This is the Chainer documentation.
1.1 Introduction to Chainer

This is the first section of the Chainer Tutorial. In this section, you will learn about the following things:

- Pros and cons of existing frameworks and why we are developing Chainer
- Simple example of forward and backward computation
- Usage of parameterized functions and their gradient computation
- Management of a set of parameterized functions (a.k.a. “model” in most frameworks)
- Parameter optimization

After reading this section, you will be able to:

- Compute gradients of some arithmetics
- Write a multi-layer perceptron with Chainer

1.1.1 Core Concept

As mentioned on the front page, Chainer is a flexible framework for neural networks. One major goal is flexibility, so it must enable us to write complex architectures simply and intuitively.

Most existing deep learning frameworks are based on the “Define-and-Run” scheme. That is, first a network is defined and fixed, and then the user periodically feeds it with minibatches. Since the network is statically defined before any forward/backward computation, all the logic must be embedded into the network architecture as data. Consequently, defining a network architecture in such systems (e.g. Caffe) follows a declarative approach. Note that one can still produce such a static network definition using imperative languages (e.g. Torch7 and Theano-based frameworks).

In contrast, Chainer adopts a “Define-by-Run” scheme, i.e., the network is defined on-the-fly via the actual forward computation. More precisely, Chainer stores the history of computation instead of programming logic. This strategy enables to fully leverage the power of programming logic in Python. For example, Chainer does not need any magic to introduce conditionals and loops into the network definitions. The Define-by-Run scheme is the core concept of Chainer. We will show in this tutorial how to define networks dynamically.

This strategy also makes it easy to write multi-GPU parallelization, since logic comes closer to network manipulation. We will review such amenities in later sections of this tutorial.

Note: In example codes of this tutorial, we assume for simplicity that the following symbols are already imported:
1.1.2 Forward/Backward Computation

As described above, Chainer uses “Define-by-Run” scheme, so forward computation itself defines the network. In order to start forward computation, we have to set the input array to Variable object. Here we start with simple ndarray with only one element:

```python
>>> x_data = np.array([5], dtype=np.float32)
>>> x = Variable(x_data)
```

A Variable object has basic arithmetic operators. In order to compute \( y = x^2 - 2x + 1 \), just write

```python
>>> y = x**2 - 2 * x + 1
```

The resulting \( y \) is also Variable object, whose value can be extracted by accessing the \( data \) attribute:

```python
>>> y.data
array([ 16.], dtype=float32)
```

What \( y \) holds is not only the result value. It also holds the history of computation (or computational graph), which enables us to compute its differentiation. This is done by calling its \( \text{backward() \text{ method:}} \)

```python
>>> y.backward()
```

This runs error backpropagation (a.k.a. backprop or reverse-mode automatic differentiation). Then, the gradient is computed and stored in the \( \text{grad} \) attribute of the input variable \( x \):

```python
>>> x.grad
array([ 8.], dtype=float32)
```

Also we can compute gradients of intermediate variables. Note that Chainer, by default, releases the gradient arrays of intermediate variables for memory efficiency. In order to preserve gradient information, pass the \( \text{retain}_\text{grad} \) argument to the backward method:

```python
>>> z = 2*x
>>> y = x**2 - z + 1
>>> y.backward(retain_grad=True)
>>> z.grad
array([-1.], dtype=float32)
```

All these computations are easily generalized to multi-element array input. Note that if we want to start backward computation from a variable holding a multi-element array, we must set the initial error manually. This is simply done by setting the \( \text{grad} \) attribute of the output variable:

```python
>>> x = Variable(np.array([[1, 2, 3], [4, 5, 6]], dtype=np.float32))
>>> y = x**2 - 2*x + 1
>>> y.grad = np.ones((2, 3), dtype=np.float32)
>>> y.backward()
>>> x.grad
```
1.1.3 Parameterized functions

In order to write neural networks, we have to use some parameterized functions and optimize their parameters. As noted above, functions are predefined in functions module, which also includes parameterized functions.

One of the most fundamental parameterized functions is the Linear function (a.k.a. fully-connected layer or affine transformation). It represents a mathematical function \( f(x) = Wx + b \), where the matrix \( W \) and the vector \( b \) are parameters. A linear function from three-dimensional space to two-dimensional space is defined by:

```python
>>> f = F.Linear(3, 2)
```

The parameters of Linear function are stored in \( W \) and \( b \) attributes. By default, the matrix \( W \) is initialized randomly, while the vector \( b \) is initialized with zeros.

```python
>>> f.W
array([[ 1.33545339, -0.01839679, 0.7662735 ],
        [-1.21562171, -0.44784674, -0.07128379]], dtype=float32)

>>> f.b
array([ 0., 0.], dtype=float32)
```

Instances of a parameterized function class act like usual functions:

```python
>>> x = Variable(np.array([[1, 2, 3], [4, 5, 6]], dtype=np.float32))
>>> y = f(x)
>>> y.data
array([[ 3.5974803 , -2.3251667 ],
        [ 9.84747124, -7.52942371]], dtype=float32)
```

Gradients of parameters are computed by `backward()` method. Note that gradients are accumulated by the method rather than overwritten. So first you must initialize gradients to zero to renew the computation. Gradients of Linear function are stored in \( gW \) and \( gb \) attributes:

```python
>>> f.gW.fill(0)
>>> f.gb.fill(0)
```

Now we can compute the gradients of parameters by simply calling backward method:

```python
>>> y.grad = np.ones((2, 2), dtype=np.float32)
>>> y.backward()
>>> f.gW
array([[ 5., 7., 9.],
        [ 5., 7., 9.]], dtype=float32)
```
1.1.4 FunctionSet

Most neural network architectures contain multiple parameterized functions. `FunctionSet` makes it easy to manage them. This class acts like a simple object, with attributes initialized by keyword arguments of the initializer:

```python
>>> model = FunctionSet(
...     l1=F.Linear(4, 3),
...     l2=F.Linear(3, 2),
... )
```

You can also add additional functions later by setting attributes:

```python
>>> model.l3 = F.Linear(2, 2)
```

Since the `model` is just an object with functions stored as its attributes, we can use these functions in forward computation:

```python
>>> x = Variable(np.array([[1, 2, 3, 4], [5, 6, 7, 8]], dtype=np.float32))
>>> h1 = model.l1(x)
>>> h2 = model.l2(h1)
>>> h3 = model.l3(h2)
```

One of the features of FunctionSet is the ability to collect parameters and gradients. A tuple of all parameters and a tuple of all gradients are extracted by `FunctionSet.parameters` and `FunctionSet.gradients` properties, respectively.

1.1.5 Optimizer

`Optimizer` is the last core feature of Chainer described in this section. It runs a numerical optimization algorithm given tuples of parameters and gradients. Many algorithms are implemented in `optimizers` module. Here we use the simplest one, called Stochastic Gradient Descent:

```python
>>> optimizer = optimizers.SGD()
>>> optimizer.setup(model.collect_parameters())
```

The method `setup()` prepares for the optimization given parameters and gradients. The interface is designed to match the return values of the `FunctionSet.collect_parameters()` method.

**Note:** Since Optimizer does not know the functions that actually own the parameters and gradients, once parameters and gradients are given to Optimizer, functions must use same parameter and gradient array objects throughout all forward/backward computations.

In order to run optimization, you first have to compute gradients. Zeroing the initial gradient arrays are simply done by calling `zero_grads()` method:

```python
>>> optimizer.zero_grads()
```

We have done the zeroing manually in the previous section. The line above is an equivalent and simpler way to initialize the gradients.
Then, after computing gradient of each parameter, `update()` method runs one iteration of optimization:

```python
>>> (compute gradient)
>>> optimizer.update()
```

Optimizer also contains some features related to parameter and gradient manipulation, e.g. weight decay and gradient clipping.

### 1.1.6 Example: Multi-layer Perceptron on MNIST

Now you can solve a multiclass classification task using a multi-layer perceptron. Here we use hand-written digits dataset called MNIST, which is the long-standing de-facto “hello world” of machine learning. This MNIST example is also found in `examples/mnist` directory of the official repository.

In order to use MNIST, we prepared `load_mnist_data` function at `examples/mnist/data.py`:

```python
>>> import data

>>> mnist = data.load_mnist_data()
```

The mnist dataset consists of 70,000 grayscale images of size 28x28 (i.e. 784 pixels) and corresponding digit labels. First, we scale pixels to [0, 1] values, and divide the dataset into 60,000 training samples and 10,000 test samples.

```python
>>> x_all = mnist['data'].astype(np.float32) / 255
>>> y_all = mnist['target'].astype(np.int32)
>>> x_train, x_test = np.split(x_all, [60000])
>>> y_train, y_test = np.split(y_all, [60000])
```

Next, we want to define the architecture. We use a simple three-layer rectifier network with 100 units per layer as an example. Before defining the forward routine, we have to prepare our parameterized functions:

```python
>>> model = FunctionSet(
...     l1 = F.Linear(784, 100),
...     l2 = F.Linear(100, 100),
...     l3 = F.Linear(100, 10),
... )

>>> optimizer = optimizers.SGD()

>>> optimizer.setup(model.collect_parameters())
```

Note that `model.l3` is the final linear layer whose output corresponds to the ten digits. We also set up the optimizer here.

