sp1 = Species("A", "0.005", "1")
      sp2 = Species("B", "0.005", "1")
      sp3 = Species("C", "0.01", "0.5")

[15]: rr1 = create_binding_reaction_rule(Species("A"), Species("B"), Species("C"), 0.01)
      rr2 = create_unbinding_reaction_rule(Species("C"), Species("A"), Species("B"), 0.3)
```

You can put the `Species` and `ReactionRule` with `add_species_attribute` and `add_reaction_rule`.

```
[16]: m1 = NetworkModel()
      m1.add_species_attribute(sp1)
      m1.add_species_attribute(sp2)
      m1.add_species_attribute(sp3)
      m1.add_reaction_rule(rr1)
      m1.add_reaction_rule(rr2)
```

Now we have a simple model with the binding and unbinding reactions. You can use `species_attributes` and `reaction_rules` to check the `Model`.

```
[17]: print([sp.serial() for sp in m1.species_attributes()])
      print([rr.as_string() for rr in m1.reaction_rules()])

['A', 'B', 'C']
['A+B>C|0.01', 'C>A+B|0.3']
```

The `Species` attributes are required for the spatial `Model`, but not required for the nonspatial `Model` (i.e. `gillespie` or `ode`). The attribute pushed first has higher priority than one pushed later. You can also attribute a `Species` based on the attributes in a `Model`.

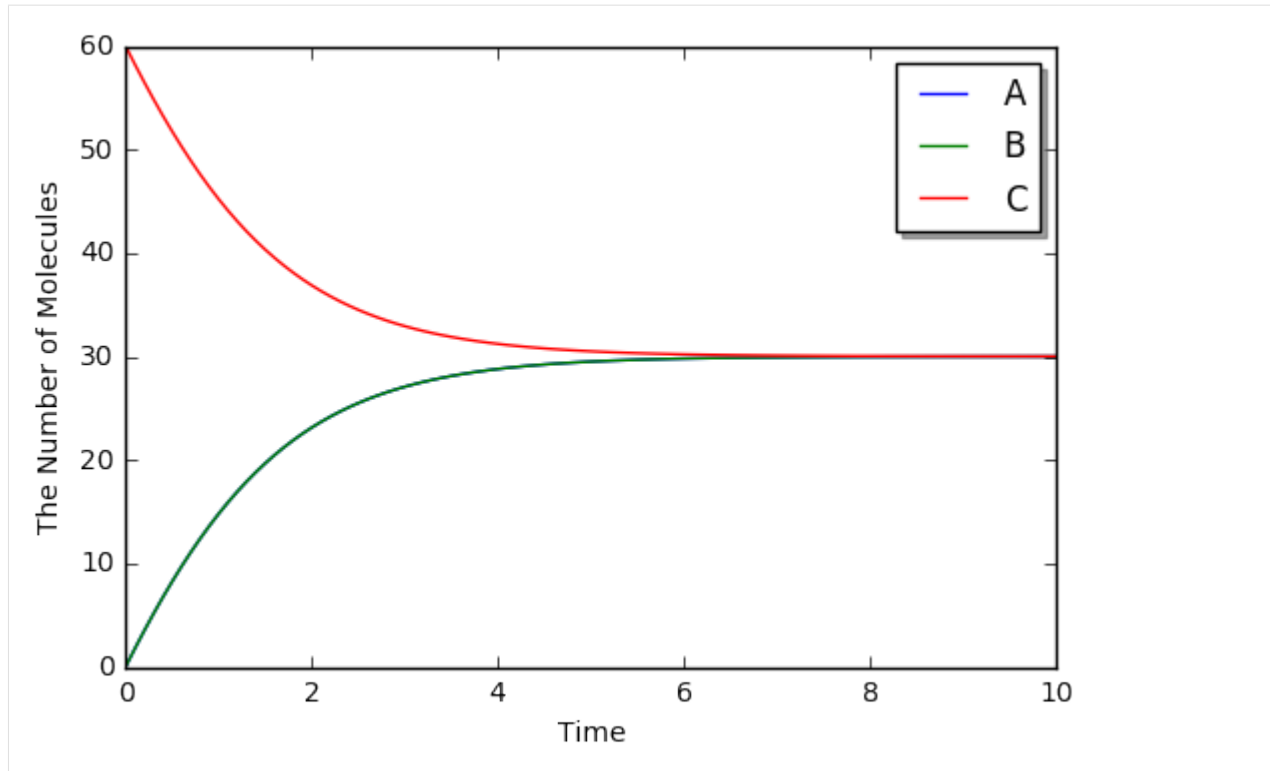
```
[18]: sp1 = Species("A")
      print(sp1.has_attribute("radius"))
      sp2 = m1.apply_species_attributes(sp1)
      print(sp2.has_attribute("radius"))
      print(sp2.get_attribute("radius"))

False
True
0.005
```

For your information, all functions related to `Species`, `ReactionRule` and `NetworkModel` above are also available on C++ in the same way.

Finally, you can solve this model with `run_simulation` as explained in **1. Brief Tour of E-Cell4 Simulations** [local ipynb](#) [readthedocs](#) :

```
[19]: run_simulation(10.0, model=m1, y0={'C': 60})
```



1.2.4 2.4. Python Utilities to Build a Model

As shown in **1. Brief Tour of E-Cell4 Simulations** [local ipynb](#) [readthedocs](#), E-Cell4 also provides the easier way to build a model using `with` statement:

```
[20]: with species_attributes():
      A | B | {'radius': '0.005', 'D': '1'}
      C | {'radius': '0.01', 'D': '0.5'}

      with reaction_rules():
          A + B == C | (0.01, 0.3)

      m1 = get_model()
```

For reversible reactions, `<>` is also available instead of `==` on Python 2, but deprecated on Python3. In the `with` statement, undeclared variables are automatically assumed to be a `Species`. Any Python variables, functions and statement are available even in the `with` block.

```
[21]: from math import log

      ka, kd, kf = 0.01, 0.3, 0.1
      tau = 10.0

      with reaction_rules():
          E0 + S == ES | (ka, kd)

          if tau > 0:
              ES > E1 + P | kf
              E1 > E0 | log(2) / tau
```

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```

else:
    ES > E0 + P | kf

m1 = get_model()
del ka, kd, kf, tau

```

Meanwhile, once some variable is declared even outside the block, you can not use its name as a `Species` as follows:

```

[22]: A = 10

try:
    with reaction_rules():
        A + B == C | (0.01, 0.3)
except Exception as e:
    print(repr(e))

del A

RuntimeError('invalid expression; "10" given',)

```

where $A + B == C$ exactly means $10 + B == C$.

In the absence of left or right hand side of `ReactionRule` like synthesis or degradation, you may want to describe like:

```

with reaction_rules():
    A > | 1.0 # XXX: will raise SyntaxError
    > A | 1.0 # XXX: will raise SyntaxError

```

However, this is not accepted because of `SyntaxError` on Python. To describe this case, a special operator, tilde `~`, is available. `~` sets a stoichiometric coefficient of the following `Species` as zero, which means the `Species` is just ignored in the `ReactionRule`.

```

[23]: with reaction_rules():
        ~A > A | 2.0 # equivalent to `create_synthesis_reaction_rule`
        A > ~A | 1.0 # equivalent to `create_degradation_reaction_rule`

m1 = get_model()
print([rr.as_string() for rr in m1.reaction_rules()])

['>A|2', '>A|1']

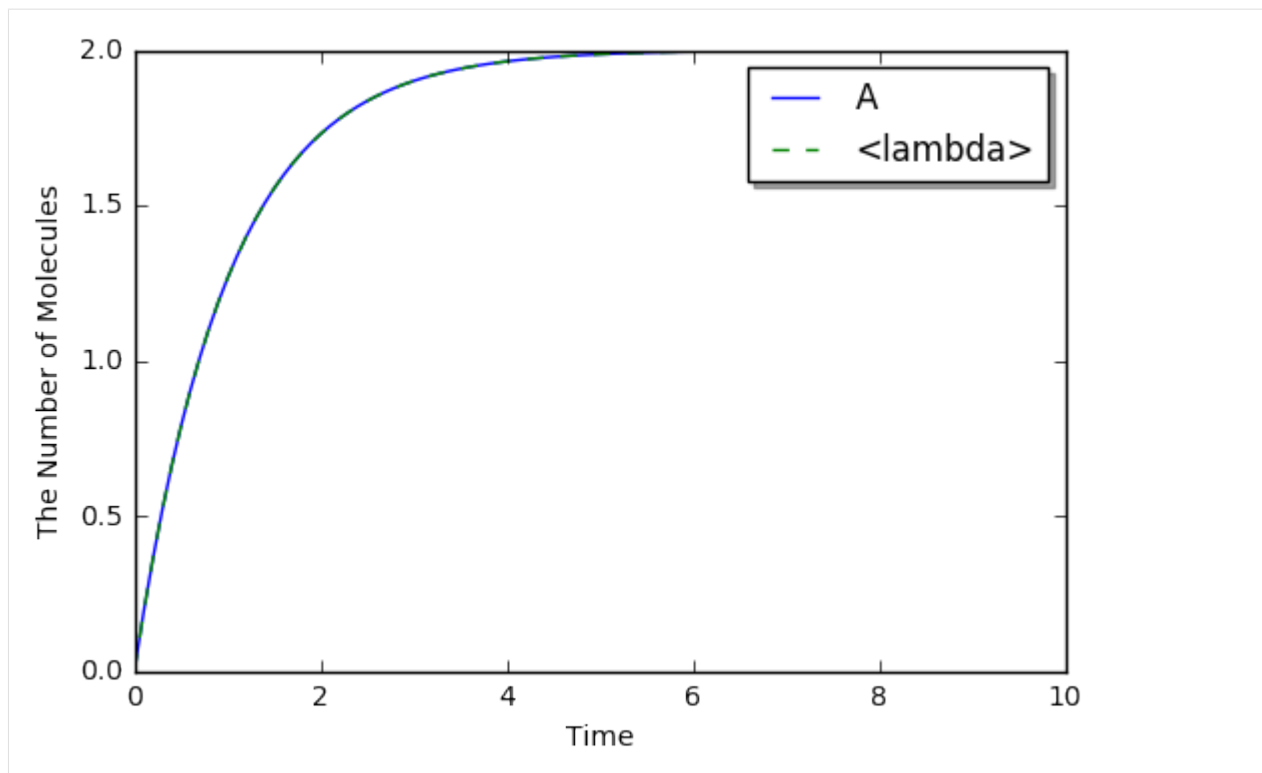
```

The following `Species`' name is not necessarily needed to be the same as others. The model above describes $[A]' = 2 - [A]$:

```

[24]: from math import exp
run_simulation(10.0, model=m1, opt_args=['-', lambda t: 2.0 * (1 - exp(-t)), '--'])

```



A chain of reactions can be described in one line. To split a line into two or more physical lines, wrap lines in a parenthesis:

```
[25]: with reaction_rules():
      (E + S == ES | (0.5, 1.0)
       > E + P | 1.5)

m1 = get_model()
print([rr.as_string() for rr in m1.reaction_rules()])

['E+S>ES|0.5', 'ES>E+S|1', 'ES>E+P|1.5']
```

The method uses global variables in `ecell4.util.decorator` (e.g. `REACTION_RULES`) to cache objects created in the `with` statement:

```
[26]: import ecell4.util.decorator

with reaction_rules():
    A + B == C | (0.01, 0.3)

print(ecell4.util.decorator.REACTION_RULES)  #XXX: Only for debugging
get_model()
print(ecell4.util.decorator.REACTION_RULES)  #XXX: Only for debugging

[<ecell4.core.ReactionRule object at 0x000001A123D02BA0>, <ecell4.core.ReactionRule_
↪object at 0x000001A123D02CD8>]
[]
```

Python decorator functions are also available. Decorator functions improve the modularity of the `Model`.

```
[27]: @species_attributes
def attrgen1(radius, D):
    A | B | {'radius': str(radius), 'D': str(D)}
    C | {'radius': str(radius * 2), 'D': str(D * 0.5)}

@reaction_rules
def rrgen1(kon, koff):
    A + B == C | (kon, koff)

attrs1 = attrgen1(0.005, 1)
rrs1 = rrgen1(0.01, 0.3)
print(attrs1)
print(rrs1)

[<ecell4.core.Species object at 0x000001A123D02CD8>, <ecell4.core.Species object at
→0x000001A123D02BA0>, <ecell4.core.Species object at 0x000001A123D02DC8>]
[<ecell4.core.ReactionRule object at 0x000001A123D02D20>, <ecell4.core.ReactionRule
→object at 0x000001A123D02DE0>]
```

In contrast to the `with` statement, do **not** add parentheses after the decorator here. The functions decorated by `reaction_rules` and `species_attributes` return a list of `ReactionRules` and `Species` respectively. The list can be registered to `Model` at once by using `add_reaction_rules` and `add_species_attributes`.

```
[28]: m1 = NetworkModel()
m1.add_species_attributes(attrs1)
m1.add_reaction_rules(rrs1)
print(m1.num_reaction_rules())

2
```

This method is modular and reusable relative to the way using `with` statement.

1.3 3. How to Setup the Initial Condition

Here, we explain the basics of `World` classes. In E-Cell4, six types of `World` classes are supported now: `spatiocyte.SpatocyteWorld`, `egfrd.EGFRDWorld`, `bd.BDWorld`, `meso.MesoscopicWorld`, `gillespie.GillespieWorld`, and `ode.ODEWorld`.

In the most of softwares, the initial condition is supposed to be a part of `Model`. But, in E-Cell4, the initial condition must be set up as `World` separately from `Model`. `World` stores an information about the state at a time point, such as a current time, the number of molecules, coordinate of molecules, structures, and random number generator. Meanwhile, `Model` contains the type of interactions between molecules and the common properties of molecules.

```
[1]: import ecell4
```

1.3.1 3.1. Common APIs of World

Even though `World` describes the spatial representation specific to the corresponding algorithm, it has compatible APIs. In this section, we introduce the common interfaces of the six `World` classes.

```
[2]: from ecell4.core import *
from ecell4.gillespie import GillespieWorld
from ecell4.ode import ODEWorld
from ecell4.spatocyte import SpatiocyteWorld
```

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```
from ecell4.bd import BDWorld
from ecell4.meso import MesoscopicWorld
from ecell4.egfrd import EGFRDWorld
```

World classes accept different sets of arguments in the constructor, which determine the parameters specific to the algorithm. However, at least, all World classes can be instantiated only with their size, named `edge_lengths`. The type of `edge_lengths` is `Real3`, which represents a triplet of `Reals`. In E-Cell4, all 3-dimensional positions are treated as a `Real3`. See also [8. More about 1. Brief Tour of E-Cell4 Simulations](#).

```
[3]: edge_lengths = Real3(1, 2, 3)
w1 = GillespieWorld(edge_lengths)
w2 = ODEWorld(edge_lengths)
w3 = SpatiocyteWorld(edge_lengths)
w4 = BDWorld(edge_lengths)
w5 = MesoscopicWorld(edge_lengths)
w6 = EGFRDWorld(edge_lengths)
```

World has getter methods for the size and volume.

```
[4]: print(tuple(w1.edge_lengths()), w1.volume())
print(tuple(w2.edge_lengths()), w2.volume())
print(tuple(w3.edge_lengths()), w3.volume())
print(tuple(w4.edge_lengths()), w4.volume())
print(tuple(w5.edge_lengths()), w5.volume())
print(tuple(w6.edge_lengths()), w6.volume())

((1.0, 2.0, 3.0), 6.0)
((1.0, 2.0, 3.0), 6.0)
((1.0, 2.0, 3.0), 6.0)
((1.0, 2.0, 3.0), 6.0)
((1.0, 2.0, 3.0), 6.0)
((1.0, 2.0, 3.0), 6.0)
```

Next, let's add molecules into the World. Here, you must give `Species` attributed with **radius** and **D** to tell the shape of molecules. In the example below **0.0025** corresponds to **radius** and **1** to **D**. Positions of the molecules are randomly determined in the World if needed. **10** in `add_molecules` function represents the number of molecules to be added.

```
[5]: sp1 = Species("A", "0.0025", "1")
w1.add_molecules(sp1, 10)
w2.add_molecules(sp1, 10)
w3.add_molecules(sp1, 10)
w4.add_molecules(sp1, 10)
w5.add_molecules(sp1, 10)
w6.add_molecules(sp1, 10)
```

After model is bound to world, you do not need to rewrite the **radius** and **D** once set in `Species` (unless you want to change it).

```
[6]: m = NetworkModel()
m.add_species_attribute(Species("A", "0.0025", "1"))
m.add_species_attribute(Species("B", "0.0025", "1"))

w1.bind_to(m)
w2.bind_to(m)
w3.bind_to(m)
w4.bind_to(m)
```

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```
w5.bind_to(m)
w6.bind_to(m)
w1.add_molecules(Species("B"), 20)
w2.add_molecules(Species("B"), 20)
w3.add_molecules(Species("B"), 20)
w4.add_molecules(Species("B"), 20)
w5.add_molecules(Species("B"), 20)
w6.add_molecules(Species("B"), 20)
```

Similarly, `remove_molecules` and `num_molecules_exact` are also available.

```
[7]: w1.remove_molecules(Species("B"), 5)
w2.remove_molecules(Species("B"), 5)
w3.remove_molecules(Species("B"), 5)
w4.remove_molecules(Species("B"), 5)
w5.remove_molecules(Species("B"), 5)
w6.remove_molecules(Species("B"), 5)

[8]: print(w1.num_molecules_exact(Species("A")), w2.num_molecules_exact(Species("A")), w3.
↳ num_molecules_exact(Species("A")), w4.num_molecules_exact(Species("A")), w5.num_
↳ molecules_exact(Species("A")), w6.num_molecules_exact(Species("A")))
print(w1.num_molecules_exact(Species("B")), w2.num_molecules_exact(Species("B")), w3.
↳ num_molecules_exact(Species("B")), w4.num_molecules_exact(Species("B")), w5.num_
↳ molecules_exact(Species("B")), w6.num_molecules_exact(Species("B")))

(10, 10, 10, 10, 10, 10)
(15, 15, 15, 15, 15, 15)
```

Unlike `num_molecules_exact`, `num_molecules` returns the numbers that match a given `Species` in rule-based fashion. When all `Species` in the `World` has no molecular interaction, `num_molecules` is same with `num_molecules_exact`.

```
[9]: print(w1.num_molecules(Species("A")), w2.num_molecules(Species("A")), w3.num_
↳ molecules(Species("A")), w4.num_molecules(Species("A")), w5.num_molecules(Species("A
↳ )), w6.num_molecules(Species("A")))
print(w1.num_molecules(Species("B")), w2.num_molecules(Species("B")), w3.num_
↳ molecules(Species("B")), w4.num_molecules(Species("B")), w5.num_molecules(Species("B
↳ )), w6.num_molecules(Species("B")))

(10, 10, 10, 10, 10, 10)
(15, 15, 15, 15, 15, 15)
```

`World` holds its simulation time.

```
[10]: print(w1.t(), w2.t(), w3.t(), w4.t(), w5.t(), w6.t())
w1.set_t(1.0)
w2.set_t(1.0)
w3.set_t(1.0)
w4.set_t(1.0)
w5.set_t(1.0)
w6.set_t(1.0)
print(w1.t(), w2.t(), w3.t(), w4.t(), w5.t(), w6.t())

(0.0, 0.0, 0.0, 0.0, 0.0, 0.0)
(1.0, 1.0, 1.0, 1.0, 1.0, 1.0)
```

Finally, you can save and load the state of a `World` into/from a HDF5 file.

```
[11]: w1.save("gillespie.h5")
w2.save("ode.h5")
w3.save("spatiocyte.h5")
w4.save("bd.h5")
w5.save("meso.h5")
w6.save("egfrd.h5")
del w1, w2, w3, w4, w5, w6
```

```
[12]: w1 = GillespieWorld()
w2 = ODEWorld()
w3 = SpatiocyteWorld()
w4 = BDWorld()
w5 = MesoscopicWorld()
w6 = EGFRDWorld()

print(w1.t(), tuple(w1.edge_lengths()), w1.volume(), w1.num_molecules(Species("A")),
↪w1.num_molecules(Species("B")))
print(w2.t(), tuple(w2.edge_lengths()), w2.volume(), w2.num_molecules(Species("A")),
↪w2.num_molecules(Species("B")))
print(w3.t(), tuple(w3.edge_lengths()), w3.volume(), w3.num_molecules(Species("A")),
↪w3.num_molecules(Species("B")))
print(w4.t(), tuple(w4.edge_lengths()), w4.volume(), w4.num_molecules(Species("A")),
↪w4.num_molecules(Species("B")))
print(w5.t(), tuple(w5.edge_lengths()), w5.volume(), w5.num_molecules(Species("A")),
↪w5.num_molecules(Species("B")))
print(w6.t(), tuple(w6.edge_lengths()), w6.volume(), w6.num_molecules(Species("A")),
↪w6.num_molecules(Species("B")))

(0.0, (1.0, 1.0, 1.0), 1.0, 0, 0)
(0.0, (1.0, 1.0, 1.0), 1.0, 0, 0)
(0.0, (1.0, 1.0, 1.0), 1.0, 0, 0)
(0.0, (1.0, 1.0, 1.0), 1.0, 0, 0)
(0.0, (1.0, 1.0, 1.0), 1.0, 0, 0)
(0.0, (1.0, 1.0, 1.0), 1.0, 0, 0)
```

```
[13]: w1.load("gillespie.h5")
w2.load("ode.h5")
w3.load("spatiocyte.h5")
w4.load("bd.h5")
w5.load("meso.h5")
w6.load("egfrd.h5")

print(w1.t(), tuple(w1.edge_lengths()), w1.volume(), w1.num_molecules(Species("A")),
↪w1.num_molecules(Species("B")))
print(w2.t(), tuple(w2.edge_lengths()), w2.volume(), w2.num_molecules(Species("A")),
↪w2.num_molecules(Species("B")))
print(w3.t(), tuple(w3.edge_lengths()), w3.volume(), w3.num_molecules(Species("A")),
↪w3.num_molecules(Species("B")))
print(w4.t(), tuple(w4.edge_lengths()), w4.volume(), w4.num_molecules(Species("A")),
↪w4.num_molecules(Species("B")))
print(w5.t(), tuple(w5.edge_lengths()), w5.volume(), w5.num_molecules(Species("A")),
↪w5.num_molecules(Species("B")))
print(w6.t(), tuple(w6.edge_lengths()), w6.volume(), w6.num_molecules(Species("A")),
↪w6.num_molecules(Species("B")))
del w1, w2, w3, w4, w5, w6

(1.0, (1.0, 2.0, 3.0), 6.0, 10, 15)
(1.0, (1.0, 2.0, 3.0), 6.0, 10, 15)
(1.0, (1.0, 2.0, 3.0), 6.0, 10, 15)
(1.0, (1.0, 2.0, 3.0), 6.0, 10, 15)
```

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```
(1.0, (1.0, 2.0, 3.0), 6.0, 10, 15)
(1.0, (1.0, 2.0, 3.0), 6.0, 10, 15)
```

All the World classes also accept a HDF5 file path as an unique argument of the constructor.

```
[14]: print(GillespieWorld("gillespie.h5").t())
      print(ODEWorld("ode.h5").t())
      print(SpatiocyteWorld("spatiocyte.h5").t())
      print(BDWorld("bd.h5").t())
      print(MesosopicWorld("meso.h5").t())
      print(EGFRDWorld("egfrd.h5").t())
```

```
1.0
1.0
1.0
1.0
1.0
1.0
```

1.3.2 3.2. How to Get Positions of Molecules

World also has the common functions to access the coordinates of the molecules.

```
[15]: w1 = GillespieWorld()
      w2 = ODEWorld()
      w3 = SpatiocyteWorld()
      w4 = BDWorld()
      w5 = MesoscopicWorld()
      w6 = EGFRDWorld()
```

First, you can place a molecule at the certain position with `new_particle`.

```
[16]: sp1 = Species("A", "0.0025", "1")
      pos = Real3(0.5, 0.5, 0.5)
      (pid1, p1), suc1 = w1.new_particle(sp1, pos)
      (pid2, p2), suc2 = w2.new_particle(sp1, pos)
      (pid3, p3), suc3 = w3.new_particle(sp1, pos)
      (pid4, p4), suc4 = w4.new_particle(sp1, pos)
      (pid5, p5), suc5 = w5.new_particle(sp1, pos)
      (pid6, p6), suc6 = w6.new_particle(sp1, pos)
```

`new_particle` returns a particle created and whether it's succeeded or not. The resolution in representation of molecules differs. For example, `GillespieWorld` has almost no information about the coordinate of molecules. Thus, it simply ignores the given position, and just counts up the number of molecules here.

`ParticleID` is a pair of Integers named `lot` and `serial`.

```
[17]: print(pid6.lot(), pid6.serial())
      print(pid6 == ParticleID((0, 1)))
```

```
(0, 1L)
True
```

Particle simulators, i.e. `spatiocyte`, `bd` and `egfrd`, provide an interface to access a particle by its id. `has_particle` returns if a particles exists or not for the given `ParticleID`.

```
[18]: # print(w1.has_particle(pid1))
      # print(w2.has_particle(pid2))
      print(w3.has_particle(pid3)) # => True
      print(w4.has_particle(pid4)) # => True
      # print(w5.has_particle(pid5))
      print(w6.has_particle(pid6)) # => True
```

```
True
True
True
```

After checking the existency, you can get the particle by `get_particle` as follows.

```
[19]: # pid1, p1 = w1.get_particle(pid1)
      # pid2, p2 = w2.get_particle(pid2)
      pid3, p3 = w3.get_particle(pid3)
      pid4, p4 = w4.get_particle(pid4)
      # pid5, p5 = w5.get_particle(pid5)
      pid6, p6 = w6.get_particle(pid6)
```

Particle consists of species, position, radius and D.

```
[20]: # print(p1.species().serial(), tuple(p1.position()), p1.radius(), p1.D())
      # print(p2.species().serial(), tuple(p2.position()), p2.radius(), p2.D())
      print(p3.species().serial(), tuple(p3.position()), p3.radius(), p3.D())
      print(p4.species().serial(), tuple(p4.position()), p4.radius(), p4.D())
      # print(p5.species().serial(), tuple(p5.position()), p5.radius(), p5.D())
      print(p6.species().serial(), tuple(p6.position()), p6.radius(), p6.D())
```

```
(u'A', (0.5062278801751902, 0.5080682368868706, 0.5), 0.0025, 1.0)
(u'A', (0.5, 0.5, 0.5), 0.0025, 1.0)
(u'A', (0.5, 0.5, 0.5), 0.0025, 1.0)
```

In the case of `spatiocyte`, a particle position is automatically round to the center of the voxel nearest to the given position.

You can even move the position of the particle. `update_particle` replace the particle specified with the given ParticleID with the given Particle and return False. If no corresponding particle is found, create new particle and return True. If you give a Particle with the different type of Species, the Species of the Particle will be also changed.

```
[21]: newp = Particle(sp1, Real3(0.3, 0.3, 0.3), 0.0025, 1)
      # print(w1.update_particle(pid1, newp))
      # print(w2.update_particle(pid2, newp))
      print(w3.update_particle(pid3, newp))
      print(w4.update_particle(pid4, newp))
      # print(w5.update_particle(pid5, newp))
      print(w6.update_particle(pid6, newp))
```

```
False
False
False
```

`list_particles` and `list_particles_exact` return a list of pairs of ParticleID and Particle in the World. World automatically makes up for the gap with random numbers. For example, `GillespieWorld` returns a list of positions randomly distributed in the World size.


```
[22]: print(w1.list_particles_exact(sp1))
      # print(w2.list_particles_exact(sp1))  # ODEWorld has no member named list_particles
      print(w3.list_particles_exact(sp1))
      print(w4.list_particles_exact(sp1))
      print(w5.list_particles_exact(sp1))
      print(w6.list_particles_exact(sp1))

[(<ecell14.core.ParticleID object at 0x7fdfd28e8b58>, <ecell14.core.Particle object at
→0x7fdfd28e8bd0>)]
[(<ecell14.core.ParticleID object at 0x7fdfd28e8b58>, <ecell14.core.Particle object at
→0x7fdfd28e8af8>)]
[(<ecell14.core.ParticleID object at 0x7fdfd28e8b58>, <ecell14.core.Particle object at
→0x7fdfd28e8a38>)]
[(<ecell14.core.ParticleID object at 0x7fdfd28e8b58>, <ecell14.core.Particle object at
→0x7fdfd28e8bd0>)]
[(<ecell14.core.ParticleID object at 0x7fdfd28e8b58>, <ecell14.core.Particle object at
→0x7fdfd28e8af8>)]
```

You can remove a specific particle with `remove_particle`.

```
[23]: # w1.remove_particle(pid1)
      # w2.remove_particle(pid2)
      w3.remove_particle(pid3)
      w4.remove_particle(pid4)
      # w5.remove_particle(pid5)
      w6.remove_particle(pid6)
      # print(w1.has_particle(pid1))
      # print(w2.has_particle(pid2))
      print(w3.has_particle(pid3))  # => False
      print(w4.has_particle(pid4))  # => False
      # print(w5.has_particle(pid5))
      print(w6.has_particle(pid6))  # => False

False
False
False
```

1.3.3 3.3. Lattice-based Coordinate

In addition to the common interface, each `World` can have their own interfaces. As an example, we explain methods to handle lattice-based coordinate here. `SpatiocyteWorld` is based on a space discretized to hexagonal close packing lattices, `LatticeSpace`.

```
[24]: w = SpatiocyteWorld(Real3(1, 2, 3), voxel_radius=0.01)
      w.bind_to(m)
```

The size of a single lattice, called `Voxel`, can be obtained by `voxel_radius()`. `SpatiocyteWorld` has methods to get the numbers of rows, columns, and layers. These sizes are automatically calculated based on the given `edge_lengths` at the construction.

```
[25]: print(w.voxel_radius())  # => 0.01
      print(tuple(w.shape()))  # => (62, 152, 116)
      # print(w.col_size(), w.row_size(), w.layer_size())  # => (62, 152, 116)
      print(w.size())  # => 1093184 = 62 * 152 * 116

0.01
(62, 152, 116)
```

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```
(62, 152, 116)
1093184
```

A position in the lattice-based space is treated as an `Integer3`, column, row and layer, called a global coordinate. Thus, `SpatiocyteWorld` provides the function to convert the `Real3` into a lattice-based coordinate.

```
[26]: # p1 = Real3(0.5, 0.5, 0.5)
# g1 = w.position2global(p1)
# p2 = w.global2position(g1)
# print(tuple(g1)) # => (31, 25, 29)
# print(tuple(p2)) # => (0.5062278801751902, 0.5080682368868706, 0.5)
```

```
(31, 25, 29)
(0.5062278801751902, 0.5080682368868706, 0.5)
```

In `SpatiocyteWorld`, the global coordinate is translated to a single integer. It is just called a coordinate. You can also treat the coordinate as in the same way with a global coordinate.

```
[27]: # p1 = Real3(0.5, 0.5, 0.5)
# c1 = w.position2coordinate(p1)
# p2 = w.coordinate2position(c1)
# g1 = w.coord2global(c1)
# print(c1) # => 278033
# print(tuple(p2)) # => (0.5062278801751902, 0.5080682368868706, 0.5)
# print(tuple(g1)) # => (31, 25, 29)
```

```
278033
(0.5062278801751902, 0.5080682368868706, 0.5)
(31, 25, 29)
```

With these coordinates, you can handle a `Voxel`, which represents a `Particle` object. Instead of `new_particle`, `new_voxel` provides the way to create a new `Voxel` with a coordinate.

```
[28]: c1 = w.position2coordinate(Real3(0.5, 0.5, 0.5))
((pid, v), is_succeeded) = w.new_voxel(Species("A"), c1)
print(pid, v, is_succeeded)
```

```
(<ecell14.core.ParticleID object at 0x7fd28e8a38>, <ecell14.core.Voxel object at_
↳0x7fd28e8c18>, True)
```

A `Voxel` consists of species, coordinate, radius and D.

```
[29]: print(v.species().serial(), v.coordinate(), v.radius(), v.D()) # => (u'A', 278033, 0.
↳0025, 1.0)
```

```
(u'A', 278033, 0.0025, 1.0)
```

Of course, you can get a voxel and list voxels with `get_voxel` and `list_voxels_exact` similar to `get_particle` and `list_particles_exact`.

```
[30]: print(w.num_voxels_exact(Species("A")))
print(w.list_voxels_exact(Species("A")))
print(w.get_voxel(pid))
```

```
1
[(<ecell14.core.ParticleID object at 0x7fd28e8ae0>, <ecell14.core.Voxel object at_
↳0x7fd28e8c30>)]
(<ecell14.core.ParticleID object at 0x7fd28e8ae0>, <ecell14.core.Voxel object at_
↳0x7fd28e8bd0>)
```

You can move and update the voxel with `update_voxel` corresponding to `update_particle`.

```
[31]: c2 = w.position2coordinate(Real3(0.5, 0.5, 1.0))
w.update_voxel(pid, Voxel(v.species(), c2, v.radius(), v.D()))
pid, newv = w.get_voxel(pid)
print(c2) # => 278058
print(newv.species().serial(), newv.coordinate(), newv.radius(), newv.D()) # => (u'A'
↪', 278058, 0.0025, 1.0)
print(w.num_voxels_exact(Species("A"))) # => 1

278058
(u'A', 278058, 0.0025, 1.0)
1
```

Finally, `remove_voxel` remove a voxel as `remove_particle` does.

```
[32]: print(w.has_voxel(pid)) # => True
w.remove_voxel(pid)
print(w.has_voxel(pid)) # => False

True
False
```

1.3.4 3.4 Structure

```
[33]: w1 = GillespieWorld()
w2 = ODEWorld()
w3 = SpatiocyteWorld()
w4 = BDWorld()
w5 = MesoscopicWorld()
w6 = EGFRDWorld()
```

By using a `Shape` object, you can confine initial positions of molecules to a part of `World`. In the case below, 60 molecules are positioned inside the given `Sphere`. Diffusion of the molecules placed here is **NOT** restricted in the `Shape`. This `Shape` is only for the initialization.

```
[34]: sp1 = Species("A", "0.0025", "1")
sphere = Sphere(Real3(0.5, 0.5, 0.5), 0.3)
w1.add_molecules(sp1, 60, sphere)
w2.add_molecules(sp1, 60, sphere)
w3.add_molecules(sp1, 60, sphere)
w4.add_molecules(sp1, 60, sphere)
w5.add_molecules(sp1, 60, sphere)
w6.add_molecules(sp1, 60, sphere)
```

A property of `Species`, `'location'`, is available to restrict diffusion of molecules. `'location'` is not fully supported yet, but only supported in `spatiocyte` and `meso`. `add_structure` defines a new structure given as a pair of `Species` and `Shape`.

```
[35]: membrane = SphericalSurface(Real3(0.5, 0.5, 0.5), 0.4) # This is equivalent to call_
↪ `Sphere(Real3(0.5, 0.5, 0.5), 0.4).surface()`
w3.add_structure(Species("M"), membrane)
w5.add_structure(Species("M"), membrane)
```

After defining a structure, you can bind molecules to the structure as follows:

```
[36]: sp2 = Species("B", "0.0025", "0.1", "M") # 'location' is the fourth argument
w3.add_molecules(sp2, 60)
w5.add_molecules(sp2, 60)
```

The molecules bound to a Species named B diffuse on a structure named M, which has a shape of SphericalSurface (a hollow sphere). In `spatiocyte`, a structure is represented as a set of particles with Species M occupying a voxel. It means that molecules not belonging to the structure is not able to overlap the voxel and it causes a collision. On the other hand, in `meso`, a structure means a list of subvolumes. Thus, a structure doesn't avoid an incursion of other particles.

1.3.5 3.5. Random Number Generator

A random number generator is also a part of World. All World except `ODEWorld` store a random number generator, and updates it when the simulation needs a random value. On `E-Cell4`, only one class `GSLRandomNumberGenerator` is implemented as a random number generator.

```
[37]: rng1 = GSLRandomNumberGenerator()
print([rng1.uniform_int(1, 6) for _ in range(20)])

[6, 1, 2, 6, 2, 3, 6, 5, 4, 5, 5, 4, 2, 5, 4, 2, 3, 3, 2, 2]
```

With no argument, the random number generator is always initialized with a seed, 0.

```
[38]: rng2 = GSLRandomNumberGenerator()
print([rng2.uniform_int(1, 6) for _ in range(20)]) # => same as above

[6, 1, 2, 6, 2, 3, 6, 5, 4, 5, 5, 4, 2, 5, 4, 2, 3, 3, 2, 2]
```

You can initialize the seed with an integer as follows:

```
[39]: rng2 = GSLRandomNumberGenerator()
rng2.seed(15)
print([rng2.uniform_int(1, 6) for _ in range(20)])

[6, 5, 2, 4, 1, 1, 3, 5, 2, 6, 4, 1, 2, 5, 2, 5, 1, 2, 2, 6]
```

When you call the `seed` function with no input, the seed is drawn from the current time.

```
[40]: rng2 = GSLRandomNumberGenerator()
rng2.seed()
print([rng2.uniform_int(1, 6) for _ in range(20)])

[6, 2, 1, 5, 6, 2, 6, 2, 6, 6, 5, 6, 2, 3, 5, 3, 6, 1, 4, 3]
```

`GSLRandomNumberGenerator` provides several ways to get a random number.

```
[41]: print(rng1.uniform(0.0, 1.0))
print(rng1.uniform_int(0, 100))
print(rng1.gaussian(1.0))

0.0303352042101
33
0.893555545521
```

World accepts a random number generator at the construction. As a default, `GSLRandomNumberGenerator()` is used. Thus, when you don't give a generator, behavior of the simulation is always same (deterministic).

```
[42]: rng = GSLRandomNumberGenerator()
      rng.seed()
      w1 = GillespieWorld(Real3(1, 1, 1), rng=rng)
```

You can access the `GSLRandomNumberGenerator` in a `World` through `rng` function.

```
[43]: print(w1.rng().uniform(0.0, 1.0))

0.966634188779
```

`rng()` returns a shared pointer to the `GSLRandomNumberGenerator`. Thus, in the example above, `rng` and `w1.rng()` point exactly the same thing.

1.4 4. How to Run a Simulation

In sections 2 and 3, we explained the way to build a model and to setup the initial state. Now, it is the time to run a simulation. Corresponding to `World` classes, six `Simulator` classes are there: `spatiocyte.SpatiocyteSimulator`, `egfrd.EGFRDSimulator`, `bd.BDSimulator`, `meso.MesoscopicSimulator`, `gillespie.GillespieSimulator`, and `ode.ODESimulator`. Each `Simulator` class only accepts the corresponding type of `World`, but all of them allow the same `Model`.

```
[1]: import eccl4
```

1.4.1 4.1. How to Setup a Simulator

Except for the initialization (so-called constructor function) with arguments specific to the algorithm, all `Simulators` have the same APIs.

```
[2]: from eccl4.core import *
      from eccl4.gillespie import GillespieWorld, GillespieSimulator
      from eccl4.ode import ODEWorld, ODESimulator
      from eccl4.spatiocyte import SpatiocyteWorld, SpatiocyteSimulator
      from eccl4.bd import BDWorld, BDSimulator
      from eccl4.meso import MesoscopicWorld, MesoscopicSimulator
      from eccl4.egfrd import EGFRDWorld, EGFRDSimulator
```

Before constructing a `Simulator`, prepare a `Model` and a `World` corresponding to the type of `Simulator`.

```
[3]: from eccl4 import species_attributes, reaction_rules, get_model

      with species_attributes():
          A | B | C | {'D': '1', 'radius': '0.005'}

      with reaction_rules():
          A + B == C | (0.01, 0.3)

      m = get_model()
```

```
[4]: w1 = GillespieWorld()
      w2 = ODEWorld()
      w3 = SpatiocyteWorld()
      w4 = BDWorld()
```

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```
w5 = MesoscopicWorld()
w6 = EGFRDWorld()
```

Simulator requires both Model and World in this order at the construction.