Now we can define the forward routine using these Linear functions. Typically it is defined as a simple python function given input arrays:

```python
>>> def forward(x_data, y_data):
...     x = Variable(x_data)
...     t = Variable(y_data)
...     h1 = F.relu(model.l1(x))
...     h2 = F.relu(model.l2(h1))
...     y = model.l3(h2)
...     return F.softmax_cross_entropy(y, t), F.accuracy(y, t)
```

This function uses `functions.relu()` as an activation function. Since ReLU does not have parameters to optimize, it does not need to be included in `model`. `functions.softmax_cross_entropy()` computes the loss function of softmax regression. `functions.accuracy()` computes the classification accuracy of this minibatch.

Finally, we can write a learning loop as following:
Only the last four lines are the code related to Chainer, which are already described above.

Here you find that, at each iteration, the network is defined by forward computation, used for backprop, and then disposed. By leveraging this “Define-by-Run” scheme, you can imagine that recurrent nets with variable length input are simply handled by just using loop over different length input for each iteration.

After or during optimization, we want to evaluate the model on the test set. It can be achieved simply by calling forward function:

```python
>>> sum_loss, sum_accuracy = 0, 0
>>> for i in range(0, 10000, batchsize):
...    x_batch = x_test[i : i + batchsize]
...    y_batch = y_test[i : i + batchsize]
...    loss, accuracy = forward(x_batch, y_batch)
...    sum_loss += loss.data * batchsize
...    sum_accuracy += accuracy.data * batchsize
...    optimizer.zero_grads()
...    loss.backward()
...    optimizer.update()
```

The example code contains GPU support, though the essential part is same as the code in this tutorial. We will review in later sections how to use GPU(s).

### 1.2 Recurrent Nets and their Computational Graph

In this section, you will learn how to write

- recurrent nets with full backprop,
- recurrent nets with truncated backprop,
- evaluation of networks with few memory.

After reading this section, you will be able to:

- Handle input sequences of variable length
- Truncate upper stream of the network during forward computation
- Use volatile variables to prevent network construction

#### 1.2.1 Recurrent Nets

Recurrent nets are neural networks with loops. They are often used to learn from sequential input/output. Given an input stream \( x_1, x_2, \ldots, x_t, \ldots \) and the initial state \( h_0 \), a recurrent net iteratively updates its state by \( h_t = f(x_t, h_{t-1}) \).
and at some or every point in time $t$, it outputs $y_t = g(h_t)$. If we expand the procedure along the time axis, it looks like a regular feed-forward network except that same parameters are periodically used within the network.

Here we learn how to write a simple one-layer recurrent net. The task is language modeling: given a finite sequence of words, we want to predict the next word at each position without peeking the successive words. Suppose that there are 1,000 different word types, and that we use 100 dimensional real vectors to represent each word (a.k.a. word embedding).

Before writing the forward computation, we have to define parameterized functions:

```python
model = FunctionSet(
    embed = F.EmbedID(1000, 100),
    x_to_h = F.Linear(100, 50),
    h_to_h = F.Linear( 50,  50),
    h_to_y = F.Linear( 50, 1000),
)
optimizer = optimizers.SGD()
optimizer.setup(model.collect_parameters())
```

Here `EmbedID` is a parameterized function class for word embedding. It converts input integers into corresponding fixed-dimensional embedding vectors. Other Linear layers represent the transformation as their names indicate. Here we use 50 hidden units.

Then, we can write down the forward computation. Suppose that the input word sequence is given as a list of integer arrays. The forward computation is simply written with a for loop:

```python
def forward_one_step(h, cur_word, next_word, volatile=False):
    word = Variable(cur_word, volatile=volatile)
    t = Variable(next_word, volatile=volatile)
    x = F.tanh(model.embed(word))
    h = F.tanh(model.x_to_h(x) + model.h_to_h(h))
    y = model.h_to_y(h)
    loss = F.softmax_cross_entropy(y, t)
    return h, loss

def forward(x_list, volatile=False):
    h = Variable(np.zeros((1, 50), dtype=np.float32), volatile=volatile)
    loss = 0
    for cur_word, next_word in zip(x_list, x_list[1:]):
        h, new_loss = forward_one_step(h, cur_word, next_word, volatile=volatile)
        loss += new_loss
    return loss
```

Note that the first dimension of $h$ and $x_list$ is always the mini-batch size. The mini-batch size is assumed to be 1 here. We implemented the one-step-forward computation as a separate function, which is a best practice of writing recurrent nets for higher extensibility. Ignore the argument `volatile` for now, we will review it in the next subsection. The `forward` function is very simple and no special care needs to be taken with respect to the length of the input sequence. This code actually handles variable length input sequences without any tricks.

Of course, the accumulated loss is a Variable object with the full history of computation. So we can just call its `backward()` method to compute gradients of the total loss according to the model parameters:

```python
optimizer.zero_grads()
loss = forward(x_list)
loss.backward()
optimizer.update()
```

Do not forget to call `Optimizer.zero_grads()` before the backward computation!
1.2.2 Truncate the Graph by Unchaining

Learning from very long sequences is also a typical use case of recurrent nets. Suppose that the input and state sequence is too long to fit into memory. In such cases, we often truncate the backpropagation into a short time range. This technique is called truncated backprop. It is heuristic, and it makes the gradients biased. However, this technique works well in practice if the time range is long enough.

How to implement truncated backprop in Chainer? Chainer has a smart mechanism to achieve truncation, called backward unchaining. It is implemented in the `Variable.unchain_backward()` method. Backward unchaining starts from the Variable object, and it chops the computation history backwards from the variable. The chopped variables are disposed automatically (if they are not referenced explicitly from any other user object). As a result, they are no longer a part of computation history, and are not involved in backprop anymore.

Let’s write an example of truncated backprop. Here we use the same network as the one used in the previous subsection. Suppose that we are given a very long sequence, and we want to run backprop truncated at every 30 time steps. We can write truncated backprop using the `forward_one_step` function that we wrote above.

```python
h = Variable(np.zeros((1, 50), dtype=np.float32))
loss = 0
count = 0
seqlen = len(x_list[1:])
for cur_word, next_word in zip(x_list, x_list[1:]):
    h, new_loss = forward_one_step(h, cur_word, next_word)
    loss += new_loss
    count += 1
    if count % 30 == 0 or count == seqlen:
        optimizer.zero_grads()
        loss.backward()
        loss.unchain_backward()
        optimizer.update()
```

State is updated at `forward_one_step`, and the losses are accumulated to `loss` variable. At each 30 steps, backprop takes place at the accumulated loss. Then, the `unchain_backward()` method is called, which deletes the computation history backward from the accumulated loss. Note that the latest state `h` itself is not lost, since above code holds a reference to it.

The implementation of truncated backprop is simple, and since there is no complicated trick on it, we can generalize this method to different situations. For example, we can easily extend the above code to use different schedules between backprop timing and truncation length.

1.2.3 Network Evaluation without Storing the Computation History

On evaluation of recurrent nets, there is typically no need to store the computation history. While unchaining enables us to walk through unlimited length of sequences with limited memory, it is a bit of a work-around.

As an alternative, Chainer provides an evaluation mode of forward computation which does not store the computation history. This is enabled by just passing `volatile` flag to all input variables. Such variables are called volatile variables.

**Warning:** It is not allowed to mix volatile and non-volatile variables as arguments to same function.

Remember that our `forward` function accepts `volatile` argument. So we can enable volatile forward computation by just passing `volatile=True` to this function:

```python
loss = forward(x_list, volatile=True)
```
Volatile variables are also useful to evaluate feed-forward networks.

Variable’s volatility can be changed directly by setting the `Variable.volatile` attribute. This enables us to combine a fixed feature extractor network and a trainable predictor network. For example, suppose that we want to train a feed-forward network `predictor_func`, which is located on top of another fixed pretrained network `fixed_func`. We want to train `predictor_func` without storing the computation history for `fixed_func`. This is simply done by following code snippets (suppose `x_data` and `y_data` indicate input data and label, respectively):

```python
x = Variable(x_data, volatile=True)
feat = fixed_func(x)
feat.volatile = False
y = predictor_func(feat)
y.backward()
```

At first, the input variable `x` is volatile, so `fixed_func` is executed in volatile mode, i.e. without memorizing the computation history. Then the intermediate variable `feat` is manually set to non-volatile, so `predictor_func` is executed in non-volatile mode, i.e., with memorizing the history of computation. Since the history of computation is only memorized between variables `feat` and `y`, the backward computation stops at the `feat` variable.

In this section we have demonstrated how to write recurrent nets in Chainer and some fundamental techniques to manage the history of computation (a.k.a. computational graph). The example in the `examples/ptb` directory implements truncated backprop learning of a LSTM language model from the Penn Treebank corpus. In the next section, we will review how to use GPU(s) in Chainer.

### 1.3 Using GPU(s) in Chainer

In this section, you will learn about the following things:

- Relationship between Chainer and PyCUDA
- Basics of GPUArray
- Single-GPU usage of Chainer
- Multi-GPU usage of model-parallel computing
- Multi-GPU usage of data-parallel computing

After reading this section, you will be able to:

- Use Chainer on a CUDA-enabled GPU
- Write model-parallel computing in Chainer
- Write data-parallel computing in Chainer

#### 1.3.1 Relationship between Chainer and PyCUDA

Chainer uses PyCUDA as its backend for GPU computation and the `pycuda.gpudarray.GPUArray` class as the GPU array implementation. GPUArray has far less features compared to `numpy.ndarray`, though it is still enough to implement the required features for Chainer.

**Note:** `chainer.cuda` module imports many important symbols from PyCUDA. For example, the GPUArray class is referred as `cuda.GPUArray` in the Chainer code.
Chainer provides wrappers of many PyCUDA functions and classes, mainly in order to support customized default allocation mechanism. As shown in the previous sections, Chainer constructs and destructs many arrays during learning and evaluating iterations. It is not well suited for CUDA architecture, since memory allocation and release in CUDA (i.e. cuMemAlloc and cuMemFree functions) synchronize CPU and GPU computations, which hurts performance. In order to avoid memory allocation and deallocation during the computation, Chainer uses PyCUDA's memory pool utilities as the standard memory allocator. Since memory pool is not the default allocator in PyCUDA, Chainer provides many wrapper functions and classes to use memory pools in a simple way. At the same time, Chainer’s wrapper functions and classes make it easy to handle multiple GPUs.

Note: Chainer also uses scikit-cuda for a wrapper of CUBLAS, and some functions use CuDNN v2 if available. We omit their usage in this tutorial.

Note: We also do not touch the detail of PyCUDA. See PyCUDA’s documentation instead.

1.3.2 Basics of GPUArray in Chainer

In order to use GPU in Chainer, we must initialize \texttt{chainer.cuda} module before any GPU-related operations:

\begin{verbatim}
cuda.init()
\end{verbatim}

The \texttt{cuda.init()} function initializes global state and PyCUDA. This function accepts an optional argument \texttt{device}, which indicates the GPU device ID to select initially.

**Warning:** If you are using \texttt{multiprocessing}, the initialization must take place for each process after the fork. The main process is no exception, i.e., \texttt{cuda.init()} should not be called before all the children that use GPU have been forked.

Then we can create a GPUArray object using functions of the \texttt{cuda} module. Chainer provides many constructor functions resembling the ones of NumPy: \texttt{empty()}, \texttt{empty_like()}, \texttt{full()}, \texttt{full_like()}, \texttt{zeros()}, \texttt{zeros_like()}, \texttt{ones()}, \texttt{ones_like()}.

Another useful function to create a GPUArray object is \texttt{to_gpu()}. This function copies a \texttt{numpy.ndarray} object to a newly allocated GPUArray object. For example, the following code

\begin{verbatim}
x_cpu = np.ones((5, 4, 3), dtype=np.float32)
x_gpu = cuda.to_gpu(x_cpu)
\end{verbatim}

generates the same \texttt{x_gpu} as the following code:

\begin{verbatim}
x_gpu = cuda.ones((5, 4, 3))
\end{verbatim}

**Note:** Allocation functions of the \texttt{cuda} module use \texttt{numpy.float32} as the default element type.

The \texttt{cuda} module also has \texttt{to_cpu()} function to copy a GPUArray object to an ndarray object:

\begin{verbatim}
x_cpu = cuda.to_cpu(x_gpu)
\end{verbatim}

All GPUArray constructors allocate memory on the current device. In order to allocate memory on a different device, we can use device switching utilities. \texttt{cuda.use_device()} function changes the current device:

\begin{verbatim}
cuda.use_device(1)
x_gpu1 = cuda.empty((4, 3))
\end{verbatim}

There are many situations in which we want to temporarily switch the device, where the \texttt{cuda.using_device()} function is useful. It returns an resource object that can be combined with the \texttt{with} statement:
with cuda.using_device(1):
    x_gpu1 = cuda.empty((4, 3))

These device switching utilities also accepts a GPUArray object as a device specifier. In this case, Chainer switches the current device to one that the array is allocated on:

with cuda.using_device(x_gpu1):
    y_gpu1 = x_gpu1 + 1

**Warning:** An array that is not allocated by Chainer’s allocator cannot be used as a device specifier.

A GPUArray object allocated by Chainer can be copied between GPUs by `cuda.copy()` function:

cuda.use_device(0)
x0 = cuda.ones((4, 3))
x1 = cuda.copy(x0, out_device=1)

### 1.3.3 Run Neural Networks on a Single GPU

Single-GPU usage is very simple. What you have to do is transferring `FunctionSet` and input arrays to the GPU beforehand. In this subsection, the code is based on our first MNIST example in this tutorial.

A `FunctionSet` object can be transferred to the specified GPU using the `to_gpu()` method. Make sure to give parameters and gradients of the GPU version to the optimizer.

```python
model = FunctionSet(
    l1 = F.Linear(784, 100),
    l2 = F.Linear(100, 100),
    l3 = F.Linear(100, 10),
).to_gpu()

optimizer = optimizers.SGD()
optimizer.setup(model.collect_parameters())
```

Note that this method returns the function set itself. The device specifier can be omitted, in which case it uses the current device.

Then, all we have to do is transferring each minibatch to the GPU:

```python
batchsize = 100
for epoch in xrange(20):
    print 'epoch', epoch
    indexes = np.random.permutation(60000)
    for i in xrange(0, 60000, batchsize):
        x_batch = cuda.to_gpu(x_train[indexes[i : i + batchsize]])
        y_batch = cuda.to_gpu(y_train[indexes[i : i + batchsize]])

        optimizer.zero_grads()
        loss, accuracy = forward(x_batch, y_batch)
        loss.backward()
        optimizer.update()
```

This is almost identical to the code of the original example, we just inserted a call to the `cuda.to_gpu()` function to the minibatch arrays.
### 1.3.4 Model-parallel Computation on Multiple GPUs

Parallelization of machine learning is roughly classified into two types called “model-parallel” and “data-parallel”. Model-parallel means parallelizations of the computations inside the model. In contrast, data-parallel means parallelizations using data sharding. In this subsection, we show how to use the model-parallel approach on multiple GPUs in Chainer.

Recall the MNIST example. Now suppose that we want to modify this example by expanding the network to 6 layers with 2000 units each using two GPUs. In order to make multi-GPU computation efficient, we only make the two GPUs communicate at the third and sixth layer. The overall architecture looks like the following diagram:

```
| GPU0 | input --> 11 --+--> 12 --+--> 13 --+--> 14 --+--> 15 --+--> 16 --+-- output |
|      |                       |                       |                       |                       |                       |
| (GPU1)|                       | 11 --+--> 12 --+--> 13 --+--> 14 --+--> 15 --+--> 16 --+ |
```

We first have to define a `FunctionSet`. Be careful that parameters that will be used on a device must reside on that device. Here is a simple example of the model definition:

```python
model = FunctionSet(
    gpu0 = FunctionSet(
        11=F.Linear( 784, 1000),
        12=F.Linear(1000, 1000),
        13=F.Linear(1000, 2000),
        14=F.Linear(2000, 1000),
        15=F.Linear(1000, 1000),
        16=F.Linear(1000, 10)
    ).to_gpu(0),
    gpu1 = FunctionSet(
        11=F.Linear( 784, 1000),
        12=F.Linear(1000, 1000),
        13=F.Linear(1000, 2000),
        14=F.Linear(2000, 1000),
        15=F.Linear(1000, 1000),
        16=F.Linear(1000, 10)
    ).to_gpu(1)
)
```

Recall that `FunctionSet.to_gpu()` returns the `FunctionSet` object itself. Note that `FunctionSet` can be nested as above.