```
[5]: sim1 = GillespieSimulator(m, w1)
sim2 = ODESimulator(m, w2)
sim3 = SpatiocyteSimulator(m, w3)
sim4 = BDSimulator(m, w4)
sim5 = MesoscopicSimulator(m, w5)
sim6 = EGFRDSimulator(m, w6)
```

If you bind the Model to the World, you need only the World to create a Simulator.

```
[6]: w1.bind_to(m)
w2.bind_to(m)
w3.bind_to(m)
w4.bind_to(m)
w5.bind_to(m)
w6.bind_to(m)
```

```
[7]: sim1 = GillespieSimulator(w1)
sim2 = ODESimulator(w2)
sim3 = SpatiocyteSimulator(w3)
sim4 = BDSimulator(w4)
sim5 = MesoscopicSimulator(w5)
sim6 = EGFRDSimulator(w6)
```

Of course, the Model and World bound to a Simulator can be drawn from Simulator in the way below:

```
[8]: print(sim1.model(), sim1.world())
print(sim2.model(), sim2.world())
print(sim3.model(), sim3.world())
print(sim4.model(), sim4.world())
print(sim5.model(), sim5.world())
print(sim6.model(), sim6.world())

(<ecell4.core.Model object at 0x7f6b329d1af8>, <ecell4.gillespie.GillespieWorld_
↪object at 0x7f6b329d1a08>)
(<ecell4.ode.ODENetworkModel object at 0x7f6b329d1af8>, <ecell4.ode.ODEWorld object_
↪at 0x7f6b329d1ae0>)
(<ecell4.core.Model object at 0x7f6b329d1af8>, <ecell4.spatocyte.SpatocyteWorld_
↪object at 0x7f6b329d1a08>)
(<ecell4.core.Model object at 0x7f6b329d1af8>, <ecell4.bd.BDWorld object at_
↪0x7f6b329d1ae0>)
(<ecell4.core.Model object at 0x7f6b329d1af8>, <ecell4.meso.MesoscopicWorld object at_
↪0x7f6b329d1ac8>)
(<ecell4.core.Model object at 0x7f6b329d1af8>, <ecell4.egfrd.EGFRDWorld object at_
↪0x7f6b329d1ae0>)
```

After updating the World by yourself, you must initialize the internal state of a Simulator before running simulation.

```
[9]: w1.add_molecules(Species('C'), 60)
w2.add_molecules(Species('C'), 60)
w3.add_molecules(Species('C'), 60)
```

(continues on next page)

(continued from previous page)

```
w4.add_molecules(Species('C'), 60)
w5.add_molecules(Species('C'), 60)
w6.add_molecules(Species('C'), 60)
```

```
[10]: sim1.initialize()
      sim2.initialize()
      sim3.initialize()
      sim4.initialize()
      sim5.initialize()
      sim6.initialize()
```

For algorithms with a fixed step interval, the Simulator also requires `dt`.

```
[11]: sim2.set_dt(1e-6) # ODESimulator. This is optional
      sim4.set_dt(1e-6) # BDSimulator
```

1.4.2 4.2. Running Simulation

For running simulation, Simulator provides two APIs, `step` and `run`.

`step()` advances a simulation for the time that the Simulator expects, `next_time()`.

```
[12]: print(sim1.t(), sim1.next_time(), sim1.dt())
      print(sim2.t(), sim2.next_time(), sim2.dt()) # => (0.0, 1e-6, 1e-6)
      print(sim3.t(), sim3.next_time(), sim3.dt())
      print(sim4.t(), sim4.next_time(), sim4.dt()) # => (0.0, 1e-6, 1e-6)
      print(sim5.t(), sim5.next_time(), sim5.dt())
      print(sim6.t(), sim6.next_time(), sim6.dt()) # => (0.0, 0.0, 0.0)

(0.0, 0.032171880483933143, 0.032171880483933143)
(0.0, 1e-06, 1e-06)
(0.0, 1.6666666666666667e-05, 1.6666666666666667e-05)
(0.0, 1e-06, 1e-06)
(0.0, 0.029999537310460653, 0.029999537310460653)
(0.0, 0.0, 0.0)
```

```
[13]: sim1.step()
      sim2.step()
      sim3.step()
      sim4.step()
      sim5.step()
      sim6.step()
```

```
[14]: print(sim1.t())
      print(sim2.t()) # => 1e-6
      print(sim3.t())
      print(sim4.t()) # => 1e-6
      print(sim5.t())
      print(sim6.t()) # => 0.0

0.0321718804839
1e-06
1.666666666667e-05
1e-06
0.0299995373105
0.0
```

`last_reactions()` returns a list of pairs of `ReactionRule` and `ReactionInfo` which occurs at the last step. Each algorithm have its own implementation of `ReactionInfo`. See `help(module.ReactionInfo)` for details.

```
[15]: print(sim1.last_reactions())
      # print(sim2.last_reactions())
      print(sim3.last_reactions())
      print(sim4.last_reactions())
      print(sim5.last_reactions())
      print(sim6.last_reactions())

[(<ecell14.core.ReactionRule object at 0x7f6b329d1ae0>, <ecell14.gillespie.ReactionInfo_
↳object at 0x7f6b329d1af8>)]
[]
[]
[(<ecell14.core.ReactionRule object at 0x7f6b329d1ae0>, <ecell14.meso.ReactionInfo_
↳object at 0x7f6b329d1af8>)]
[]
```

`step(upto)` advances a simulation for `next_time` if `next_time` is less than `upto`, or for `upto` otherwise. `step(upto)` returns whether the time does **NOT** reach the limit, `upto`.

```
[16]: print(sim1.step(1.0), sim1.t())
      print(sim2.step(1.0), sim2.t())
      print(sim3.step(1.0), sim3.t())
      print(sim4.step(1.0), sim4.t())
      print(sim5.step(1.0), sim5.t())
      print(sim6.step(1.0), sim6.t())

(True, 0.11785771174833615)
(True, 2e-06)
(True, 3.3333333333333335e-05)
(True, 2e-06)
(True, 0.0709074540101994)
(True, 0.0)
```

To run a simulation just until the time, `upto`, call `step(upto)` while it returns `True`.

```
[17]: while sim1.step(1.0): pass
      while sim2.step(0.001): pass
      while sim3.step(0.001): pass
      while sim4.step(0.001): pass
      while sim5.step(1.0): pass
      while sim6.step(0.001): pass
```

```
[18]: print(sim1.t()) # => 1.0
      print(sim2.t()) # => 0.001
      print(sim3.t()) # => 0.001
      print(sim4.t()) # => 0.001
      print(sim5.t()) # => 1.0
      print(sim6.t()) # => 0.001
```

```
1.0
0.001
0.001
0.001
1.0
0.001
```

This is just what `run` does. `run(tau)` advances a simulation upto `t() + tau`.


```
[19]: sim1.run(1.0)
      sim2.run(0.001)
      sim3.run(0.001)
      sim4.run(0.001)
      sim5.run(1.0)
      sim6.run(0.001)
```

```
[20]: print(sim1.t()) # => 2.0
      print(sim2.t()) # => 0.002
      print(sim3.t()) # => 0.002
      print(sim4.t()) # => 0.002
      print(sim5.t()) # => 2.0
      print(sim6.t()) # => 0.02
```

```
2.0
0.002
0.002
0.002
2.0
0.002
```

`num_steps` returns the number of steps during the simulation.

```
[21]: print(sim1.num_steps())
      print(sim2.num_steps())
      print(sim3.num_steps())
      print(sim4.num_steps())
      print(sim5.num_steps())
      print(sim6.num_steps())
```

```
37
2001
120
2001
34
581
```

1.4.3 4.3. Capsulizing Algorithm into a Factory Class

Owing to the portability of a `Model` and consistent APIs of `Worlds` and `Simulators`, it is very easy to write a script common in algorithms. However, when switching the algorithm, still we have to rewrite the name of classes in the code, one by one.

To avoid the trouble, E-Cell4 also provides a `Factory` class for each algorithm. `Factory` encapsulates `World` and `Simulator` with their arguments needed for the construction. By using `Factory` class, your script could be portable and robust against changes in the algorithm.

```
[22]: from ecell4.gillespie import GillespieFactory
      from ecell4.ode import ODEFactory
      from ecell4.spatiocyte import SpatiocyteFactory
      from ecell4.bd import BDFactory
      from ecell4.meso import MesoscopicFactory
      from ecell4.egfrd import EGFRDFactory
```

`Factory` just provides two functions, `create_world` and `create_simulator`.

```
[23]: def singlerun(f, m):  
    w = f.create_world(Real3(1, 1, 1))  
    w.bind_to(m)  
    w.add_molecules(Species('C'), 60)  
  
    sim = f.create_simulator(w)  
    sim.run(0.01)  
    print(sim.t(), w.num_molecules(Species('C')))
```

singlerun above is free from the algorithm. Thus, by just switching Factory, you can easily compare the results.

```
[24]: singlerun(GillespieFactory(), m)  
singlerun(ODEFactory(), m)  
singlerun(SpatiocyteFactory(), m)  
singlerun(BDFactory(bd_dt_factor=1), m)  
singlerun(MesosopicFactory(), m)  
singlerun(EGFRDFactory(), m)  
  
(0.01, 60)  
(0.01, 59)  
(0.01, 60)  
(0.01, 60)  
(0.01, 60)  
(0.01, 60)
```

When you need to provide several parameters to initialize World or Simulator, run_simulation also accepts Factory instead of solver.

```
[25]: from ecell4.util import run_simulation  
print(run_simulation(0.01, model=m, y0={'C': 60}, return_type='array',  
    ↪ solver=GillespieFactory())[-1])  
print(run_simulation(0.01, model=m, y0={'C': 60}, return_type='array',  
    ↪ solver=ODEFactory())[-1])  
print(run_simulation(0.01, model=m, y0={'C': 60}, return_type='array',  
    ↪ solver=SpatiocyteFactory())[-1])  
print(run_simulation(0.01, model=m, y0={'C': 60}, return_type='array',  
    ↪ solver=BDFactory(bd_dt_factor=1))[-1])  
print(run_simulation(0.01, model=m, y0={'C': 60}, return_type='array',  
    ↪ solver=MesosopicFactory())[-1])  
print(run_simulation(0.01, model=m, y0={'C': 60}, return_type='array',  
    ↪ solver=EGFRDFactory())[-1])  
  
[0.01, 0.0, 0.0, 60.0]  
[0.01, 0.17972919304001073, 0.17972919304001067, 59.82027080696036]  
[0.01, 0.0, 0.0, 60.0]  
[0.01, 0.0, 0.0, 60.0]  
[0.01, 0.0, 0.0, 60.0]  
[0.01, 0.0, 0.0, 60.0]
```

1.5 5. How to Log and Visualize Simulations

Here we explain how to take a log of simulation results and how to visualize it.

```
[1]: %matplotlib inline  
import math  
from ecell4 import *
```

1.5.1 5.1. Logging Simulations with Observers

E-Cell4 provides special classes for logging, named `Observer`. `Observer` class is given when you call the `run` function of `Simulator`.

```
[2]: def create_simulator(f=gillespie.GillespieFactory()):
    m = NetworkModel()
    A, B, C = Species('A', '0.005', '1'), Species('B', '0.005', '1'), Species('C', '0.
    ↪005', '1')
    m.add_reaction_rule(create_binding_reaction_rule(A, B, C, 0.01))
    m.add_reaction_rule(create_unbinding_reaction_rule(C, A, B, 0.3))
    w = f.create_world()
    w.bind_to(m)
    w.add_molecules(C, 60)
    sim = f.create_simulator(w)
    sim.initialize()
    return sim
```

One of most popular `Observer` is `FixedIntervalNumberObserver`, which logs the number of molecules with the given time interval. `FixedIntervalNumberObserver` requires an interval and a list of serials of `Species` for logging.

```
[3]: obs1 = FixedIntervalNumberObserver(0.1, ['A', 'B', 'C'])
    sim = create_simulator()
    sim.run(1.0, obs1)
```

`data` function of `FixedIntervalNumberObserver` returns the data logged.

```
[4]: print(obs1.data())

[[0.0, 0.0, 0.0, 60.0], [0.1, 0.0, 0.0, 60.0], [0.2, 0.0, 0.0, 60.0], [0.
    ↪300000000000000004, 5.0, 5.0, 55.0], [0.4, 8.0, 8.0, 52.0], [0.5, 8.0, 8.0, 52.0],
    ↪[0.600000000000000001, 8.0, 8.0, 52.0], [0.700000000000000001, 11.0, 11.0, 49.0], [0.8,
    ↪14.0, 14.0, 46.0], [0.9, 14.0, 14.0, 46.0], [1.0, 15.0, 15.0, 45.0]]
```

`targets()` returns a list of `Species`, which you specified as an argument of the constructor.

```
[5]: print([sp.serial() for sp in obs1.targets()])

['A', 'B', 'C']
```

`NumberObserver` logs the number of molecules after every steps when a reaction occurs. This observer is useful to log all reactions, but not available for `ode`.

```
[6]: obs1 = NumberObserver(['A', 'B', 'C'])
    sim = create_simulator()
    sim.run(1.0, obs1)
    print(obs1.data())

[[0.0, 0.0, 0.0, 60.0], [0.143979748309557, 1.0, 1.0, 59.0], [0.263959301731782, 2.0,
    ↪2.0, 58.0], [0.28549985484415447, 3.0, 3.0, 57.0], [0.2920290844608921, 4.0, 4.0,
    ↪56.0], [0.3151450201904092, 5.0, 5.0, 55.0], [0.32962099109027987, 6.0, 6.0, 54.0],
    ↪[0.33943151256600035, 7.0, 7.0, 53.0], [0.38459684239249475, 8.0, 8.0, 52.0], [0.
    ↪4402392101074317, 9.0, 9.0, 51.0], [0.4488367232148584, 10.0, 10.0, 50.0], [0.
    ↪4724492407095052, 11.0, 11.0, 49.0], [0.48969169545303415, 12.0, 12.0, 48.0], [0.
    ↪5926648902430811, 13.0, 13.0, 47.0], [0.7112014766673606, 14.0, 14.0, 46.0], [0.
    ↪7268968273742534, 15.0, 15.0, 45.0], [0.7889733307696482, 16.0, 16.0, 44.0], [0.
    ↪7938779425321273, 17.0, 17.0, 43.0], [0.9703902424683863, 18.0, 18.0, 42.0], [0.
    ↪9712948910756202, 17.0, 17.0, 43.0], [1.0, 17.0, 17.0, 43.0]]
```

TimingNumberObserver allows you to give the times for logging as an argument of its constructor.

```
[7]: obs1 = TimingNumberObserver([0.0, 0.1, 0.2, 0.5, 1.0], ['A', 'B', 'C'])
sim = create_simulator()
sim.run(1.0, obs1)
print(obs1.data())

[[0.0, 0.0, 0.0, 60.0], [0.1, 0.0, 0.0, 60.0], [0.2, 0.0, 0.0, 60.0], [0.5, 10.0, 10.
↪0, 50.0], [1.0, 16.0, 16.0, 44.0]]
```

run function accepts multiple Observers at once.

```
[8]: obs1 = NumberObserver(['C'])
obs2 = FixedIntervalNumberObserver(0.1, ['A', 'B'])
sim = create_simulator()
sim.run(1.0, [obs1, obs2])
print(obs1.data())
print(obs2.data())

[[0.0, 60.0], [0.22087040257109863, 59.0], [0.22720792132387785, 58.0], [0.
↪24968763863882104, 57.0], [0.2637930785790673, 56.0], [0.27337221983130383, 55.0],
↪[0.35394818219048224, 54.0], [0.36231206722433756, 53.0], [0.38536272493723256, 52.
↪0], [0.6152314487155562, 51.0], [0.6759207676775343, 50.0], [0.6807518102635762, 49.
↪0], [0.7009006683808036, 48.0], [0.7485557651303876, 47.0], [0.7530285146153741, 46.
↪0], [0.9214853607237395, 45.0], [1.0, 45.0]]
[[0.0, 0.0, 0.0], [0.1, 0.0, 0.0], [0.2, 0.0, 0.0], [0.30000000000000004, 5.0, 5.0],
↪[0.4, 8.0, 8.0], [0.5, 8.0, 8.0], [0.6000000000000001, 8.0, 8.0], [0.
↪7000000000000001, 11.0, 11.0], [0.8, 14.0, 14.0], [0.9, 14.0, 14.0], [1.0, 15.0, 15.
↪0]]
```

FixedIntervalHDF5Observer logs the whole data in a World to an output file with the fixed interval. Its second argument is a prefix for output filenames. filename() returns the name of a file scheduled to be saved next. At most one format string like %02d is allowed to use a step count in the file name. When you do not use the format string, it overwrites the latest data to the file.

```
[9]: obs1 = FixedIntervalHDF5Observer(0.2, 'test%02d.h5')
print(obs1.filename())
sim = create_simulator()
sim.run(1.0, obs1) # Now you have stepped 5 (1.0/0.2) times
print(obs1.filename())

test00.h5
test06.h5
```

```
[10]: w = load_world('test05.h5')
print(w.t(), w.num_molecules(Species('C')))

1.0 44
```

The usage of FixedIntervalCSVObserver is almost same with that of FixedIntervalHDF5Observer. It saves positions (x, y, z) of particles with the radius (r) and serial number of Species (sid) to a CSV file.

```
[11]: obs1 = FixedIntervalCSVObserver(0.2, "test%02d.csv")
print(obs1.filename())
sim = create_simulator()
sim.run(1.0, obs1)
print(obs1.filename())

test00.csv
test06.csv
```

Here is the first 10 lines in the output CSV file.

```
[12]: print(''.join(open("test05.csv").readlines()[: 10]))

x,y,z,r,sid
0.17508278810419142,0.12197625380940735,0.53627523058094084,0,0
0.24078186159022152,0.62765785818919539,0.7254820850212127,0,0
0.40445487247779965,0.16720660566352308,0.92957371729426086,0,0
0.24083335651084781,0.59580284473486245,0.51183571317233145,0,0
0.90290508698672056,0.4137285016477108,0.39729581261053681,0,0
0.51044316007755697,0.26319809840060771,0.40705726365558803,0,0
0.84177179471589625,0.085374288959428668,0.64473599148914218,0,0
0.54177056765183806,0.098819603677839041,0.17240164172835648,0,0
0.28669063560664654,0.71829434810206294,0.91102162329480052,0,0
```

For particle simulations, E-Cell4 also provides Observer to trace a trajectory of a molecule, named `FixedIntervalTrajectoryObserver`. When no `ParticleID` is specified, it logs all the trajectories. Once some `ParticleID` is lost for the reaction during a simulation, it just stop to trace the particle any more.

```
[13]: sim = create_simulator(spatiocyte.SpatiocyteFactory(0.005))
      obs1 = FixedIntervalTrajectoryObserver(0.01)
      sim.run(0.1, obs1)

[14]: print([tuple(pos) for pos in obs1.data()[0]])

[(0.46540305112880387, 0.739008344562721, 0.48), (0.2122891110412088, 0.
→ 9266471820493494, 0.665), (0.49806291436591293, 0.8689121551303868, 0.685), (0.
→ 7838367176906171, 0.8313843876330611, 0.64), (0.9961258287318259, 0.
→ 7967433714816836, 0.5), (0.7920016834998943, 0.9122134253196088, 0.63), (0.
→ 7348469228349536, 0.7534421012924616, 0.515), (0.9716309313039941, 0.
→ 851591647054698, 0.525), (1.1349302474895393, 0.9122134253196088, 0.63), (0.
→ 9961258287318259, 0.9439676901250381, 0.725), (0.718516991216399, 0.
→ 8833459118601275, 0.93)]
```

Generally, `World` assumes a periodic boundary for each plane. To avoid the big jump of a particle at the edge due to the boundary condition, `FixedIntervalTrajectoryObserver` tries to keep the shift of positions. Thus, the positions stored in the Observer are not necessarily limited in the cuboid given for the `World`. To track the diffusion over the boundary condition accurately, the step interval for logging must be small enough. Of course, you can disable this option. See `help(FixedIntervalTrajectoryObserver)`.

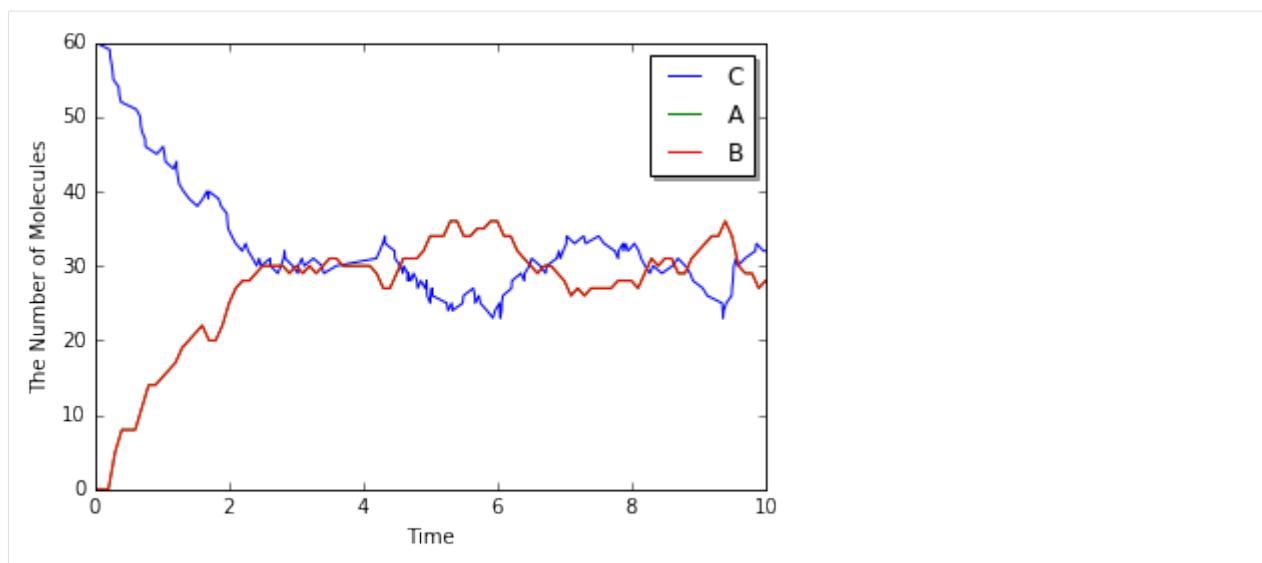
1.5.2 5.2. Visualization of Data Logged

In this section, we explain the visualization tools for data logged by Observer.

Firstly, for time course data, `viz.plot_number_observer` plots the data provided by `NumberObserver`, `FixedIntervalNumberObserver` and `TimingNumberObserver`. For the detailed usage of `viz.plot_number_observer`, see `help(viz.plot_number_observer)`.

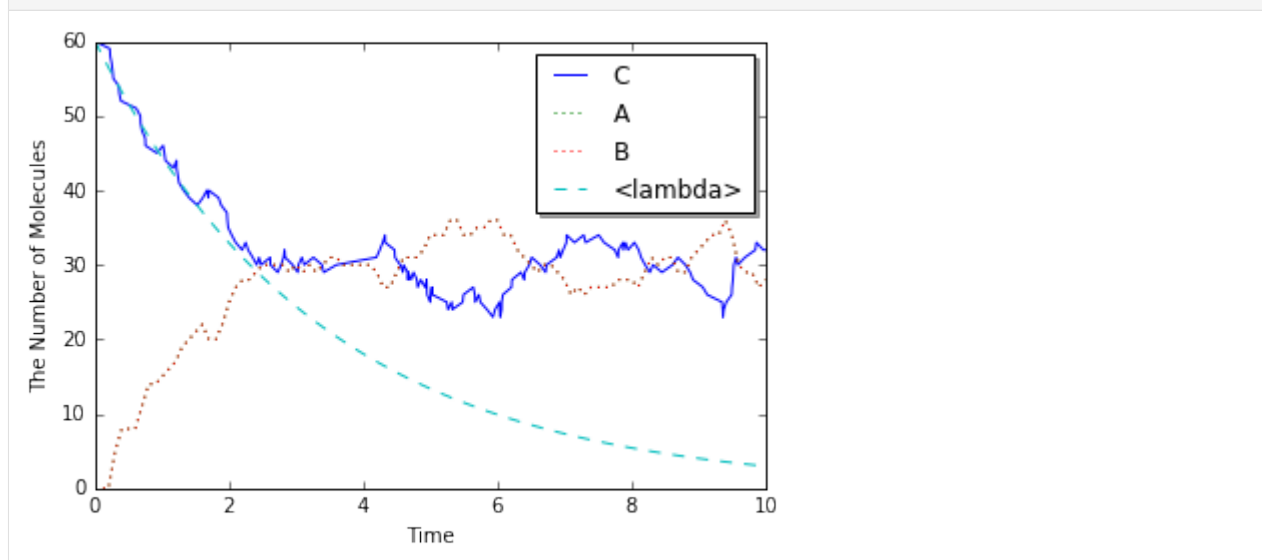
```
[15]: obs1 = NumberObserver(['C'])
      obs2 = FixedIntervalNumberObserver(0.1, ['A', 'B'])
      sim = create_simulator()
      sim.run(10.0, [obs1, obs2])
```

```
[16]: viz.plot_number_observer(obs1, obs2)
```



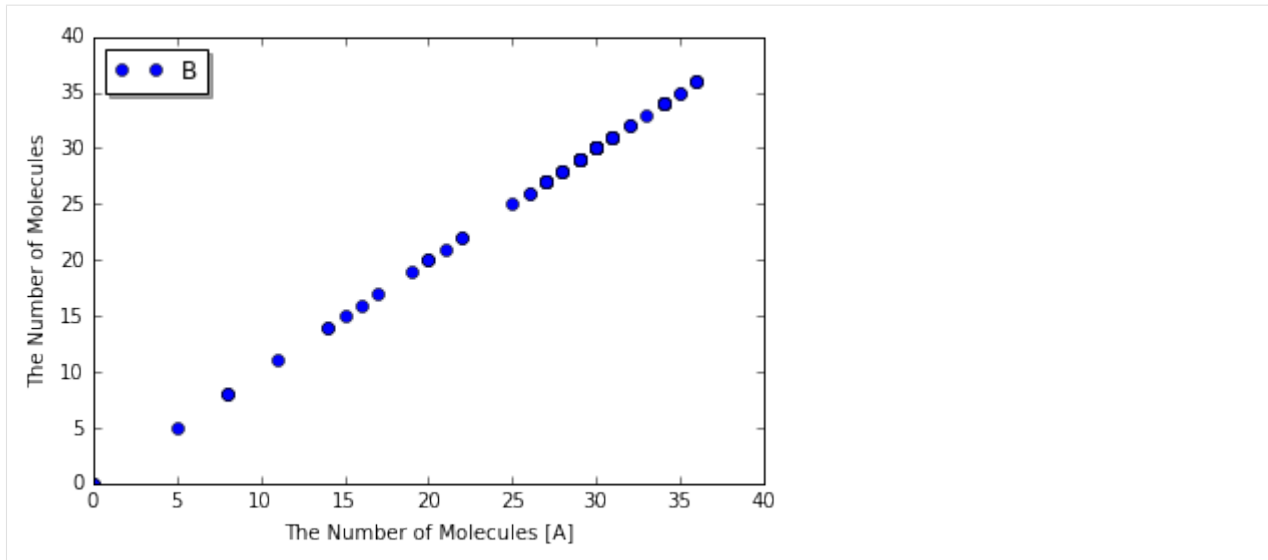
You can set the style for plotting, and even add an arbitrary function to plot.

```
[17]: viz.plot_number_observer(obs1, '-', obs2, ':', lambda t: 60 * math.exp(-0.3 * t), '--
      ↪')
```



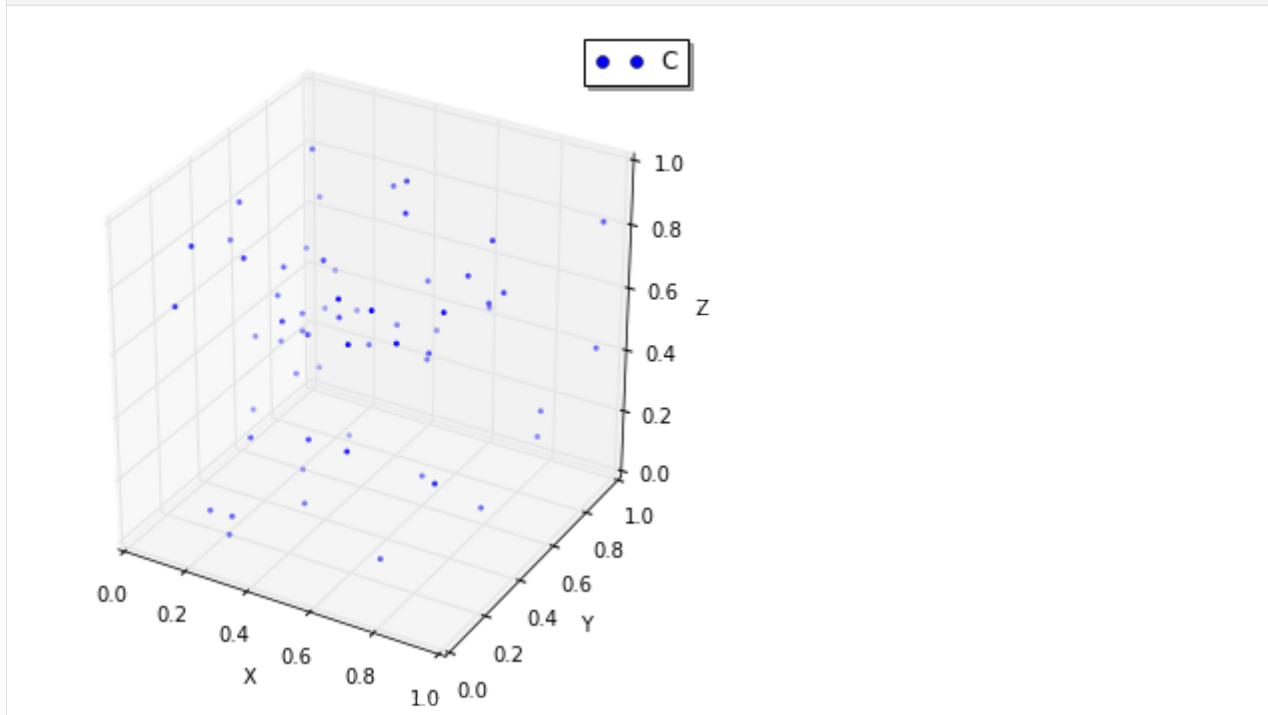
Plotting in the phase plane is also available by specifying the x-axis and y-axis.

```
[18]: viz.plot_number_observer(obs2, 'o', x='A', y='B')
```



For spatial simulations, to visualize the state of World, `viz.plot_world` is available. This function plots the points of particles in three-dimensional volume in the interactive way. You can save the image by clicking a right button on the drawing region.

```
[19]: sim = create_simulator(spatiocyte.SpatiocyteFactory(0.005))
# viz.plot_world(sim.world())
viz.plot_world(sim.world(), interactive=False)
```



You can also make a movie from a series of HDF5 files, given as a `FixedIntervalHDF5Observer`. NOTE: `viz.plot_movie` requires an extra library, `ffmpeg`, when `interactive=False`.

```
[20]: sim = create_simulator(spatiocyte.SpatiocyteFactory(0.005))
obs1 = FixedIntervalHDF5Observer(0.02, 'test%02d.h5')
```

(continues on next page)

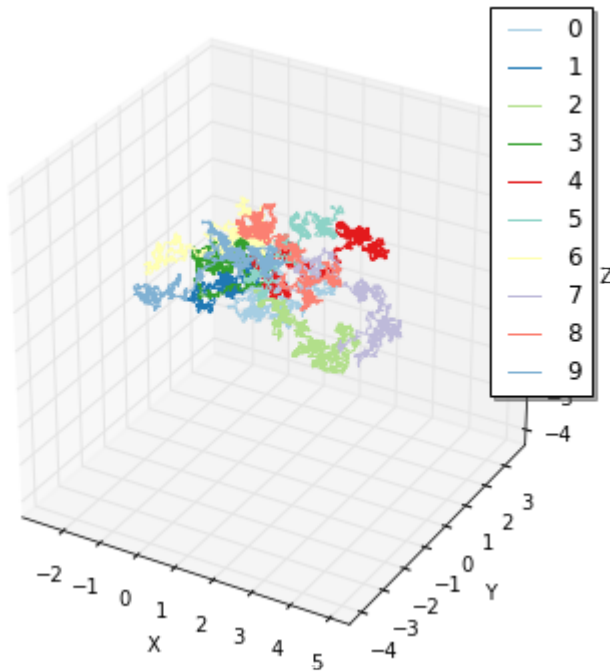
(continued from previous page)

```
sim.run(1.0, obs1)
viz.plot_movie(obs1)

<IPython.core.display.HTML object>
```

Finally, corresponding to `FixedIntervalTrajectoryObserver`, `viz.plot_trajectory` provides a visualization of particle trajectories.

```
[21]: sim = create_simulator(spatiocyte.SpatiocyteFactory(0.005))
      obs1 = FixedIntervalTrajectoryObserver(1e-3)
      sim.run(1, obs1)
      # viz.plot_trajectory(obs1)
      viz.plot_trajectory(obs1, interactive=False)
```



1.6 6. How to Solve ODEs with Rate Law Functions

Although the ode solver accepts `NetworkModel`, `ode.ODESimulator` owns its model class `ode.ODENetworkModel` and `ode.ODEReactionRule` for the extension. The interface of these classes are almost same with `Model` classes and `ReactionRule`. Here, we explain the usage specific to ode especially about `ode.ODERatelaw`.

```
[1]: %matplotlib inline
      from eccl14 import *
```

However, the rate law support in ode is under development. Some functions might be deprecated in the future. Currently, to enable rate laws, the option `ecell14.util.decorator.ENABLE_RATELAW` must be activated as follows:

```
[2]: util.decorator.ENABLE_RATELAW = True
```


1.6.1 6.1. ode.ODEReactionRule

ode.ODEReactionRule has almost same members with ReactionRule.

```
[3]: rr1 = ReactionRule()
      rr1.add_reactant(Species("A"))
      rr1.add_reactant(Species("B"))
      rr1.add_product(Species("C"))
      rr1.set_k(1.0)
      print(len(rr1.reactants())) # => 2
      print(len(rr1.products())) # => 1
      print(rr1.k()) # => 1.0
      print(rr1.as_string()) # => A+B>C|1
```

```
2
1
1.0
A+B>C|1
```

```
[4]: rr2 = ode.ODEReactionRule()
      rr2.add_reactant(Species("A"))
      rr2.add_reactant(Species("B"))
      rr2.add_product(Species("C"))
      rr2.set_k(1.0)
      print(len(rr2.reactants())) # => 2
      print(len(rr2.products())) # => 1
      print(rr2.k()) # => 1.0
      print(rr2.as_string()) # => A+B>C|1
```

```
2
1
1.0
A+B>C|1
```

In addition to the common members, ode.ODEReactionRule can store stoichiometric coefficients for each Species:

```
[5]: rr2 = ode.ODEReactionRule()
      rr2.add_reactant(Species("A"), 1.0)
      rr2.add_reactant(Species("B"), 2.0)
      rr2.add_product(Species("C"), 2.5)
      rr2.set_k(1.0)
      print(rr2.as_string())
```

```
A+2*B>2.5*C|1
```

You can also access to the coefficients as follows:

```
[6]: print(rr2.reactants_coefficients()) # => [1.0, 2.0]
      print(rr2.products_coefficients()) # => [2.5]
```

```
[1.0, 2.0]
[2.5]
```

1.6.2 6.2. ode.ODERatelaw

ode.ODEReactionRule can be bound to a ode.ODERatelaw. ode.ODERatelaw provides a function to calculate a derivative (flux or velocity) based on the given values of Species. ode.ODERatelawMassAction

is a default class bound to `ode.ODEReactionRule`.

```
[7]: rr1 = ode.ODEReactionRule()
      rr1.add_reactant(Species("A"))
      rr1.add_reactant(Species("B"))
      rr1.add_product(Species("C"))
      rl1 = ode.ODERatelawMassAction(2.0)
      rr1.set_ratelaw(rl1) # equivalent to rr1.set_k(2.0)
      print(rr1.as_string())
```

```
A+B>C|2
```

`ode.ODERatelawCallback` enables the user-defined function for calculating a flux.

```
[8]: def mass_action(reactants, products, volume, t, rr):
      veloc = 2.0 * volume
      for value in reactants:
          veloc *= value / volume
      return veloc

      rl2 = ode.ODERatelawCallback(mass_action)
      rr1.set_ratelaw(rl2)
      print(rr1.as_string())
```

```
A+B>C|mass_action
```

The function bound must accept five arguments and return a floating number as a velocity. The first and second list contain a value for each reactants and products respectively. When you need to access the stoichiometric coefficients, use `rr` (`ode.ODEReactionRule`) in the arguments.

A lambda function is available too.

```
[9]: rl2 = ode.ODERatelawCallback(lambda r, p, v, t, rr: 2.0 * r[0] * r[1])
      rr1.set_k(0)
      rr1.set_ratelaw(rl2)
      print(rr1.as_string())
```

```
A+B>C|<lambda>
```

1.6.3 6.3. ode.ODENetworkModel

`ode.ODENetworkModel` accepts both `ReactionRule` and `ode.ODEReactionRule`. `ReactionRule` is implicitly converted and stored as a `ode.ODEReactionRule`.

```
[10]: m1 = ode.ODENetworkModel()
      rr1 = create_unbinding_reaction_rule(Species("C"), Species("A"), Species("B"), 3.0)
      m1.add_reaction_rule(rr1)
      rr2 = ode.ODEReactionRule(create_binding_reaction_rule(Species("A"), Species("B"),
      ↪Species("C"), 0.0))
      rr2.set_ratelaw(ode.ODERatelawCallback(lambda r, p, v, t, rr: 0.1 * r[0] * r[1]))
      m1.add_reaction_rule(rr2)
```

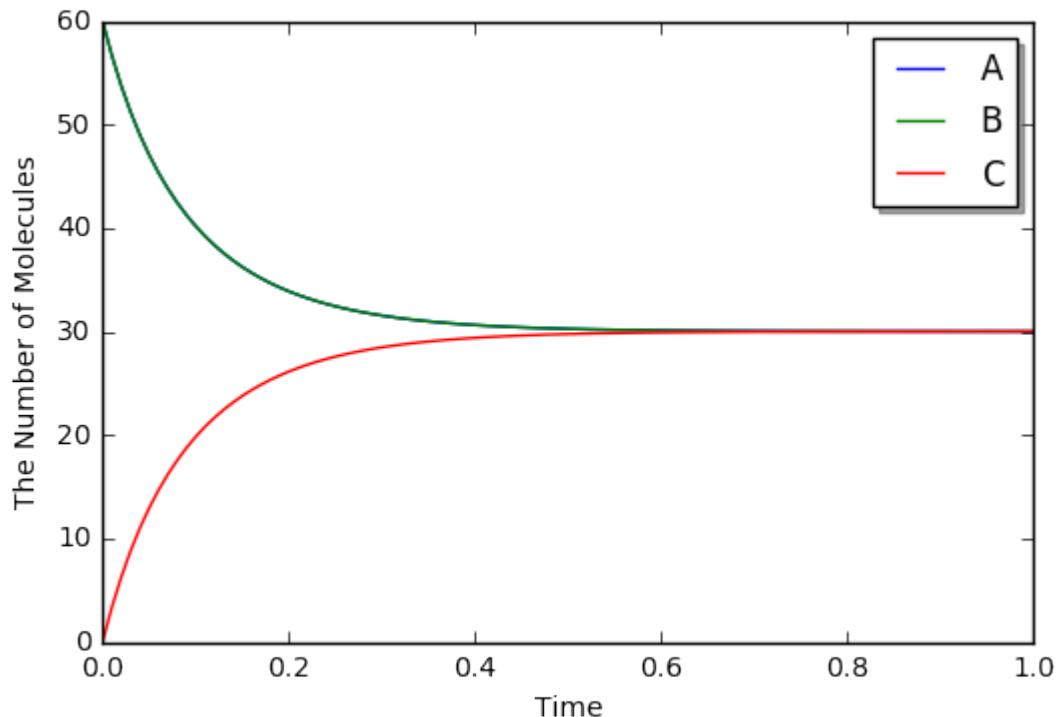
You can access to the list of `ode.ODEReactionRules` in `ode.ODENetworkModel` via its member `reaction_rules()`.