Now we can define the network architecture that we have shown in the diagram:

```python
def forward(x_data, y_data):
    x_0 = Variable(cuda.to_gpu(x_data, 0))
    x_1 = Variable(cuda.to_gpu(x_data, 1))
    t = Variable(cuda.to_gpu(y_data, 0))

    h1_0 = F.relu(model.gpu0.l1(x_0))
    h1_1 = F.relu(model.gpu1.l1(x_1))

    h2_0 = F.relu(model.gpu0.l2(h1_0))
    h2_1 = F.relu(model.gpu1.l2(h1_1))

    h3_0 = F.relu(model.gpu0.l3(h2_0))
    h3_1 = F.relu(model.gpu1.l3(h2_1))

    # Synchronize
    h3_0 += F.copy(h3_1, 0)
    h3_1 = F.copy(h3_0, 1)
```
h4_0 = F.relu(model.gpu0.l4(h3_0))
h4_1 = F.relu(model.gpu1.l4(h3_1))

h5_0 = F.relu(model.gpu0.l5(h4_0))
h5_1 = F.relu(model.gpu1.l5(h4_1))

h6_0 = F.relu(model.gpu0.l6(h5_0))
h6_1 = F.relu(model.gpu1.l6(h5_1))

# Synchronize
y = h6_0 + F.copy(h6_1, 0)
return F.softmax_cross_entropy(y, t), F.accuracy(y, t)

First, recall that `cuda.to_gpu()` accepts an optional argument to specify the device identifier. We use this to transfer the input minibatch to both the 0th and the 1st devices. Then, we can write this model-parallel example employing the `functions.copy()` function. This function transfers an input array to another device. Since it is a function on `Variable`, the operation supports backprop, which reversely transfers an output gradient to the input device.

**Note:** Above code is not parallelized on CPU, but is parallelized on GPU. This is because most of the GPU computation is asynchronous to the host CPU.

An almost identical example code can be found at `examples/mnist/train_mnist_model_parallel.py`.

### 1.3.5 Data-parallel Computation on Multiple GPUs

Data-parallel computation is another strategy to parallelize online processing. In the context of neural networks, it means that a different device does computation on a different subset of the input data. In this subsection, we review the way to achieve data-parallel learning on two GPUs.

Suppose again our task is the MNIST example. This time we want to directly parallelize the three-layer network. The most simple form of data-parallelization is parallelizing the gradient computation for a distinct set of data. First, define the model:

```python
model = FunctionSet(
    l1 = F.Linear(784, 100),
    l2 = F.Linear(100, 100),
    l3 = F.Linear(100, 10),
)
```

We have to copy this model into two different devices. This is done by using `copy.deepcopy()` and `FunctionSet.to_gpu()` method:

```python
import copy
model_0 = copy.deepcopy(model).to_gpu(0)
model_1 = model.to_gpu(1)
```

Then, set up optimizer as:

```python
optimizer = optimizers.SGD()
optimizer.setup(model_0.collect_parameters())
```

Here we use the first copy of the model as the master model. Before its update, gradients of `model_1` must be aggregated to those of `model_0`.

Forward function is almost same as the original example:
The only difference is that `forward` accepts `model` as an argument. We can feed it with a model and arrays on an appropriate device. Then, we can write a data-parallel learning loop as follows:

```python
batchsize = 100
for epoch in xrange(20):
    print 'epoch', epoch
    indexes = np.random.permutation(60000)
    for i in xrange(0, 60000, batchsize):
        x_batch = x_train[indexes[i : i + batchsize]]
        y_batch = y_train[indexes[i : i + batchsize]]

        optimizer.zero_grads()

        loss_0, accuracy_0 = forward(
            cuda.to_gpu(x_batch[:batchsize//2], 0),
            cuda.to_gpu(y_batch[:batchsize//2], 0),
            model_0)
        loss_0.backward()

        loss_1, accuracy_1 = forward(
            cuda.to_gpu(x_batch[batchsize//2:], 1),
            cuda.to_gpu(y_batch[batchsize//2:], 1),
            model_1)
        loss_1.backward()

        optimizer.acumulate_grads(model_1.gradients)
        optimizer.update()

    model_1.copy_parameters_from(model_0.parameters)
```

One half of the minibatch is forwarded to GPU 0, the other half to GPU 1. Then the gradients are accumulated by the `Optimizer.acumulate_grads()` method. After the gradients are prepared, we can update the optimizer in usual way. Note that the update only modifies the parameters of `model_0`. So we must manually copy them to `model_1` using `FunctionSet.copy_parameters_from()` method.

Now you can use Chainer with GPUs. All examples in the `examples` directory support GPU computation, so please refer to them if you want to know more practices on using GPUs. In the next section, we will show how to define a differentiable (i.e. `backpropable`) function on Variable objects. We will also show there how to write a simple (elementwise) CUDA kernel using Chainer’s CUDA utilities.

### 1.4 Define your own function

In this section, you will learn about the following things:

- How to define a non-parameterized function
- Useful tools to write a function using a GPU
• How to define a parameterized function
• How to test the function definition

After reading this section, you will be able to:
• Write your own non-parameterized function
• Define simple kernels in the function definition
• Write your own parameterized function

1.4.1 Non-parameterized Functions

Chainer provides a collection of functions in the \texttt{functions} module. It covers typical use cases in deep learning, so many existing works can be implemented with them. On the other hand, deep learning is evolving rapidly and we cannot cover all possible functions to define unseen architectures. So it is important to learn how to define your own functions.

Since they are simpler, we first show how to define non-parameterized functions. First, suppose we want to define an elementwise function $f(x, y, z) = x * y + z$. While it is possible to implement this equation using a combination of the \* and + functions, defining it as a single function may reduce memory consumption, so it is not only a toy example. Here we call this function \textit{MulAdd}.

Let’s start with defining MulAdd working on the CPU. Any function must inherit the \texttt{Function} class. The skeleton of a non-parameterized function looks like:

```python
class MulAdd(Function):
    def forward_cpu(self, inputs):
        # do forward computation on CPU
        return some_tuple

    def backward_cpu(self, inputs, grad_outputs):
        # do backward computation on CPU
        return some_tuple
```

We must implement \texttt{forward_cpu()} and \texttt{backward_cpu()} methods. The non-self arguments of these functions are tuples of array(s), and these functions must return a tuple of array(s).

\textbf{Warning:} Be careful to return a tuple of arrays even if you have just one array to return.

MulAdd is simple and implemented as follows:

```python
class MulAdd(Function):
    def forward_cpu(self, inputs):
        x, y, z = inputs
        w = x * y + z
        return w,

    def backward_cpu(self, inputs, grad_outputs):
        x, y, z = inputs
        gw = grad_outputs[0]
        gx = y * gw
        gy = x * gw
        gz = gw
        return gx, gy, gz
```

1.4. Define your own function
As per the warning above, `forward_cpu` function returns a tuple of single element. Note that all arrays appearing in CPU functions are `numpy.ndarray`. The forward function is straightforward: It unpacks the input tuple, computes the output, and packs it into a tuple. The backward function is a bit more complicated. Recall the rule of differentiation of multiplication. This example just implements the rule. Look at the return values, the function just packs the gradient of each input in same order and returns them.

By just defining the core computation of forward and backward, Function class provides a chaining logic on it (i.e. storing the history of computation, etc.).

Now let’s define the corresponding GPU methods. You can easily predict that the methods we have to write are named `forward_gpu()` and `backward_gpu()`:

```python
class MulAdd(Function):
    def forward_cpu(self, inputs):
        ...

    def backward_cpu(self, inputs, grad_outputs):
        ...

    def forward_gpu(self, inputs):
        x, y, z = inputs
        w = x * y + z
        return w,

    def backward_gpu(self, inputs, grad_outputs):
        x, y, z = inputs
        gw = grad_outputs[0]
        gx = y * gw
        gy = x * gw
        gz = gw
        return gx, gy, gz
```

In GPU methods, arrays are of type `pycuda.gpuaarray.GPUArray` We use arithmetic operators defined for GPUArray. These operators implement the basic elementwise arithmetics.

You maybe find that the definitions of GPU methods are exactly same as those of CPU methods. In that case, we can reduce them to `forward()` and `backward()` methods:

```python
class MulAdd(Function):
    def forward(self, inputs):
        x, y, z = inputs
        w = x * y + z
        return w,

    def backward(self, inputs, grad_outputs):
        x, y, z = inputs
        gw = grad_outputs[0]
        gx = y * gw
        gy = x * gw
        gz = gw
        return gx, gy, gz
```

Note that this is a very rare case, since GPUArray does not implement most features of `numpy.ndarray`. 

1.4.2 Write an Elementwise Kernel Function

The GPU implementation of MulAdd as shown above is already fast and parallelized on GPU cores. However, it invokes two kernels during each of forward and backward computations, which may hurt performance. We can reduce the number of invocations by defining our own kernel.