```
[11]: print([rr.as_string() for rr in m1.reaction_rules()])
```

```
['C>A+B|3', 'A+B>C|<lambda>']
```

Finally, you can run simulations in the same way with other solvers as follows:

```
[12]: run_simulation(1.0, model=m1, y0={'A': 60, 'B': 60})
```



Modeling with Python decorators is also available by specifying a function instead of a rate (floating number). When a floating number is set, it is assumed to be a kinetic rate of a mass action reaction, but not a constant velocity.

```
[13]: with reaction_rules():
      A + B == C | (lambda r, *args: 0.1 * reduce(mul, r), 3.0)

m1 = get_model()
```

For the simplicity, you can directly defining the equation with Species names as follows:

```
[14]: with reaction_rules():
      A + B == C | (0.1 * A * B, 3.0)

m1 = get_model()
```

When you call a Species (in the rate law) which is not listed as a reactant or product, it is automatically added to the list as an enzyme.

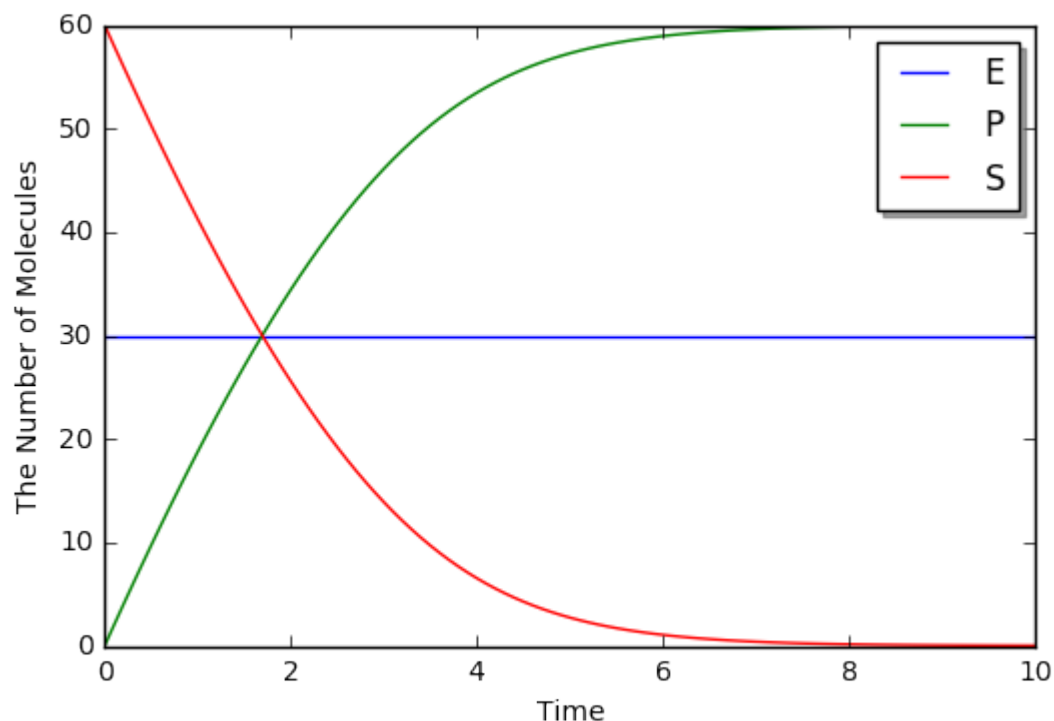
```
[15]: with reaction_rules():
      S > P | 1.0 * E * S / (30.0 + S)

m1 = get_model()
print(m1.reaction_rules()[0].as_string())

S+E>P+E|((1.0*E*S)/(30.0+S))
```

where E in the equation is appended to both reactant and product lists.

```
[16]: run_simulation(10.0, model=m1, y0={'S': 60, 'E': 30})
```



Please be careful about typo in Species' name. When you make a typo, it is unintentionally recognized as a new enzyme:

```
[17]: with reaction_rules():
      A13P2G > A23P2G | 1500 * A13B2G # typo: A13P2G -> A13B2G

m1 = get_model()
print(m1.reaction_rules()[0].as_string())

A13P2G+A13B2G>A23P2G+A13B2G|(1500*A13B2G)
```

When you want to disable the automatic declaration of enzymes, inactivate `util.decorator.ENABLE_IMPLICIT_DECLARATION`. If its value is `False`, the above case will raise an error:

```
[20]: util.decorator.ENABLE_IMPLICIT_DECLARATION = False

try:
    with reaction_rules():
        A13P2G > A23P2G | 1500 * A13B2G
except RuntimeError as e:
    print(repr(e))

util.decorator.ENABLE_IMPLICIT_DECLARATION = True

RuntimeError('unknown variable [A13B2G] was used.',)
```

Although E-Cell4 is specialized for a simulation of biochemical reaction network, by using a synthetic reaction rule,

ordinary differential equations can be translated intuitively. For example, the Lotka-Volterra equations:

$$\frac{dx}{dt} = Ax - Bxy$$

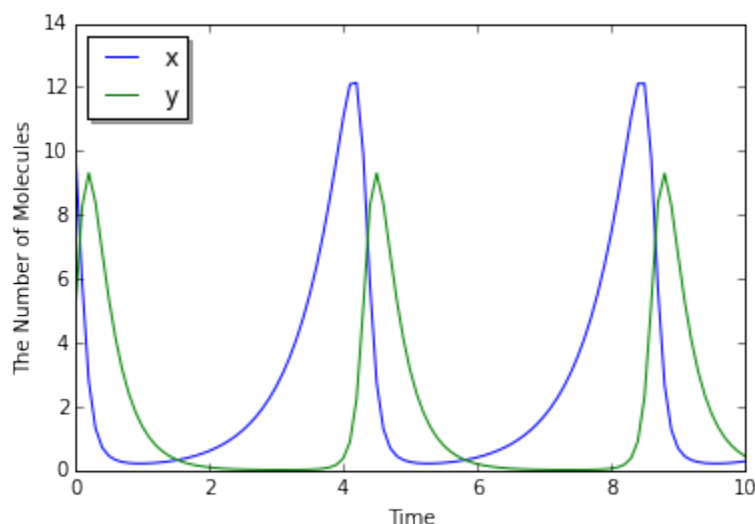
$$\frac{dy}{dt} = -Cx + Dxy$$

where $A = 1.5, B = 1, C = 3, D = 1, x(0) = 10, y(0) = 5$, are solved as follows:

```
[19]: with reaction_rules():
      A, B, C, D = 1.5, 1, 3, 1

      ~x > x | A * x - B * x * y
      ~y > y | -C * y + D * x * y

run_simulation(10, model=get_model(), y0={'x': 10, 'y': 5})
```



1.6.4 6.4. References in a Rate Law

Here, we explain the details in the rate law definition.

First, when you use simpler definitions of a rate law with `Species`, only a limited number of mathematical functions (e.g. `exp`, `log`, `sin`, `cos`, `tan`, `asin`, `acos`, `atan`, and `pi`) are available there even if you declare the function outside the block.

```
[20]: try:
      from math import erf

      with reaction_rules():
          S > P | erf(S / 30.0)
except TypeError as e:
    print(repr(e))

TypeError('a float is required',)
```

This is because `erf` is tried to be evaluated against `S / 30.0` first, but it is not a floating number. In contrast, the following case is acceptable:

```
[21]: from math import erf

with reaction_rules():
    S > P | erf(2.0) * S

m1 = get_model()
print(m1.reaction_rules()[0].as_string())

S>P| (0.995322265019*S)
```

where only the result of `erf(2.0)`, `0.995322265019`, is passed to the rate law. Thus, the rate law above has no reference to the `erf` function. Similarly, a value of variables declared outside is acceptable, but not as a reference.

```
[22]: kcat, Km = 1.0, 30.0

with reaction_rules():
    S > P | kcat * E * S / (Km + S)

m1 = get_model()
print(m1.reaction_rules()[0].as_string())
kcat = 2.0
print(m1.reaction_rules()[0].as_string())

S+E>P+E| ((1.0*E*S)/(30.0+S))
S+E>P+E| ((1.0*E*S)/(30.0+S))
```

Even if you change the value of a variable, it does **not** affect the rate law.

On the other hand, when you use your own function to define a rate law, it can hold a reference to variables outside.

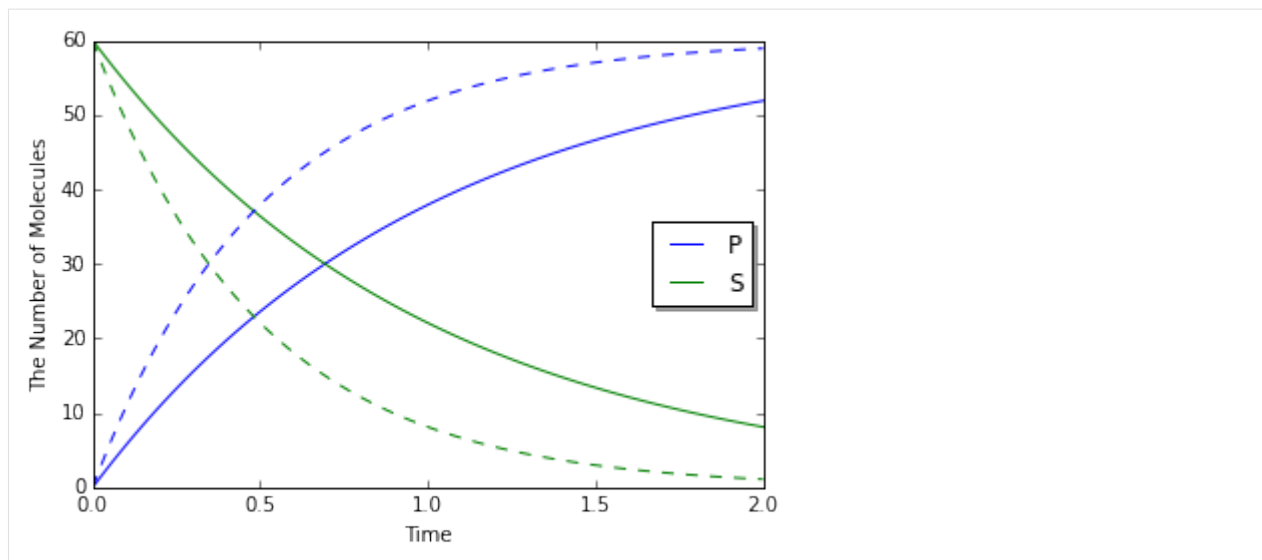
```
[23]: k1 = 1.0

with reaction_rules():
    S > P | (lambda r, *args: k1 * r[0]) # referring k1

m1 = get_model()

obs1 = run_simulation(2, model=m1, y0={"S": 60}, return_type='observer')
k1 = 2.0
obs2 = run_simulation(2, model=m1, y0={"S": 60}, return_type='observer')

viz.plot_number_observer(obs1, '-', obs2, '--')
```



However, in this case, it is better to make a new model for each set of parameters.

```
[24]: def create_model(k):
      with reaction_rules():
          S > P | k

      return get_model()

obs1 = run_simulation(2, model=create_model(k=1.0), y0={"S": 60}, return_type=
↳ 'observer')
obs2 = run_simulation(2, model=create_model(k=2.0), y0={"S": 60}, return_type=
↳ 'observer')
# viz.plot_number_observer(obs1, '-', obs2, '--')
```

1.6.5 6.5. More about ode

In `ode.ODEWorld`, a value for each Species is a floating number. However, for the compatibility, the common member `num_molecules` and `add_molecules` regard the value as an integer.

```
[25]: w = ode.ODEWorld()
w.add_molecules(Species("A"), 2.5)
print(w.num_molecules(Species("A")))

2
```

To set/get a real number, use `set_value` and `get_value`:

```
[26]: w.set_value(Species("B"), 2.5)
print(w.get_value(Species("A")))
print(w.get_value(Species("B")))

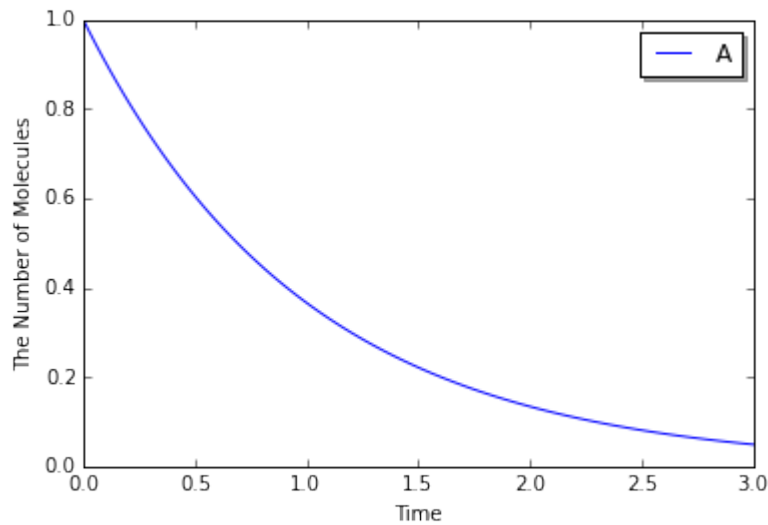
2.0
2.5
```

As a default, `ode.ODESimulator` employs the Rosenblock method, called `ROSENBROCK4_CONTROLLER`, to solve ODEs. In addition to that, two solvers, `EULER` and `RUNGE_KUTTA_CASH_KARP54`, are available. `ROSENBROCK4_CONTROLLER` and `RUNGE_KUTTA_CASH_KARP54` adaptively change the step size during time evolution due to error controll, but `EULER` does not.

```
[27]: with reaction_rules():  
      A > ~A | 1.0  
  
m1 = get_model()  
  
w1 = ode.ODEWorld()  
w1.set_value(Species("A"), 1.0)  
sim1 = ode.ODESimulator(m1, w1, ode.EULER)  
sim1.set_dt(0.01) # This is only effective for EULER  
sim1.run(3.0, obs1)
```

`ode.ODEFactory` also accepts a solver type and a default step interval.

```
[28]: run_simulation(3.0, model=m1, y0={"A": 1.0}, solver=('ode', ode.EULER, 0.01))
```



See also examples listed below:

- [Glycolysis of Human Erythrocytes](#)
- [Drosophila Circadian Clock](#)
- [Attractors](#)

1.7 7. Introduction of Rule-based Modeling

E-Cell4 provides the rule-based modeling environment.

```
[1]: %matplotlib inline  
from ecell4 import *
```

1.7.1 7.1. Species.count

First, `Species` provides a function `count`. `Species.count` counts the number of matches between `Species`.


```
[2]: sp1 = Species("A(b^1).B(b^1)")
      sp2 = Species("A(b^1).A(b^1)")
      ptnrn1 = Species("A")
      print(ptnrn1.count(sp1)) # => 1
      print(ptnrn1.count(sp2)) # => 2
```

```
1
2
```

In the above case, `Species.count` just returns the number of `UnitSpecies` named A in `Species` regardless of its sites. To specify the occupancy of a bond:

```
[3]: ptnrn1 = Species("A(b)")
      ptnrn2 = Species("A(b^_)")
      print(ptnrn1.count(sp1)) # => 0
      print(ptnrn2.count(sp1)) # => 1
```

```
0
1
```

where `A(b)` suggests that bond `b` is empty, and `A(b^_)` does that bond `b` is occupied. Underscore `_` means wildcard here. Similarly, you can also specify the state of sites.

```
[4]: sp1 = Species("A(b=u)")
      ptnrn1 = Species("A(b)")
      ptnrn2 = Species("A(b=u)")
      print(ptnrn1.count(sp1)) # => 1
      print(ptnrn2.count(sp1)) # => 1
```

```
1
1
```

`A(b)` says nothing about the state, but `A(b=u)` specifies both state and bond. `A(b=u)` means that `UnitSpecies` named A has a site named `b` which state is `u` and the bond is empty. Wildcard `_` is acceptable even in a state and name.

```
[5]: sp1 = Species("A(b=u^1).B(b=p^1)")
      ptnrn1 = Species("A(b=_^_)") # This is equivalent to `A(b^_)` here
      ptnrn2 = Species("_ (b^_)")
      print(ptnrn1.count(sp1)) # => 1
      print(ptnrn2.count(sp1)) # => 2
```

```
1
2
```

Wildcard `_` matches anything, and the pattern matched is not consistent between wildcards even in the `Species`. On the other hand, named wildcards, `_1`, `_2` and so on, confer the consistency within the match.

```
[6]: sp1 = Species("A(b^1).B(b^1)")
      ptnrn1 = Species("_._")
      ptnrn2 = Species("_1._1")
      print(ptnrn1.count(sp1)) # => 2
      print(ptnrn2.count(sp1)) # => 0
```

```
2
0
```

where the first pattern matches in two ways (`A.B` and `B.A`), but the second matches nothing. `Species.count` always distinguishes the order of `UnitSpecies` even in the symmetric case. Thus, `_1._1` does **not** mean the number of dimers.

```
[7]: sp1 = Species("A(b^1).A(b^1)")
      ptnr1 = Species("_1._1")
      print(ptnr1.count(sp1)) # => 2
```

2

1.7.2 7.2. ReactionRule.count and generate

ReactionRule also has a function to count matches against the given list of reactants.

```
[8]: rrl = create_unimolecular_reaction_rule(Species("A(p=u)"), Species("A(p=p)"), 1.0)
      sp1 = Species("A(b^1,p=u).B(b^1)")
      print(rrl.count([sp1])) # => 1
```

1

ReactionRule.generate returns a list of ReactionRules generated based on the matches.

```
[9]: print([rr.as_string() for rr in rrl.generate([sp1])])
```

[u'A(b^1,p=u).B(b^1)>A(b^1,p=p).B(b^1)|1']

ReactionRule.generate matters the order of Species in the given list:

```
[10]: rrl = create_binding_reaction_rule(Species("A(b)"), Species("B(b)"), Species("A(b^1).
      ↪B(b^1)"), 1.0)
      sp1 = Species("A(b)")
      sp2 = Species("B(b)")
      print([rr.as_string() for rr in rrl.generate([sp1, sp2])])
      print([rr.as_string() for rr in rrl.generate([sp2, sp1])])
```

[u'A(b)+B(b)>A(b^1).B(b^1)|1']
[]

On the current implementation, ReactionRule.generate does **not** always return a list of unique ReactionRules.

```
[11]: sp1 = Species("A(b,c^1).A(b,c^1)")
      sp2 = Species("B(b,c^1).B(b,c^1)")
      print(rrl.count([sp1, sp2])) # => 4
      print([rr.as_string() for rr in rrl.generate([sp1, sp2])])
```

4
[u'A(b,c^1).A(b,c^1)+B(b,c^1).B(b,c^1)>A(b^1,c^2).A(b,c^2).B(b^1,c^3).B(b,c^3)|1',
↪u'A(b,c^1).A(b,c^1)+B(b,c^1).B(b,c^1)>A(b^1,c^2).A(b,c^2).B(b,c^3).B(b^1,c^3)|1',
↪u'A(b,c^1).A(b,c^1)+B(b,c^1).B(b,c^1)>A(b,c^1).A(b^2,c^1).B(b^2,c^3).B(b,c^3)|1',
↪u'A(b,c^1).A(b,c^1)+B(b,c^1).B(b,c^1)>A(b,c^1).A(b^2,c^1).B(b,c^3).B(b^2,c^3)|1']

ReactionRules listed above look different, but all the products suggest the same.

```
[12]: print(set([unique_serial(rr.products()[0]) for rr in rrl.generate([sp1, sp2])]))
```

set([u'A(b,c^1).A(b^2,c^1).B(b^2,c^3).B(b,c^3)'])

This is because these ReactionRules are generated based on the different matches though they produce the same Species. For details, See the section below.

Wildcard is also available in ReactionRule.

```
[13]: rr1 = create_unimolecular_reaction_rule(Species("A(p=u^_)"), Species("A(p=p^_)"), 1.0)
print([rr.as_string() for rr in rr1.generate([Species("A(p=u^1).B(p^1)"))])

[u'A(p=u^1).B(p^1)>A(p=p^1).B(p^1)|1']
```

Of course, wildcard is accepted as a name of UnitSpecies.

```
[14]: rr1 = create_unimolecular_reaction_rule(Species("_ (p=u)"), Species("_ (p=p)"), 1.0)
print([rr.as_string() for rr in rr1.generate([Species("A(p=u)"))])
print([rr.as_string() for rr in rr1.generate([Species("B(b^1,p=u).C(b^1,p=u)"))])

[u'A(p=u)>A(p=p)|1']
[u'B(b^1,p=u).C(b^1,p=u)>B(b^1,p=p).C(b^1,p=u)|1', u'B(b^1,p=u).C(b^1,p=u)>B(b^1,p=u).
↪C(b^1,p=p)|1']
```

Named wildcards in a state is useful to specify the correspondence between sites.

```
[15]: rr1 = create_unbinding_reaction_rule(Species("AB(a=_1, b=_2)"), Species("B(b=_2)"), ↪
↪Species("A(a=_1)"), 1.0)
print([rr.as_string() for rr in rr1.generate([Species("AB(a=x, b=y)"))])
print([rr.as_string() for rr in rr1.generate([Species("AB(a=y, b=x)"))])

[u'AB(a=x,b=y)>B(b=y)+A(a=x)|1']
[u'AB(a=y,b=x)>B(b=x)+A(a=y)|1']
```

Nameless wildcard `_` does not care about equality between matches. Products are generated in order.

```
[16]: rr1 = create_binding_reaction_rule(Species("_ (b)"), Species("_ (b)"), Species("_ (b^1). ↪
↪_ (b^1)"), 1.0)
print(rr1.as_string())
print([rr.as_string() for rr in rr1.generate([Species("A(b)"), Species("A(b)"))])
print([rr.as_string() for rr in rr1.generate([Species("A(b)"), Species("B(b)"))])

_ (b)+_ (b)>_ (b^1)._ (b^1)|1
[u'A(b)+A(b)>A(b^1).A(b^1)|1']
[u'A(b)+B(b)>A(b^1).B(b^1)|1']
```

For its symmetry, the former case above is sometimes preferred to have a half of the original kinetic rate. This is because the number of combinations of molecules in the former is $n(n-1)/2$ even though that in the later is n^2 , where both numbers of A and B molecules are n . This is true for gillespie and ode. However, in egfrd and spatiocyte, a kinetic rate is intrinsic one, and not affected by the number of combinations. Thus, in E-Cell4, no modification in the rate is done even for the case. See [Homodimerization and Annihilation](#) for the difference between algorithms.

In contrast to nameless wildcard, named wildcard keeps its consistency, and always suggests the same value in the ReactionRule.

```
[17]: rr1 = create_binding_reaction_rule(Species("_1(b)"), Species("_1(b)"), Species("_1(b^ ↪
↪_1)._1(b^1)"), 1.0)
print(rr1.as_string())
print([rr.as_string() for rr in rr1.generate([Species("A(b)"), Species("A(b)"))])
print([rr.as_string() for rr in rr1.generate([Species("A(b)"), Species("B(b)"))]) # ↪
↪=> []

_1(b)+_1(b)>_1(b^1)._1(b^1)|1
[u'A(b)+A(b)>A(b^1).A(b^1)|1']
[]
```

Named wildcard is consistent even between UnitSpecies' and site's names, technically.

```
[18]: rr1 = create_binding_reaction_rule(Species("A(b=_1)"), Species("_1(b)"), Species(
↪ "A(b=_1^1)._1(b^1)"), 1.0)
print(rr1.as_string())
print([rr.as_string() for rr in rr1.generate([Species("A(b=B)"), Species("A(b)"])]])
↪ # => []
print([rr.as_string() for rr in rr1.generate([Species("A(b=B)"), Species("B(b)"])]])

A(b=_1)+_1(b)>A(b=_1^1)._1(b^1)|1
[]
[u'A(b=B)+B(b)>A(b=B^1).B(b^1)|1']
```

1.7.3 7.3. NetfreeModel

NetfreeModel is a Model class for the rule-based modeling. The interface of NetfreeModel is almost same with NetworkModel, but takes into account rules and matches.

```
[19]: rr1 = create_binding_reaction_rule(Species("A(r)"), Species("A(l)"), Species("A(r^1).
↪ A(l^1)"), 1.0)

m1 = NetfreeModel()
m1.add_reaction_rule(rr1)
print(m1.num_reaction_rules())

m2 = NetworkModel()
m2.add_reaction_rule(rr1)
print(m2.num_reaction_rules())

1
1
```

Python notation explained in 2. [How to Build a Model](#) is available too. To get a model as NetfreeModel, set `is_netfree=True` in `get_model`:

```
[20]: with reaction_rules():
      A(r) + A(l) > A(r^1).A(l^1) | 1.0

m1 = get_model(is_netfree=True)
print(repr(m1))

<ecell14.core.NetfreeModel object at 0x7fbb44dc7708>
```

`Model.query_reaction_rules` returns a list of ReactionRules against the given reactants. `NetworkModel` just returns ReactionRules based on the equality of Species.

```
[21]: print(len(m2.query_reaction_rules(Species("A(r)"), Species("A(l)")))) # => 1
print(len(m2.query_reaction_rules(Species("A(l,r)"), Species("A(l,r)")))) # => 0

1
0
```

On the other hand, NetfreeModel generates the list by applying the stored ReactionRules in the rule-based way.

```
[22]: print(len(m1.query_reaction_rules(Species("A(r)"), Species("A(l)")))) # => 1
print(len(m1.query_reaction_rules(Species("A(l,r)"), Species("A(l,r)")))) # => 1

1
1
```

NetfreeModel does not cache generated objects. Thus, NetfreeModel.query_reaction_rules is slow, but needs less memory.

```
[23]: print(m1.query_reaction_rules(Species("A(1,r)"), Species("A(1,r)"))[0].as_string())
      print(m1.query_reaction_rules(Species("A(1,r^1).A(1^1,r)"), Species("A(1,r)"))[0].as_
      ↪string())
      print(m1.query_reaction_rules(Species("A(1,r^1).A(1^1,r)"), Species("A(1,r^1).A(1^1,r)
      ↪"))[0].as_string())

A(1,r)+A(1,r)>A(1,r^1).A(1^1,r)|2
A(1,r^1).A(1^1,r)+A(1,r)>A(1,r^1).A(1^1,r^2).A(1^2,r)|2
A(1,r^1).A(1^1,r)+A(1,r^1).A(1^1,r)>A(1,r^1).A(1^1,r^2).A(1^2,r^3).A(1^3,r)|2
```

NetfreeModel.expand expands NetfreeModel to NetworkModel by iteratively applying ReactionRules against the given seeds.

```
[24]: with reaction_rules():
      _ (b) + _ (b) == _ (b^1) ._ (b^1) | (1.0, 1.0)

m3 = get_model(True)
print(m3.num_reaction_rules())

m4 = m3.expand([Species("A(b)"), Species("B(b)")])
print(m4.num_reaction_rules())
print([rr.as_string() for rr in m4.reaction_rules()])

2
6
[u'A(b)+A(b)>A(b^1).A(b^1)|1', u'A(b)+B(b)>A(b^1).B(b^1)|1', u'B(b)+B(b)>B(b^1).
↪B(b^1)|1', u'A(b^1).A(b^1)>A(b)+A(b)|1', u'A(b^1).B(b^1)>A(b)+B(b)|1', u'B(b^1).
↪B(b^1)>B(b)+B(b)|1']
```

To avoid the infinite iteration for expansion, you can limit the maximum number of iterations and of UnitSpecies in a Species.

```
[25]: m2 = m1.expand([Species("A(1, r)"), 100, {Species("A"): 4})
      print(m2.num_reaction_rules()) # => 4
      print([rr.as_string() for rr in m2.reaction_rules()])

4
[u'A(1,r)+A(1,r)>A(1,r^1).A(1^1,r)|2', u'A(1,r^1).A(1^1,r)+A(1,r^1).A(1^1,r)>A(1,r^1).
↪A(1^1,r^2).A(1^2,r^3).A(1^3,r)|2', u'A(1,r)+A(1,r^1).A(1^1,r)>A(1,r^1).A(1^1,r^2).
↪A(1^2,r)|2', u'A(1,r)+A(1,r^1).A(1^1,r^2).A(1^2,r)>A(1,r^1).A(1^1,r^2).A(1^2,r^3).
↪A(1^3,r)|2']
```

1.7.4 7.4. Differences between Species, ReactionRule and NetfreeModel

The functions explained above is similar, but there are some differences in the criteria.

```
[26]: sp1 = Species("A(b^1).A(b^1)")
      sp2 = Species("A(b)")
      rr1 = create_unbinding_reaction_rule(sp1, sp2, sp2, 1.0)
      print(sp1.count(sp1))
      print([rr.as_string() for rr in rr1.generate([sp1])])

2
[u'A(b^1).A(b^1)>A(b)+A(b)|1']
```

Though `Species.count` suggests two different ways for matching (left-right and right-left), `ReactionRule.generate` returns only one `ReactionRule` because the order doesn't affect the product.

```
[27]: sp1 = Species("A(b^1).B(b^1)")
      rr1 = create_unbinding_reaction_rule(
          sp1, Species("A(b)"), Species("B(b)"), 1.0)
      sp2 = Species("A(b^1,c^2).A(b^3,c^2).B(b^1).B(b^3)")
      print(sp1.count(sp2))
      print([rr.as_string() for rr in rr1.generate([sp2])])

2
[u'A(b^1,c^2).A(b^3,c^2).B(b^1).B(b^3)>A(b,c^1).A(b^2,c^1).B(b^2)+B(b)|1', u'A(b^1,
↪c^2).A(b^3,c^2).B(b^1).B(b^3)>A(b^1,c^2).A(b,c^2).B(b^1)+B(b)|1']
```

In this case, `ReactionRule.generate` works similarly with `Species.count`. However, `Netfree.query_reaction_rules` returns only one `ReactionRule` with higher kinetic rate:

```
[28]: m1 = NetfreeModel()
      m1.add_reaction_rule(rr1)
      print([rr.as_string() for rr in m1.query_reaction_rules(sp2)])

[u'A(b^1,c^2).A(b^3,c^2).B(b^1).B(b^3)>A(b,c^1).A(b^2,c^1).B(b^2)+B(b)|2']
```

`NetfreeModel.query_reaction_rules` checks if each `ReactionRule` generated is the same with others, and summarizes it if possible.

As explained above, `ReactionRule.generate` matters the order of `Species`, but `Netfree.query_reaction_rules` does not.

```
[29]: sp1 = Species("A(b)")
      sp2 = Species("B(b)")
      rr1 = create_binding_reaction_rule(sp1, sp2, Species("A(b^1).B(b^1)"), 1.0)
      m1 = NetfreeModel()
      m1.add_reaction_rule(rr1)
      print([rr.as_string() for rr in rr1.generate([sp1, sp2])])
      print([rr.as_string() for rr in m1.query_reaction_rules(sp1, sp2)])
      print([rr.as_string() for rr in rr1.generate([sp2, sp1])]) # => []
      print([rr.as_string() for rr in m1.query_reaction_rules(sp2, sp1)])

[u'A(b)+B(b)>A(b^1).B(b^1)|1']
[u'A(b)+B(b)>A(b^1).B(b^1)|1']
[]
[u'B(b)+A(b)>A(b^1).B(b^1)|1']
```

Named wildcards must be consistent in the context while nameless wildcards are not necessarily consistent.

```
[30]: sp1 = Species("_ (b)")
      sp2 = Species("_1 (b)")
      sp3 = Species("A(b)")
      sp4 = Species("B(b)")
      rr1 = create_binding_reaction_rule(sp1, sp1, Species("_ (b^1)._(b^1)"), 1)
      rr2 = create_binding_reaction_rule(sp2, sp2, Species("_1 (b^1)._1 (b^1)"), 1)
      print(sp1.count(sp2)) # => 1
      print(sp1.count(sp3)) # => 1
      print(sp2.count(sp2)) # => 1
      print(sp2.count(sp3)) # => 1
      print([rr.as_string() for rr in rr1.generate([sp3, sp3])])
      print([rr.as_string() for rr in rr1.generate([sp3, sp4])])
      print([rr.as_string() for rr in rr2.generate([sp3, sp3])])
      print([rr.as_string() for rr in rr2.generate([sp3, sp4])]) # => []
```

```

1
1
1
1
[u'A(b)+A(b)>A(b^1) .A(b^1) |1']
[u'A(b)+B(b)>A(b^1) .B(b^1) |1']
[u'A(b)+A(b)>A(b^1) .A(b^1) |1']
[]

```

1.8 8. More about 1. Brief Tour of E-Cell4 Simulations

Once you read through [1. Brief Tour of E-Cell4 Simulations](#), it is NOT difficult to use `World` and `Simulator`. `volume` and `{'C': 60}` is equivalent of the `World` and solver is the `Simulator` below.

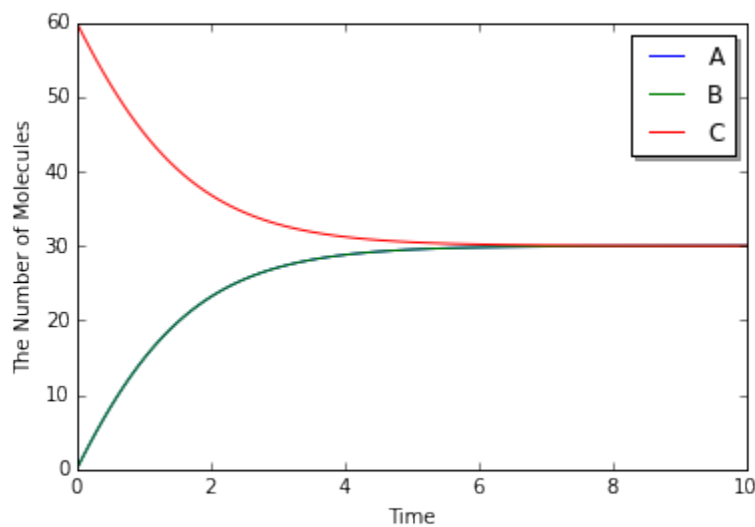
```

[1]: %matplotlib inline
from ecell4 import *

with reaction_rules():
    A + B == C | (0.01, 0.3)

y = run_simulation(10.0, {'C': 60}, volume=1.0)

```



Here we give you a breakdown for `run_simulation`. `run_simulation` use ODE simulator by default, so we create `ODEWorld` step by step.

1.8.1 8.1. Creating ODEWorld

You can create `World` like this.

```

[2]: w = ode.ODEWorld(Real3(1, 1, 1))

```

`Real3` is a coordinate vector. In this example, the first argument for `ODEWorld` constructor is a cube. Note that you can NOT use `volume` for `ode.ODEWorld` argument, like `run_simulation` argument.

Now you created a cube box for simulation, next let's throw molecules into the cube.

```
[3]: w = ode.ODEWorld(Real3(1, 1, 1))
w.add_molecules(Species('C'), 60)
print(w.t(), w.num_molecules(Species('C'))) # must return (0.0, 60)

(0.0, 60)
```

Use `add_molecules` to add molecules, `remove_molecules` to remove molecules, `num_molecules` to know the number of molecules. First argument for each method is the `Species` you want to know. You can get current time by `t` method. However the number of molecules in ODE solver is real number, in these `_molecules` functions work only for integer number. When you handle real numbers in ODE, use `set_value` and `get_value`.

1.8.2 8.2. How to Use Real3

Before the detail of `Simulator`, we explaining more about `Real3`.

```
[4]: pos = Real3(1, 2, 3)
print(pos) # must print like <ecell4.core.Real3 object at 0x7f44e118b9c0>
print(tuple(pos)) # must print (1.0, 2.0, 3.0)

<ecell4.core.Real3 object at 0x7f05b0e6f630>
(1.0, 2.0, 3.0)
```

You can not print the contents in `Real3` object directly. You need to convert `Real3` to Python tuple or list once.

```
[5]: pos1 = Real3(1, 1, 1)
x, y, z = pos[0], pos[1], pos[2]
pos2 = pos1 + pos1
pos3 = pos1 * 3
pos4 = pos1 / 5
print(length(pos1)) # must print 1.73205080757
print(dot_product(pos1, pos3)) # must print 9.0

1.73205080757
9.0
```

You can use basic function like `dot_product`. Of course, you can convert `Real3` to numpy array too.

```
[6]: import numpy
a = numpy.asarray(tuple(Real3(1, 2, 3)))
print(a) # must print [ 1.  2.  3.]

[ 1.  2.  3.]
```

`Integer3` represents a triplet of integers.

```
[7]: g = Integer3(1, 2, 3)
print(tuple(g))

(1, 2, 3)
```

Of course, you can also apply simple arithmetics to `Integer3`.

```
[8]: print(tuple(Integer3(1, 2, 3) + Integer3(4, 5, 6))) # => (5, 7, 9)
print(tuple(Integer3(4, 5, 6) - Integer3(1, 2, 3))) # => (3, 3, 3)
print(tuple(Integer3(1, 2, 3) * 2)) # => (2, 4, 6)
print(dot_product(Integer3(1, 2, 3), Integer3(4, 5, 6))) # => 32
print(length(Integer3(1, 2, 3))) # => 3.74165738677
```



```
(5, 7, 9)
(3, 3, 3)
(2, 4, 6)
32
3.74165738677
```

1.8.3 8.3. Creating and Running ODESimulator

You can create a Simulator with Model and World like

```
[9]: with reaction_rules():
      A + B > C | 0.01 # equivalent to create_binding_reaction_rule
      C > A + B | 0.3  # equivalent to create_unbinding_reaction_rule

m = get_model()

sim = ode.ODESimulator(m, w)
sim.run(10.0)
```

then call run method, the simulation will run. In this example the simulation runs for 10seconds.

You can check the state of the World like this.

```
[10]: print(w.t(), w.num_molecules(Species('C'))) # must return (10.0, 30)

(10.0, 30)
```

You can see that the number of the Species C decreases from 60 to 30.

World describes the state of a timepoint, so you can NOT see the transition of the simulation with the World. To obtain the time-series result, use Observer.

```
[11]: w = ode.ODEWorld(Real3(1, 1, 1))
      w.add_molecules(Species('C'), 60)
      sim = ode.ODESimulator(m, w)

      obs = FixedIntervalNumberObserver(0.1, ('A', 'C'))
      sim.run(10.0, obs)
      print(obs.data()) # must return [[0.0, 0.0, 60.0], ..., [10.0, 29.994446899691276,
      ↪ 30.005553100308752]]

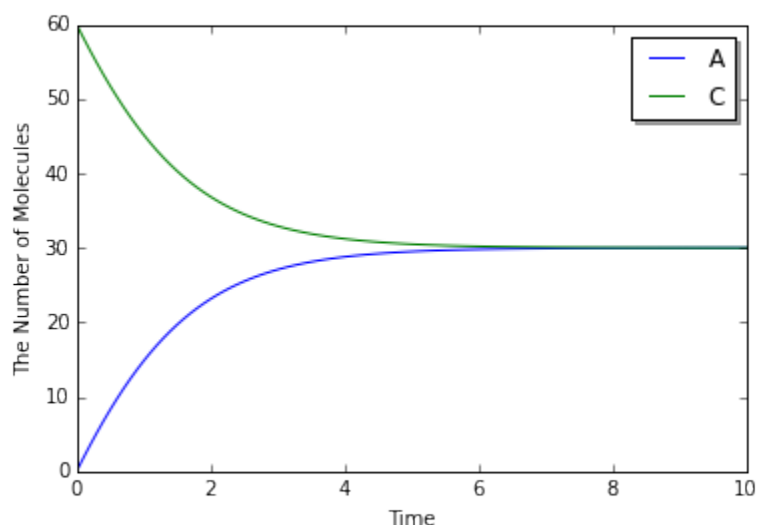
[[0.0, 0.0, 60.0], [0.1, 1.7722206098711988, 58.227779390128795], [0.2, 3.
↪ 4860124889661757, 56.51398751103382], [0.30000000000000004, 5.1376332715496495, 54.
↪ 862366728450354], [0.4, 6.724090809612153, 53.27590919038786], [0.5, 8.
↪ 243129756755453, 51.75687024324456], [0.6000000000000001, 9.69320376680592, 50.
↪ 3067962331941], [0.7000000000000001, 11.073435590968808, 48.92656440903121], [0.8,
↪ 12.383567691608423, 47.616432308391595], [0.9, 13.62390591657045, 46.
↪ 37609408342957], [1.0, 14.795258681171735, 45.20474131882829], [1.1, 15.
↪ 898873899780316, 44.10112610021971], [1.2000000000000002, 16.936375633755194, 43.
↪ 06362436624483], [1.3, 17.90970211303103, 42.090297886969], [1.4000000000000001, 18.
↪ 821046466966358, 41.17895353303366], [1.5, 19.67280118133671, 40.32719881866331],
↪ [1.6, 20.46750699887015, 39.53249300112988], [1.7000000000000002, 21.
↪ 207806714875233, 38.792193285124796], [1.8, 21.896404094818397, 38.10359590518163],
↪ [1.9000000000000001, 22.536027939969333, 37.463972060030684], [2.0, 23.
↪ 129401186565122, 36.8705988134349], [2.1, 23.679214801318086, 36.320785198681946],
↪ [2.2, 24.188106157761755, 35.81189384223828], [2.3000000000000003, 24.
↪ 658641522840725, 35.34135847715931], [2.4000000000000004, 25.093302252968826, 34.
↪ 9066977470312], [2.5, 25.49447428958285, 34.50552571041718], [2.6, 25.
↪ 86444054777012, 34.13555945222991], [2.7, 26.205375806607968, 33.79462419339207],
↪ [2.8000000000000003, 26.51934373464207, 33.48065626535796], [2.9000000000000004, 26.
↪ 80829570797557, 33.19170429202446], [3.0, 27.07407111744664, 32.92592888255339], [3.
↪ 1, 27.318398885233666, 32.68160111476636], [3.2, 27.542899949227504, 32.
↪ 457100050772524], [3.3000000000000003, 27.749090501388586, 32.25090949861144], [3.
↪ 40000000000000004, 27.938385796523626, 32.0616142034764], [3.5, 28.112104375214862,
↪ 31.88789562478517], [3.6, 28.271472567998387, 31.728527432001645], [3.7, 28.
```

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There are several types of Observers for E-Cell4. `FixedIntervalNumberObserver` is the simplest Observer to obtain the time-series result. As its name suggests, this Observer records the number of molecules for each time-step. The 1st argument is the time-step, the 2nd argument is the molecule types. You can check the result with `data` method, but there is a shortcut for this.

```
[12]: viz.plot_number_observer(obs)
```



This plots the time-series result easily.

We explained the internal of `run_simulation` function. When you change the World after creating the Simulator, you need to indicate it to Simulator. So do NOT forget to call `sim.initialize()` after that.

1.8.4 8.4. Switching the Solver

It is NOT difficult to switch the solver to stochastic method, as we showed `run_simulation`.

```
[13]: from ecell4 import *

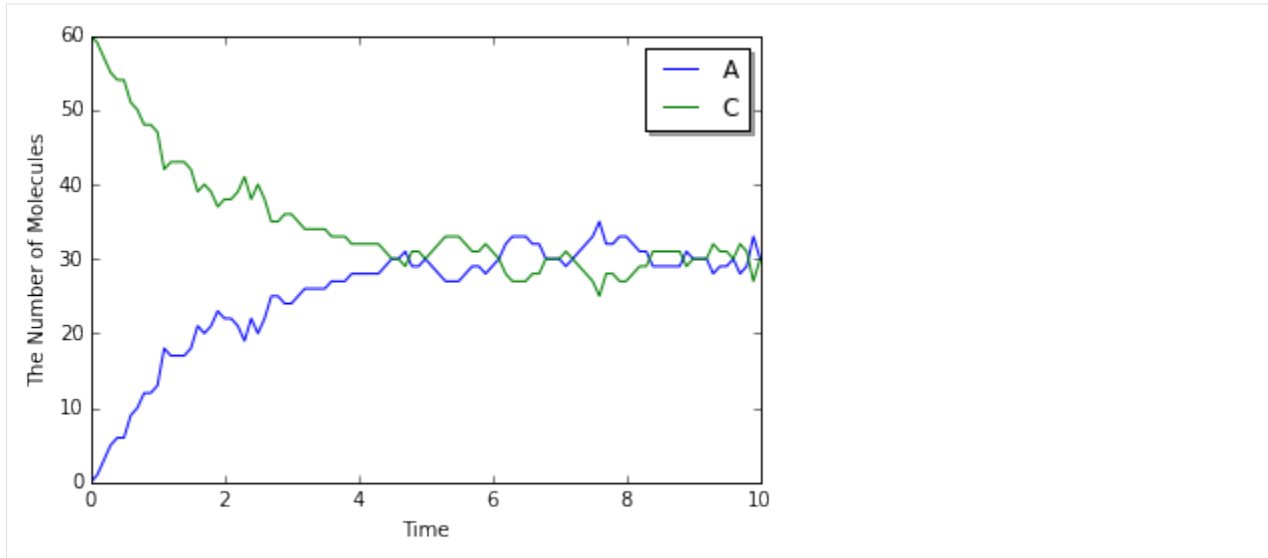
with reaction_rules():
    A + B == C | (0.01, 0.3)

m = get_model()

# ode.ODEWorld -> gillespie.GillespieWorld
w = gillespie.GillespieWorld(Real3(1, 1, 1))
w.add_molecules(Species('C'), 60)

# ode.ODESimulator -> gillespie.GillespieSimulator
sim = gillespie.GillespieSimulator(m, w)
obs = FixedIntervalNumberObserver(0.1, ('A', 'C'))
sim.run(10.0, obs)

viz.plot_number_observer(obs)
```



World and Simulator never change the Model itself, so you can switch several Simulators for 1 Model.

1.9 9. Spatial Gillespie Method

1.9.1 9.1. Spaces in E-Cell4

What the space in E-Cell4 looks like?

```
[1]: from ecell4 import *

w1 = ode.ODEWorld(Real3(1, 1, 1))
w2 = gillespie.GillespieWorld(Real3(1, 1, 1))
```

We created a cube size, 1, on a side for ODEWorld and GillespieWorld. In this case the volume only matters, that is

```
[2]: w3 = ode.ODEWorld(Real3(2, 0.5, 1)) # is almost equivalent to 'w1'
w4 = gillespie.GillespieWorld(Real3(2, 2, 0.25)) # is almost equivalent to 'w2'
```

This returns the same results. Because the volume is same as 1.

This seems reasonable in homogeneous system, but the cell is NOT homogeneous. So we need to consider a space for molecular localization.

You can use several types of space and simulation methods in E-Cell4. We show an example with spatial Gillespie method here.

1.9.2 9.2. Spatial Gillespie Method

In E-Cell4, the Spatial Gillespie method is included in meso module. Let's start with `run_simulation` like ode.

```
[3]: %matplotlib inline
import numpy
from ecell4 import *
```

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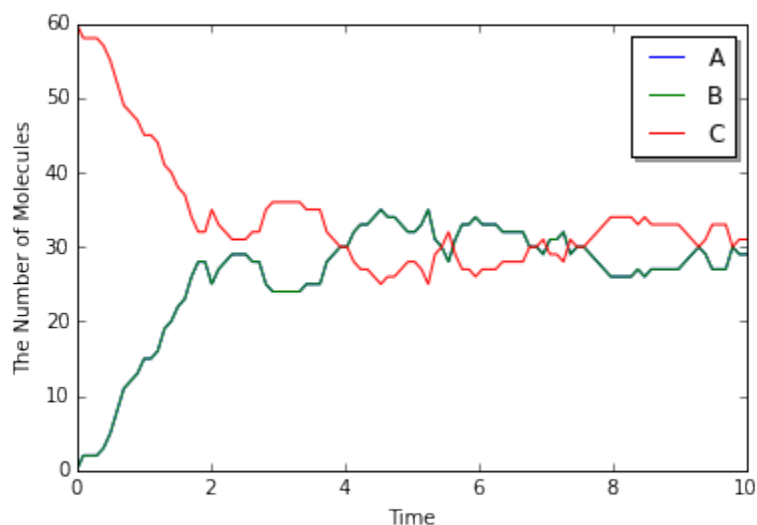
(continued from previous page)

```

with reaction_rules():
    A + B == C | (0.01, 0.3)

y = run_simulation(numpy.linspace(0, 10, 100), {'C': 60}, solver='meso')

```



At the steady state, the number of C is given as follows:

$$\begin{aligned}\frac{dC}{dt} &= 0.01 \cdot \frac{A}{V} \cdot \frac{B}{V} - 0.3 \cdot \frac{C}{V} = 0 \\ 0.01 (60 - C)^2 &= 0.3C \times V \\ C &= 30.\end{aligned}$$

You will obtain almost the same result with ode or gillespie (may take longer time than ode or gillespie). This is not surprising because meso module is almost same with Gillespie unless you give additional spatial parameter.

Next we will decompose run_simulation.

```

[4]: from ecell14 import *

with reaction_rules():
    A + B == C | (0.01, 0.3)

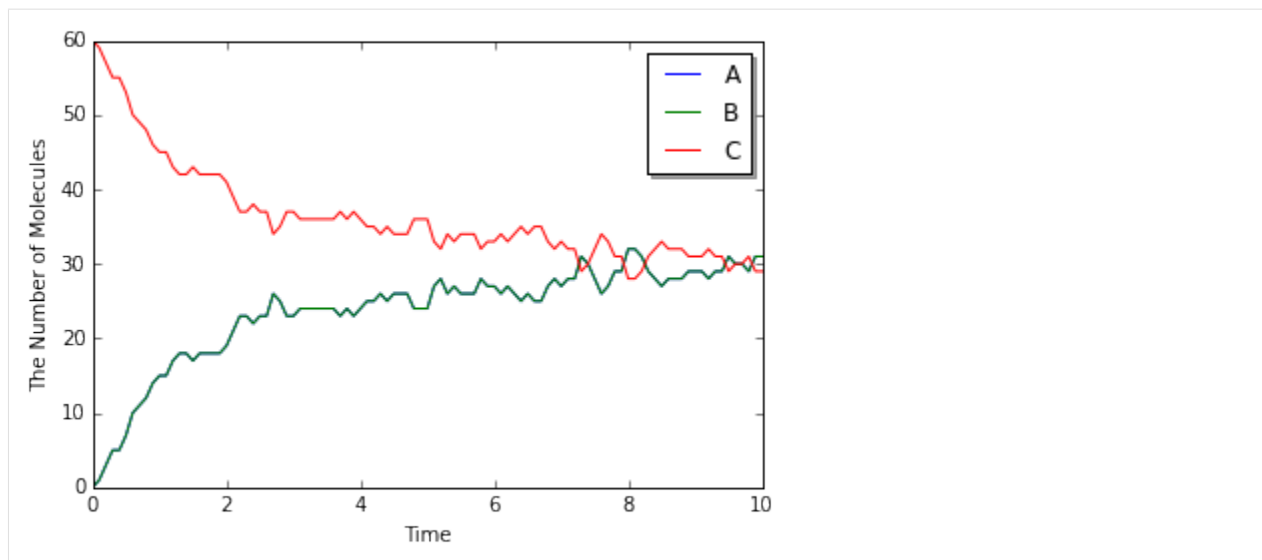
m = get_model()

w = meso.MesoscopicWorld(Real3(1, 1, 1), Integer3(1, 1, 1)) # XXX: Point2
w.bind_to(m) # XXX: Point1
w.add_molecules(Species('C'), 60)

sim = meso.MesoscopicSimulator(w) # XXX: Point1
obs = FixedIntervalNumberObserver(0.1, ('A', 'B', 'C'))
sim.run(10, obs)

viz.plot_number_observer(obs)

```



This is nothing out of the ordinary one except for `MesoscopicWorld` and `MesoscopicSimulator`, but you can see some new elements.

First in `w.bind_to(m)` we associated a `Model` to the `World`. In the basic exercises before, we did NOT do this. In spatial methods, `Species` attributes are necessary. Do not forget to call this. After that, only the `World` is required to create a `MesoscopicSimulator`.

Next, the important difference is the second argument for `MesoscopicWorld`, i.e. `Integer3(1, 1, 1)`. `ODEWorld` and `GillespieWorld` do NOT have this second argument. Before we explain this, let's change this argument and run the simulation again.

```
[5]: from eccl14 import *

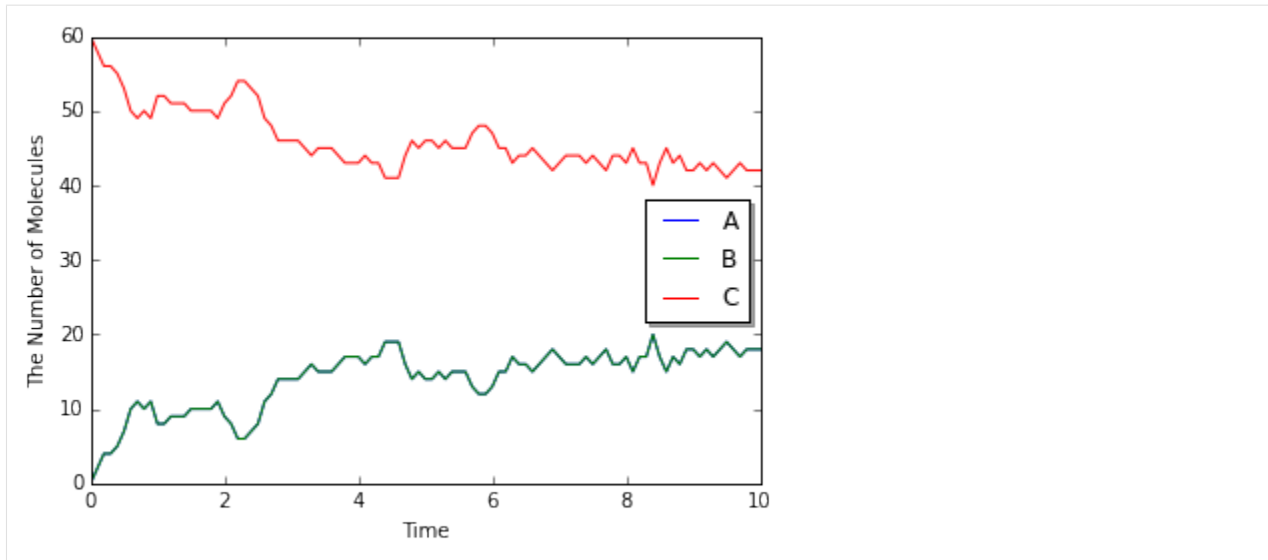
with reaction_rules():
    A + B == C | (0.01, 0.3)

m = get_model()

w = meso.MesoscopicWorld(Real3(1, 1, 1), Integer3(4, 4, 4)) # XXX: Point2
w.bind_to(m) # XXX: Point1
w.add_molecules(Species('C'), 60)

sim = meso.MesoscopicSimulator(w) # XXX: Point1
obs = FixedIntervalNumberObserver(0.1, ('A', 'B', 'C'))
sim.run(10, obs)

viz.plot_number_observer(obs)
```



You must have the different plot. If you increase value in the `Integer3`, you will have more different one.

Actually this second argument means the number of spatical partitions. `meso` is almost same with `gillespie`, but `meso` divides the space into cuboids (we call these cuboids subvolumes) and each subvolume has different molecular concentration by contrast `gillespie` has only one uniform closed space. So in the preceding example, we divided 1 cube with sides 1 into 64 (4x4x4) cubes with sides 0.25. We threw 60 C molecules into the `World`. Thus, each subvolume has 1 species at most.

1.9.3 9.3. Defining Molecular Diffusion Coefficient

Where the difference is coming from? This is because we do NOT consider molecular diffusion coefficient, although we got a space with `meso`. To setup diffusion coefficient, use `Species` attribute 'D' in the way described before (2. [How to Build a Model](#)). As shown in 1. [Brief Tour of E-Cell4 Simulations](#), we use E-Cell4 special notation here.

```
[6]: with species_attributes():
    A | {'D': '1'}
    B | {'D': '1'}
    C | {'D': '1'}

    # A | B | C | {'D': '1'} # means the same as above

get_model()

[6]: <ecell4.core.NetworkModel at 0x7ff0add53c48>
```

You can setup diffusion coefficient with `with species_attributes():` statement. Here we set all the diffusion coefficient as 1. Let's simulate this model again. Now you must have the almost same result with `gillespie` even with large `Integer3` value (the simulation will takes much longer than `gillespie`).

How did the molecular diffusion work for the problem? Think about free diffusion (the diffusion coefficient of a Species is D) in 3D space. The unit of diffusion coefficient is the square of length divided by time like $\mu\text{m}^2/\text{s}$ or $\text{nm}^2/\mu\text{s}$.

It is known that the average of the square of point distance from time 0 to t is equal to $6Dt$. Conversely the average of the time scale in a space with length scale l is about $l^2/6D$.

In the above case, the size of each subvolume is 0.25 and the diffusion coefficient is 1. Thus the time scale is about 0.01 sec. If the molecules of the Species A and B are in the same subvolume, it takes about 1.5 sec to react, so in most cases the diffusion is faster than the reaction and the molecules move to other subvolume even dissociated in the same subvolume. The smaller l , the smaller subvolume's volume l^3 , so the reaction rate after dissociation is faster, and the time of the diffusion and the transition between the subvolume gets smaller too.

1.9.4 9.4. Molecular localization

We have used `add_molecules` function to add molecules to `World` in the same manner as `ode` or `gillespie`. Meanwhile in `MesoscopicWorld`, you can put in molecules according to the spatial presentation.

```
[7]: from ecell14 import *

w = meso.MesoscopicWorld(Real3(1, 1, 1), Integer3(3, 3, 3))
w.add_molecules(Species('A'), 120)
w.add_molecules(Species('B'), 120, Integer3(1, 1, 1))
```

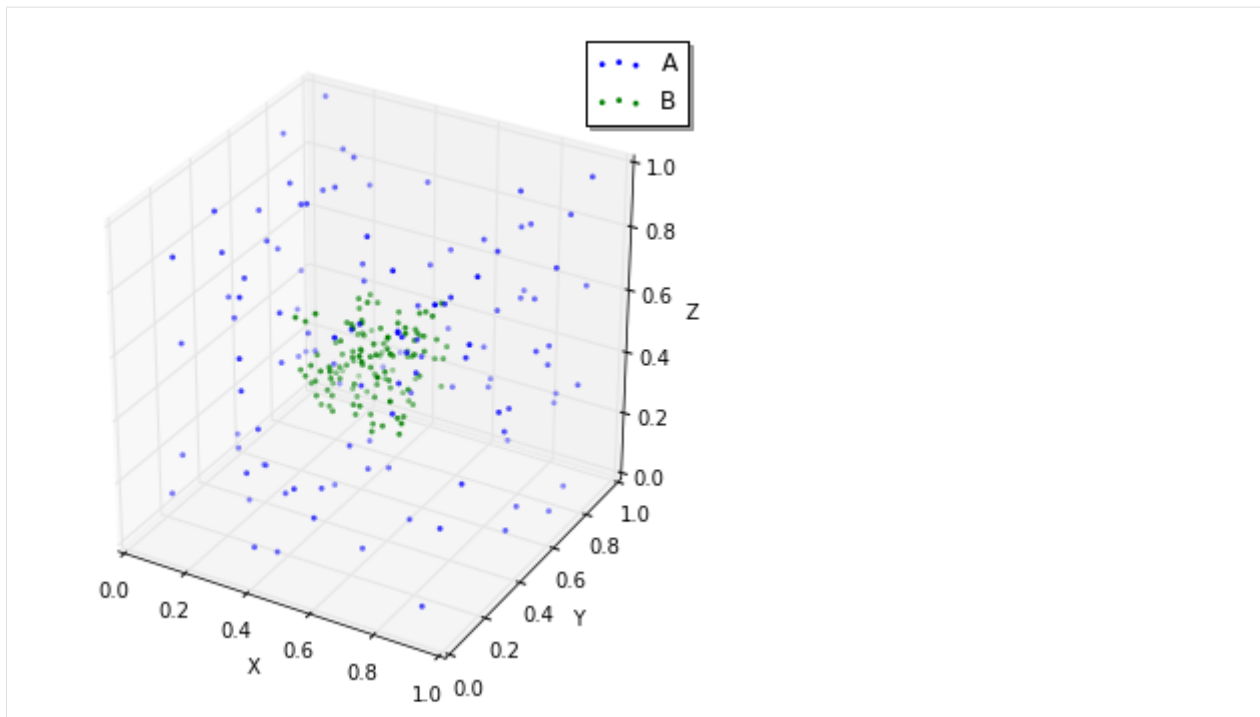
In `MesoscopicWorld`, you can set the subvolume and the molecule locations by giving the third argument `Integer3` to `add_molecules`. In the above example, the molecule type A spreads all over the space, but the molecule type B only locates in a subvolume at the center of the volume. To check this, use `num_molecules` function with a coordinate.

```
[8]: print(w.num_molecules(Species('B'))) # must print 120
      print(w.num_molecules(Species('B'), Integer3(0, 0, 0))) # must print 0
      print(w.num_molecules(Species('B'), Integer3(1, 1, 1))) # must print 120

120
0
120
```

Furthermore, if you have IPython Notebook environment, you can visualize the molecular localization with `ecell14.viz` module.

```
[9]: # viz.plot_world(w, radius=0.01)
      viz.plot_world(w, interactive=False)
```



`viz.plot_world` function visualize the location of the molecules in IPython Notebook cell by giving the `World`. You can set the molecule size with `radius`. Now you can set the molecular localization to the `World`, next let's simulate this. In the above example, we set the diffusion coefficient 1 and the `World` side 1, so 10 seconds is enough to stir this. After the simulation, check the result with calling `viz.plot_world` again.

1.9.5 9.5. Molecular initial location and the reaction

This is an extreme example to check how the molecular localization affects the reaction.

```
[10]: %matplotlib inline
from eccl4 import *

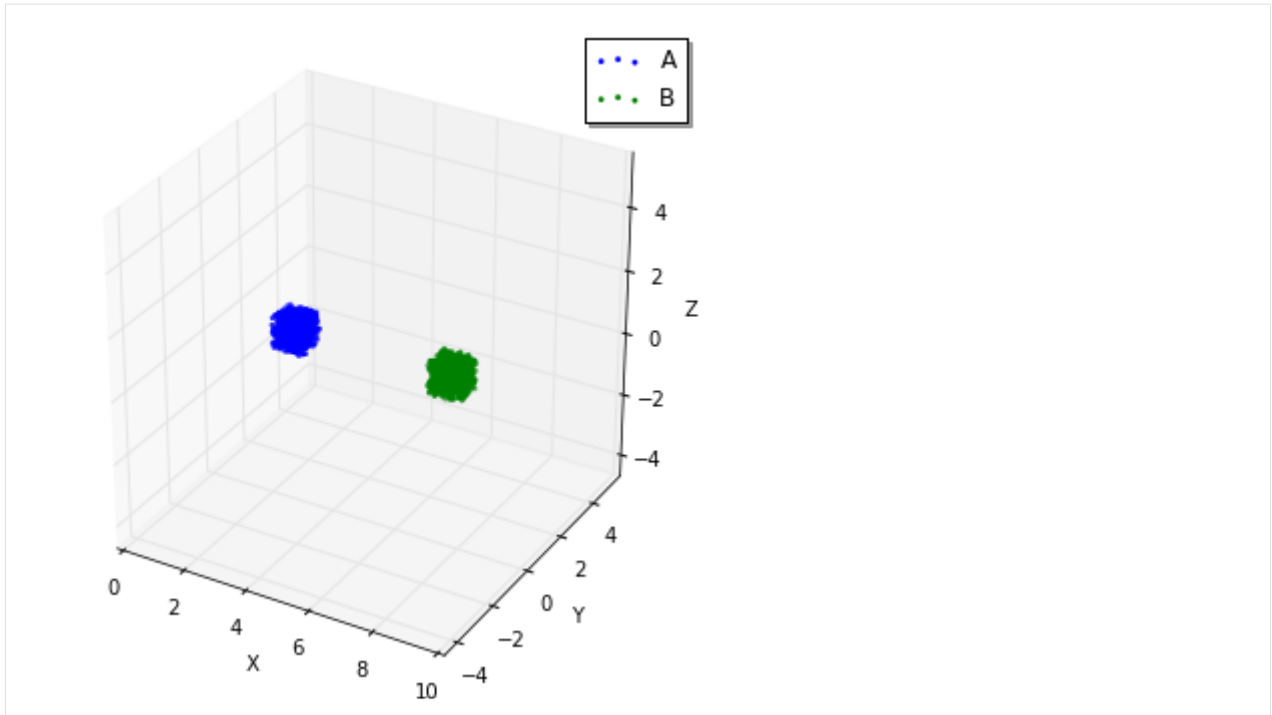
with species_attributes():
    A | B | C | {'D': '1'}

with reaction_rules():
    A + B > C | 0.01

m = get_model()
w = meso.MesoscopicWorld(Real3(10, 1, 1), Integer3(10, 1, 1))
w.bind_to(m)
```

This model consists only of a simple binding reaction. The `World` is a long x axis cuboid, and molecules are located off-center.

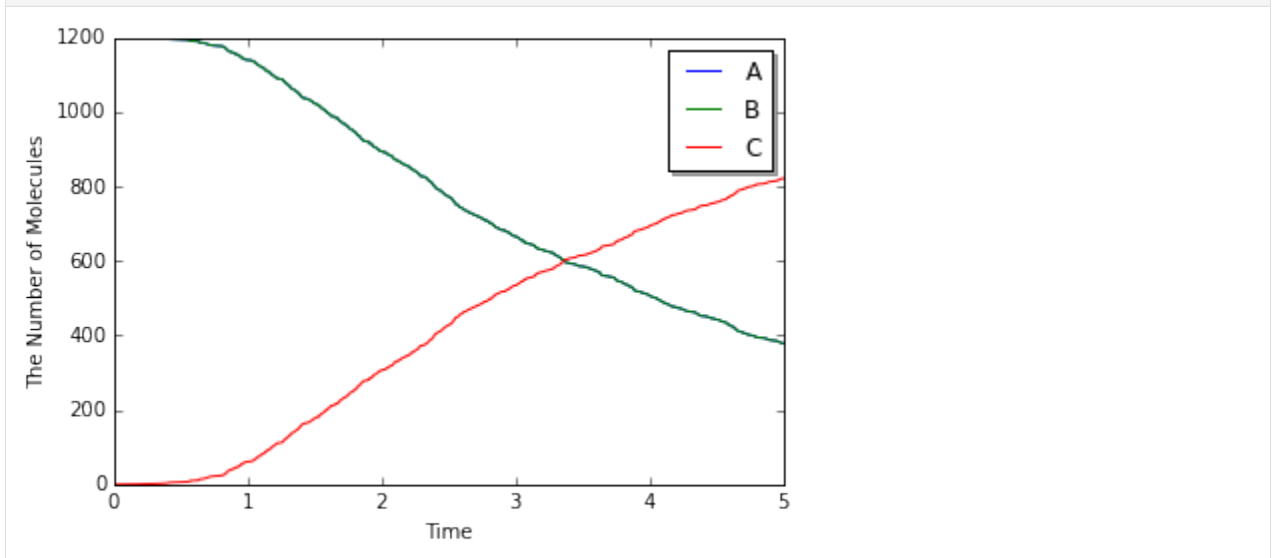
```
[11]: w.add_molecules(Species('A'), 1200, Integer3(2, 0, 0))
w.add_molecules(Species('B'), 1200, Integer3(7, 0, 0))
# viz.plot_world(w, radius=0.025)
viz.plot_world(w, interactive=False)
```

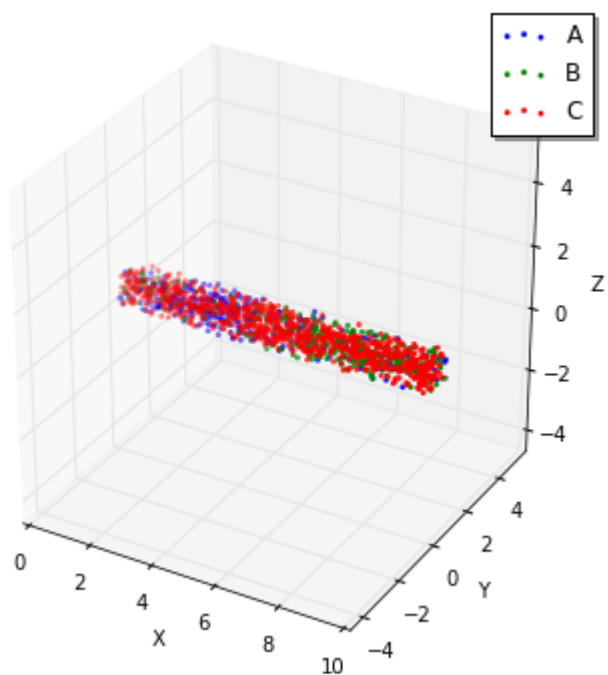
On a different note, there is a reason not to set `Integer3(0, 0, 0)` or `Integer3(9, 0, 0)`. In E-Cell4, basically we adopt periodic boundary condition for everything. So the forementioned two subvolumes are actually adjoining.

After realizing the location expected, simulate it with `MesoscopicSimulator`.

```
[12]: sim = meso.MesoscopicSimulator(w)
      obs1 = NumberObserver(('A', 'B', 'C')) # XXX: saves the numbers after every steps
      sim.run(5, obs1)
      viz.plot_number_observer(obs1)
```



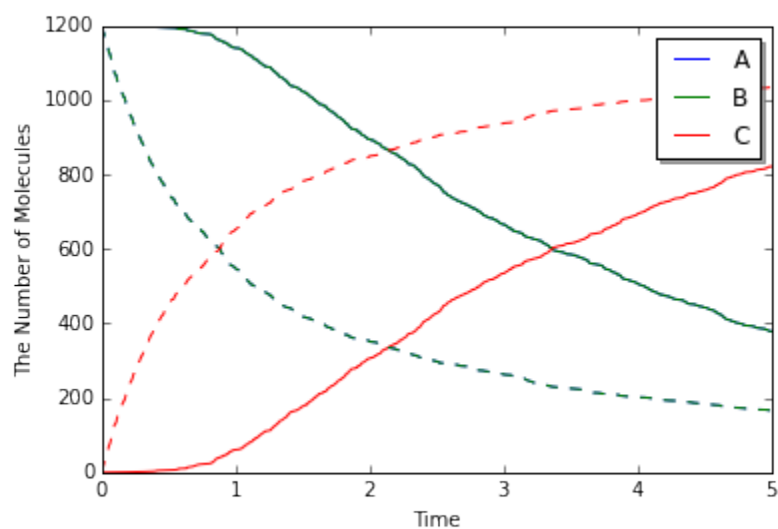
```
[13]: # viz.plot_world(w, radius=0.025)
      viz.plot_world(w, interactive=False)
```



To check the effect of initial coordinates, we recommend that you locate the molecules homogeneously with `meso` or simulate with `gillespie`.

```
[14]: w = meso.MesoscopicWorld(Real3(10, 1, 1), Integer3(10, 1, 1))
w.bind_to(m)
w.add_molecules(Species('A'), 1200)
w.add_molecules(Species('B'), 1200)

sim = meso.MesoscopicSimulator(w)
obs2 = NumberObserver(['A', 'B', 'C']) # XXX: saves the numbers after every steps
sim.run(5, obs2)
viz.plot_number_observer(obs1, "-", obs2, "--")
```



The solid line is biased case, and the dash line is non-biased. The biased reaction is obviously slow. And you may notice that the shape of time-series is also different between the solid and dash lines. This is because it takes some time for the molecule A and B to collide due to the initial separation. Actually it takes $4^2/2(D_A + D_B) = 4$ seconds to move the initial distance between A and B (about 4).

1.10 10. Spatiocyte Simulations at Single-Molecule Resolution

We showed an example of E-Cell4 spatial representation.

Next let's simulate the models with more detailed spatial representation called "single molecule resolution".

```
[1]: %matplotlib inline
from ecell4 import *
```

1.10.1 10.1. Spatiocyte Lattice-based Method

In spatial Gillespie method, we divided the `Space` into smaller `Space`, then we diffuse the molecules in the subvolumes. However, we treated the molecules in each subvolume just as the number of the molecules, and the location of the molecules are NOT determined.

In other words, the spatial resolution of spatial Gillespie method is equal to the side of a subvolume l . To improve this resolution, we need to make the size of l small. But in this method the l must be larger than the (at least) 10 times the diameter of molecule R .

How can we improve the spatial resolution to the size of the molecule? The answer is the simulation with single-molecule resolution. This method simulate the molecule not with the number of the molecules, but with the spatial reaction diffusion of each molecule.

E-Cell4 has multiple single-molecule resolution method, here we explain about Spatiocyte lattice-based method. Spatiocyte treats each molecule as hard spheres, and diffuses the molecules on hexagonal close-packed lattice.

Spatiocyte has an ID for each molecule and the position of the molecule with single-molecule resolution. For the higher spatial resolution, Spatiocyte has 100 times smaller time-step than spatial Gillespie, because the time scale of diffusion increases with the square of the distance.

Next, let's try the Spatiocyte method.

```
[2]: with species_attributes():
      A | B | C | {'D': '1'}

      with reaction_rules():
          A + B == C | (0.01, 0.3)

m = get_model()

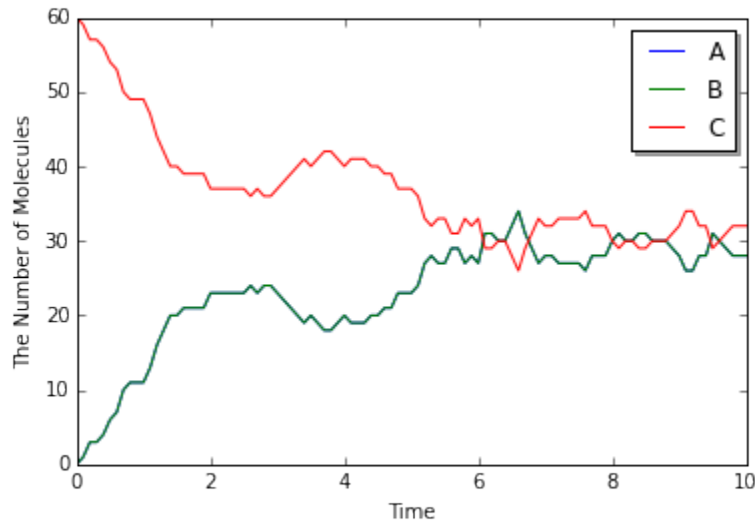
w = spatiocyte.SpatiocyteWorld(Real3(1, 1, 1), 0.005) # The second argument is
↳ 'voxel_radius'.
w.bind_to(m)
w.add_molecules(Species('C'), 60)

sim = spatiocyte.SpatiocyteSimulator(w)
obs = FixedIntervalNumberObserver(0.1, ('A', 'B', 'C'))
sim.run(10, obs)
```

There is a distinct difference in the second argument for `SpatiocyteWorld`. This is called `voxel radius`. `Spatiocyte` defines the locations of the molecules with dividing the space with molecule size, and call the minimum unit for this space as `Voxel`.

In most cases the size of the molecule would be good for `voxel radius`. In this example, we set 5 nm as the radius of the molecule in the space with the side 1 μm . It takes more time to simulate, but the result is same with ODE or Gillespie.

```
[3]: viz.plot_number_observer(obs)
```



1.10.2 10.2. The Diffusion Movement of Single Molecule

Next let's simulate single molecule diffusion to check the resolution.

```
[4]: with species_attributes():
      A | {'D': '1'}

m = get_model()

w = spatiocyte.SpatiocyteWorld(Real3(1, 1, 1), 0.005)
w.bind_to(m)

(pid, p), suc = w.new_particle(Species('A'), Real3(0.5, 0.5, 0.5))
```

`new_particle` method tries to place a particle to a coordinate in `SpatiocyteWorld`. It returns the particle's `ParticleID` (`pid`), the `Particle` object (`p`), and the boolean value (`suc`). If `new_particle` succeeds in putting the particle, `suc` will be `True`. If a particle is already placed in the coordinate, you can NOT place a particle over it and `suc` will be `False` and fail.

`p` contains the particle position, species type, radius, and diffusion coefficient. You can inspect the `p` with the particle's ID, `pid`.

Let's check `p` first.

```
[5]: pid, p = w.get_particle(pid)
      print(p.species().serial()) # must print: A
      print(p.radius(), p.D())   # must print: (0.005, 1.0)
      print(tuple(p.position()))  # must print: (0.49806291436591293, 0.49652123150307814,
      ↪ 0.5)
      (continues on next page)
```

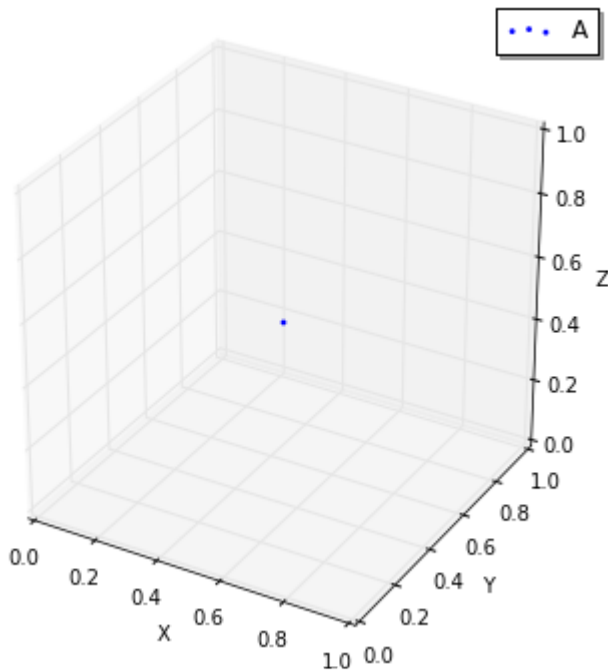
(continued from previous page)

```
A
(0.005, 1.0)
(0.49806291436591293, 0.49652123150307814, 0.5)
```

`get_particle` method receives a particle ID and returns the ID and particle (of course the ID are same with the given one). You can inspect the coordinate of the particle as `Real3` with `position()` method. It is hard to directly read the coordinate, here we printed it after converting to tuple. As you can see the tuple coordinate is slightly different from the original position given as a `Real3`. This is because `Spatiocyte` can place the molecule only on the lattice. `SpatiocyteWorld` places the molecule a center position of the nearest lattice for the argument `Real3`.

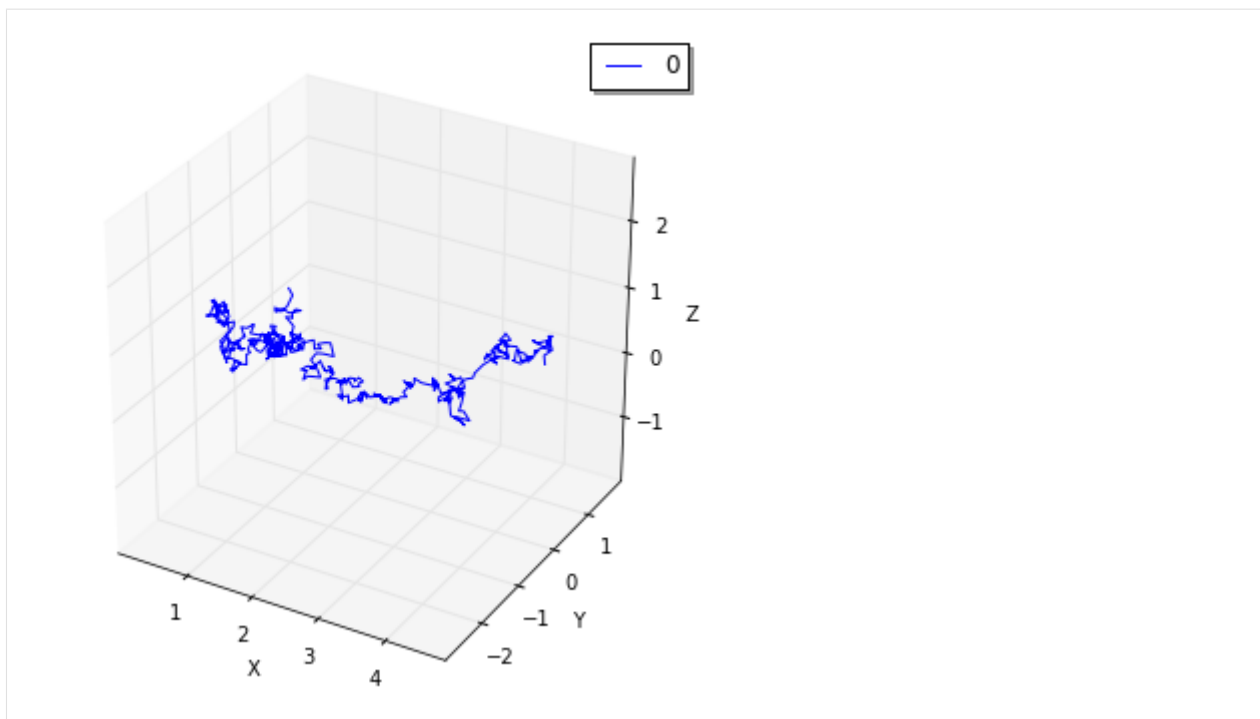
You can visualize the coordinate of the molecule with `viz.plot_world` method, and check the molecule in the center of the World.