Most functions only require elementwise operations like MulAdd. PyCUDA provides a useful tool to define elementwise kernels, the `pycuda.elementwise.ElementwiseKernel` class, and Chainer wraps it by `cuda.elementwise()` function. Our MulAdd implementation can be improved as follows:

```python
class MulAdd(Function):
    def forward_cpu(self, inputs):
        ...

    def backward_cpu(self, inputs, grad_outputs):
        ...

    def forward_gpu(self, inputs):
        x, y, z = inputs
        w = cuda.empty_like(x)
        cuda.elementwise(
            'float* w, const float* x, const float* y, const float* z',
            'w[i] = x[i] * y[i] + z[i]',
            'muladd_fwd')(w, x, y, z)
        return w,

    def backward_gpu(self, inputs, grad_outputs):
        x, y, z = inputs
        gw = grad_outputs[0]
        gx = cuda.empty_like(x)
        gy = cuda.empty_like(y)
        cuda.elementwise(
            '',
            'float* gx, float* gy,
            const float* x, const float* y, const float* gw
            ',
            'gx[i] = gy[i] * gw[i];
            gy[i] = gx[i] * gw[i];
            ',
            'muladd_bwd')(gx, gy, x, y, gw)
        gz = gw # no copy
        return gx, gy, gz
```

`cuda.elementwise()` function accepts the essential implementation of the kernel function, and returns a kernel invocation function (actually, it returns `ElementwiseKernel` object, which is callable). In typical usage, we pass three arguments to this function. The first is an argument list of the kernel function. The second is a body of parallel loop, where the variable `i` indicates the index in the loop. Note that `i` runs through all indexes of the first array argument by default. The third is the name of the kernel function, which is shown in debugger and profilers.

Above code is not compiled on every forward/backward computation thanks to two caching mechanisms provided by `cuda.elementwise()`.

The first one is binary caching: `cuda.elementwise()` function caches the compiled binary in the `/tmp` directory with a hash value of the CUDA code, and reuses it if the given code matches the hash value. This caching mechanism is actually implemented in PyCUDA.

The second one is upload caching: Given a compiled binary code, we have to upload it to the current GPU in order to execute it. `cuda.elementwise()` function memoizes the arguments and the current context, and if it is called with
the same arguments and the same context, it reuses the previously uploaded kernel code.

### 1.4.3 Parameterized Functions

Next we show how to define a parameterized function. At this time, suppose that we want to implement elementwise product function between the input array and the parameter array.

**Note:** Note that the elementwise product between a variable and parameters can be simply implemented by `functions.Parameter` function:

```python
p = F.Parameter(np.random.rand((4, 3), dtype=np.float32))
x = Variable(...)
y = p() * x
```

The Parameter function takes no arguments and just returns a variable holding the parameter array. The example in this subsection may be slightly more efficient with respect to memory consumption, though.

There are two differences between parameterized functions and non-parameterized functions:

- Parameterized functions have parameter arrays and corresponding gradient arrays. They are typically stored as attributes of the function class, where the function should provide `parameter_names` and `gradient_names` attributes (or properties). Otherwise, the function must override `parameters` and `gradients` properties directly.

- Parameterized functions must accumulate gradients on backward.

Note that gradient arrays are automatically zeroed by an optimizer, so function implementation only need to initialize their shapes. Then, the implementation of elementwise product may be as following:

```python
class EltwiseParamProduct(Function):
    parameter_names = 'w',
    gradient_names = 'gw',

    def __init__(self, shape):
        self.w = np.random.randn(shape).astype(np.float32)
        self.gw = np.empty_like(self.w)

    def forward(self, inputs):
        x = inputs[0]
        y = self.w * x
        return y,

    def backward(self, inputs, grad_outputs):
        x = inputs[0]
        gy = grad_outputs[0]
        self.gw += gy * x
        gx = gy * self.w
        return gx,
```

**Note:** An advanced tip to implement functions: if you want to preserve some information between forward and backward computations (e.g. to cache some arrays), you can store it as attributes. It does not make any trouble even if the function object is used more than once in the same network, since `Function.__call__()` operator copies itself before the forward computation.
Warning: You should not assume a one-to-one match of calls of forward and backward. Some users may call backward more than once after one forward call.

1.4.4 Testing Function

In order to isolate the cause of learning failure from implementation bugs, it is important to test function implementations. Chainer provides simple utilities to help writing unit tests. They are defined in the `gradient_check` module.

The most important test utility is the `numerical_grad()` function. This function computes the numerical gradient of given function using finite differences. It can be used as follows:

```python
x = np.random.randn(4, 3).astype(np.float32)
gy = np.ones((4, 3), dtype=np.float32)
f = lambda: (x * x,)
gx = gradient_check.numerical_grad(f, (x,), (gy,))
```

`f` is a closure that returns a tuple of array(s) computed from input arrays. The second and third arguments of `numerical_grad()` are tuples of input arrays and output gradient arrays, respectively. The code above computes the numerical gradients of `sum(f(x))`, where `sum` indicates the summation over all elements. The summation can be weighted by changing `gy`. `numerical_grad()` function also accepts additional `eps` argument, which indicates the quantization width of finite differences.

Note: `numerical_grad()` function accepts both CPU and GPU arrays. Note that we cannot mix CPU and GPU arrays.

Another utility is `assert_allclose()` function. This is similar to `numpy.testing.assert_allclose()` function. The difference is that Chainer’s version accepts CPU and GPU arrays as inputs. We can mix them in one invocation of `assert_allclose`. The default values of optional arguments are also different.

Here is a typical usage of gradient checking utilities. This is a test example of `functions.relu()` function:

```python
class TestReLU(TestCase):
    def test_backward_cpu(self):
        x = Variable(np.random.randn(3, 2).astype(np.float32))
y = F.relu(x)
y.grad = np.random.randn(3, 2).astype(np.float32)
y.backward()

        func = y.creator
        f = lambda: func.forward((x.data,))
gx, = gradient_check.numerical_grad(f, (x.data,), (y.grad,))

        gradient_check.assert_allclose(gx, x.grad)
```

We used `Variable.creator` to extract creator function object of a variable. The first four lines of the test code are simple forward and backward computation of ReLU function. The next three lines compute numerical gradient using the same forward function without backward routine. And at last, we compare these two results elementwise. Note that above test code can be easily modified to test GPU version just by replacing CPU arrays to GPU arrays.

You can find many examples of function tests under `tests/function_tests` directory.
1.5 Type check

In this section, you will learn about the following things:

- Basic usage of type check
- Detail of type information
- Internal mechanism of type check
- More complicated cases
- Call functions
- Typical type check example

After reading this section, you will be able to:

- Write a code to check types of input arguments of your own functions

1.5.1 Basic usage of type check

When you call a function with an invalid type of array, you sometimes receive no error, but get an unexpected result by broadcasting. When you use CUDA with an illegal type of array, it causes memory corruption, and you get a serious error. These bugs are hard to fix. Chainer can check preconditions of each function, and helps to prevent such problems. These conditions may help a user to understand specification of functions.

Each implementation of Function has a method for type check, check_type_forward(). This function is called just before the forward() method of the Function class. You can override this method to check the condition on types and shapes of arguments.

```python
def check_type_forward(self, in_types):
  ...
```

in_types is an instance of `utils.type_check.TypeInfoTuple`, which is a sub-class of `tuple`. To get type information about the first argument, use `in_types[0]`. If the function gets multiple arguments, we recommend to use new variables for readability:

```python
x_type, y_type = in_types
```

In this case, `x_type` represents the type of the first argument, and `y_type` represents the second one.

We describe usage of `in_types` with an example. When you want to check if the number of dimension of `x_type` equals to 2, write this code:

```python
utils.type_check.expect(x_type.ndim == 2)
```

When this condition is true, nothing happens. Otherwise this code throws an exception, and a user gets a message like this:

```
Expect: in_types[0].ndim == 2
Actual: 3 != 2
```

This error message means that “`ndim` of the first argument expected to be 2, but actually it is 3”.
1.5.2 Detail of type information

You can access three information of x_type.

- .shape is a tuple of ints. Each value is size of each dimension.
- .ndim is int value representing the number of dimensions. Note that ndim == len(shape)
- .dtype is numpy.dtype representing data type of the value.

You can check all members. For example, the size of the first dimension must be positive, you can write like this:

```python
utils.type_check.expect(x_type.shape[0] > 0)
```

You can also check data types with .dtype:

```python
utils.type_check.expect(x_type.dtype == numpy.float32)
```

And an error is like this:

```
Expect: in_types[0].dtype == numpy.float32
Actual: numpy.float64 != numpy.float32
```

You can also check kind of dtype. This code checks if the type is floating point:

```python
utils.type_check.expect(x_type.dtype.kind == 'f')
```

You can compare between variables. For example, the following code checks if the first argument and the second argument have the same length:

```python
utils.type_check.expect(x_type.shape[0] == y_type.shape[0])
```

1.5.3 Internal mechanism of type check

How does it show an error message like "in_types[0].ndim == 2"? If x_type is an object containing ndim member variable, we cannot show such an error message because this equation is evaluated as a boolean value by Python interpreter.

Actually x_type is a `utils.type_check.Expr` objects, and doesn't have a ndim member variable itself. `utils.type_check.Expr` represents a syntax tree. x_type.ndim makes a `utils.type_check.Expr` object representing (getattr, x_type, 'ndim'). x_type.ndim == 2 makes an object like (eq, (getattr, x_type, 'ndim'), 2). `type_check.expect()` gets a `utils.type_check.Expr` object and evaluate it. When it is True, it causes no error and shows nothing. Otherwise, this method shows a readable error message.