```
[6]: viz.plot_world(w, interactive=False)
# viz.plot_world(w)
```



And you can use `FixedIntervalTrajectoryObserver` to track the trajectory of molecular diffusion process.

```
[7]: sim = spatiocyte.SpatiocyteSimulator(w)
obs = FixedIntervalTrajectoryObserver(0.002, (pid,))
sim.run(1, obs)
viz.plot_trajectory(obs, interactive=False)
# viz.plot_trajectory(obs)
```



Here we visualized the trajectory with `viz.plot_trajectory` method, you can also obtain it as `Real3` list with `data()` method.

```
[8]: print(len(obs.data())) # => 1
      print(len(obs.data()[0])) # => 501
```

```
1
501
```

`data()` method returns nested list. First index means the index of the particle. Second index means the index of the `Real3`. In this case we threw just one particle, so the first result is 1, and next 501 means time-series coordinate of the only one particle (initial coordinate and the coordinates in $1/0.002 = 500$ time points).

Also you can obtain the particles in bulk with `list_particles_exact` method and a `Species`.

```
[9]: w.add_molecules(Species('A'), 5)

particles = w.list_particles_exact(Species('A'))
for pid, p in particles:
    print(p.species().serial(), tuple(p.position()))

(u'A', (0.7103520254071217, 0.8256108849411649, 0.88))
(u'A', (0.5062278801751902, 0.034641016151377546, 0.77))
(u'A', (0.4082482904638631, 0.7188010851410841, 0.985))
(u'A', (0.30210373494325865, 0.30599564267050167, 0.68))
(u'A', (0.28577380332470415, 0.26269437248127975, 1.0050000000000001))
(u'A', (0.563382640840131, 0.0202072594216369, 0.545))
```

Please remember `list_particles_exact` method, this method can be used for other `World` as well as `add_molecules` method.

On a different note, in `Spatioocyte` proper method to inspect the single molecule is `list_voxels_exact`, and the coordinate is described with index of voxel (not `Real3`).

1.10.3 10.3 The Diffusion Coefficient and the Second-order Reaction

The models we have addressed contains a second-order reaction. Let's look at the relationship between this second-order reaction and the diffusion coefficient in Spatiocyte.

```
[10]: with species_attributes():
      A | B | C | {'D': '1'}

      with reaction_rules():
          A + B > C | 1.0

      m = get_model()
```

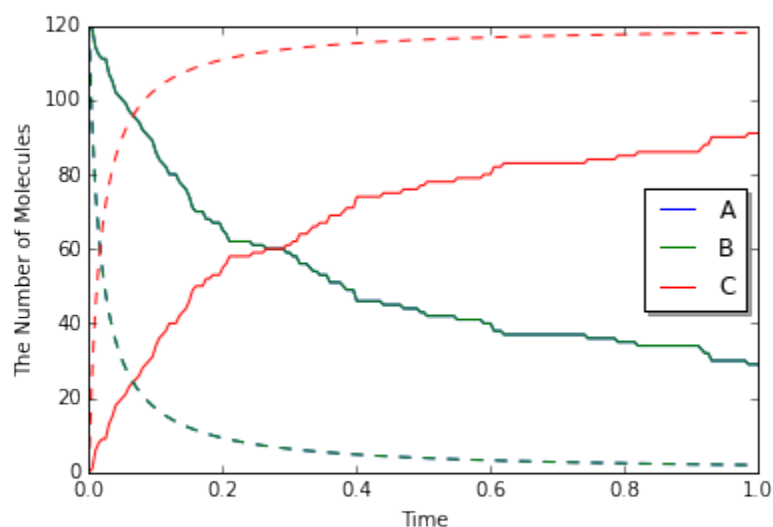
```
[11]: w = spatiocyte.SpatiocyteWorld(Real3(2, 1, 1), 0.005)
      w.bind_to(m)
      w.add_molecules(Species('A'), 120)
      w.add_molecules(Species('B'), 120)

      obs = FixedIntervalNumberObserver(0.005, ('A', 'B', 'C'))
      sim = spatiocyte.SpatiocyteSimulator(w)
      sim.run(1.0, obs)
```

```
[12]: odew = ode.ODEWorld(Real3(2, 1, 1))
      # odew.bind_to(m)
      odew.add_molecules(Species('A'), 120)
      odew.add_molecules(Species('B'), 120)

      odeobs = FixedIntervalNumberObserver(0.005, ('A', 'B', 'C'))
      odesim = ode.ODESimulator(m, odew)
      odesim.run(1.0, odeobs)
```

```
[13]: viz.plot_number_observer(obs, "--", odeobs, "--")
```



Although we used faster kinetic constant than before, the result is same. But by contrast with ODE simulation, you can find the difference between them (solid line is `spatiocyte`, dash line is `ode`). Is this fault of Spatiocyte? (No) Actually Spatiocyte reaction rate couldn't be faster, while ODE reaction rate can be faster infinitely.

This is caused by the difference between the definition of reaction rate constant in ODE solver and single molecule

simulation method. The former is called “macroscopic” or “effective” reaction rate constant, the latter is called “microscopic” or “intrinsic” reaction rate constant.

The “macroscopic” rate represents the reaction rate in mixed molecular state, meanwhile “microscopic” rate represents the reactivity in molecule collision. So in “microscopic” perspective, the first thing molecules need to react is collision. In Spatiocyte, however, you make this “microscopic” rate faster, you can NOT make the actual reaction rate faster than collision rate. This is called “diffusion-limited” condition. This is similar to what the molecules coordinated disproportionately need time to react.

It is known that there is a relationship between this macroscopic rate constant k_{on} and microscopic rate constant k_a in 3D space.

$$\frac{1}{k_{\text{on}}} = \frac{1}{k_a} + \frac{1}{4\pi R D_{\text{tot}}},$$

where R is the sum of two molecule’s radius in collision, D_{tot} is the sum of diffusion coefficients.

In the case of the above Jupyter Notebook cell, $k_D = 4\pi R D_{\text{tot}}$ is almost 0.25 and “microscopic” rate constant is 1.0. So the “macroscopic” rate constant is almost 0.2. (However unless you specify the configuration for Spatiocyte, the second order reaction rate must be slower than $3\sqrt{2}RD$, and the dissociation constant k_D is also $3\sqrt{2}RD$.) The single molecule simulation method can separate molecular “diffusion” and “reaction” in accurate manner contrary to ODE or Gillespie method supposed well mixed system (that is diffusion coefficient is infinite). However if the microscopic rate constant k_D is small enough, the macroscopic rate constant is almost equal to microscopic one (reaction late-limit).

1.10.4 10.4. The Structure in the Spatiocyte Method

Next we explain a way to create a structure like cell membrane. Although The structure feature in E-Cell4 is still in development, Spatiocyte supports the structure on some level. Let’s look a sphere structure as an example.

To restrict the molecular diffusion inside of the sphere, first we create it.

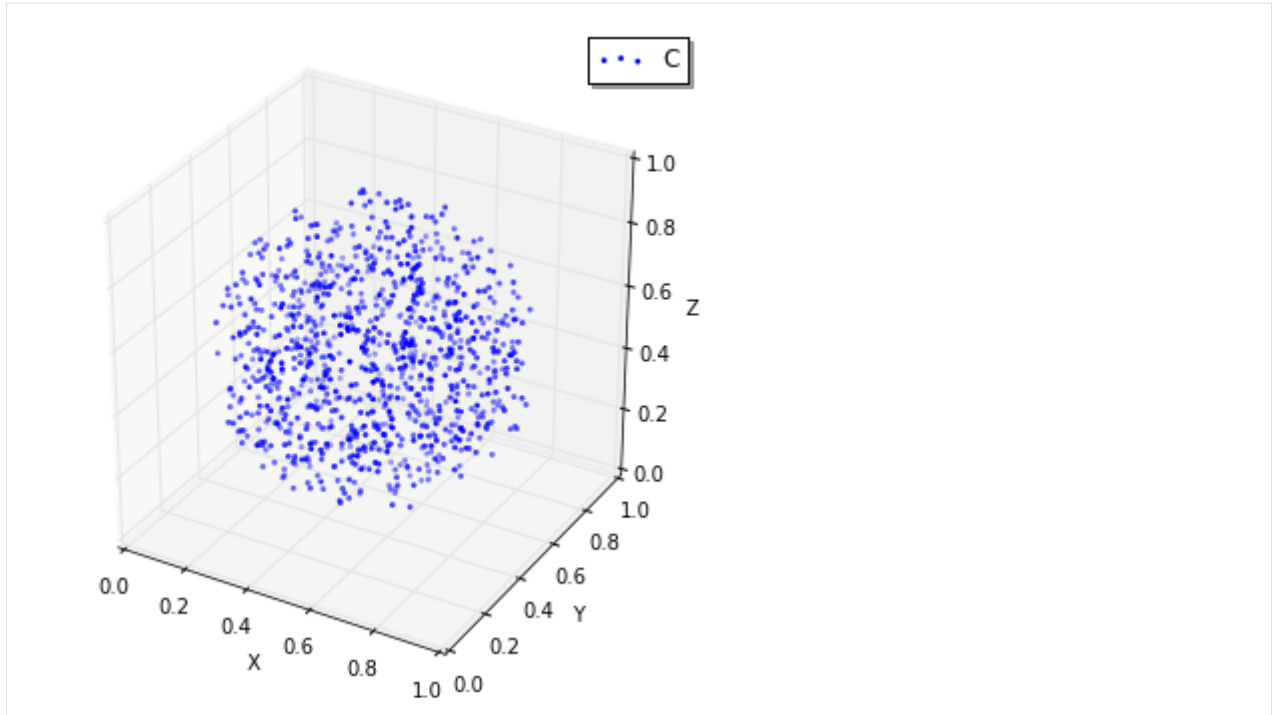
```
[14]: with species_attributes():
      A | {'D': '1', 'location': 'C'}

m = get_model()

[15]: w = spatiocyte.SpatiocyteWorld(Real3(1, 1, 1), 0.005)
      w.bind_to(m)
      sph = Sphere(Real3(0.5, 0.5, 0.5), 0.45)
      print(w.add_structure(Species('C'), sph)) # will print 539805
539805
```

Visualize the state of the World.

```
[16]: viz.plot_world(w, interactive=False)
      # viz.plot_world(w)
```

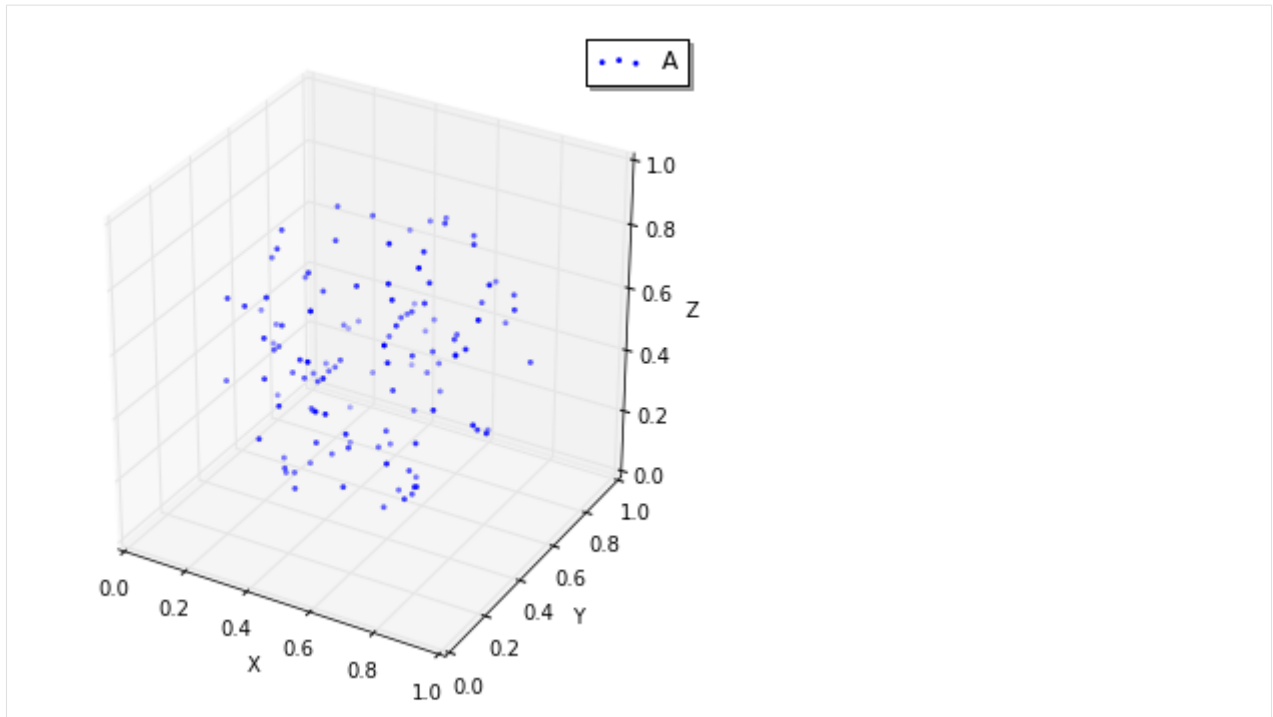
The `Sphere` class first argument is the center of the sphere, and second argument is the radius. Then we created a `Species` named `C` and added it inside the `Sphere`. The structure in the `Spatiocyte` method is described by filling the space with the `Voxel`. In the example above, the `Voxels` in the sphere are occupied with `Species` named `C`.

You can see those distribution with `viz.plot_world` as above. (However, the number of the species is too large to visualize all. So we plot only a part of it, but actually the sphere is fully occupied with the `Species`.)

Next we create `Species` moving inside this sphere. To that end we give `location` attribute to the `Species`. After that, you just throw-in molecules to the `World` with `add_molecules` function.

```
[17]: w.add_molecules(Species('A'), 120)
```

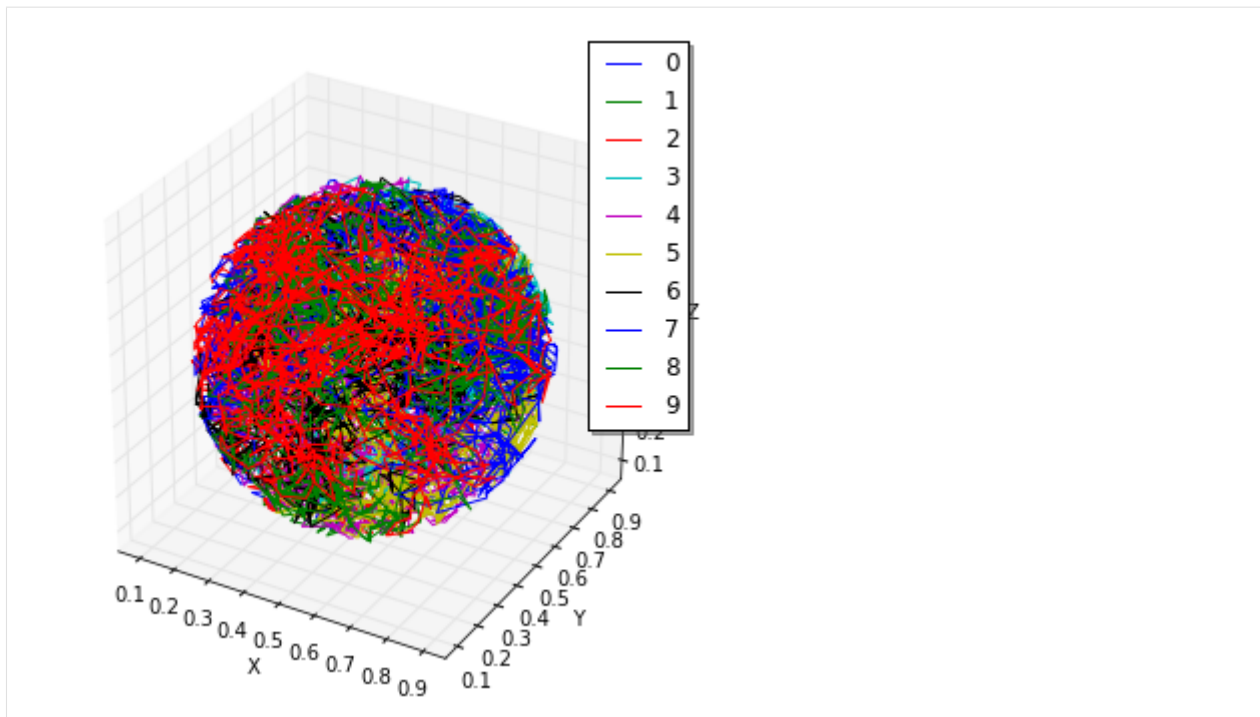
```
[18]: viz.plot_world(w, species_list=('A',), interactive=False) # visualize A-molecules_
      ↪ only
      # viz.plot_world(w, species_list=('A',)) # visualize A-molecules only
```



Now we restricted the trajectories of Species A on the structure of Species C, and `add_molecules` works like that. As a note, you need to create the structure before `add_molecule`.

We can use `FixedIntervalTrajectoryObserver` to check the restriction of the diffusion area.

```
[19]: pid_list = [pid for pid, p in w.list_particles(Species('A'))[: 10]]
obs = FixedIntervalTrajectoryObserver(1e-3, pid_list)
sim = spatiocyte.SpatiocyteSimulator(w)
sim.run(1, obs)
viz.plot_trajectory(obs, interactive=False)
# viz.plot_trajectory(obs)
```



`pid_list` is a list of the first 10 ParticleIDs of A molecules. The trajectories are colored by this 10 species. Certainly the trajectories are restricted in the sphere.

1.10.5 10.5 The structure and the reaction

At the end, we explain about molecular translocation among the structures.

A Species without `location` attribute is not a member of any structures. In the example above, if you do NOT write `location` attribute with Species A, A is placed outside of the sphere.

Next let's create a planar surface structure. To create a surface, we need to use three `Real3`, those are original point (origin) and two axis vector (`unit0`, `unit1`): `ps = PlanarSurface(origin, unit0, unit1)`.

Suppose Species A on the surface, `ps`, and a normal Species B.

```
[20]: with species_attributes():
      A | {'D': '0.1', 'location': 'M'}
      B | {'D': '1'}

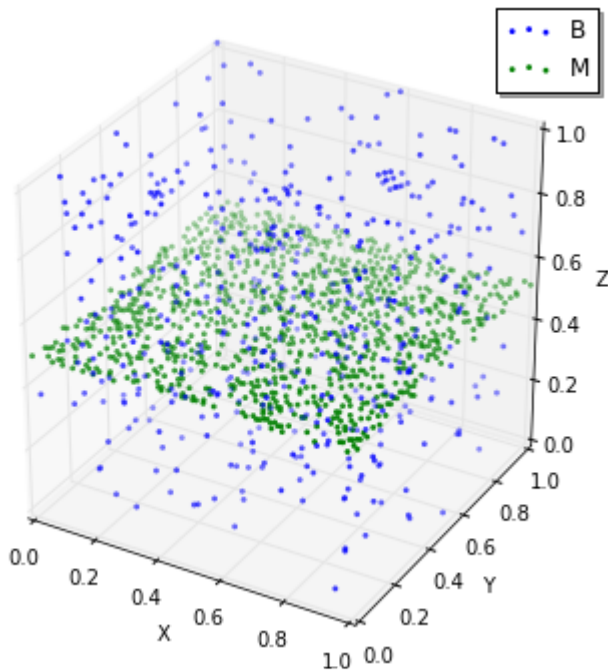
m = get_model()

w = spatiocyte.SpatiocyteWorld(Real3(1, 1, 1))
w.bind_to(m)

origin = Real3(0, 0, 0.5)
unit0 = Real3(1, 0, 0)
unit1 = Real3(0, 1, 0)
w.add_structure(
    Species('M'), PlanarSurface(origin, unit0, unit1)) # Create a structure first

w.add_molecules(Species('B'), 480) # Throw-in B-molecules
```

```
[21]: viz.plot_world(w, species_list=('B', 'M'), interactive=False)
# viz.plot_world(w, species_list=('B', 'M'))
```



It might be hard to see them, but actually the Species B are placed only not on a surface. Then how can we make absorbed this Species B to a surface M and synthesize a Species A?

```
[22]: with species_attributes():
    A | {'D': '0.1', 'location': 'M'}
    B | {'D': '1'}

with reaction_rules():
    B + M == A | (1.0, 1.5)

m = get_model()
```

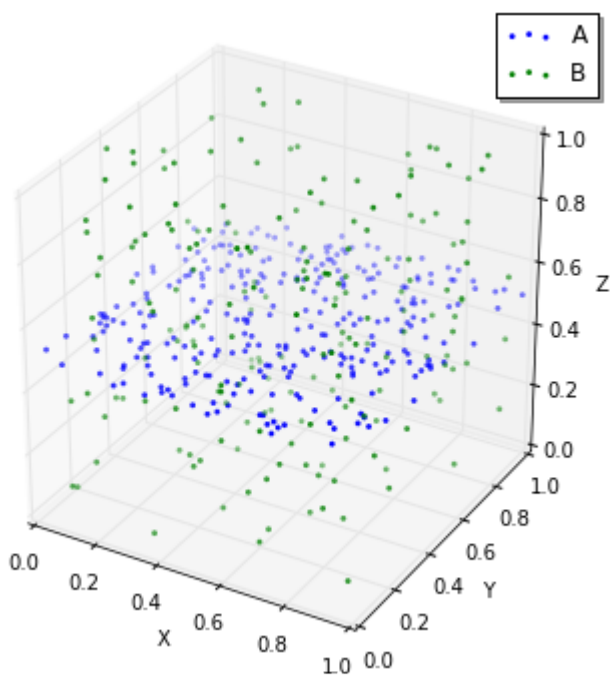
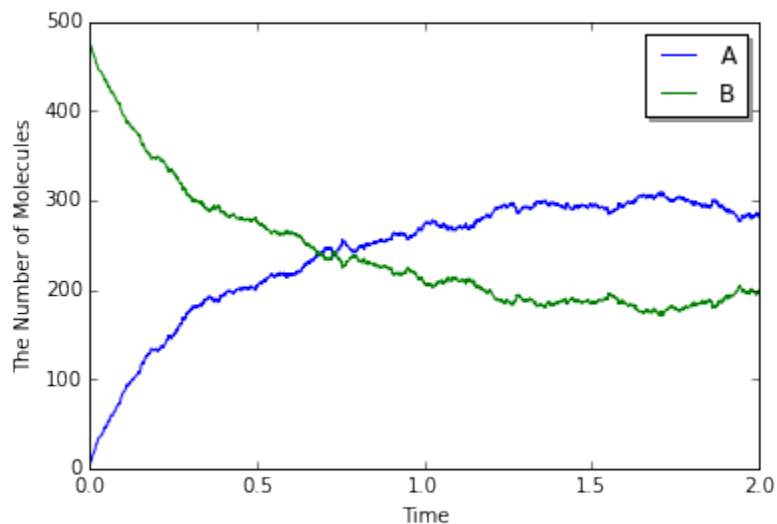
This means that a Species B becomes A when B collides with a structure M. On the other hand, a species A dissociates from the structure, and becomes M and B on as the reverse reaction direction.

Now you can simulate this model with a structure.

```
[23]: w.bind_to(m)

sim = spatiocyte.SpatiocyteSimulator(w)
obs = NumberObserver(('A', 'B'))
sim.run(2, obs)
```

```
[24]: viz.plot_number_observer(obs)
viz.plot_world(w, species_list=('A', 'B'), interactive=False)
# viz.plot_world(w, species_list=('A', 'B'))
```



In the dissociation from a structure, you can skip to write the structure. Thus, $A > B$ just means the same as $A > B + M$ in the above. But in the binding, you can **NOT**. Because it is impossible to create A from B with no M around there. By contrast the species A wherever on the sphere M can create the species B. The first order reaction occurs in either presence or absence of the structure. But, in the case of the binding, the second order reaction turns into the first order reaction and the meaning of rate constant also changes if you ignore M in the left-hand side.

EXAMPLES

2.1 Attractors

```
[1]: %matplotlib inline
import numpy
from eccl14 import *
util.decorator.ENABLE_RATELAW = True
```

2.1.1 Rössler attractor

```
[2]: a, b, c = 0.2, 0.2, 5.7

with reaction_rules():
    ~x > x | (-y - z)
    ~y > y | (x + a * y)
    ~z > z | (b + z * (x - c))

[3]: run_simulation(numpy.linspace(0, 200, 4001), y0={'x': 1.0}, return_type='nyaplot',
                    opt_args={'x': 'x', 'y': ('y', 'z'), 'to_png': True})

<IPython.core.display.HTML object>
```

2.1.2 Modified Chua chaotic attractor

```
[4]: alpha, beta = 10.82, 14.286
a, b, d = 1.3, 0.1, 0.2

with reaction_rules():
    h = -b * sin(numpy.pi * x / (2 * a) + d)
    ~x > x | (alpha * (y - h))
    ~y > y | (x - y + z)
    ~z > z | (-beta * y)

[5]: run_simulation(numpy.linspace(0, 250, 5001),
                    y0={'x': 0, 'y': 0.49899, 'z': 0.2}, return_type='nyaplot',
                    opt_args={'x': 'x', 'y': 'y', 'to_png': True})

<IPython.core.display.HTML object>
```

2.1.3 Lorenz system

```
[6]: p, r, b = 10, 28, 8.0 / 3

with reaction_rules():
    ~x > x | (-p * x + p * y)
    ~y > y | (-x * z + r * x - y)
    ~z > z | (x * y - b * z)

[7]: run_simulation(numpy.linspace(0, 25, 2501),
                    y0={'x': 10, 'y': 1, 'z': 1}, return_type='nyaplot',
                    opt_args={'x': 'x', 'y': ('y', 'z'), 'to_png': True})

<IPython.core.display.HTML object>
```

2.1.4 Tamari attractor

```
[8]: a = 1.013
b = -0.021
c = 0.019
d = 0.96
e = 0
f = 0.01
g = 1
u = 0.05
i = 0.05

with reaction_rules():
    ~x > x | ((x - a * y) * cos(z) - b * y * sin(z))
    ~y > y | ((x + c * y) * sin(z) + d * y * cos(z))
    ~z > z | (e + f * z + g * a * atan((1 - u) / (1 - i) * x * y))

[9]: run_simulation(numpy.linspace(0, 800, 8001),
                    y0={'x': 0.9, 'y': 1, 'z': 1}, return_type='nyaplot',
                    opt_args={'x': 'x', 'y': ('y', 'z'), 'to_png': True})

<IPython.core.display.HTML object>
```

2.1.5 Moore-Spiegel attractor

```
[10]: T, R = 6, 20
with reaction_rules():
    ~x > x | y
    ~y > y | z
    ~z > z | (-z - (T - R + R * x * x) * y - T * x)

[11]: run_simulation(numpy.linspace(0, 100, 5001),
                    y0={'x': 1, 'y': 0, 'z': 0}, return_type='nyaplot',
                    opt_args={'x': 'x', 'y': 'y', 'to_png': True})

<IPython.core.display.HTML object>
```


2.2 Drosophila Circadian Clock

This is a model of the oscillating Drosophila period protein(PER). This model is based on the model introduced in the following publication.

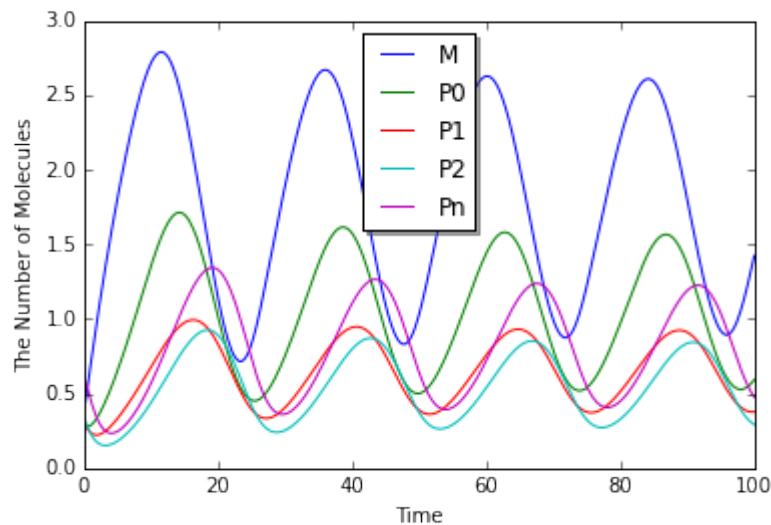
- A. Goldbeter, “A model for circadian oscillations in the Drosophila period protein(PER)”, Proc R Soc Lond B Biol Sci, Vol.261:319-324, Sep 1995.

```
[1]: %matplotlib inline
import numpy
from eccl14 import *
util.decorator.ENABLE_RATELAW = True
```

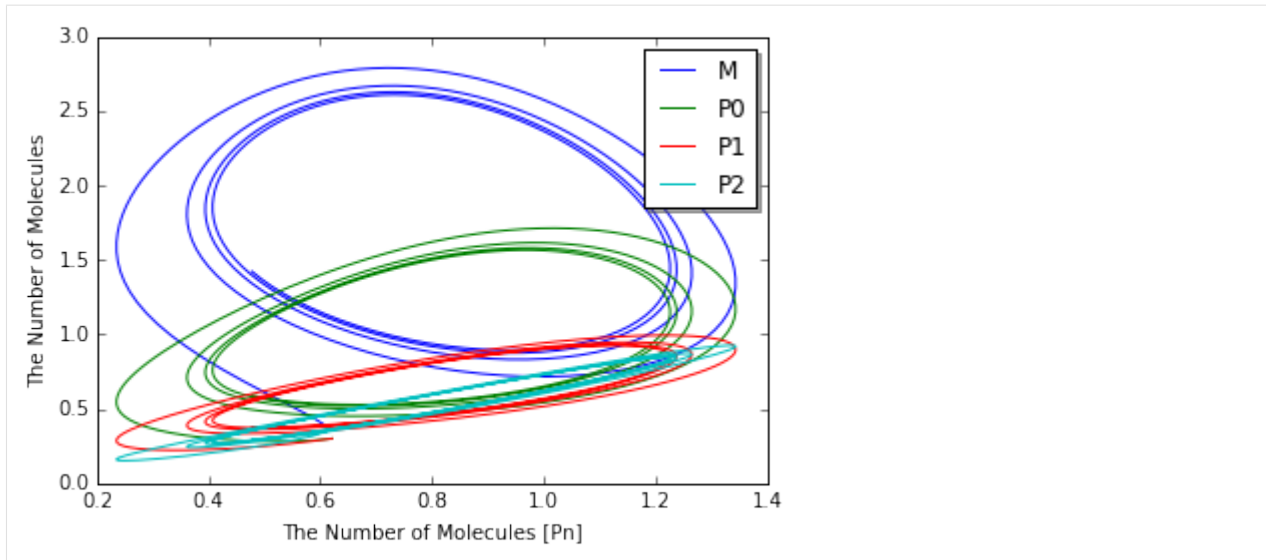
```
[2]: with reaction_rules():
    ~M > M | 0.76 / (1 + Pn ** 3)
    M > ~M | 0.65 * M / (0.5 + M)
    ~P0 > P0 | 0.38 * M
    P0 == P1 | (3.2 * P0 / (2 + P0), 1.58 * P1 / (2 + P1))
    P1 == P2 | (5 * P1 / (2 + P1), 2.5 * P2 / (2 + P2))
    P2 == Pn | (1.9, 1.3)
    P2 > ~P2 | 0.95 * P2 / (0.2 + P2)
```

```
[3]: y0 = {"M": 3.61328202E-01, "Pn": 6.21367E-01, "P0": 3.01106835E-01, "P1": 3.01106835E-
    ↪01, "P2": 3.61328202E-01}
obs = run_simulation(numpy.linspace(0, 100, 400), y0, return_type='observer')
```

```
[4]: # viz.plot_number_observer(obs, interactive=True)
viz.plot_number_observer(obs)
```



```
[5]: # viz.plot_number_observer(obs, x="Pn", y=("M", "P0", "P1", "P2"), interactive=True)
viz.plot_number_observer(obs, x="Pn", y=("M", "P0", "P1", "P2"))
```



2.3 Dual Phosphorylation Cycle

```
[1]: from eccl14.core import *
     from eccl14.util import *
```

```
[2]: @species_attributes
     def attrgen(radius, D):
         K | {"radius": radius, "D": D}
         Kp | {"radius": radius, "D": D}
         Kpp | {"radius": radius, "D": D}
         KK | {"radius": radius, "D": D}
         PP | {"radius": radius, "D": D}
         K_KK | {"radius": radius, "D": D}
         Kp_KK | {"radius": radius, "D": D}
         Kpp_PP | {"radius": radius, "D": D}
         Kp_PP | {"radius": radius, "D": D}

     @reaction_rules
     def rulegen(kon1, koff1, kcat1, kon2, koff2, kcat2):
         (K + KK == K_KK | (kon1, koff1)
          > Kp + KK | kcat1
          == Kp_KK | (kon2, koff2)
          > Kpp + KK | kcat2)

         (Kpp + PP == Kpp_PP | (kon1, koff1)
          > Kp + PP | kcat1
          == Kp_PP | (kon2, koff2)
          > K + PP | kcat2)
```

```
[3]: m = NetworkModel()
```

```
[4]: for i, sp in enumerate(attrgen("0.0025", "1")):
     print(i, sp.serial(), sp.get_attribute("radius"), sp.get_attribute("D"))
     m.add_species_attribute(sp)
```

```
(0, u'K', u'0.0025', u'1')
(1, u'Kp', u'0.0025', u'1')
(2, u'Kpp', u'0.0025', u'1')
(3, u'KK', u'0.0025', u'1')
(4, u'PP', u'0.0025', u'1')
(5, u'K_KK', u'0.0025', u'1')
(6, u'Kp_KK', u'0.0025', u'1')
(7, u'Kpp_PP', u'0.0025', u'1')
(8, u'Kp_PP', u'0.0025', u'1')
```

```
[5]: ka1, kd1, kcat1 = 0.04483455086786913, 1.35, 1.5
     ka2, kd2, kcat2 = 0.09299017957780264, 1.73, 15.0
```

```
for i, rr in enumerate(rulegen(ka1, kd2, kcat1, ka2, kd2, kcat2)):
    reactants, products, k = rr.reactants(), rr.products(), rr.k()
    print(i, rr.as_string())
    m.add_reaction_rule(rr)
```

```
(0, u'K+KK>K_KK|0.0448346')
(1, u'K_KK>K+KK|1.73')
(2, u'K_KK>Kp+KK|1.5')
(3, u'Kp+KK>Kp_KK|0.0929902')
(4, u'Kp_KK>Kp+KK|1.73')
(5, u'Kp_KK>Kpp+KK|15')
(6, u'Kpp+PP>Kpp_PP|0.0448346')
(7, u'Kpp_PP>Kpp+PP|1.73')
(8, u'Kpp_PP>Kp+PP|1.5')
(9, u'Kp+PP>Kp_PP|0.0929902')
(10, u'Kp_PP>Kp+PP|1.73')
(11, u'Kp_PP>K+PP|15')
```

```
[6]: from eccl14.gillespie import GillespieWorld as world_type, GillespieSimulator as_
     ↪ simulator_type
     # from eccl14.ode import ODEWorld as world_type, ODESimulator as simulator_type

w = world_type(Real3(1, 1, 1))
# w.bind_to(m)
w.add_molecules(Species("K"), 120)
w.add_molecules(Species("KK"), 30)
w.add_molecules(Species("PP"), 30)
sim = simulator_type(m, w)
```

```
[7]: obs = FixedIntervalNumberObserver(1.0, ["K", "K_KK", "Kp", "Kp_KK", "Kp_PP", "Kpp",
     ↪ "Kpp_PP"])
     sim.run(60, [obs])
```

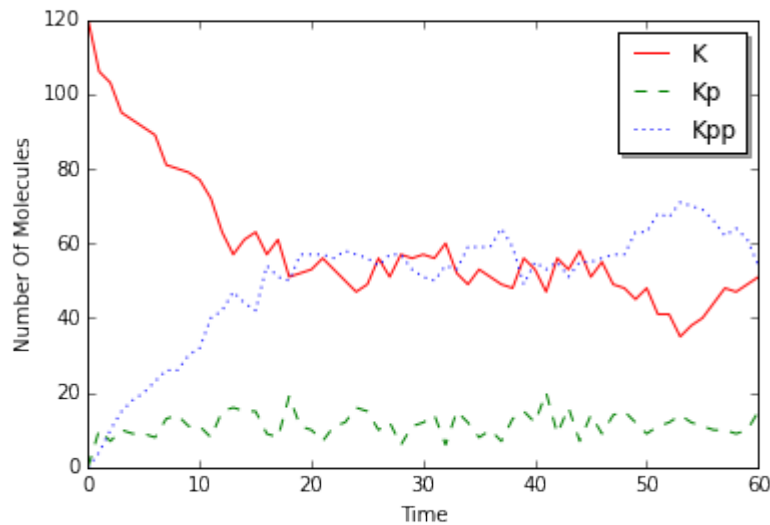
```
[8]: %matplotlib inline
import matplotlib.pyplot as plt
from numpy import array

data = array(obs.data()).T
plt.plot(data[0], data[1] + data[2], "r-", label="K")
plt.plot(data[0], data[3] + data[4] + data[5], "g--", label="Kp")
plt.plot(data[0], data[6] + data[7], "b:", label="Kpp")
plt.xlabel("Time")
plt.ylabel("Number Of Molecules")
```

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```
plt.xlim(data[0][0], data[0][-1])
plt.legend(loc="best", shadow=True)
plt.show()
```



2.4 Simple EGFR model

- http://bionetgen.org/index.php/Simple_EGFR_model
- M.L. Blinov, J.R. Faeder, B. Goldstein, W.S. Hlavacek, "A network model of early events in epidermal growth factor receptor signaling that accounts for combinatorial complexity.", Biosystems, 83(2-3), 136-151, 2006.

```
[1]: %matplotlib inline
from eccl14 import *
```

```
[2]: NA = 6.02e23 # Avogadro's number (molecules/mol)
f = 1 # Fraction of the cell to simulate
Vo = f * 1.0e-10 # Extracellular volume=1/cell_density (L)
V = f * 3.0e-12 # Cytoplasmic volume (L)

EGF_init = 20 * 1e-9 * NA * Vo # Initial amount of ligand (20 nM) converted to
↪copies per cell

# Initial amounts of cellular components (copies per cell)
EGFR_init = f * 1.8e5
Grb2_init = f * 1.5e5
Sos1_init = f * 6.2e4

# Rate constants
# Divide by NA*V to convert bimolecular rate constants
# from /M/sec to /(molecule/cell)/sec
kp1 = 9.0e7 / (NA * Vo) # ligand-monomer binding
km1 = 0.06 # ligand-monomer dissociation
kp2 = 1.0e7 / (NA * V) # aggregation of bound monomers
km2 = 0.1 # dissociation of bound monomers
kp3 = 0.5 # dimer transphosphorylation
```