If you want to evaluate a `utils.type_check.Expr` object, call eval() method:

```python
actual_type = x_type.eval()
```

actual_type is an instance of TypeInfo, while x_type is an instance of `utils.type_check.Expr`. In the same way, x_type.shape[0].eval() returns an int value.

1.5.4 More powerfull methods

`utils.type_check.Expr` class is more powerfull. It supports all mathematical operators such as + and *. You can write a condition that the first dimension of x_type is the first dimension of y_type times four:
x_type.shape[0] == y_type.shape[0] * 4

When x_type.shape[0] == 3 and y_type.shape[0] == 1, users can get the error message below:

Expect: in_types[0].shape[0] == in_types[1].shape[0] * 4
Actual: 3 != 4

To compare a member variable of your function, wrap a value with utils.type_check.Variable to show readable error message:

x_type.shape[0] == utils.type_check.Variable(self.in_size, "in_size")

This code can check the equivalent condition below:

x_type.shape[0] == self.in_size

However, the latter condition doesn’t know meaning of this value. When this condition is not satisfied, the latter code shows unreadable error message:

Expect: in_types[0].shape[0] == 4 # what does '4' mean?
Actual: 3 != 4

Note that the second argument of utils.type_check.Variable is only for readability.

The former shows this message:

Expect: in_types[0].shape[0] == in_size # OK, 'in_size' is a value that is given to the constructor
Actual: 3 != 4 # You can also check actual value here

1.5.5 Call functions

How to check summation of all values of shape? utils.type_check.Expr also supports function call.

sum = utils.type_check.Variable('sum', numpy.sum)
utils.type_check.expect(sum(x_type.shape) == 10)

Why do we need to wrap the function numpy.sum with utils.type_check.Variable? x_type.shape is not a tuple but an object of utils.type_check.Expr as we have seen before. Therefore, numpy.sum(x_type.shape) fails. We need to evaluate this function lazily.

The above example makes an error message like this:

Expect: sum(in_types[0].shape) == 10
Actual: 7 != 10

1.5.6 More complicated cases

How to write a more complicated condition that can’t be written with these operators? You can evaluate utils.type_check.Expr and get its result value with eval() method. And, check the condition and show warning message by your hand:

x_shape = x_type.shape.eval() # get actual shape (int tuple)
if not more_complicated_condition(x_shape):
    expect_msg = 'Shape is expected to be ...'
    actual_msg = 'Shape is ...
raise utils.type_check.InvalidType(expect_msg, actual_msg)

Please make a readable error message. This code generates an error below:
1.5.7 Typical type check example

We show a typical type check for a function.

First check the number of arguments:

```python
utils.type_check.expect(in_types.size() == 2)
```

`in_types.size()` returns a `utils.type_check.Expr` object representing a number of arguments. You can check it in the same way.

And then, get each type:

```python
x_type, y_type = in_types
```

Don’t get each value before check `in_types.size()`. When the number of argument is illegal, this process may fail. For example, this code doesn’t work when the size of `in_types` is zero:

```python
utils.type_check.expect(
    in_types.size() == 1,
    in_types[0].ndim == 1,
)
```

After that, check each type:

```python
utils.type_check.expect(
    x_type.dtype == numpy.float32,
    x_type.ndim == 2,
    x_type.shape[1] == 4,
)
```

The above example works correctly even when `x_type.ndim == 0` as all conditions are evaluated lazily.
2.1 Core functionalities

2.1.1 Variable

class chainer.Variable (data, volatile=False)

Array with a structure to keep track of computation.

Every variable holds a data array of type either ndarray or GPUArray.

A Variable object may be constructed in two ways: by the user or by some function. When a variable is created by some function as one of its outputs, the variable holds a reference to that function. This reference is used in error backpropagation (a.k.a. backprop). It is also used in backward unchaining. A variable that does not hold a reference to its creator is called a root variable. A variable is root if it is created by the user, or if the reference is deleted by unchain_backward().

Users can disable this chaining behavior by setting the volatile flag for the initial variables. When a function gets volatile variables as its inputs, the output variables do not hold references to the function. This acts like unchaining on every function application.

data

Data array of type either ndarray or GPUArray.

grad

Gradient array. It is None until backprop reaches this variable.

creator

The function who creates this variable. It is None if the variable is not created by any function.

volatile

Boolean flag. If True, the variable does not keep track of any function applications.

__len__()  

Returns the number of elements of the data array.

Returns the number of elements of the data array.

Return type int

backward (retain_grad=False)

Runs error backpropagation (a.k.a. backprop) from this variable.

On backprop, Function.backward() is called on each Function object appearing in the backward graph starting from this variable. The backward graph is represented by backward references from variables to their creators, and from functions to their inputs. The backprop stops at all root variables. Some
functions set None as gradients of some inputs, where further backprop does not take place at such input variables.

This method uses grad as the initial error array. User can manually set a gradient array before calling this method. If data contains only one element (i.e., it is scalar) and grad is None, then this method automatically complement 1.0 as the initial error. This is useful on starting backprop from some scalar loss value.

Parameters

- retain_grad (bool) – If True, the gradient arrays of all intermediate variables are kept. Otherwise, grad of the intermediate variables are set to None on appropriate timing, which may reduce the maximum memory consumption.

In most cases of training some model, the purpose of backprop is to compute gradients of parameters, not of variables, so it is recommended to set this flag False.

- label
  Short text that represents the function.

- set_creator (gen_func)
  Notifies the variable that the given function is its creator.

Parameters gen_func (Function) – Function object that creates this variable as one of its outputs.

- unchain_backward()
  Deletes references between variables and functions backward.

  After this method completes, intermediate variables and functions that are not referenced from anywhere are deallocated by reference count GC. Also this variable itself deletes the reference to its creator function, i.e. this variable becomes root in the computation graph. It indicates that backprop after unchaining stops at this variable. This behavior is useful to implement truncated BPTT.

2.1.2 Function

class chainer.Function

Function on variables with backpropagation ability.

All function implementations defined in chainer.functions inherit this class.

The main feature of this class is keeping track of function applications as a backward graph. When a function is applied to Variable objects, the function is copied, and its forward() method is called on data fields of input variables, and at the same time it chains references from output variables to the function and from the function to its inputs.

Note: Strictly speaking, when a function is applied to some variable, a special Function object called splitter is inserted between the variable and the function. The splitter is used to manipulate multiple function applications on the same variable, where gradients from different backward paths are accumulated at the variable.

Note: __call__() copies the function instance before the forward computation and chaining. This enables us to reuse one function object for multiple function applications, where the different calls must use different references to the function object. Note that the copy is shallow, so implementations of Function must take care of any member attributes shared accross forward and backward computations.

Example

Let \( x \) an instance of Variable and \( f \) an instance of Function taking only one argument. Then a line
```python
>>> y = f(x)
```

computes a new variable $y$ and creates backward references. Actually, backward references are set as per the following diagram:

```
x <---- (splitter) <---- x' <---- f' <---- y
```

where prime """" indicates a copy of the original object. If another application the function occurs as

```python
>>> z = f(x)
```

then the splitter acts like a branch as the following new diagram:

```
x <---- (splitter) <--- f' <--- y
|--- x' <--- f' <--- y

x <---- (splitter) <-+ 
|--- x'' <--- f'' <--- z
```

Note that the splitter is implicitly inserted and user does not need to take any special care of it; just remember that such branching is correctly managed by chainer.

Every function implementation should provide `forward_cpu()`, `forward_gpu()`, `backward_cpu()` and `backward_gpu()`. Alternatively, one can provide `forward()` and `backward()` instead of separate methods. Backward methods have default implementations that just return `None`, which indicates that the function is non-differentiable.

Function implementations are classified into two types: parameterized ones and non-parameterized ones. A parameterized function holds parameter arrays and corresponding gradient arrays. Implementation can choose any way to keep these arrays, but it is recommended to keep them as attributes to easily migrate between CPU and GPU. Parameterized function must provide accessors to these arrays called `parameters()` and `gradients()`.

**inputs**

A tuple or list of input variables.

**outputs**

A tuple or list of output variables.

**parameter_names**

A tuple or list of names of parameter attributes. It is set to an empty tuple by default. This attribute is used by the default implementation of `parameters()` property to gather the collection of parameter arrays. Implementation of parameterized function should override this field as an attribute or a property, or otherwise it should override `parameters()` property.

**gradient_names**

A tuple or list of names of gradient attributes. The detail is same as `parameter_names`.

**__call__(*)inputs**

Applies forward propagation with chaining backward references.

Basic behavior is also expressed in documentation of `Function` class. This function first copies itself to avoid conflict over multiple invocations.

**Note:** If the `data` attribute of input variables reside on GPU device, then, before it calls `forward()` method, the appropriate device is selected, so in most cases implementor does not need to take care of device selection.

**Parameters inputs** – Tuple of input `Variable` objects. All input variables must have same volatile flag.
Returns One `Variable` object or a tuple of multiple `Variable` objects.

`backward(inputs, grad_outputs)`
Applies backprop to output gradient arrays.

It delegates the procedure to `backward_cpu()` or `backward_gpu()` by default. Which it selects is determined by the type of input arrays and output gradient arrays. Implementations of `Function` must implement either cpu/gpu methods or this method, if the function is intended to be backprop-ed.

Parameters
- `inputs` – Tuple of input arrays.
- `grad_outputs` – Tuple of output gradient arrays.

Returns Tuple of input gradient arrays. Some or all of them can be `None`, if the function is not differentiable on inputs.

Return type `tuple`

Warning: Implementations of `Function` must take care that the return value must be a tuple even if it returns only one array.

`backward_cpu(inputs, grad_outputs)`
Applies backprop to output gradient arrays on CPU.

Parameters
- `inputs` – Tuple of input `ndarray` object(s).
- `grad_outputs` – Tuple of output gradient `ndarray` object(s).

Returns Tuple of input gradient `ndarray` object(s). Some or all of them can be `None`, if the function is not differentiable on corresponding inputs.

Return type `tuple`

Warning: Implementations of `Function` must take care that the return value must be a tuple even if it returns only one array.

`backward_gpu(inputs, grad_outputs)`
Applies backprop to output gradient arrays on GPU.

Parameters
- `inputs` – Tuple of input `GPUArray` object(s).
- `grad_outputs` – Tuple of output gradient `GPUArray` object(s).

Returns Tuple of input gradient `GPUArray` object(s). Some or all of them can be `None`, if the function is not differentiable on corresponding inputs.

Return type `tuple`

Warning: Implementations of `Function` must take care that the return value must be a tuple even if it returns only one array.

`check_type_backward(in_types, grad_types)`
Checks types of gradient data before back propagation.

Before `backward()` is called, this function is called. You need to validate types of gradient data in this function using the type checking utilities.
check_type_backward() is always called after check_type_forward(), so each function does not need to check the same condition here.

Parameters

- **in_types** (TypeInfoTuple) – The type information of input data for backward().
- **grad_types** (TypeInfoTuple) – The type information of gradient data for backward().

check_type_forward(in_types)
Checks types of input data before forward propagation.
Before forward() is called, this function is called. You need to validate types of input data in this function using the type checking utilities.

Parameters **in_types** (TypeInfoTuple) – The type information of input data for forward().

forward(inputs)
Applies forward propagation to input arrays.
It delegates the procedure to forward_cpu() or forward_gpu() by default. Which it selects is determined by the type of input arrays. Implementations of Function must implement either cpu/gpu methods or this method.

Parameters **inputs** – Tuple of input array(s).

Returns Tuple of output array(s).

**Warning:** Implementations of Function must take care that the return value must be a tuple even if it returns only one array.

forward_cpu(inputs)
Applies forward propagation to input arrays on CPU.

Parameters **inputs** – Tuple of ndarray object(s).

Returns Tuple of ndarray object(s).

Return type tuple

**Warning:** Implementations of Function must take care that the return value must be a tuple even if it returns only one array.

forward_gpu(inputs)
Applies forward propagation to input arrays on GPU.

Parameters **inputs** – Tuple of GPUArray object(s).

Returns Tuple of GPUArray object(s).

Return type tuple

**Warning:** Implementations of Function must take care that the return value must be a tuple even if it returns only one array.

gradients
A tuple of gradient arrays.
Default implementation collects gradient arrays based on gradient_names attribute.
label
Short text that represents the function.

The default implementation returns its type name. Each function should override it to give more information.

parameters
A tuple of parameter arrays.

Default implementation collects parameter arrays based on parameter_names attribute.

to_cpu()  
Migrates the function to CPU and returns self.

The default implementation moves all fields of type pycuda.gpucarray.GPUArray onto CPU.

Returns self.

to_gpu(device=None)  
Migrates the function to GPU and returns self.

The default implementation moves all fields of type ndarray onto GPU.

Parameters device (int or pycuda.driver.Device or None) – Device ID of GPU that the function will be migrated on. If this is None, the current device is used.

Returns self.

unchain()  
Purges in/out variables and this function itself from the graph.

This method is called from Variable.unchain_backward() method.

2.1.3 FunctionSet
class chainer.FunctionSet(**functions)  
Set of objects with parameters and gradients properties.

FunctionSet is useful to collect parameters and gradients of multiple parameterized Function objects. FunctionSet itself also implements parameters and gradients, so it can be nested in another FunctionSet object.

Function registration is done by just adding an attribute to FunctionSet object.

collect_parameters()  
Returns a tuple of parameters and gradients.

Returns Tuple (pair) of two tuples. The first element is a tuple of parameter arrays, and the second is a tuple of gradient arrays.

copy_parameters_from(params)  
Copies parameters from another source without reallocation.

Parameters params (Iterable) – Iterable of parameter arrays.

gradients  
Tuple of gradient arrays of all registered functions.

The order of gradients is consistent with parameters() property.

parameters  
Tuple of parameter arrays of all registered functions.

The order of parameters is consistent with gradients() property.
to_cpu()
Migrates all parameters and gradients onto CPU.
This method calls to_cpu method of each registered object.

Returns self
to_gpu(device=None)
Migrates all parameters and gradients onto GPU.
This method calls to_gpu method of each registered object.

Parameters device (int or pycuda.driver.Device or None) – Device ID of GPU. If None is given, it uses the current device.

Returns self

2.1.4 Optimizer
class chainer.Optimizer
Base class of all numerical optimizers.

Optimizer is set up with references to parameters and gradients, and then on every call of update(), it updates parameters based on corresponding gradients. Optimizer implementations must override update_one() method, which updates one parameter array using the corresponding gradient array.

Optimizer can optionally use state for each parameter/gradient pair. It is initialized by init_state() method at set up.

t
int
Number of update steps. It can be used in update_one() implementation, where t is incremented beforehand.

accumulate_grads(grads)
Accumulates gradients from other source.

This method just adds given gradient arrays to gradients that this optimizer holds. It is typically used in data-parallel optimization, where gradients for different shards are computed in parallel and aggregated by this method. This method correctly treats multiple GPU devices.

Parameters grads (Iterable) – Iterable of gradient arrays to be accumulated.

clip_grads(maxnorm)
Clips the norm of whole gradients up to given threshold.

Parameters maxnorm (float) – Threshold of gradient L2 norm.

See also:
compute_grads_norm() It uses this method to compute the gradient norm to be clipped.

compute_grads_norm()
Computes the norm of whole gradients.

Returns L2 norm of whole gradients, i.e. square root of sum of square of all gradient elements.

Return type float
Warning: This method returns a CPU-computed value, which means that this method synchronizes between CPU and GPU if at least one of the gradients reside on the GPU.

init_state (param, grad)
Returns the initial state for given parameter and gradient.

Default implementation delegates the procedure to init_state_cpu() or init_state_gpu() depending on the type of param.

Parameters
• param – Parameter array.
• grad – Gradient array corresponding to param.

Returns
Initial state value.

Warning: Note that, on every call of update_one(), the state value is passed by value and then the method updates its content, so the state must be a reference. Especially, one cannot use a value of built-in numeric type. If the state is one scalar value, it is recommended to use scalar array, i.e. ndarray with shape ()

init_state_cpu (param, grad)
Returns the initial state for given parameter and gradient on GPU.

Parameters
• param (ndarray) – Parameter array.
• grad (ndarray) – Gradient array.

Returns Initial state value.

See also: init_state(), init_state_gpu()

init_state_gpu (param, grad)
Returns the initial state for given parameter and gradient on CPU.

Parameters
• param (GPUArray) – Parameter array.
• grad (GPUArray) – Gradient array.

Returns Initial state value.

See also: init_state(), init_state_gpu()

setup (params_grads)
Prepares states for all given parameter/gradient pairs.

Parameters params_grads – Tuple (pair) of two tuples. The first element is a tuple of parameter arrays, and the second is a tuple of corresponding gradient arrays. Return value of FunctionSet.collect_parameters() method can be used.

update ()
Updates all parameters and states using corresponding gradients.
This method iteratively calls `update_one()` for each parameter/gradient/state tuple. Beforehand, `t` attribute is incremented.

**update_one** *(param, grad, state)*

Updates a parameter array and its state using given gradient.

The default implementation delegates the procedure to `update_one_cpu()` or `update_one_gpu()` depending on the type of the parameter array. Optimizer implementation must override these type-specific methods or this `update_one()` method directly.

**Parameters**

- **param** – Parameter array.
- **grad** – Gradient array.
- **state** – State value.

**See also:**

`update_one_cpu()`, `update_one_gpu()`

**update_one_cpu** *(param, grad, state)*

Updates a parameter array and its state using given gradient on CPU.