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```

km3 = 4.505 # dimer dephosphorylation
kp4 = 1.5e6 / (NA * V) # binding of Grb2 to receptor
km4 = 0.05 # dissociation of Grb2 from receptor
kp5 = 1.0e7 / (NA * V) # binding of Grb2 to Sos1
km5 = 0.06 # dissociation of Grb2 from Sos1
deg = 0.01 # degradation of receptor dimers

```

```

[3]: with reaction_rules():
    # R1: Ligand-receptor binding
    EGFR(L, CR1) + EGF(R) == EGFR(L^1, CR1).EGF(R^1) | (kp1, km1)

    # R2: Receptor-aggregation
    EGFR(L^_, CR1) + EGFR(L^_, CR1) == EGFR(L^_, CR1^1).EGFR(L^_, CR1^1) | (kp2, km2)

    # R3: Transphosphorylation of EGFR by RTK
    EGFR(CR1^_, Y1068=U) > EGFR(CR1^_, Y1068=P) | kp3

    # R4: Dephosphorylation
    EGFR(Y1068=P) > EGFR(Y1068=U) | km3

    # R5: Grb2 binding to pY1068
    EGFR(Y1068=P) + Grb2(SH2) == EGFR(Y1068=P^1).Grb2(SH2^1) | (kp4, km4)

    # R6: Grb2 binding to Sos1
    Grb2(SH3) + Sos1(PxxP) == Grb2(SH3^1).Sos1(PxxP^1) | (kp5, km5)

    # R7: Receptor dimer internalization/degradation
    (EGF(R^1).EGF(R^2).EGFR(L^1, CR1^3).EGFR(L^2, CR1^3) > ~EmptySet | deg
     | _policy(ReactionRule.STRICT | ReactionRule.DESTROY))

m = get_model(is_netfree=True, effective=True)

[4]: y0 = {"EGF(R)": EGF_init, "EGFR(L, CR1, Y1068=U)": EGFR_init, "Grb2(SH2, SH3)": Grb2_
    ↪init, "Sos1(PxxP)": Sos1_init}

[5]: newm = m.expand([Species(serial) for serial in y0.keys()])

[6]: print("{} species and {} reactions were generated.".format(len(newm.list_species()),
    ↪len(newm.reaction_rules())))

for i, sp in enumerate(newm.list_species()):
    print("{}: {}".format(i + 1, sp.serial()))

for i, rr in enumerate(newm.reaction_rules()):
    print("{}: {}".format(i + 1, rr.as_string()))

22 species and 86 reactions were generated.
1: EGF(R)
2: EGF(R^1).EGFR(CR1, L^1, Y1068=P)
3: EGF(R^1).EGFR(CR1, L^1, Y1068=P^2).Grb2(SH2^2, SH3)
4: EGF(R^1).EGFR(CR1, L^1, Y1068=P^2).Grb2(SH2^2, SH3^3).Sos1(PxxP^3)
5: EGF(R^1).EGFR(CR1, L^1, Y1068=U)
6: EGF(R^1).EGFR(CR1^2, L^1, Y1068=P).EGFR(CR1^2, L^3, Y1068=P).EGF(R^3)
7: EGF(R^1).EGFR(CR1^2, L^1, Y1068=P).EGFR(CR1^2, L^3, Y1068=P^4).EGF(R^3).Grb2(SH2^4, SH3)
8: EGF(R^1).EGFR(CR1^2, L^1, Y1068=P).EGFR(CR1^2, L^3, Y1068=P^4).EGF(R^3).Grb2(SH2^4,
    ↪SH3^5).Sos1(PxxP^5)

```

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```

9: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=U).EGF(R^3)
10: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,
    ↪SH3).Grb2(SH2^3,SH3)
11: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,
    ↪SH3).Grb2(SH2^3,SH3^6).Sos1(PxxP^6)
12: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,
    ↪SH3^6).Sos1(PxxP^6).Grb2(SH2^3,SH3^7).Sos1(PxxP^7)
13: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=U).EGF(R^4).Grb2(SH2^3,
    ↪SH3)
14: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=U).EGF(R^4).Grb2(SH2^3,
    ↪SH3^5).Sos1(PxxP^5)
15: EGF(R^1).EGFR(CR1^2,L^1,Y1068=U).EGFR(CR1^2,L^3,Y1068=U).EGF(R^3)
16: EGFR(CR1,L,Y1068=P)
17: EGFR(CR1,L,Y1068=P^1).Grb2(SH2^1,SH3)
18: EGFR(CR1,L,Y1068=P^1).Grb2(SH2^1,SH3^2).Sos1(PxxP^2)
19: EGFR(CR1,L,Y1068=U)
20: Grb2(SH2,SH3)
21: Grb2(SH2,SH3^1).Sos1(PxxP^1)
22: Sos1(PxxP)
1: EGF(R)+EGFR(CR1,L,Y1068=U)>EGF(R^1).EGFR(CR1,L^1,Y1068=U)|1.49502e-06
2: Grb2(SH2,SH3)+Sos1(PxxP)>Grb2(SH2,SH3^1).Sos1(PxxP^1)|5.5371e-06
3: EGF(R^1).EGFR(CR1,L^1,Y1068=U)>EGF(R)+EGFR(CR1,L,Y1068=U)|0.06
4: EGF(R^1).EGFR(CR1,L^1,Y1068=U)+EGF(R^1).EGFR(CR1,L^1,Y1068=U)>EGF(R^1).EGFR(CR1^2,
    ↪L^1,Y1068=U).EGFR(CR1^2,L^3,Y1068=U).EGF(R^3)|2.76855e-06
5: Grb2(SH2,SH3^1).Sos1(PxxP^1)>Grb2(SH2,SH3)+Sos1(PxxP)|0.06
6: EGF(R^1).EGFR(CR1^2,L^1,Y1068=U).EGFR(CR1^2,L^3,Y1068=U).EGF(R^3)>EGF(R^1).
    ↪EGFR(CR1,L^1,Y1068=U)+EGF(R^1).EGFR(CR1,L^1,Y1068=U)|0.1
7: EGF(R^1).EGFR(CR1^2,L^1,Y1068=U).EGFR(CR1^2,L^3,Y1068=U).EGF(R^3)>EGF(R^1).
    ↪EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=U).EGF(R^3)|1
8: EGF(R^1).EGFR(CR1^2,L^1,Y1068=U).EGFR(CR1^2,L^3,Y1068=U).EGF(R^3)>|0.01
9: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=U).EGF(R^3)>EGF(R^1).
    ↪EGFR(CR1,L^1,Y1068=P)+EGF(R^1).EGFR(CR1,L^1,Y1068=U)|0.1
10: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=U).EGF(R^3)>EGF(R^1).
    ↪EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P).EGF(R^3)|0.5
11: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=U).EGF(R^3)>EGF(R^1).
    ↪EGFR(CR1^2,L^1,Y1068=U).EGFR(CR1^2,L^3,Y1068=U).EGF(R^3)|4.505
12: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=U).EGF(R^3)+Grb2(SH2,SH3^1).
    ↪Sos1(PxxP^1)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=U).EGF(R^4).
    ↪Grb2(SH2^3,SH3^5).Sos1(PxxP^5)|8.30565e-07
13: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=U).EGF(R^3)+Grb2(SH2,
    ↪SH3)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=U).EGF(R^4).Grb2(SH2^3,
    ↪SH3)|8.30565e-07
14: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=U).EGF(R^3)>|0.01
15: EGF(R^1).EGFR(CR1,L^1,Y1068=P)>EGF(R)+EGFR(CR1,L,Y1068=P)|0.06
16: EGF(R^1).EGFR(CR1,L^1,Y1068=P)+EGF(R^1).EGFR(CR1,L^1,Y1068=P)>EGF(R^1).EGFR(CR1^2,
    ↪L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P).EGF(R^3)|2.76855e-06
17: EGF(R^1).EGFR(CR1,L^1,Y1068=P)+EGF(R^1).EGFR(CR1,L^1,Y1068=U)>EGF(R^1).EGFR(CR1^2,
    ↪L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=U).EGF(R^3)|5.5371e-06
18: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P).EGF(R^3)>EGF(R^1).
    ↪EGFR(CR1,L^1,Y1068=P)+EGF(R^1).EGFR(CR1,L^1,Y1068=P)|0.1
19: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=U).EGF(R^4).Grb2(SH2^3,
    ↪SH3^5).Sos1(PxxP^5)>EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,SH3^3).
    ↪Sos1(PxxP^3)+EGF(R^1).EGFR(CR1,L^1,Y1068=U)|0.1
20: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=U).EGF(R^4).Grb2(SH2^3,
    ↪SH3)>EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,SH3)+EGF(R^1).EGFR(CR1,L^1,
    ↪Y1068=U)|0.1
21: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=U).EGF(R^4).Grb2(SH2^3,
    ↪SH3^5).Sos1(PxxP^5)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=U).EGF(R^3).Grb2(SH2^4,SH3^5).Sos1(PxxP^5)|0.5

```

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```

22: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=U).EGF(R^4).Grb2(SH2^3,
    ↪SH3)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).Grb2(SH2^4,
    ↪SH3)|0.5
23: EGF(R^1).EGFR(CR1,L^1,Y1068=P)>EGF(R^1).EGFR(CR1,L^1,Y1068=U)|4.505
24: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P).EGF(R^3)>EGF(R^1).
    ↪EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=U).EGF(R^3)|9.01
25: EGF(R^1).EGFR(CR1,L^1,Y1068=P)+Grb2(SH2,SH3^1).Sos1(PxxP^1)>EGF(R^1).EGFR(CR1,L^1,
    ↪Y1068=P^2).Grb2(SH2^2,SH3^3).Sos1(PxxP^3)|8.30565e-07
26: EGF(R^1).EGFR(CR1,L^1,Y1068=P)+Grb2(SH2,SH3)>EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).
    ↪Grb2(SH2^2,SH3)|8.30565e-07
27: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P).EGF(R^3)+Grb2(SH2,SH3^1).
    ↪Sos1(PxxP^1)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).
    ↪Grb2(SH2^4,SH3^5).Sos1(PxxP^5)|1.66113e-06
28: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P).EGF(R^3)+Grb2(SH2,
    ↪SH3)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).Grb2(SH2^4,
    ↪SH3)|1.66113e-06
29: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=U).EGF(R^4).Grb2(SH2^3,
    ↪SH3^5).Sos1(PxxP^5)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=U).
    ↪EGF(R^3)+Grb2(SH2,SH3^1).Sos1(PxxP^1)|0.05
30: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=U).EGF(R^4).Grb2(SH2^3,
    ↪SH3)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=U).EGF(R^3)+Grb2(SH2,
    ↪SH3)|0.05
31: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=U).EGF(R^4).Grb2(SH2^3,
    ↪SH3)+Sos1(PxxP)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=U).EGF(R^4).
    ↪Grb2(SH2^3,SH3^5).Sos1(PxxP^5)|5.5371e-06
32: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=U).EGF(R^4).Grb2(SH2^3,
    ↪SH3^5).Sos1(PxxP^5)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=U).
    ↪EGF(R^4).Grb2(SH2^3,SH3)+Sos1(PxxP)|0.06
33: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P).EGF(R^3)>|0.01
34: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=U).EGF(R^4).Grb2(SH2^3,
    ↪SH3^5).Sos1(PxxP^5)>|0.01
35: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=U).EGF(R^4).Grb2(SH2^3,
    ↪SH3)>|0.01
36: EGF(R)+EGFR(CR1,L,Y1068=P)>EGF(R^1).EGFR(CR1,L^1,Y1068=P)|1.49502e-06
37: EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,SH3^3).Sos1(PxxP^3)>EGF(R)+EGFR(CR1,L,
    ↪Y1068=P^1).Grb2(SH2^1,SH3^2).Sos1(PxxP^2)|0.06
38: EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,SH3)>EGF(R)+EGFR(CR1,L,Y1068=P^1).
    ↪Grb2(SH2^1,SH3)|0.06
39: EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,SH3^3).Sos1(PxxP^3)+EGF(R^1).EGFR(CR1,
    ↪L^1,Y1068=P^2).Grb2(SH2^2,SH3^3).Sos1(PxxP^3)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).
    ↪EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,SH3^6).Sos1(PxxP^6).Grb2(SH2^3,SH3^7).
    ↪Sos1(PxxP^7)|2.76855e-06
40: EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,SH3)+EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).
    ↪Grb2(SH2^2,SH3^3).Sos1(PxxP^3)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,
    ↪Y1068=P^5).EGF(R^4).Grb2(SH2^5,SH3).Grb2(SH2^3,SH3^6).Sos1(PxxP^6)|5.5371e-06
41: EGF(R^1).EGFR(CR1,L^1,Y1068=P)+EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,SH3^3).
    ↪Sos1(PxxP^3)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).
    ↪Grb2(SH2^4,SH3^5).Sos1(PxxP^5)|5.5371e-06
42: EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,SH3^3).Sos1(PxxP^3)+EGF(R^1).EGFR(CR1,
    ↪L^1,Y1068=U)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=U).EGF(R^4).
    ↪Grb2(SH2^3,SH3^5).Sos1(PxxP^5)|5.5371e-06
43: EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,SH3)+EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).
    ↪Grb2(SH2^2,SH3)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=P^5).
    ↪EGF(R^4).Grb2(SH2^5,SH3).Grb2(SH2^3,SH3)|2.76855e-06
44: EGF(R^1).EGFR(CR1,L^1,Y1068=P)+EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,
    ↪SH3)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).Grb2(SH2^4,
    ↪SH3)|5.5371e-06

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45: EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,SH3)+EGF(R^1).EGFR(CR1,L^1,
→Y1068=U)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=U).EGF(R^4).
→Grb2(SH2^3,SH3)|5.5371e-06
46: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).Grb2(SH2^4,
→SH3^5).Sos1(PxxP^5)>EGF(R^1).EGFR(CR1,L^1,Y1068=P)+EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).
→Grb2(SH2^2,SH3^3).Sos1(PxxP^3)|0.1
47: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).Grb2(SH2^4,
→SH3)>EGF(R^1).EGFR(CR1,L^1,Y1068=P)+EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,
→SH3)|0.1
48: EGFR(CR1,L,Y1068=P)>EGFR(CR1,L,Y1068=U)|4.505
49: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).Grb2(SH2^4,
→SH3^5).Sos1(PxxP^5)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=U).
→EGF(R^4).Grb2(SH2^3,SH3^5).Sos1(PxxP^5)|4.505
50: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).Grb2(SH2^4,
→SH3)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=U).EGF(R^4).Grb2(SH2^3,
→SH3)|4.505
51: EGFR(CR1,L,Y1068=P)+Grb2(SH2,SH3^1).Sos1(PxxP^1)>EGFR(CR1,L,Y1068=P^1).Grb2(SH2^1,
→SH3^2).Sos1(PxxP^2)|8.30565e-07
52: EGFR(CR1,L,Y1068=P)+Grb2(SH2,SH3)>EGFR(CR1,L,Y1068=P^1).Grb2(SH2^1,SH3)|8.
→30565e-07
53: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).Grb2(SH2^4,
→SH3^5).Sos1(PxxP^5)+Grb2(SH2,SH3^1).Sos1(PxxP^1)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).
→EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,SH3^6).Sos1(PxxP^6).Grb2(SH2^3,SH3^7).
→Sos1(PxxP^7)|8.30565e-07
54: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).Grb2(SH2^4,
→SH3^5).Sos1(PxxP^5)+Grb2(SH2,SH3)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,
→Y1068=P^5).EGF(R^4).Grb2(SH2^5,SH3).Grb2(SH2^3,SH3^6).Sos1(PxxP^6)|8.30565e-07
55: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).Grb2(SH2^4,
→SH3)+Grb2(SH2,SH3^1).Sos1(PxxP^1)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,
→Y1068=P^5).EGF(R^4).Grb2(SH2^5,SH3).Grb2(SH2^3,SH3^6).Sos1(PxxP^6)|8.30565e-07
56: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).Grb2(SH2^4,
→SH3)+Grb2(SH2,SH3)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=P^5).
→EGF(R^4).Grb2(SH2^5,SH3).Grb2(SH2^3,SH3)|8.30565e-07
57: EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,SH3^3).Sos1(PxxP^3)>EGF(R^1).EGFR(CR1,
→L^1,Y1068=P)+Grb2(SH2,SH3^1).Sos1(PxxP^1)|0.05
58: EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,SH3)>EGF(R^1).EGFR(CR1,L^1,
→Y1068=P)+Grb2(SH2,SH3)|0.05
59: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).Grb2(SH2^4,
→SH3^5).Sos1(PxxP^5)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P).
→EGF(R^3)+Grb2(SH2,SH3^1).Sos1(PxxP^1)|0.05
60: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).Grb2(SH2^4,
→SH3)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P).EGF(R^3)+Grb2(SH2,
→SH3)|0.05
61: EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,SH3)+Sos1(PxxP)>EGF(R^1).EGFR(CR1,L^1,
→Y1068=P^2).Grb2(SH2^2,SH3^3).Sos1(PxxP^3)|5.5371e-06
62: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).Grb2(SH2^4,
→SH3)+Sos1(PxxP)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).
→Grb2(SH2^4,SH3^5).Sos1(PxxP^5)|5.5371e-06
63: EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,SH3^3).Sos1(PxxP^3)>EGF(R^1).EGFR(CR1,
→L^1,Y1068=P^2).Grb2(SH2^2,SH3)+Sos1(PxxP)|0.06
64: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).Grb2(SH2^4,
→SH3^5).Sos1(PxxP^5)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).
→EGF(R^3).Grb2(SH2^4,SH3)+Sos1(PxxP)|0.06
65: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).Grb2(SH2^4,
→SH3^5).Sos1(PxxP^5)>|0.01
66: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).Grb2(SH2^4,
→SH3)>|0.01

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67: EGF(R)+EGFR(CR1,L,Y1068=P^1).Grb2(SH2^1,SH3^2).Sos1(PxxP^2)>EGF(R^1).EGFR(CR1,L^1,
↪Y1068=P^2).Grb2(SH2^2,SH3^3).Sos1(PxxP^3)|1.49502e-06
68: EGF(R)+EGFR(CR1,L,Y1068=P^1).Grb2(SH2^1,SH3)>EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).
↪Grb2(SH2^2,SH3)|1.49502e-06
69: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,
↪SH3^6).Sos1(PxxP^6).Grb2(SH2^3,SH3^7).Sos1(PxxP^7)>EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).
↪Grb2(SH2^2,SH3^3).Sos1(PxxP^3)+EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,SH3^3).
↪Sos1(PxxP^3)|0.1
70: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,
↪SH3).Grb2(SH2^3,SH3^6).Sos1(PxxP^6)>EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,
↪SH3)+EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,SH3^3).Sos1(PxxP^3)|0.1
71: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,
↪SH3).Grb2(SH2^3,SH3)>EGF(R^1).EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,SH3)+EGF(R^1).
↪EGFR(CR1,L^1,Y1068=P^2).Grb2(SH2^2,SH3)|0.1
72: EGFR(CR1,L,Y1068=P^1).Grb2(SH2^1,SH3^2).Sos1(PxxP^2)>EGFR(CR1,L,Y1068=P)+Grb2(SH2,
↪SH3^1).Sos1(PxxP^1)|0.05
73: EGFR(CR1,L,Y1068=P^1).Grb2(SH2^1,SH3)>EGFR(CR1,L,Y1068=P)+Grb2(SH2,SH3)|0.05
74: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,
↪SH3^6).Sos1(PxxP^6).Grb2(SH2^3,SH3^7).Sos1(PxxP^7)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).
↪EGFR(CR1^2,L^3,Y1068=P^4).EGF(R^3).Grb2(SH2^4,SH3^5).Sos1(PxxP^5)+Grb2(SH2,SH3^1).
↪Sos1(PxxP^1)|0.1
75: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,
↪SH3).Grb2(SH2^3,SH3^6).Sos1(PxxP^6)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,
↪Y1068=P^4).EGF(R^3).Grb2(SH2^4,SH3)+Grb2(SH2,SH3^1).Sos1(PxxP^1)|0.05
76: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,
↪SH3).Grb2(SH2^3,SH3^6).Sos1(PxxP^6)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,
↪Y1068=P^4).EGF(R^3).Grb2(SH2^4,SH3^5).Sos1(PxxP^5)+Grb2(SH2,SH3)|0.05
77: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,
↪SH3).Grb2(SH2^3,SH3)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P).EGFR(CR1^2,L^3,Y1068=P^4).
↪EGF(R^3).Grb2(SH2^4,SH3)+Grb2(SH2,SH3)|0.1
78: EGFR(CR1,L,Y1068=P^1).Grb2(SH2^1,SH3)+Sos1(PxxP)>EGFR(CR1,L,Y1068=P^1).Grb2(SH2^1,
↪SH3^2).Sos1(PxxP^2)|5.5371e-06
79: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,
↪SH3).Grb2(SH2^3,SH3^6).Sos1(PxxP^6)+Sos1(PxxP)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).
↪EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,SH3^6).Sos1(PxxP^6).Grb2(SH2^3,SH3^7).
↪Sos1(PxxP^7)|5.5371e-06
80: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,
↪SH3).Grb2(SH2^3,SH3)+Sos1(PxxP)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,
↪Y1068=P^5).EGF(R^4).Grb2(SH2^5,SH3).Grb2(SH2^3,SH3^6).Sos1(PxxP^6)|1.10742e-05
81: EGFR(CR1,L,Y1068=P^1).Grb2(SH2^1,SH3^2).Sos1(PxxP^2)>EGFR(CR1,L,Y1068=P^1).
↪Grb2(SH2^1,SH3)+Sos1(PxxP)|0.06
82: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,
↪SH3^6).Sos1(PxxP^6).Grb2(SH2^3,SH3^7).Sos1(PxxP^7)>EGF(R^1).EGFR(CR1^2,L^1,
↪Y1068=P^3).EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,SH3).Grb2(SH2^3,SH3^6).
↪Sos1(PxxP^6)+Sos1(PxxP)|0.12
83: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,
↪SH3).Grb2(SH2^3,SH3^6).Sos1(PxxP^6)>EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,
↪L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,SH3).Grb2(SH2^3,SH3)+Sos1(PxxP)|0.06
84: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,
↪SH3^6).Sos1(PxxP^6).Grb2(SH2^3,SH3^7).Sos1(PxxP^7)>|0.01
85: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,
↪SH3).Grb2(SH2^3,SH3^6).Sos1(PxxP^6)>|0.01
86: EGF(R^1).EGFR(CR1^2,L^1,Y1068=P^3).EGFR(CR1^2,L^4,Y1068=P^5).EGF(R^4).Grb2(SH2^5,
↪SH3).Grb2(SH2^3,SH3)>|0.01

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[7]: species_list = ["EGFR",

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```

        "EGF(R) ",
        "EGFR(CR1^_) ",
        "EGFR(Y1068=P^_0) ",
        "Grb2(SH2, SH3^1).Sos1(PxxP^1) ",
        "EGFR(Y1068^1).Grb2(SH2^1, SH3^2).Sos1(PxxP^2)"]
run_simulation(120, model=newm, y0=y0, species_list=species_list,
               opt_kwargs={'interactive': True, 'to_png': True})

<IPython.core.display.HTML object>

```

2.5 A Simple Model of the Glycolysis of Human Erythrocytes

This is a model for the glycolysis of human erythrocytes which takes into account ATP-synthesis and -consumption. This model is based on the model introduced in the following publication.

- Rapoport, T.A. and Heinrich, R. (1975) “Mathematical analysis of multienzyme systems. I. Modelling of the glycolysis of human erythrocytes.”, Biosystems., 7, 1, 120-129.
- Heinrich, R. and Rapoport, T.A. (1975) “Mathematical analysis of multienzyme systems. II. Steady state and transient control.”, Biosystems., 7, 1, 130-136.

```

[1]: %matplotlib inline
from eccl14 import *
util.decorator.ENABLE_RATELAW = True

```

```

[2]: with reaction_rules():
    2 * ATP > 2 * A13P2G + 2 * ADP | (3.2 * ATP / (1.0 + (ATP / 1.0) ** 4.0))
    A13P2G > A23P2G | 1500
    A23P2G > PEP | 0.15
    A13P2G + ADP > PEP + ATP | 1.57e+4
    PEP + ADP > ATP | 559
    AMP + ATP > 2 * ADP | (1.0 * (AMP * ATP - 2.0 * ADP * ADP))
    ATP > ADP | 1.46

```

```

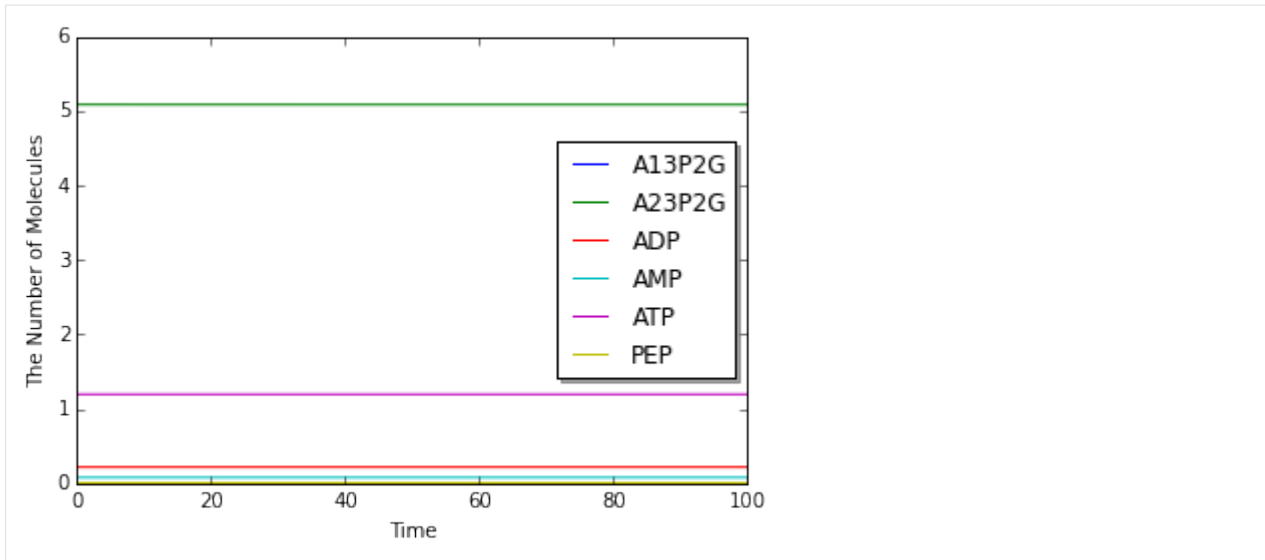
[3]: y0 = {"A13P2G": 0.0005082, "A23P2G": 5.0834, "PEP": 0.020502,
          "AMP": 0.080139, "ADP": 0.2190, "ATP": 1.196867}

```

```

[4]: run_simulation(100, y0=y0)

```



2.6 Hodgkin-Huxley Model

- A.L. Hodgkin, A.F. Huxley, “A quantitative description of membrane current and its application to conduction and excitation in nerve”, J. Physiol., 117, 500-544, 1952.

```
[1]: %matplotlib inline
import numpy as np
from ecell14 import *
```

```
[2]: Q10 = 3.0
GNa = 120.0 # mS/cm^2
GK = 36.0 # mS/cm^2
gL = 0.3 # mS/cm^2
EL = -64.387 # mV
ENa = 40.0 # mV
EK = -87.0 # mV
Cm = 1.0 # uF/cm^2

T = 6.3 # degrees C
Iext = 10.0 # nA

with reaction_rules():
    Q = Q10 ** ((T - 6.3) / 10)

    alpha_m = -0.1 * (Vm + 50) / (exp(-(Vm + 50) / 10) - 1)
    beta_m = 4 * exp(-(Vm + 75) / 18)
    ~m > m | Q * (alpha_m * (1 - m) - beta_m * m)

    alpha_h = 0.07 * exp(-(Vm + 75) / 20)
    beta_h = 1.0 / (exp(-(Vm + 45) / 10) + 1)
    ~h > h | Q * (alpha_h * (1 - h) - beta_h * h)

    alpha_n = -0.01 * (Vm + 65) / (exp(-(Vm + 65) / 10) - 1)
    beta_n = 0.125 * exp(-(Vm + 75) / 80)
    ~n > n | Q * (alpha_n * (1 - n) - beta_n * n)
```

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```

gNa = (m ** 3) * h * GNa
INa = gNa * (Vm - ENa)
gK = (n ** 4) * GK
IK = gK * (Vm - EK)
IL = gL * (Vm - EL)
~Vm > Vm | (Iext - (IL + INa + IK)) / Cm

hbm = get_model()

```

```

[3]: for rr in hbm.reaction_rules():
      print(rr.as_string())

```

```

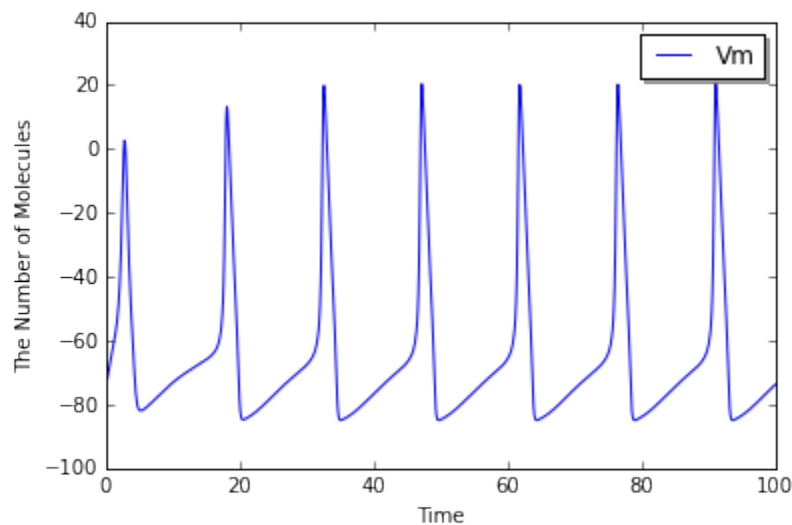
Vm>m+Vm| (1.0*((( -0.1*(Vm+50))/(exp((- (Vm+50)/10))-1))*(1-m))-(4*exp((- (Vm+75)/
↪ 18))*m)))
Vm>h+Vm| (1.0*((0.07*exp((- (Vm+75)/20))*(1-h))-((1.0/(exp((- (Vm+45)/10))+1))*h)))
Vm>n+Vm| (1.0*((( -0.01*(Vm+65))/(exp((- (Vm+65)/10))-1))*(1-n))-(0.125*exp((- (Vm+75)/
↪ 80))*n)))
m+h+n>Vm+m+h+n| ((10.0-((0.3*(Vm-64.387))+((m**3)*h*120.0*(Vm-40.0))+((n**4)*36.
↪ 0*(Vm-87.0))))/1.0)

```

```

[4]: run_simulation(np.linspace(0, 100, 1001), model=hbm, y0={'Vm': -75}, species_list=['Vm
↪'])

```



2.7 FitzHugh–Nagumo Model

- R. FitzHugh, “Mathematical models of threshold phenomena in the nerve membrane.”, Bull. Math. Biophysics, 17:257—278, 1955.

```

[5]: a = 0.7
      b = 0.8
      c = 12.5
      Iext = 0.5

```

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```

with reaction_rules():
    ~u > u | -v + u - (u ** 3) / 3 + Iext
    ~v > v | (u - b * v + a) / c

fnm = get_model()

```

```

[6]: for rr in fnm.reaction_rules():
      print(rr.as_string())

```

```

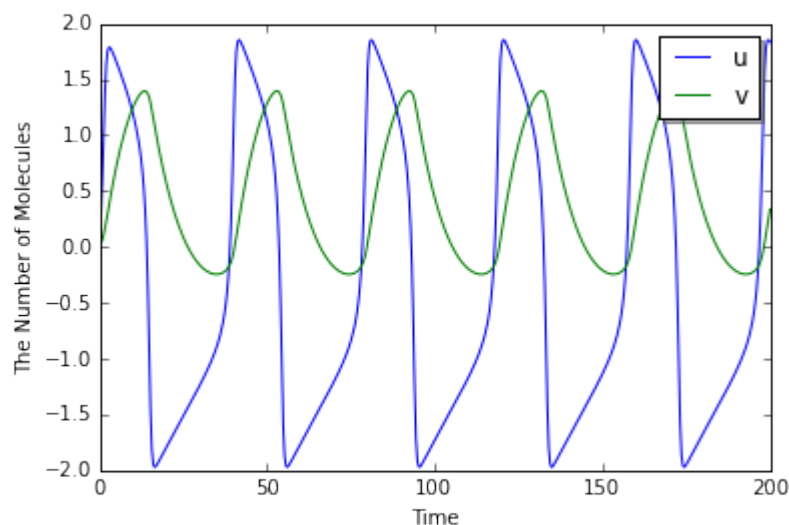
v>u+v| (((-v+u)-((u**3)/3))+0.5)
u>v+u| (((u-(0.8*v))+0.7)/12.5)

```

```

[7]: run_simulation(np.linspace(0, 200, 501), model=fnm)

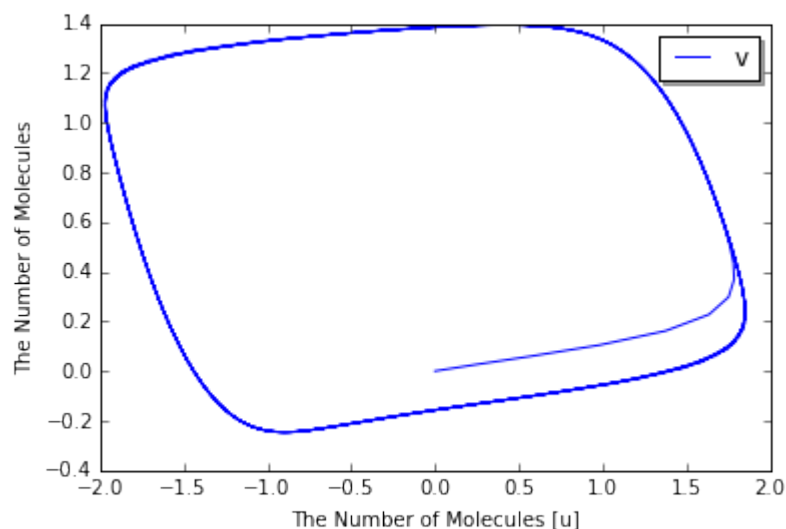
```



```

[8]: run_simulation(np.linspace(0, 200, 501), model=fnm, # return_type='nyaplot',
                  opt_kwargs={'x': 'u', 'y': ['v']})

```



2.8 Lotka-Volterra 2D

2.8.1 The Original Model in Ordinary Differential Equations

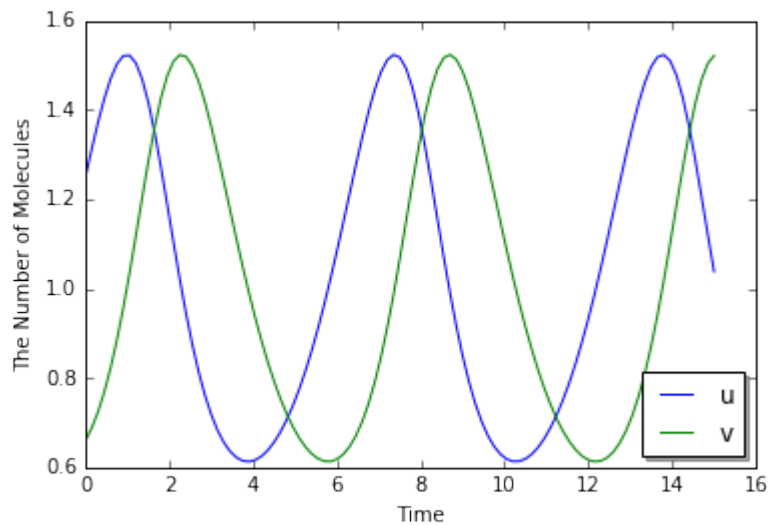
```
[1]: %matplotlib inline
from eccl14 import *
```

```
[2]: alpha = 1

with reaction_rules():
    ~u > u | u * (1 - v)
    ~v > v | alpha * v * (u - 1)

m = get_model()
```

```
[3]: run_simulation(15, {'u': 1.25, 'v': 0.66}, model=m)
```



2.8.2 The Modified Model Decomposed into Elementary Reactions

```
[4]: alpha = 1

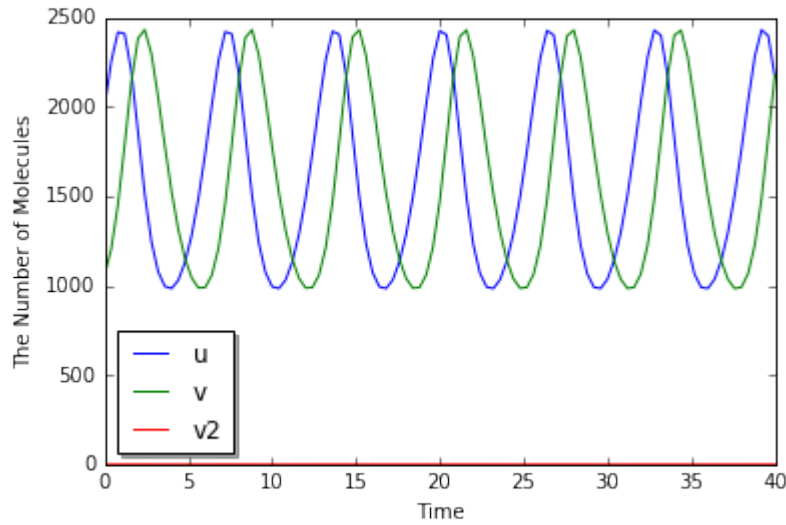
with species_attributes():
    u | {'D': '0.1'}
    v | {'D': '0.1'}

with reaction_rules():
    u > u + u | 1.0
    u + v > v | 1.0

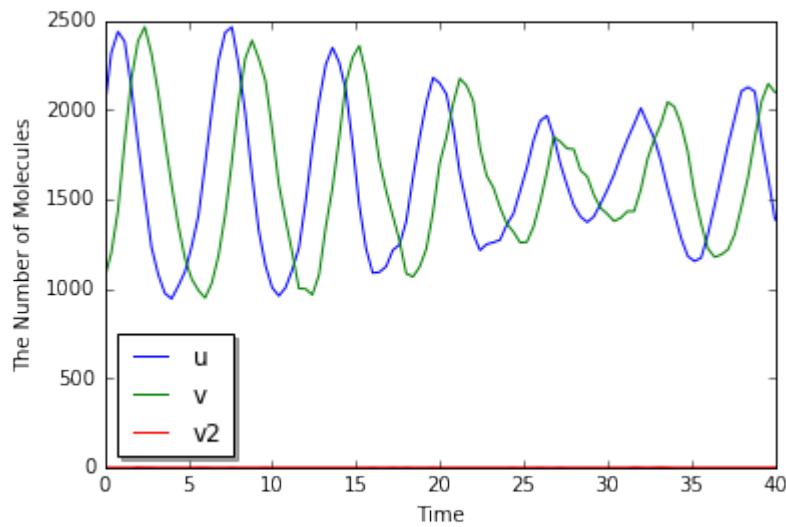
    u + v > u + v2 | alpha
    v2 > v + v | alpha * 10000.0
    v > ~v | alpha

m = get_model()
```

```
[5]: run_simulation(40, {'u': 1.25 * 1600, 'v': 0.66 * 1600}, volume=1600, model=m)
```



```
[6]: run_simulation(40, {'u': 1.25 * 1600, 'v': 0.66 * 1600}, volume=1600, model=m, solver=
      ↪ 'gillespie')
```



2.8.3 A Lotka-Volterra-like Model in 2D

```
[7]: rng = GSLRandomNumberGenerator()
      rng.seed(0)
```

```
[8]: w = meso.MesososcopicWorld(Real3(40, 40, 1), Integer3(160, 160, 1), rng)
      w.bind_to(m)
```

```
[9]: V = w.volume()
      print(V)
```

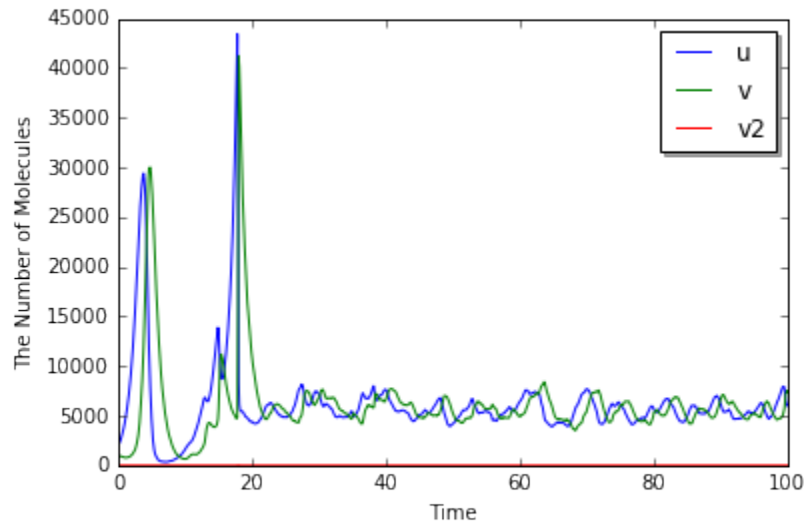
```
1600.0
```

```
[10]: w.add_molecules(Species("u"), int(1.25 * V))
      w.add_molecules(Species("v"), int(0.66 * V))
```

```
[11]: sim = meso.MesoscopicSimulator(w)
      obs1 = FixedIntervalNumberObserver(0.1, ('u', 'v', 'v2'))
      obs2 = FixedIntervalHDF5Observer(2, "test%03d.h5")
```

```
[12]: sim.run(100, (obs1, obs2))
```

```
[13]: viz.plot_number_observer(obs1)
```



```
[14]: viz.plot_world(w, radius=0.2)

<IPython.core.display.HTML object>
```

```
[15]: viz.plot_movie_with_attractive_mpl(
      obs2, linewidth=0, noaxis=True, figsize=6, whratio=1.4,
      angle=(-90, 90, 6), bitrate='10M')

<IPython.core.display.HTML object>
```

```
[16]: # from zipfile import ZipFile
      # with ZipFile('test.zip', 'w') as myzip:
      #     for i in range(obs2.num_steps()):
      #         myzip.write('test{:03d}.h5'.format(i))
```

2.9 MinDE System with Mesoscopic Simulator

Fange D, Elf J (2006) Noise-Induced Min Phenotypes in E. coli. PLoS Comput Biol 2(6): e80. doi:10.1371/journal.pcbi.0020080


```
[1]: %matplotlib inline
from ecell14 import *
```

Declaring Species and ReactionRules:

```
[2]: with species_attributes():
    D | DE | {"D": "0.01", "location": "M"}
    D_ADP | D_ATP | E | {"D": "2.5", "location": "C"}

    with reaction_rules():
        D_ATP + M > D | 0.0125
        D_ATP + D > D + D | 9e+6 * (1e+15 / N_A)
        D + E > DE | 5.58e+7 * (1e+15 / N_A)
        DE > D_ADP + E | 0.7
        D_ADP > D_ATP | 0.5

m = get_model()
```

Make a World. The second argument, 0.05, means its subvolume length:

```
[3]: w = meso.MesoscopicWorld(Real3(4.6, 1.1, 1.1), 0.05)
w.bind_to(m)
```

Make a structures. Species C is for cytoplasm, and M is for membrane:

```
[4]: rod = Rod(3.5, 0.55, w.edge_lengths() * 0.5)
w.add_structure(Species("C"), rod)
w.add_structure(Species("M"), rod.surface())
```

Throw-in molecules:

```
[5]: w.add_molecules(Species("D_ATP"), 2001)
w.add_molecules(Species("D_ADP"), 2001)
w.add_molecules(Species("E"), 1040)
```

Run a simulation for 120 seconds. Two Observers below are for logging. obs1 logs only the number of molecules, and obs2 does a whole state of the World.

```
[6]: sim = meso.MesoscopicSimulator(w)
obs1 = FixedIntervalNumberObserver(0.1, [sp.serial() for sp in m.list_species()])
obs2 = FixedIntervalHDF5Observer(1.0, 'minde%03d.h5')
```

```
[7]: from ecell14.util.progressbar import progressbar
```

```
[8]: duration = 120
progressbar(sim, timeout=1).run(duration, (obs1, obs2))

##### 100.0% Elapsed: 00:28:11 ETA: 00:00:00
```

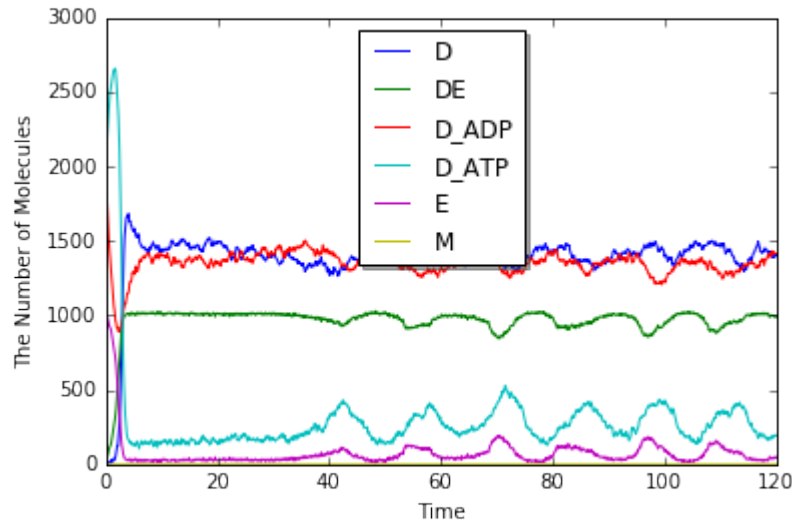
Visualize the final state of the World:

```
[9]: viz.plot_world(w, radius=0.01, species_list=('D', 'DE'))

<IPython.core.display.HTML object>
```

Plot a time course of the number of molecules:

```
[10]: viz.plot_number_observer(obs1)
```



```
[11]: viz.plot_movie_with_matplotlib(obs2, species_list=('D', 'DE'))
```

```
<IPython.core.display.HTML object>
```

```
[ ]:
```

2.10 MinDE System with Spatiocyte Simulator

```
[1]: %matplotlib inline
from ecell14 import *
```

Declaring Species and ReactionRules:

```
[2]: with species_attributes():
    cytoplasm | {'radius': '1e-8', 'D': '0'}
    MinDatp | MinDadp | {'radius': '1e-8', 'D': '16e-12', 'location': 'cytoplasm'}
    MinEE_C | {'radius': '1e-8', 'D': '10e-12', 'location': 'cytoplasm'}
    membrane | {'radius': '1e-8', 'D': '0', 'location': 'cytoplasm'}
    MinD | MinEE_M | MinDEE | MinDEED | {'radius': '1e-8', 'D': '0.02e-12', 'location'
    ↪ ': 'membrane'}

    with reaction_rules():
        membrane + MinDatp > MinD | 2.2e-8
        MinD + MinDatp > MinD + MinD | 3e-20
        MinD + MinEE_C > MinDEE | 5e-19
        MinDEE > MinEE_M + MinDadp | 1
        MinDadp > MinDatp | 5
        MinDEE + MinD > MinDEED | 5e-15
        MinDEED > MinDEE + MinDadp | 1
        MinEE_M > MinEE_C | 0.83

    m = get_model()
```

Make a World.

```
[3]: f = spatiocyte.SpatocyteFactory(1e-8)
w = f.create_world(Real3(4.6e-6, 1.1e-6, 1.1e-6))
w.bind_to(m)
```

Make a Structures.

```
[4]: rod = Rod(3.5e-6, 0.51e-6, w.edge_lengths() * 0.5)
w.add_structure(Species('cytoplasm'), rod)
w.add_structure(Species('membrane'), rod.surface())
```

```
[4]: 47500
```

Throw-in molecules.

```
[5]: w.add_molecules(Species('MinDadp'), 1300)
w.add_molecules(Species('MinDEE'), 700)
```

Run a simulation for 240 seconds.

```
[6]: sim = f.create_simulator(m, w)
```

```
[7]: # from functools import reduce
# alpha = reduce(lambda x, y: min(x, sim.calculate_alpha(y)), m.reaction_rules())
# sim.set_alpha(alpha)
```

```
[8]: from ecell14.util.progressbar import progressbar
```

```
[9]: obs1 = FixedIntervalNumberObserver(0.1, ('MinDatp', 'MinDadp', 'MinEE_C', 'MinD',
↪ 'MinEE_M', 'MinDEE', 'MinDEED'))
```

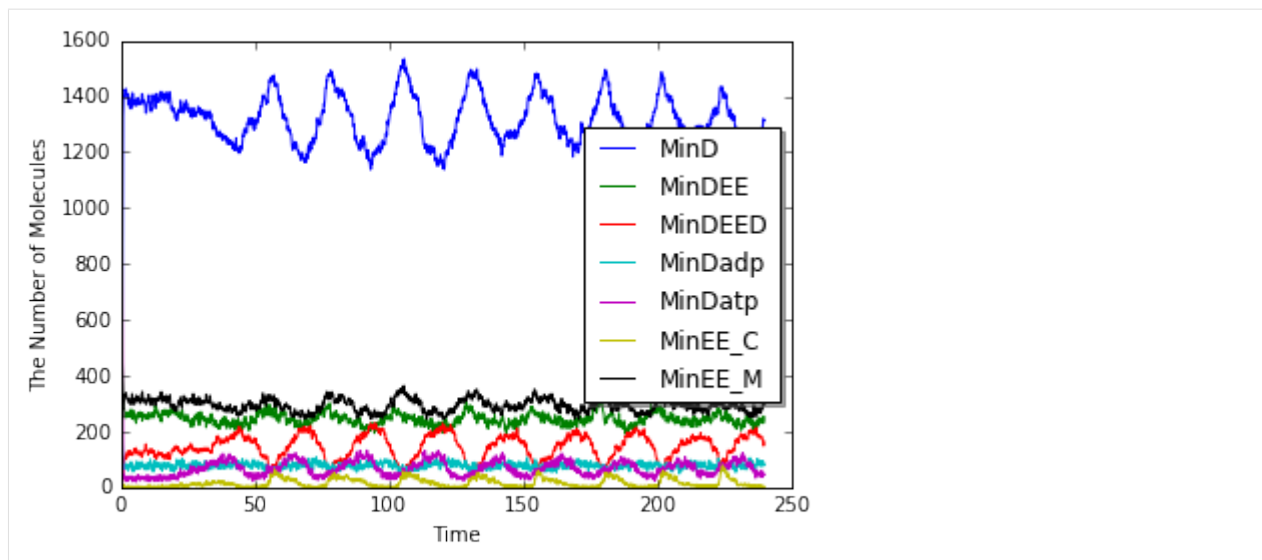
```
[10]: obs2 = FixedIntervalHDF5Observer(1.0, "minde%03d.h5")
```

```
[11]: duration = 240
```

```
[12]: progressbar(sim, timeout=1).run(duration, (obs1, obs2))
```

```
##### 100.0% Elapsed: 01:04:40 ETA: 00:00:00
```

```
[13]: viz.plot_number_observer(obs1)
```



```
[14]: viz.plot_movie_with_matplotlib([spatiocyte.SpatiocyteWorld("minde%03d.h5" % i) for i_
    ↪ in range(obs2.num_steps())], species_list=('MinD', 'MinEE_M', 'MinDEE', 'MinDEED'))

<IPython.core.display.HTML object>
```

```
[15]: viz.plot_world(spatiocyte.SpatiocyteWorld("minde240.h5"), species_list=('MinD',
    ↪ 'MinEE_M', 'MinDEE', 'MinDEED'))

<IPython.core.display.HTML object>
```

```
[ ]:
```

2.11 Simple Equilibrium

This is a simple equilibrium model as an example. Here, we explain how to model and run a simulation without using decorators (`species_attributes` and `reaction_rules`) and `run_simulation` method.

```
[1]: %matplotlib inline
from ecell14 import *
```

Choose one module from a list of methods supported on E-Cell4.

```
[2]: # f = gillespie.GillespieFactory
# f = ode.ODEFactory()
# f = spatiocyte.SpatiocyteFactory()
# f = bd.BDFactory()
# f = meso.MesoscopicFactory()
f = egfrd.EGFRDFactory()
```

Set up parameters:

```
[3]: L, N, kd, U, D, radius = 1.0, 60, 0.1, 0.5, "1", "0.01"
volume = L * L * L
ka = kd * volume * (1 - U) / (U * U * N)
```

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```

sp1, sp2, sp3 = Species("A", radius, D), Species("B", radius, D), Species("A_B",
↪radius, D)
rr1, rr2 = create_binding_reaction_rule(sp1, sp2, sp3, ka), create_unbinding_reaction_
↪rule(sp3, sp1, sp2, kd)

```

Create a model:

```

[4]: m = NetworkModel()
m.add_species_attribute(sp1)
m.add_species_attribute(sp2)
m.add_species_attribute(sp3)
m.add_reaction_rule(rr1)
m.add_reaction_rule(rr2)

```

Create a world and simulator:

```

[5]: w = f.create_world(Real3(L, L, L))
w.bind_to(m)
w.add_molecules(Species("A"), N)
w.add_molecules(Species("B"), N)

sim = f.create_simulator(w)
sim.set_dt(1e-3) #XXX: This is too large to get the accurate result with BDSimulator.

```

Run a simulation:

```

[6]: next_time, dt = 0.0, 0.05
data = [(w.t(), w.num_molecules(sp1), w.num_molecules(sp2), w.num_molecules(sp3))]
for i in range(100):
    next_time += dt
    while (sim.step(next_time)): pass
    data.append((w.t(), w.num_molecules(sp1), w.num_molecules(sp2), w.num_
↪molecules(sp3)))

```

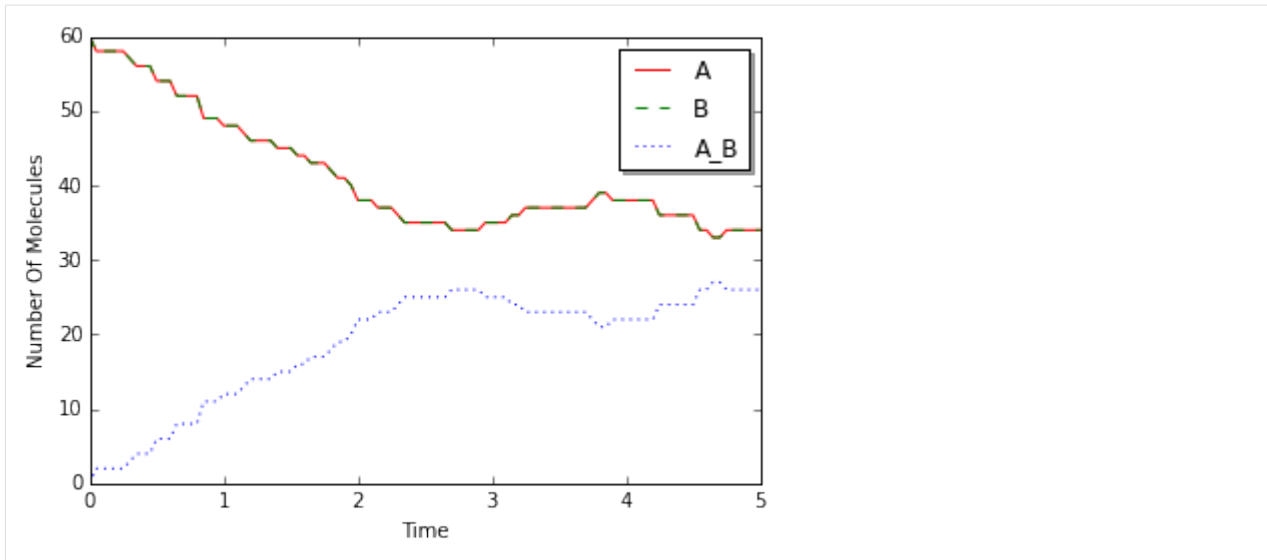
Plot with Matplotlib:

```

[7]: import matplotlib.pyplot as plt
from numpy import array

data = array(data)
plt.plot(data.T[0], data.T[1], "r-", label=sp1.serial())
plt.plot(data.T[0], data.T[2], "g--", label=sp2.serial())
plt.plot(data.T[0], data.T[3], "b:", label=sp3.serial())
plt.xlabel("Time")
plt.ylabel("Number Of Molecules")
plt.xlim(data.T[0][0], data.T[0][-1])
plt.legend(loc="best", shadow=True)
plt.show()

```



See also [Reversible](#) and [Reversible \(Diffusion-limited\)](#) in the Tests section for more detailed comparisons between methods.

2.12 Tyson1991

This model is described in the article:

- J.J. Tyson, “Modeling the cell division cycle: cdc2 and cyclin interactions.”, Proc. Natl. Acad. Sci. U.S.A., 88(16), 7328-32, 1991.

Abstract: The proteins cdc2 and cyclin form a heterodimer (maturation promoting factor) that controls the major events of the cell cycle. A mathematical model for the interactions of cdc2 and cyclin is constructed. Simulation and analysis of the model show that the control system can operate in three modes: as a steady state with high maturation promoting factor activity, as a spontaneous oscillator, or as an excitable switch. We associate the steady state with metaphase arrest in unfertilized eggs, the spontaneous oscillations with rapid division cycles in early embryos, and the excitable switch with growth-controlled division cycles typical of nonembryonic cells.

```
[1]: %matplotlib inline
from eccl14 import *

[2]: with reaction_rules():
    YT = Y + YP + M + pM
    CT = C2 + CP + M + pM

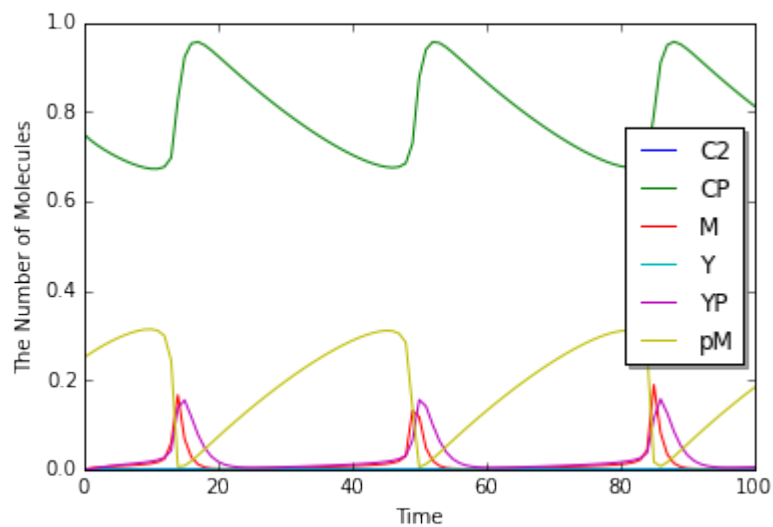
    ~Y > Y | 0.015 / CT
    Y > ~Y | 0.0 * Y
    CP + Y > pM | 200.0 * CP * Y / CT
    pM > M | pM * (0.018 + 180 * ((M / CT) ** 2))
    M > pM | 0.0 * M
    M > C2 + YP | 1.0 * M
    YP > ~YP | 0.6 * YP
    C2 > CP | 1000000.0 * C2
    CP > C2 | 1000.0 * CP

m = get_model()
```

```
[3]: for rr in m.reaction_rules():
      print(rr.as_string())
```

```
C2+CP+M+pM>Y+C2+CP+M+pM| (0.015/ (C2+CP+M+pM) )
Y>| (0.0*Y)
CP+Y+C2+M>pM+C2+M| ( (200.0*CP*Y) / (C2+CP+M+pM) )
pM+C2+CP>M+C2+CP| (pM*(0.018+(180*(M/(C2+CP+M+pM))**2)))
M>pM| (0.0*M)
M>C2+YP| (1.0*M)
YP>| (0.6*YP)
C2>CP| (1000000.0*C2)
CP>C2| (1000.0*CP)
```

```
[4]: run_simulation(100.0, model=m, y0={'CP': 0.75, 'pM': 0.25})
```



3.1 E-Cell4 core API

A submodule of `ecell4_base`

class `ecell4_base.core.AABB`
Bases: `ecell4_base.core.Shape`

Methods

<code>dimension()</code>
<code>distance()</code>
<code>is_inside()</code>
<code>lower()</code>
<code>surface()</code>
<code>upper()</code>

distance()

lower()

surface()

upper()

class `ecell4_base.core.AffineTransformation`
Bases: `ecell4_base.core.Shape`

Methods

<code>dimension()</code>
<code>first()</code>
<code>is_inside()</code>
<code>rescale()</code>
<code>root()</code>
<code>second()</code>
<code>shift()</code>
<code>surface()</code>
<code>third()</code>

Continued on next page

Table 2 – continued from previous page

translate()

xroll()

yroll()

zroll()

first()
rescale()
root()
second()
shift()
surface()
third()
translate()
xroll()
yroll()
zroll()**class** `ecell14_base.core.CSVObserver`
Bases: `ecell14_base.core.Observer`**Methods**

filename()

log()

next_time()

num_steps()

reset()

set_formatter()

set_header()

filename()
log()
set_formatter()
set_header()**class** `ecell14_base.core.Complement`
Bases: `ecell14_base.core.Shape`**Methods**

another()

dimension()

is_inside()

Continued on next page

Table 4 – continued from previous page

one()

surface()

another()**one()****surface()****class** `ecell4_base.core.Cylinder`Bases: `ecell4_base.core.Shape`**Methods**

axis()

center()

dimension()

distance()

half_height()

is_inside()

surface()

axis()**center()****distance()****half_height()****surface()****class** `ecell4_base.core.CylindricalSurface`Bases: `ecell4_base.core.Shape`**Methods**

axis()

center()

dimension()

distance()

half_height()

inside()

is_inside()

radius()

axis()**center()****distance()****half_height()****inside()**

radius()

class `ecell4_base.core.FixedIntervalCSVObserver`

Bases: `ecell4_base.core.Observer`

Methods

`filename()`

`log()`

`next_time()`

`num_steps()`

`reset()`

`set_formatter()`

`set_header()`

filename()

log()

set_formatter()

set_header()

class `ecell4_base.core.FixedIntervalHDF5Observer`

Bases: `ecell4_base.core.Observer`

Methods

`filename()`

Overloaded function.

`next_time()`

`num_steps()`

`prefix()`

`reset()`

filename()

Overloaded function.

1. `filename(self: ecell4_base.core.FixedIntervalHDF5Observer) -> str`

2. `filename(self: ecell4_base.core.FixedIntervalHDF5Observer, arg0: int) -> str`

prefix()

class `ecell4_base.core.FixedIntervalNumberObserver`

Bases: `ecell4_base.core.Observer`

Methods

`data()`

`next_time()`

`num_steps()`

`reset()`

Continued on next page

Table 9 – continued from previous page

`save()`

`targets()`

`data()`

`save()`

`targets()`

class `ecell4_base.core.FixedIntervalPythonHooker`
 Bases: `ecell4_base.core.Observer`

Methods

`next_time()`

`num_steps()`

`reset()`

class `ecell4_base.core.FixedIntervalTrackingObserver`
 Bases: `ecell4_base.core.Observer`

Methods

`data()`

`next_time()`

`num_steps()`

`num_tracers()`

`reset()`

`t()`

`data()`

`num_tracers()`

`t()`

class `ecell4_base.core.FixedIntervalTrajectoryObserver`
 Bases: `ecell4_base.core.Observer`

Methods

`data()`

`next_time()`

`num_steps()`

`num_tracers()`

`reset()`

`t()`

`data()`

```
num_tracers()
```

```
t()
```

```
class ecell4_base.core.GSLRandomNumberGenerator
```

```
    Bases: ecell4_base.core.RandomNumberGenerator
```

Methods

```
binomial()
```

```
gaussian()
```

```
load()
```

```
save()
```

```
seed()
```

```
seed()
```

```
uniform()
```

```
uniform()
```

```
uniform_int()
```

```
class ecell4_base.core.Integer3
```

```
    Bases: pybind11_builtins.pybind11_object
```

Attributes

```
col
```

```
layer
```

```
row
```

```
col
```

```
layer
```

```
row
```

```
class ecell4_base.core.MeshSurface
```

```
    Bases: ecell4_base.core.Shape
```

Methods

```
dimension()
```

```
edge_lengths()
```

```
filename()
```

```
is_inside()
```

```
edge_lengths()
```

```
filename()
```

```
class ecell4_base.core.Model
```

```
    Bases: pybind11_builtins.pybind11_object
```

Methods

<code>add_reaction_rule()</code>	
<code>add_reaction_rules()</code>	
<code>add_species_attribute()</code>	
<code>add_species_attributes()</code>	
<code>apply_species_attributes()</code>	
<code>expand()</code>	Overloaded function.
<code>has_reaction_rule()</code>	
<code>has_species_attribute()</code>	
<code>list_species()</code>	
<code>num_reaction_rules()</code>	
<code>query_reaction_rules()</code>	Overloaded function.
<code>reaction_rules()</code>	
<code>remove_reaction_rule()</code>	
<code>remove_species_attribute()</code>	
<code>species_attributes()</code>	
<code>update_species_attribute()</code>	

`add_reaction_rule()`

`add_reaction_rules()`

`add_species_attribute()`

`add_species_attributes()`

`apply_species_attributes()`

`expand()`

Overloaded function.

1. `expand(self: ecell4_base.core.Model, arg0: List[ecell4_base.core.Species], arg1: int, arg2: Dict[ecell4_base.core.Species, int]) -> ecell4_base.core.Model`
2. `expand(self: ecell4_base.core.Model, arg0: List[ecell4_base.core.Species], arg1: int) -> ecell4_base.core.Model`
3. `expand(self: ecell4_base.core.Model, arg0: List[ecell4_base.core.Species]) -> ecell4_base.core.Model`

`has_reaction_rule()`

`has_species_attribute()`

`list_species()`

`num_reaction_rules()`

`query_reaction_rules()`

Overloaded function.

1. `query_reaction_rules(self: ecell4_base.core.Model, arg0: ecell4_base.core.Species) -> List[ecell4_base.core.ReactionRule]`
2. `query_reaction_rules(self: ecell4_base.core.Model, arg0: ecell4_base.core.Species, arg1: ecell4_base.core.Species) -> List[ecell4_base.core.ReactionRule]`

`reaction_rules()`

`remove_reaction_rule()`

`remove_species_attribute()`

species_attributes()

update_species_attribute()

class `ecell4_base.core.NetfreeModel`

Bases: `ecell4_base.core.Model`

Methods

`add_reaction_rule()`

`add_reaction_rules()`

`add_species_attribute()`

`add_species_attributes()`

`apply_species_attributes()`

`effective()`

`expand()` Overloaded function.

`has_reaction_rule()`

`has_species_attribute()`

`list_species()`

`num_reaction_rules()`

`query_reaction_rules()` Overloaded function.

`reaction_rules()`

`remove_reaction_rule()`

`remove_species_attribute()`

`set_effective()`

`species_attributes()`

`update_species_attribute()`

effective()

set_effective()

class `ecell4_base.core.NetworkModel`

Bases: `ecell4_base.core.Model`

Methods

`add_reaction_rule()`

`add_reaction_rules()`

`add_species_attribute()`

`add_species_attributes()`

`apply_species_attributes()`

`expand()` Overloaded function.

`has_reaction_rule()`

`has_species_attribute()`

`list_species()`

`num_reaction_rules()`

`query_reaction_rules()` Overloaded function.

`reaction_rules()`

`remove_reaction_rule()`

`remove_species_attribute()`

Continued on next page

Table 17 – continued from previous page

<code>species_attributes()</code>
<code>update_species_attribute()</code>

class `ecell4_base.core.NumberObserver`

Bases: `ecell4_base.core.Observer`

Methods

<code>data()</code>
<code>next_time()</code>
<code>num_steps()</code>
<code>reset()</code>
<code>save()</code>
<code>targets()</code>

data()

save()

targets()

class `ecell4_base.core.Observer`

Bases: `pybind11_builtins.pybind11_object`

Methods

<code>next_time()</code>
<code>num_steps()</code>
<code>reset()</code>

next_time()

num_steps()

reset()

class `ecell4_base.core.Particle`

Bases: `pybind11_builtins.pybind11_object`

Methods

<code>D()</code>
<code>position()</code>
<code>radius()</code>
<code>species()</code>

D()

position()

radius()

species()

class `ecell4_base.core.ParticleID`

Bases: `pybind11_builtins.pybind11_object`

Methods

`lot()`

`serial()`

lot()

serial()

class `ecell4_base.core.ParticleVoxel`

Bases: `pybind11_builtins.pybind11_object`

Methods

`D()`

`coordinate()`

`loc()`

`radius()`

`species()`

D()

coordinate()

loc()

radius()

species()

class `ecell4_base.core.PlanarSurface`

Bases: `ecell4_base.core.Shape`

Methods

`dimension()`

`e0()`

`e1()`

`is_inside()`

`normal()`

`origin()`

e0()

e1()

normal()

origin()

`ecell4_base.core.Quantity`
 alias of `ecell4_base.core.Quantity_Real`

class `ecell4_base.core.Quantity_Integer`
 Bases: `pybind11_builtins.pybind11_object`

Attributes

magnitude

units

magnitude

units

class `ecell4_base.core.Quantity_Real`
 Bases: `pybind11_builtins.pybind11_object`

Attributes

magnitude

units

magnitude

units

class `ecell4_base.core.RandomNumberGenerator`
 Bases: `pybind11_builtins.pybind11_object`

Methods

<code>binomial()</code>	
<code>gaussian()</code>	
<code>load()</code>	
<code>save()</code>	
<code>seed()</code>	Overloaded function.
<code>uniform()</code>	Overloaded function.
<code>uniform_int()</code>	

binomial()

gaussian()

load()

save()

seed()

Overloaded function.

1. `seed(self: ecell4_base.core.RandomNumberGenerator) -> None`

2. `seed(self: ecell4_base.core.RandomNumberGenerator, arg0: int) -> None`

uniform()

Overloaded function.

1. `uniform(self: ecell4_base.core.RandomNumberGenerator, arg0: float, arg1: float) -> float`

2. `uniform(self: ecell4_base.core.RandomNumberGenerator, arg0: float, arg1: float) -> float`

```
uniform_int()
```

```
class ecell4_base.core.ReactionRule
    Bases: pybind11_builtins.pybind11_object
```

Methods

<code>add_product()</code>	
<code>add_reactant()</code>	
<code>as_string()</code>	
<code>count()</code>	
<code>generate()</code>	
<code>get_descriptor()</code>	
<code>get_k()</code>	
<code>has_descriptor()</code>	
<code>k()</code>	
<code>policy()</code>	
<code>products()</code>	
<code>reactants()</code>	
<code>reset_descriptor()</code>	
<code>set_descriptor()</code>	
<code>set_k()</code>	Overloaded function.
<code>set_policy()</code>	

```
add_product()
```

```
add_reactant()
```

```
as_string()
```

```
count()
```

```
generate()
```

```
get_descriptor()
```

```
get_k()
```

```
has_descriptor()
```

```
k()
```

```
policy()
```

```
products()
```

```
reactants()
```

```
reset_descriptor()
```

```
set_descriptor()
```

```
set_k()
```

```
Overloaded function.
```

```
1. set_k(self: ecell4_base.core.ReactionRule, arg0: float) -> None
```

```
2. set_k(self: ecell4_base.core.ReactionRule, arg0: ecell4_base.core.Quantity_Real) -> None
```

```
set_policy()
```

```
class ecell4_base.core.ReactionRuleDescriptor
    Bases: pybind11_builtins.pybind11_object
```

Methods

```
product_coefficients()
propensity()
reactant_coefficients()
set_product_coefficient()
set_product_coefficients()
set_reactant_coefficient()
set_reactant_coefficients()
```

```
product_coefficients()
propensity()
reactant_coefficients()
set_product_coefficient()
set_product_coefficients()
set_reactant_coefficient()
set_reactant_coefficients()
```

```
class ecell4_base.core.ReactionRuleDescriptorMassAction
    Bases: ecell4_base.core.ReactionRuleDescriptor
```

Methods

```
get_k()
k()
product_coefficients()
propensity()
reactant_coefficients()
set_k() Overloaded function.
set_product_coefficient()
set_product_coefficients()
set_reactant_coefficient()
set_reactant_coefficients()
```

```
get_k()
k()
set_k()
    Overloaded function.
    1. set_k(self: ecell4_base.core.ReactionRuleDescriptorMassAction, arg0: float) -> None
    2. set_k(self: ecell4_base.core.ReactionRuleDescriptorMassAction, arg0:
        ecell4_base.core.Quantity_Real) -> None
```

```
class ecell4_base.core.ReactionRuleDescriptorPyfunc
```

Bases: *ecell4_base.core.ReactionRuleDescriptor*

Methods

as_string()

get()

product_coefficients()

propensity()

reactant_coefficients()

set_name()

set_product_coefficient()

set_product_coefficients()

set_reactant_coefficient()

set_reactant_coefficients()

as_string()
get()
set_name()

class *ecell4_base.core.ReactionRulePolicy*

Bases: *pybind11_builtins.pybind11_object*

Members:

STRICT

IMPLICIT

DESTROY

Attributes

name (self: handle) -> str

DESTROY = **ReactionRulePolicy.DESTROY**

IMPLICIT = **ReactionRulePolicy.IMPLICIT**

STRICT = **ReactionRulePolicy.STRICT**

name

(self: handle) -> str

class *ecell4_base.core.Real3*

Bases: *pybind11_builtins.pybind11_object*

class *ecell4_base.core.Rod*

Bases: *ecell4_base.core.Shape*

Methods

dimension()

distance()

is_inside()

length()

Continued on next page

Table 29 – continued from previous page

origin()

radius()

shift()

surface()

distance()

length()

origin()

radius()

shift()

surface()

class `ecell4_base.core.RodSurface`
 Bases: `ecell4_base.core.Shape`

Methods

dimension()

distance()

is_inside()

length()

origin()

radius()

shift()

distance()

length()

origin()

radius()

shift()

class `ecell4_base.core.Shape`
 Bases: `pybind11_builtins.pybind11_object`

Methods

dimension()

is_inside()

dimension()

is_inside()

class `ecell4_base.core.Simulator`
 Bases: `pybind11_builtins.pybind11_object`

Methods

<code>check_reaction()</code>	
<code>dt()</code>	
<code>initialize()</code>	
<code>next_time()</code>	
<code>num_steps()</code>	
<code>set_dt()</code>	
<code>step()</code>	Overloaded function.
<code>t()</code>	

check_reaction()

dt()

initialize()

next_time()

num_steps()

set_dt()

step()

Overloaded function.

1. `step(self: ecell4_base.core.Simulator) -> None`
2. `step(self: ecell4_base.core.Simulator, arg0: float) -> bool`

t()

class ecell4_base.core.Species

Bases: `pybind11_builtins.pybind11_object`

Methods

<code>D()</code>	
<code>add_unit()</code>	
<code>count()</code>	
<code>dimension()</code>	
<code>get_attribute()</code>	
<code>has_attribute()</code>	
<code>list_attributes()</code>	
<code>location()</code>	
<code>radius()</code>	
<code>remove_attribute()</code>	
<code>serial()</code>	
<code>set_attribute()</code>	Overloaded function.
<code>units()</code>	

D()

add_unit()

count()

dimension()

get_attribute()

has_attribute()

list_attributes()

location()

radius()

remove_attribute()

serial()

set_attribute()

Overloaded function.

1. set_attribute(self: ecell4_base.core.Species, arg0: str, arg1: str) -> None
2. set_attribute(self: ecell4_base.core.Species, arg0: str, arg1: str) -> None
3. set_attribute(self: ecell4_base.core.Species, arg0: str, arg1: float) -> None
4. set_attribute(self: ecell4_base.core.Species, arg0: str, arg1: int) -> None
5. set_attribute(self: ecell4_base.core.Species, arg0: str, arg1: ecell4_base.core.Quantity_Real) -> None
6. set_attribute(self: ecell4_base.core.Species, arg0: str, arg1: ecell4_base.core.Quantity_Integer) -> None

units()

class ecell4_base.core.Sphere

Bases: *ecell4_base.core.Shape*

Methods

center()

dimension()

distance()

is_inside()

radius()

surface()

center()

distance()

radius()

surface()

class ecell4_base.core.SphericalSurface

Bases: *ecell4_base.core.Shape*

Methods

```

center()
dimension()
distance()
inside()
is_inside()
radius()

```

```

center ()
distance ()
inside ()
radius ()

```

```

class ecell14_base.core.Surface
    Bases: ecell14_base.core.Shape

```

Methods

```

dimension()
is_inside()
root()

```

```

root ()

```

```

class ecell14_base.core.TimeoutObserver
    Bases: ecell14_base.core.Observer

```

Methods

```

accumulation()
duration()
interval()
next_time()
num_steps()
reset()

```

```

accumulation ()
duration ()
interval ()

```

```

class ecell14_base.core.TimingNumberObserver
    Bases: ecell14_base.core.Observer

```

Methods

```

data()

```

Continued on next page

Table 38 – continued from previous page

<code>next_time()</code>
<code>num_steps()</code>
<code>reset()</code>
<code>save()</code>
<code>targets()</code>

`data()``save()``targets()`**class** `ecell4_base.core.TimingTrajectoryObserver`Bases: `ecell4_base.core.Observer`**Methods**

<code>data()</code>
<code>next_time()</code>
<code>num_steps()</code>
<code>num_tracers()</code>
<code>reset()</code>
<code>t()</code>

`data()``num_tracers()``t()`**class** `ecell4_base.core.Union`Bases: `ecell4_base.core.Shape`**Methods**

<code>another()</code>
<code>dimension()</code>
<code>is_inside()</code>
<code>one()</code>
<code>surface()</code>

`another()``one()``surface()`**class** `ecell4_base.core.UnitSpecies`Bases: `pybind11_builtins.pybind11_object`**Methods**

add_site()

deserialize()

name()

serial()

add_site()
deserialize()
name()
serial()**class** ecell4_base.core.WorldInterface
Bases: pybind11_builtins.pybind11_object

Methods

edge_lengths()

get_particle()

get_value()

get_value_exact()

has_particle()

has_species()

list_particles() Overloaded function.

list_particles_exact()

list_species()

load()

num_molecules()

num_molecules_exact()

num_particles() Overloaded function.

num_particles_exact()

save()

set_t()

t()

volume()

edge_lengths()
get_particle()
get_value()
get_value_exact()
has_particle()
has_species()
list_particles()
Overloaded function.

1. `list_particles(self: ecell4_base.core.WorldInterface) -> List[Tuple[ecell4_base.core.ParticleID, ecell4_base.core.Particle]]`

```

    2. list_particles(self: ecell4_base.core.WorldInterface, arg0: ecell4_base.core.Species) ->
       List[Tuple[ecell4_base.core.ParticleID, ecell4_base.core.Particle]]

list_particles_exact()

list_species()

load()

num_molecules()

num_molecules_exact()

num_particles()
    Overloaded function.
    1. num_particles(self: ecell4_base.core.WorldInterface) -> int
    2. num_particles(self: ecell4_base.core.WorldInterface, arg0: ecell4_base.core.Species) -> int

num_particles_exact()

save()

set_t()

t()

volume()

ecell4_base.core.cbrt()

ecell4_base.core.count_species_matches()

ecell4_base.core.create_binding_reaction_rule()

ecell4_base.core.create_degradation_reaction_rule()

ecell4_base.core.create_synthesis_reaction_rule()

ecell4_base.core.create_unbinding_reaction_rule()

ecell4_base.core.create_unimolecular_reaction_rule()

ecell4_base.core.create_x_plane()

ecell4_base.core.create_y_plane()

ecell4_base.core.create_z_plane()

ecell4_base.core.cross_product()

ecell4_base.core.dot_product()
    Overloaded function.
    1. dot_product(arg0: ecell4_base.core.Real3, arg1: ecell4_base.core.Real3) -> float
    2. dot_product(arg0: ecell4_base.core.Integer3, arg1: ecell4_base.core.Integer3) -> int

ecell4_base.core.format_species()

ecell4_base.core.integer3_abs()

ecell4_base.core.integer3_add()

ecell4_base.core.integer3_dot_product()

ecell4_base.core.integer3_length()

ecell4_base.core.integer3_length_sq()

```

```

ecell4_base.core.integer3_multiply()
ecell4_base.core.integer3_subtract()
ecell4_base.core.length()
    Overloaded function.
        1. length(arg0: ecell4_base.core.Real3) -> float
        2. length(arg0: ecell4_base.core.Integer3) -> float
ecell4_base.core.length_sq()
    Overloaded function.
        1. length_sq(arg0: ecell4_base.core.Real3) -> float
        2. length_sq(arg0: ecell4_base.core.Integer3) -> int
ecell4_base.core.load_version_information()
ecell4_base.core.ones()
ecell4_base.core.real3_abs()
ecell4_base.core.real3_add()
ecell4_base.core.real3_divide()
ecell4_base.core.real3_dot_product()
ecell4_base.core.real3_length()
ecell4_base.core.real3_length_sq()
ecell4_base.core.real3_multiply()
ecell4_base.core.real3_subtract()
ecell4_base.core.unitx()
ecell4_base.core.unity()
ecell4_base.core.unitz()

```

3.2 E-Cell4 gillespie API

A submodule of `ecell4_base`

```

ecell4_base.gillespie.Factory
    alias of ecell4_base.gillespie.GillespieFactory
class ecell4_base.gillespie.GillespieFactory
    Bases: pybind11_builtins.pybind11_object

```

Methods

<i>rng()</i>	
<i>simulator()</i>	Overloaded function.
<i>world()</i>	Overloaded function.

rng()

simulator()

Overloaded function.

1. simulator(self: ecell4_base.gillespie.GillespieFactory, world: ecell4::gillespie::GillespieWorld) -> ecell4::gillespie::GillespieSimulator
2. simulator(self: ecell4_base.gillespie.GillespieFactory, world: ecell4::gillespie::GillespieWorld, model: ecell4_base.core.Model) -> ecell4::gillespie::GillespieSimulator

world()

Overloaded function.

1. world(self: ecell4_base.gillespie.GillespieFactory, edge_lengths: ecell4_base.core.Real3 = <ecell4_base.core.Real3 object at 0x7fb3e1a9c998>) -> ecell4::gillespie::GillespieWorld
2. world(self: ecell4_base.gillespie.GillespieFactory, volume: float) -> ecell4::gillespie::GillespieWorld
3. world(self: ecell4_base.gillespie.GillespieFactory, filename: str) -> ecell4::gillespie::GillespieWorld
4. world(self: ecell4_base.gillespie.GillespieFactory, model: ecell4_base.core.Model) -> ecell4::gillespie::GillespieWorld

class ecell4_base.gillespie.GillespieSimulatorBases: *ecell4_base.core.Simulator***Methods**

check_reaction()	
dt()	
initialize()	
<i>last_reactions()</i>	
<i>model()</i>	
next_time()	
num_steps()	
<i>run()</i>	Overloaded function.
set_dt()	
<i>set_t()</i>	
step()	Overloaded function.
t()	
<i>world()</i>	

last_reactions()**model()****run()**

Overloaded function.

1. run(self: ecell4_base.gillespie.GillespieSimulator, duration: float, is_dirty: bool = True) -> None
2. run(self: ecell4_base.gillespie.GillespieSimulator, duration: float, observer: ecell4_base.core.Observer, is_dirty: bool = True) -> None
3. run(self: ecell4_base.gillespie.GillespieSimulator, duration: float, observers: List[ecell4_base.core.Observer], is_dirty: bool = True) -> None

set_t()**world()**

```
class ecell4_base.gillespie.GillespieWorld
```

```
    Bases: ecell4_base.core.WorldInterface
```

Methods

<i>add_molecules()</i>	Overloaded function.
<i>bind_to()</i>	
<i>edge_lengths()</i>	
<i>get_particle()</i>	
<i>get_value()</i>	
<i>get_value_exact()</i>	
<i>has_particle()</i>	
<i>has_species()</i>	
<i>list_particles()</i>	Overloaded function.
<i>list_particles_exact()</i>	
<i>list_species()</i>	
<i>load()</i>	
<i>new_particle()</i>	Overloaded function.
<i>num_molecules()</i>	
<i>num_molecules_exact()</i>	
<i>num_particles()</i>	Overloaded function.
<i>num_particles_exact()</i>	
<i>remove_molecules()</i>	
<i>rng()</i>	
<i>save()</i>	
<i>set_t()</i>	
<i>set_value()</i>	
<i>t()</i>	
<i>volume()</i>	

```
add_molecules ()
```

```
    Overloaded function.
```

1. `add_molecules(self: ecell4_base.gillespie.GillespieWorld, arg0: ecell4_base.core.Species, arg1: int) -> None`
2. `add_molecules(self: ecell4_base.gillespie.GillespieWorld, arg0: ecell4_base.core.Species, arg1: int, arg2: ecell4_base.core.Shape) -> None`

```
bind_to ()
```

```
new_particle ()
```

```
    Overloaded function.
```

1. `new_particle(self: ecell4_base.gillespie.GillespieWorld, arg0: ecell4_base.core.Particle) -> Tuple[Tuple[ecell4_base.core.ParticleID, ecell4_base.core.Particle], bool]`
2. `new_particle(self: ecell4_base.gillespie.GillespieWorld, arg0: ecell4_base.core.Species, arg1: ecell4_base.core.Real3) -> Tuple[Tuple[ecell4_base.core.ParticleID, ecell4_base.core.Particle], bool]`

```
remove_molecules ()
```

```
rng ()
```

```
set_value ()
```



```
class ecell4_base.gillespie.ReactionInfo
    Bases: pybind11_builtins.pybind11_object
```

Methods

<i>products()</i>
<i>reactants()</i>
<i>t()</i>

```
products ()
reactants ()
t ()
```

```
ecell4_base.gillespie.Simulator
    alias of ecell4_base.gillespie.GillespieSimulator
ecell4_base.gillespie.World
    alias of ecell4_base.gillespie.GillespieWorld
```

3.3 E-Cell4 ode API

A submodule of ecell4_base

```
ecell4_base.ode.Factory
    alias of ecell4_base.ode.ODEFactory
```

```
class ecell4_base.ode.ODEFactory
    Bases: pybind11_builtins.pybind11_object
```

Methods

<i>rng()</i>	
<i>simulator()</i>	Overloaded function.
<i>world()</i>	Overloaded function.

```
rng ()
simulator ()
    Overloaded function.
    1. simulator(self: ecell4_base.ode.ODEFactory, world: ecell4::ode::ODEWorld) ->
        ecell4::ode::ODESimulator
    2. simulator(self: ecell4_base.ode.ODEFactory, world: ecell4::ode::ODEWorld, model:
        ecell4_base.core.Model) -> ecell4::ode::ODESimulator
world ()
    Overloaded function.
    1. world(self: ecell4_base.ode.ODEFactory, edge_lengths: ecell4_base.core.Real3 =
        <ecell4_base.core.Real3 object at 0x7fb3e1ab9298>) -> ecell4::ode::ODEWorld
    2. world(self: ecell4_base.ode.ODEFactory, volume: float) -> ecell4::ode::ODEWorld
```

3. world(self: ecell4_base.ode.ODEFactory, filename: str) -> ecell4::ode::ODEWorld
4. world(self: ecell4_base.ode.ODEFactory, model: ecell4_base.core.Model) -> ecell4::ode::ODEWorld

class ecell4_base.ode.ODESimulator
Bases: *ecell4_base.core.Simulator*

Methods

<i>absolute_tolerance()</i>	
<i>check_reaction()</i>	
<i>dt()</i>	
<i>initialize()</i>	
<i>model()</i>	
<i>next_time()</i>	
<i>num_steps()</i>	
<i>relative_tolerance()</i>	
<i>run()</i>	Overloaded function.
<i>set_absolute_tolerance()</i>	
<i>set_dt()</i>	
<i>set_relative_tolerance()</i>	
<i>set_t()</i>	
<i>step()</i>	Overloaded function.
<i>t()</i>	
<i>world()</i>	

absolute_tolerance()

model()

relative_tolerance()

run()

Overloaded function.

1. run(self: ecell4_base.ode.ODESimulator, duration: float, is_dirty: bool = True) -> None
2. run(self: ecell4_base.ode.ODESimulator, duration: float, observer: ecell4_base.core.Observer, is_dirty: bool = True) -> None
3. run(self: ecell4_base.ode.ODESimulator, duration: float, observers: List[ecell4_base.core.Observer], is_dirty: bool = True) -> None

set_absolute_tolerance()

set_relative_tolerance()

set_t()

world()

class ecell4_base.ode.ODESolverType
Bases: *pybind11_builtins.pybind11_object*

Members:

RUNGE_KUTTA_CASH_KARP54

ROSENBROCK4_CONTROLLER

EULER

Attributes

name (self: handle) -> str

EULER = ODESolverType.EULER

ROSENBROCK4_CONTROLLER = ODESolverType.ROSENBROCK4_CONTROLLER

RUNGE_KUTTA_CASH_KARP54 = ODESolverType.RUNGE_KUTTA_CASH_KARP54

name

(self: handle) -> str

class ecell4_base.ode.ODEWorld

Bases: *ecell4_base.core.WorldInterface*

Methods

<i>add_molecules()</i>	Overloaded function.
<i>bind_to()</i>	
<i>edge_lengths()</i>	
<i>evaluate()</i>	
<i>get_particle()</i>	
<i>get_value()</i>	
<i>get_value_exact()</i>	
<i>has_particle()</i>	
<i>has_species()</i>	
<i>list_particles()</i>	Overloaded function.
<i>list_particles_exact()</i>	
<i>list_species()</i>	
<i>load()</i>	
<i>new_particle()</i>	Overloaded function.
<i>num_molecules()</i>	
<i>num_molecules_exact()</i>	
<i>num_particles()</i>	Overloaded function.
<i>num_particles_exact()</i>	
<i>release_species()</i>	
<i>remove_molecules()</i>	
<i>reserve_species()</i>	
<i>save()</i>	
<i>set_t()</i>	
<i>set_value()</i>	
<i>set_volume()</i>	
<i>t()</i>	
<i>volume()</i>	

add_molecules()

Overloaded function.

1. add_molecules(self: ecell4_base.ode.ODEWorld, arg0: ecell4_base.core.Species, arg1: float) -> None
2. add_molecules(self: ecell4_base.ode.ODEWorld, arg0: ecell4_base.core.Species, arg1: int, arg2: ecell4_base.core.Shape) -> None

bind_to()

evaluate()

new_particle()

Overloaded function.

1. `new_particle(self: ecell4_base.ode.ODEWorld, arg0: ecell4_base.core.Particle) -> Tuple[Tuple[ecell4_base.core.ParticleID, ecell4_base.core.Particle], bool]`
2. `new_particle(self: ecell4_base.ode.ODEWorld, arg0: ecell4_base.core.Species, arg1: ecell4_base.core.Real3) -> Tuple[Tuple[ecell4_base.core.ParticleID, ecell4_base.core.Particle], bool]`

release_species()

remove_molecules()

reserve_species()

set_value()

set_volume()

`ecell4_base.ode.Simulator`

alias of `ecell4_base.ode.ODESimulator`

`ecell4_base.ode.World`

alias of `ecell4_base.ode.ODEWorld`

3.4 E-Cell4 meso API

A submodule of `ecell4_base`

`ecell4_base.meso.Factory`

alias of `ecell4_base.meso.MesoscopicFactory`

class `ecell4_base.meso.MesoscopicFactory`

Bases: `pybind11_builtins.pybind11_object`

Methods

<code>rng()</code>	
<code>simulator()</code>	Overloaded function.
<code>world()</code>	Overloaded function.

rng()

simulator()

Overloaded function.

1. `simulator(self: ecell4_base.meso.MesoscopicFactory, world: ecell4::meso::MesoscopicWorld) -> ecell4::meso::MesoscopicSimulator`
2. `simulator(self: ecell4_base.meso.MesoscopicFactory, world: ecell4::meso::MesoscopicWorld, model: ecell4_base.core.Model) -> ecell4::meso::MesoscopicSimulator`

world()

Overloaded function.

1. world(self: ecell4_base.meso.MesoscopicFactory, edge_lengths: ecell4_base.core.Real3 = <ecell4_base.core.Real3 object at 0x7fb3e1a9c810>) -> ecell4::meso::MesoscopicWorld
2. world(self: ecell4_base.meso.MesoscopicFactory, volume: float) -> ecell4::meso::MesoscopicWorld
3. world(self: ecell4_base.meso.MesoscopicFactory, filename: str) -> ecell4::meso::MesoscopicWorld
4. world(self: ecell4_base.meso.MesoscopicFactory, model: ecell4_base.core.Model) -> ecell4::meso::MesoscopicWorld

class ecell4_base.meso.MesoscopicSimulator

Bases: *ecell4_base.core.Simulator*

Methods

check_reaction()	
dt()	
initialize()	
last_reactions()	
model()	
next_time()	
num_steps()	
run()	Overloaded function.
set_dt()	
set_t()	
step()	Overloaded function.
t()	
world()	

last_reactions()

model()

run()

Overloaded function.

1. run(self: ecell4_base.meso.MesoscopicSimulator, duration: float, is_dirty: bool = True) -> None
2. run(self: ecell4_base.meso.MesoscopicSimulator, duration: float, observer: ecell4_base.core.Observer, is_dirty: bool = True) -> None
3. run(self: ecell4_base.meso.MesoscopicSimulator, duration: float, observers: List[ecell4_base.core.Observer], is_dirty: bool = True) -> None

set_t()

world()

class ecell4_base.meso.MesoscopicWorld

Bases: *ecell4_base.core.WorldInterface*

Methods

add_molecules()	Overloaded function.
add_structure()	

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Table 52 – continued from previous page

<i>bind_to()</i>	
<i>check_structure()</i>	
<i>coord2global()</i>	
<i>edge_lengths()</i>	
<i>get_occupancy()</i>	Overloaded function.
<i>get_particle()</i>	
<i>get_value()</i>	
<i>get_value_exact()</i>	
<i>get_volume()</i>	
<i>global2coord()</i>	
<i>has_particle()</i>	
<i>has_species()</i>	
<i>has_structure()</i>	
<i>list_coordinates()</i>	
<i>list_coordinates_exact()</i>	
<i>list_particles()</i>	Overloaded function.
<i>list_particles_exact()</i>	
<i>list_species()</i>	
<i>load()</i>	
<i>matrix_sizes()</i>	
<i>new_particle()</i>	Overloaded function.
<i>num_molecules()</i>	Overloaded function.
<i>num_molecules_exact()</i>	
<i>num_particles()</i>	Overloaded function.
<i>num_particles_exact()</i>	
<i>num_subvolumes()</i>	Overloaded function.
<i>on_structure()</i>	
<i>position2coordinate()</i>	
<i>position2global()</i>	
<i>remove_molecules()</i>	Overloaded function.
<i>rng()</i>	
<i>save()</i>	
<i>set_t()</i>	
<i>set_value()</i>	
<i>subvolume()</i>	
<i>subvolume_edge_lengths()</i>	
<i>t()</i>	
<i>volume()</i>	

add_molecules ()

Overloaded function.

1. `add_molecules(self: eccl4_base.meso.MesoscopicWorld, arg0: eccl4_base.core.Species, arg1: int)`
-> None
2. `add_molecules(self: eccl4_base.meso.MesoscopicWorld, arg0: eccl4_base.core.Species, arg1: int, arg2: int)` -> None
3. `add_molecules(self: eccl4_base.meso.MesoscopicWorld, arg0: eccl4_base.core.Species, arg1: int, arg2: eccl4_base.core.Integer3)` -> None
4. `add_molecules(self: eccl4_base.meso.MesoscopicWorld, arg0: eccl4_base.core.Species, arg1: int, arg2: eccl4_base.core.Shape)` -> None

```

add_structure ()
bind_to ()
check_structure ()
coord2global ()
get_occupancy ()
    Overloaded function.
    1. get_occupancy(self: ecell4_base.meso.MesoscopicWorld, arg0: ecell4_base.core.Species, arg1: int)
       -> float
    2. get_occupancy(self: ecell4_base.meso.MesoscopicWorld, arg0: ecell4_base.core.Species, arg1:
       ecell4_base.core.Integer3) -> float
get_volume ()
global2coord ()
has_structure ()
list_coordinates ()
list_coordinates_exact ()
matrix_sizes ()
new_particle ()
    Overloaded function.
    1. new_particle(self: ecell4_base.meso.MesoscopicWorld, arg0: ecell4_base.core.Particle) -> Tu-
       ple[Tuple[ecell4_base.core.ParticleID, ecell4_base.core.Particle], bool]
    2. new_particle(self: ecell4_base.meso.MesoscopicWorld, arg0: ecell4_base.core.Species, arg1:
       ecell4_base.core.Real3) -> Tuple[Tuple[ecell4_base.core.ParticleID, ecell4_base.core.Particle], bool]
num_molecules ()
    Overloaded function.
    1. num_molecules(self: ecell4_base.meso.MesoscopicWorld, arg0: ecell4_base.core.Species) -> int
    2. num_molecules(self: ecell4_base.meso.MesoscopicWorld, arg0: ecell4_base.core.Species, arg1: int)
       -> int
    3. num_molecules(self: ecell4_base.meso.MesoscopicWorld, arg0: ecell4_base.core.Species, arg1:
       ecell4_base.core.Integer3) -> int
num_subvolumes ()
    Overloaded function.
    1. num_subvolumes(self: ecell4_base.meso.MesoscopicWorld) -> int
    2. num_subvolumes(self: ecell4_base.meso.MesoscopicWorld, arg0: ecell4_base.core.Species) -> int
on_structure ()
position2coordinate ()
position2global ()
remove_molecules ()
    Overloaded function.
    1. remove_molecules(self: ecell4_base.meso.MesoscopicWorld, arg0: ecell4_base.core.Species, arg1:
       int) -> None

```

2. `remove_molecules(self: ecell4_base.meso.MesoscopicWorld, arg0: ecell4_base.core.Species, arg1: int, arg2: ecell4_base.core.Integer3) -> None`
3. `remove_molecules(self: ecell4_base.meso.MesoscopicWorld, arg0: ecell4_base.core.Species, arg1: int, arg2: int) -> None`

rng()

set_value()

subvolume()

subvolume_edge_lengths()

class `ecell4_base.meso.ReactionInfo`
Bases: `pybind11_builtins.pybind11_object`

Methods

coordinate()

products()

reactants()

t()

coordinate()

products()

reactants()

t()

`ecell4_base.meso.Simulator`
alias of *ecell4_base.meso.MesoscopicSimulator*

`ecell4_base.meso.World`
alias of *ecell4_base.meso.MesoscopicWorld*

3.5 E-Cell4 spatiocyte API

A submodule of `ecell4_base`

`ecell4_base.spatiocyte.Factory`
alias of *ecell4_base.spatiocyte.SpatiocyteFactory*

class `ecell4_base.spatiocyte.ReactionInfo`
Bases: `pybind11_builtins.pybind11_object`

Methods

products()

reactants()

t()

products()

reactants()

t()

class `ecell4_base.spatiocyte.ReactionInfoItem`

Bases: `pybind11_builtins.pybind11_object`

Attributes

pid

species

voxel

pid

species

voxel

`ecell4_base.spatiocyte.Simulator`

alias of `ecell4_base.spatiocyte.SpatiocyteSimulator`

class `ecell4_base.spatiocyte.SpatiocyteFactory`

Bases: `pybind11_builtins.pybind11_object`

Methods

rng()

simulator()

Overloaded function.

world()

Overloaded function.

rng()

simulator()

Overloaded function.

1. `simulator(self: ecell4_base.spatiocyte.SpatiocyteFactory, world: ecell4::spatiocyte::SpatiocyteWorld)`
-> `ecell4::spatiocyte::SpatiocyteSimulator`
2. `simulator(self: ecell4_base.spatiocyte.SpatiocyteFactory, world: ecell4::spatiocyte::SpatiocyteWorld, model: ecell4_base.core.Model)` -> `ecell4::spatiocyte::SpatiocyteSimulator`

world()

Overloaded function.

1. `world(self: ecell4_base.spatiocyte.SpatiocyteFactory, edge_lengths: ecell4_base.core.Real3 = <ecell4_base.core.Real3 object at 0x7fb3e1ab9b90>)` -> `ecell4::spatiocyte::SpatiocyteWorld`
2. `world(self: ecell4_base.spatiocyte.SpatiocyteFactory, volume: float)` -> `ecell4::spatiocyte::SpatiocyteWorld`
3. `world(self: ecell4_base.spatiocyte.SpatiocyteFactory, filename: str)` -> `ecell4::spatiocyte::SpatiocyteWorld`
4. `world(self: ecell4_base.spatiocyte.SpatiocyteFactory, model: ecell4_base.core.Model)` -> `ecell4::spatiocyte::SpatiocyteWorld`

class `ecell4_base.spatiocyte.SpatiocyteSimulator`

Bases: `ecell4_base.core.Simulator`

Methods

<code>check_reaction()</code>	
<code>dt()</code>	
<code>initialize()</code>	
<code>last_reactions()</code>	
<code>model()</code>	
<code>next_time()</code>	
<code>num_steps()</code>	
<code>run()</code>	Overloaded function.
<code>set_dt()</code>	
<code>set_t()</code>	
<code>step()</code>	Overloaded function.
<code>t()</code>	
<code>world()</code>	

last_reactions()

model()

run()

Overloaded function.

1. `run(self: ecell4_base.spatiocyte.SpatiocyteSimulator, duration: float, is_dirty: bool = True) -> None`
2. `run(self: ecell4_base.spatiocyte.SpatiocyteSimulator, duration: float, observer: ecell4_base.core.Observer, is_dirty: bool = True) -> None`
3. `run(self: ecell4_base.spatiocyte.SpatiocyteSimulator, duration: float, observers: List[ecell4_base.core.Observer], is_dirty: bool = True) -> None`

set_t()

world()

class `ecell4_base.spatiocyte.SpatiocyteWorld`

Bases: `ecell4_base.core.WorldInterface`

Methods

<code>add_molecules()</code>	Overloaded function.
<code>add_structure()</code>	
<code>bind_to()</code>	
<code>calculate_hcp_lengths()</code>	
<code>calculate_shape()</code>	
<code>calculate_volume()</code>	
<code>calculate_voxel_volume()</code>	
<code>edge_lengths()</code>	
<code>get_particle()</code>	
<code>get_value()</code>	
<code>get_value_exact()</code>	
<code>get_volume()</code>	
<code>get_voxel()</code>	
<code>get_voxel_at()</code>	

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Table 57 – continued from previous page

<code>get_voxel_near_by()</code>	
<code>has_particle()</code>	
<code>has_species()</code>	
<code>list_non_structure_particles()</code>	
<code>list_particles()</code>	Overloaded function.
<code>list_particles_exact()</code>	
<code>list_species()</code>	
<code>list_structure_particles()</code>	
<code>load()</code>	
<code>new_particle()</code>	Overloaded function.
<code>new_voxel()</code>	
<code>new_voxel_structure()</code>	
<code>num_molecules()</code>	
<code>num_molecules_exact()</code>	
<code>num_particles()</code>	Overloaded function.
<code>num_particles_exact()</code>	
<code>remove_molecules()</code>	
<code>remove_particle()</code>	
<code>rng()</code>	
<code>save()</code>	
<code>set_t()</code>	
<code>set_value()</code>	
<code>shape()</code>	
<code>size()</code>	
<code>t()</code>	
<code>update_particle()</code>	
<code>volume()</code>	
<code>voxel_radius()</code>	
<code>voxel_volume()</code>	

add_molecules()

Overloaded function.

1. `add_molecules(self: ecell4_base.spatiocyte.SpatiocyteWorld, arg0: ecell4_base.core.Species, arg1: int) -> bool`
2. `add_molecules(self: ecell4_base.spatiocyte.SpatiocyteWorld, arg0: ecell4_base.core.Species, arg1: int, arg2: ecell4_base.core.Shape) -> bool`

add_structure()**bind_to()****calculate_hcp_lengths()****calculate_shape()****calculate_volume()****calculate_voxel_volume()****get_volume()****get_voxel()****get_voxel_at()****get_voxel_near_by()**

```
list_non_structure_particles()
list_structure_particles()
new_particle()
    Overloaded function.
    1. new_particle(self: ecell4_base.spatiocyte.SpatiocyteWorld, arg0: ecell4_base.core.Particle) -> Optional[ecell4_base.core.ParticleID]
    2. new_particle(self: ecell4_base.spatiocyte.SpatiocyteWorld, arg0: ecell4_base.core.Species, arg1: ecell4_base.core.Real3) -> Optional[ecell4_base.core.ParticleID]
new_voxel()
new_voxel_structure()
remove_molecules()
remove_particle()
rng()
set_value()
shape()
size()
update_particle()
voxel_radius()
voxel_volume()
class ecell4_base.spatiocyte.Voxel
    Bases: pybind11_builtins.pybind11_object
```

Methods

```
list_neighbors()
position()
```

```
list_neighbors()
position()
ecell4_base.spatiocyte.World
    alias of ecell4_base.spatiocyte.SpatiocyteWorld
ecell4_base.spatiocyte.create_spatiocyte_world_cell_list_impl()
ecell4_base.spatiocyte.create_spatiocyte_world_square_offlattice_impl()
ecell4_base.spatiocyte.create_spatiocyte_world_vector_impl()
```

3.6 E-Cell4 bd API

A submodule of `ecell4_base`

```
class ecell4_base.bd.BDFactory
    Bases: pybind11_builtins.pybind11_object
```

Methods

<i>rng()</i>	
<i>simulator()</i>	Overloaded function.
<i>world()</i>	Overloaded function.

rng()

simulator()
Overloaded function.

1. simulator(self: ecell4_base.bd.BDFactory, world: ecell4::bd::BDWorld) -> ecell4::bd::BDSimulator
2. simulator(self: ecell4_base.bd.BDFactory, world: ecell4::bd::BDWorld, model: ecell4_base.core.Model) -> ecell4::bd::BDSimulator

world()
Overloaded function.

1. world(self: ecell4_base.bd.BDFactory, edge_lengths: ecell4_base.core.Real3 = <ecell4_base.core.Real3 object at 0x7fb3e1abd570>) -> ecell4::bd::BDWorld
2. world(self: ecell4_base.bd.BDFactory, volume: float) -> ecell4::bd::BDWorld
3. world(self: ecell4_base.bd.BDFactory, filename: str) -> ecell4::bd::BDWorld
4. world(self: ecell4_base.bd.BDFactory, model: ecell4_base.core.Model) -> ecell4::bd::BDWorld

```
class ecell4_base.bd.BDSimulator
    Bases: ecell4_base.core.Simulator
```

Methods

<i>check_reaction()</i>	
<i>dt()</i>	
<i>initialize()</i>	
<i>last_reactions()</i>	
<i>model()</i>	
<i>next_time()</i>	
<i>num_steps()</i>	
<i>run()</i>	Overloaded function.
<i>set_dt()</i>	
<i>set_t()</i>	
<i>step()</i>	Overloaded function.
<i>t()</i>	
<i>world()</i>	

last_reactions()

model()

run()
Overloaded function.

1. `run(self: ecell4_base.bd.BDSimulator, duration: float, is_dirty: bool = True) -> None`
2. `run(self: ecell4_base.bd.BDSimulator, duration: float, observer: ecell4_base.core.Observer, is_dirty: bool = True) -> None`
3. `run(self: ecell4_base.bd.BDSimulator, duration: float, observers: List[ecell4_base.core.Observer], is_dirty: bool = True) -> None`

set_t()

world()

class `ecell4_base.bd.BDWorld`

Bases: `ecell4_base.core.WorldInterface`

Methods

<code>add_molecules()</code>	Overloaded function.
<code>apply_boundary()</code>	
<code>bind_to()</code>	
<code>distance()</code>	
<code>distance_sq()</code>	
<code>edge_lengths()</code>	
<code>get_particle()</code>	
<code>get_value()</code>	
<code>get_value_exact()</code>	
<code>has_particle()</code>	
<code>has_species()</code>	
<code>list_particles()</code>	Overloaded function.
<code>list_particles_exact()</code>	
<code>list_particles_within_radius()</code>	Overloaded function.
<code>list_species()</code>	
<code>load()</code>	
<code>new_particle()</code>	Overloaded function.
<code>num_molecules()</code>	
<code>num_molecules_exact()</code>	
<code>num_particles()</code>	Overloaded function.
<code>num_particles_exact()</code>	
<code>periodic_transpose()</code>	
<code>remove_molecules()</code>	
<code>remove_particle()</code>	
<code>rng()</code>	
<code>save()</code>	
<code>set_t()</code>	
<code>t()</code>	
<code>update_particle()</code>	
<code>volume()</code>	

add_molecules()

Overloaded function.

1. `add_molecules(self: ecell4_base.bd.BDWorld, arg0: ecell4_base.core.Species, arg1: int) -> None`
2. `add_molecules(self: ecell4_base.bd.BDWorld, arg0: ecell4_base.core.Species, arg1: int, arg2: ecell4_base.core.Shape) -> None`

apply_boundary()

bind_to()

distance()

distance_sq()

list_particles_within_radius()

Overloaded function.

1. `list_particles_within_radius(self: ecell4_base.bd.BDWorld, arg0: ecell4_base.core.Real3, arg1: float) -> List[Tuple[Tuple[ecell4_base.core.ParticleID, ecell4_base.core.Particle], float]]`
2. `list_particles_within_radius(self: ecell4_base.bd.BDWorld, arg0: ecell4_base.core.Real3, arg1: float, arg2: ecell4_base.core.ParticleID) -> List[Tuple[Tuple[ecell4_base.core.ParticleID, ecell4_base.core.Particle], float]]`
3. `list_particles_within_radius(self: ecell4_base.bd.BDWorld, arg0: ecell4_base.core.Real3, arg1: float, arg2: ecell4_base.core.ParticleID, arg3: ecell4_base.core.ParticleID) -> List[Tuple[Tuple[ecell4_base.core.ParticleID, ecell4_base.core.Particle], float]]`

new_particle()

Overloaded function.

1. `new_particle(self: ecell4_base.bd.BDWorld, arg0: ecell4_base.core.Particle) -> Tuple[Tuple[ecell4_base.core.ParticleID, ecell4_base.core.Particle], bool]`
2. `new_particle(self: ecell4_base.bd.BDWorld, arg0: ecell4_base.core.Species, arg1: ecell4_base.core.Real3) -> Tuple[Tuple[ecell4_base.core.ParticleID, ecell4_base.core.Particle], bool]`

periodic_transpose()

remove_molecules()

remove_particle()

rng()

update_particle()

ecell4_base.bd.Factory

alias of *ecell4_base.bd.BDFactory*

class ecell4_base.bd.ReactionInfo

Bases: `pybind11_builtins.pybind11_object`

Methods

products()

reactants()

t()

products()

reactants()

t()

ecell4_base.bd.Simulator

alias of *ecell4_base.bd.BDSimulator*

`ecell4_base.bd.World`
alias of `ecell4_base.bd.BDWorld`

3.7 E-Cell4 egfrd API

A submodule of `ecell4_base`

class `ecell4_base.egfrd.BDFactory`
Bases: `pybind11_builtins.pybind11_object`

Methods

<code>rng()</code>	
<code>simulator()</code>	Overloaded function.
<code>world()</code>	Overloaded function.

<code>rng()</code>	
<code>simulator()</code>	Overloaded function.
	1. <code>simulator(self: ecell4_base.egfrd.BDFactory, world: World<CyclicWorldTraits<double> >) -> ecell4_base.egfrd.BDSimulator</code>
	2. <code>simulator(self: ecell4_base.egfrd.BDFactory, world: World<CyclicWorldTraits<double> >, model: ecell4_base.core.Model) -> ecell4_base.egfrd.BDSimulator</code>
<code>world()</code>	Overloaded function.
	1. <code>world(self: ecell4_base.egfrd.BDFactory, edge_lengths: ecell4_base.core.Real3 = <ecell4_base.core.Real3 object at 0x7fb3e1ab19d0>) -> World<CyclicWorldTraits<double> ></code>
	2. <code>world(self: ecell4_base.egfrd.BDFactory, volume: float) -> World<CyclicWorldTraits<double> ></code>
	3. <code>world(self: ecell4_base.egfrd.BDFactory, filename: str) -> World<CyclicWorldTraits<double> ></code>
	4. <code>world(self: ecell4_base.egfrd.BDFactory, model: ecell4_base.core.Model) -> World<CyclicWorldTraits<double> ></code>

class `ecell4_base.egfrd.BDSimulator`
Bases: `ecell4_base.core.Simulator`

Methods

<code>add_potential()</code>	Overloaded function.
<code>check_reaction()</code>	
<code>dt()</code>	
<code>dt_factor()</code>	
<code>initialize()</code>	
<code>last_reactions()</code>	
<code>model()</code>	

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<code>next_time()</code>	
<code>num_steps()</code>	
<code>run()</code>	Overloaded function.
<code>set_dt()</code>	
<code>set_t()</code>	
<code>step()</code>	Overloaded function.
<code>t()</code>	
<code>world()</code>	

add_potential()

Overloaded function.

1. `add_potential(self: ecell4_base.egfrd.BDSimulator, arg0: ecell4_base.core.Species, arg1: float) -> None`
2. `add_potential(self: ecell4_base.egfrd.BDSimulator, arg0: ecell4_base.core.Species, arg1: ecell4_base.core.Shape) -> None`
3. `add_potential(self: ecell4_base.egfrd.BDSimulator, arg0: ecell4_base.core.Species, arg1: ecell4_base.core.Shape, arg2: float) -> None`

dt_factor()**last_reactions()****model()****run()**

Overloaded function.

1. `run(self: ecell4_base.egfrd.BDSimulator, duration: float, is_dirty: bool = True) -> None`
2. `run(self: ecell4_base.egfrd.BDSimulator, duration: float, observer: ecell4_base.core.Observer, is_dirty: bool = True) -> None`
3. `run(self: ecell4_base.egfrd.BDSimulator, duration: float, observers: List[ecell4_base.core.Observer], is_dirty: bool = True) -> None`

set_t()**world()****class ecell4_base.egfrd.EGFRDFactory**Bases: `pybind11_builtins.pybind11_object`**Methods**

<code>rng()</code>	
<code>simulator()</code>	Overloaded function.
<code>world()</code>	Overloaded function.

rng()**simulator()**

Overloaded function.

1. `simulator(self: ecell4_base.egfrd.EGFRDFactory, world: World<CyclicWorldTraits<double> >) -> EGFRDSimulator<EGFRDSimulatorTraitsBase<World<CyclicWorldTraits<double> > > >`

2. `simulator(self: ecell4_base.egfrd.EGFRDFactory, world: World<CyclicWorldTraits<double> >, model: ecell4_base.core.Model) -> EGFRDSimulator<EGFRDSimulatorTraitsBase<World<CyclicWorldTraits<double> >>>`

world()

Overloaded function.

1. `world(self: ecell4_base.egfrd.EGFRDFactory, edge_lengths: ecell4_base.core.Real3 = <ecell4_base.core.Real3 object at 0x7fb3e1ab1768>) -> World<CyclicWorldTraits<double> >`
2. `world(self: ecell4_base.egfrd.EGFRDFactory, volume: float) -> World<CyclicWorldTraits<double> >`
3. `world(self: ecell4_base.egfrd.EGFRDFactory, filename: str) -> World<CyclicWorldTraits<double> >`
4. `world(self: ecell4_base.egfrd.EGFRDFactory, model: ecell4_base.core.Model) -> World<CyclicWorldTraits<double> >`

class `ecell4_base.egfrd.EGFRDSimulator`

Bases: `ecell4_base.core.Simulator`

Methods

<code>check_reaction()</code>	
<code>dt()</code>	
<code>initialize()</code>	
<code>last_reactions()</code>	
<code>model()</code>	
<code>next_time()</code>	
<code>num_steps()</code>	
<code>run()</code>	Overloaded function.
<code>set_dt()</code>	
<code>set_paranoiatic()</code>	
<code>set_t()</code>	
<code>step()</code>	Overloaded function.
<code>t()</code>	
<code>world()</code>	

last_reactions()

model()

run()

Overloaded function.

1. `run(self: ecell4_base.egfrd.EGFRDSimulator, duration: float, is_dirty: bool = True) -> None`
2. `run(self: ecell4_base.egfrd.EGFRDSimulator, duration: float, observer: ecell4_base.core.Observer, is_dirty: bool = True) -> None`
3. `run(self: ecell4_base.egfrd.EGFRDSimulator, duration: float, observers: List[ecell4_base.core.Observer], is_dirty: bool = True) -> None`

set_paranoiatic()

set_t()

world()

```
class ecell4_base.egfrd.EGFRDWorld
    Bases: ecell4_base.core.WorldInterface
```

Methods

<i>add_molecules()</i>	Overloaded function.
<i>apply_boundary()</i>	
<i>bind_to()</i>	
<i>distance()</i>	
<i>edge_lengths()</i>	
<i>get_particle()</i>	
<i>get_value()</i>	
<i>get_value_exact()</i>	
<i>has_particle()</i>	
<i>has_species()</i>	
<i>list_particles()</i>	Overloaded function.
<i>list_particles_exact()</i>	
<i>list_particles_within_radius()</i>	Overloaded function.
<i>list_species()</i>	
<i>load()</i>	
<i>matrix_sizes()</i>	
<i>new_particle()</i>	Overloaded function.
<i>num_molecules()</i>	
<i>num_molecules_exact()</i>	
<i>num_particles()</i>	Overloaded function.
<i>num_particles_exact()</i>	
<i>remove_molecules()</i>	
<i>remove_particle()</i>	
<i>rng()</i>	
<i>save()</i>	
<i>set_t()</i>	
<i>set_value()</i>	
<i>t()</i>	
<i>update_particle()</i>	
<i>volume()</i>	

add_molecules()

Overloaded function.

1. `add_molecules(self: ecell4_base.egfrd.EGFRDWorld, arg0: ecell4_base.core.Species, arg1: int) -> None`
2. `add_molecules(self: ecell4_base.egfrd.EGFRDWorld, arg0: ecell4_base.core.Species, arg1: int, arg2: ecell4_base.core.Shape) -> None`

apply_boundary()

bind_to()

distance()

list_particles_within_radius()

Overloaded function.

1. `list_particles_within_radius(self: ecell4_base.egfrd.EGFRDWorld, arg0: ecell4_base.core.Real3, arg1: float) -> List[Tuple[Tuple[ecell4_base.core.ParticleID, ecell4_base.core.Particle], float]]`
2. `list_particles_within_radius(self: ecell4_base.egfrd.EGFRDWorld, arg0: ecell4_base.core.Real3, arg1: float, arg2: ecell4_base.core.ParticleID) -> List[Tuple[Tuple[ecell4_base.core.ParticleID, ecell4_base.core.Particle], float]]`
3. `list_particles_within_radius(self: ecell4_base.egfrd.EGFRDWorld, arg0: ecell4_base.core.Real3, arg1: float, arg2: ecell4_base.core.ParticleID, arg3: ecell4_base.core.ParticleID) -> List[Tuple[Tuple[ecell4_base.core.ParticleID, ecell4_base.core.Particle], float]]`

matrix_sizes()

new_particle()

Overloaded function.

1. `new_particle(self: ecell4_base.egfrd.EGFRDWorld, arg0: ecell4_base.core.Particle) -> Tuple[Tuple[ecell4_base.core.ParticleID, ecell4_base.core.Particle], bool]`
2. `new_particle(self: ecell4_base.egfrd.EGFRDWorld, arg0: ecell4_base.core.Species, arg1: ecell4_base.core.Real3) -> Tuple[Tuple[ecell4_base.core.ParticleID, ecell4_base.core.Particle], bool]`

remove_molecules()

remove_particle()

rng()

set_value()

update_particle()

`ecell4_base.egfrd.Factory`

alias of `ecell4_base.egfrd.EGFRDFactory`

class ecell4_base.egfrd.ReactionInfo

Bases: `pybind11_builtins.pybind11_object`

Methods

`products()`

`reactants()`

`t()`

products()

reactants()

t()

`ecell4_base.egfrd.Simulator`

alias of `ecell4_base.egfrd.EGFRDSimulator`

`ecell4_base.egfrd.World`

alias of `ecell4_base.egfrd.EGFRDWorld`

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