**Parameters**

- **param** *(ndarray)* – Parameter array.
- **grad** *(ndarray)* – Gradient array.
- **state** – State value.

**See also:**

`update_one()`, `update_one_gpu()`

**update_one_gpu** *(param, grad, state)*

Updates a parameter array and its state using given gradient on GPU.

**Parameters**

- **param** *(GPUArray)* – Parameter array.
- **grad** *(GPUArray)* – Gradient array.
- **state** – State value.

**See also:**

`update_one()`, `update_one_cpu()`

**weight_decay** *(decay)*

Applies weight decay to the parameter/gradient pairs.

**Parameters**

- **decay** *(float)* – Coefficient of weight decay

**zero_grads** *

Fills all gradient arrays by zeros.

This method should be call before backprop takes place, since gradients are accumulated on backprop.
2.2 Utilities

2.2.1 CUDA utilities

Device, context and memory management on PyCUDA and scikit-cuda.

Chainer uses PyCUDA facilities (with very thin wrapper) to exploit the speed of GPU computation. Following modules and classes are imported to cuda module for convenience (refer to this table when reading chainer’s source codes).

<table>
<thead>
<tr>
<th>imported name</th>
<th>original name</th>
</tr>
</thead>
<tbody>
<tr>
<td>chainer.cuda.cublas</td>
<td>skcuda.cublas</td>
</tr>
<tr>
<td>chainer.cuda.cumath</td>
<td>pycuda.cumath</td>
</tr>
<tr>
<td>chainer.cuda.curandom</td>
<td>pycuda.curandom</td>
</tr>
<tr>
<td>chainer.cuda.culinalg</td>
<td>skcuda.linalg</td>
</tr>
<tr>
<td>chainer.cuda.cumisc</td>
<td>skcuda.misc</td>
</tr>
<tr>
<td>chainer.cuda.gpufarray</td>
<td>pycuda.gpufarray</td>
</tr>
<tr>
<td>chainer.cuda.Context</td>
<td>pycuda.driver.Context</td>
</tr>
<tr>
<td>chainer.cuda.Device</td>
<td>pycuda.driver.Device</td>
</tr>
<tr>
<td>chainer.cuda.Event</td>
<td>pycuda.driver.Event</td>
</tr>
<tr>
<td>chainer.cuda.GPUArray</td>
<td>pycuda.gpufarray.GPUArray</td>
</tr>
<tr>
<td>chainer.cuda.Stream</td>
<td>pycuda.driver.Stream</td>
</tr>
</tbody>
</table>

Chainer provides thin wrappers of GPUArray allocation routines, which use `mem_alloc()` as the allocator. This allocator uses device-wise instance of DeviceMemoryPool, which enables the reuse of device memory over multiple forward/backward computations. `mem_alloc()` also inserts an additional attribute to the allocated memory called `device`, which indicates the device that the memory is allocated on. Functions of cuda uses this attribute to select appropriate device on each manipulation routine.

Initialization and global states

`chainer.cuda.init(device=None)`

Initializes CUDA global state.

Chainer maintains CUDA context, CUBLAS context, random number generator and device memory pool for each GPU device and for each process (the main process or a process forked by `multiprocessing`) as global states. When called for the first time on the process, this function initializes these global states.

**Warning:** This function also initializes PyCUDA and scikit-cuda. Since these packages do not support forking after initialization, do not call this function before forking the process.

This function also registers `shutdown()` to `atexit` slot.

It also initializes random number generator. User can set fixed seed with `CHAINER_SEED` environment variable.

**Parameters**

- `device` (int or Device or None) – Device ID to initialize on.

`chainer.cuda.shutdown()`

Finalizes CUDA global state.

This function is automatically called by `atexit`. Multiple calls are allowed, so user can manually call this function if necessary.

`chainer.cuda.mem_alloc(nbytes)`

Allocates device memory of given size from memory pool.

This function chooses memory pool corresponding to the current device.
Parameters \texttt{nbytes (int)} – The size of memory in bytes.

Returns Allocated memory with additional \texttt{device} attribute. This attribute is used to determine on which GPU the memory resides.

Return type \texttt{pycuda.tools.PooledDeviceAllocation}

Devices and contexts

\texttt{chainer.cuda.get_device} (\texttt{arg=None})

Gets the device from ID \texttt{arg} or given chainer’s.

\texttt{GPUArray}.

Args: \texttt{arg}: Value to specify a GPU device.

Returns: Device object specified by given \texttt{arg}.

The rule of device selection is following.

<table>
<thead>
<tr>
<th>Type of arg</th>
<th>Return value</th>
</tr>
</thead>
<tbody>
<tr>
<td>None</td>
<td>Current device</td>
</tr>
<tr>
<td>int</td>
<td>Device of ID \texttt{arg}</td>
</tr>
<tr>
<td>Device</td>
<td>\texttt{arg}</td>
</tr>
<tr>
<td>GPUArray</td>
<td>Device given array was allocated on</td>
</tr>
<tr>
<td>ndarray</td>
<td>None</td>
</tr>
</tbody>
</table>

\texttt{chainer.cuda.use_device} (\texttt{arg}, \texttt{pop=True})

Switches the CUDA context to use given device.

Parameters

- \texttt{arg} – Argument of \texttt{get_device()}.  
- \texttt{pop (bool)} – If True, pop the current context from context stack.

\texttt{chainer.cuda.using_device} (*\texttt{args})

Returns a DeviceUser object of the first GPUArray argument.

If none of the arguments specifies a GPU device, then it returns a dummy \texttt{DeviceUser} object which is inactive.

Parameters \texttt{*\texttt{args}} – Objects based on which an appropriate device should be selected.

Returns Device user instance of selected argument.

Return type \texttt{DeviceUser}

Example

Suppose \texttt{arrays} is a list of arrays of type either \texttt{ndarray} or \texttt{GPUArray}. Then, the following code invokes \texttt{do_something_on} with an appropriate context:

```python
with using_device(*arrays):
    do_something_on(arrays)
```

class \texttt{chainer.cuda.DeviceUser} (\texttt{arg})

RAII-style CUDA context swithcer.

Parameters \texttt{arg} – Argument of \texttt{get_device()}.  

2.2. Utilities
device

~pycuda.driver.Device

Selected device.

criminator.cuda.get_context(arg=None)

Gets the context corresponding to the specified device.

Parameters arg – Argument of get_device().

Returns Context object corresponding to the specified device.

Return type Context

criminator.cuda.get_cublas_handle()

Gets CUBLAS handle for the current device.

Returns CUBLAS handle.

criminator.cuda.using_cumisc(handle=None)

Temporarily set chainer’s CUBLAS handle to scikit-cuda.

The usage is similar to using_device().

Parameters handle – CUBLAS handle. If None is specified, it uses CUBLAS handle for the current device.

Returns Misc user object.

Return type CumiscUser

class chriminator.cuda.CumiscUser(handle)

RAII-style switcher of scikits-cuda’s default CUBLAS handle.

GPUArray allocation and copy

cominator.cuda.copy(array, out=None, out_device=None)

Copies a GPUArray object using the default stream.

This function can copy the device array to the destination array on another device.

Parameters

• array (GPUArray) – Array to be copied.

• out (GPUArray) – Destination array. If it is not None, then out_device argument is ignored.

• out_device – Destination device specifier. Actual device object is obtained by passing this value to get_device().

Returns

Copied array.

If out is not specified, then the array is allocated on the device specified by out_device argument.

Return type GPUArray

cominator.cuda.copy_async(array, out=None, out_device=None, stream=None)

Copies a GPUArray object using the given stream.

This function can copy the device array to the destination array on another device.

Parameters
• **array** (*GPUArray*) – Array to be copied.
• **out** (*GPUArray*) – Destination array. If it is not `None`, then `out_device` argument is ignored.
• **out_device** – Destination device specifier. Actual device object is obtained by passing this value to `get_device()`.
• **stream** (*Stream*) – CUDA stream.

Returns
Copied array.

If `out` is not specified, then the array is allocated on the device specified by `out_device` argument.

Return type **GPUArray**

**Warning:** Currently, `copy_async` over different devices raises exception, since PyCUDA drops the definition of `pycuda.driver.memcopy_peer_async()`.

`chainer.cuda.empty(shape, dtype=<type ‘numpy.float32’>)`
Creates an uninitialized GPUArray object.

Parameters
• **shape** (*tuple of ints*) – The shape of array.
• **dtype** (*numpy.dtype*) – Element type.

Returns Uninitialized GPU array allocated by memory pool.

Return type **GPUArray**

`chainer.cuda.empty_like(array)`
Alias to `pycuda.gpudarray.empty_like()`.

`chainer.cuda.full(shape, fill_value, dtype=<type ‘numpy.float32’>, stream=None)`
Creates a constant-filled GPUArray object.

Parameters
• **shape** (*tuple of ints*) – The shape of array.
• **fill_value** – Constant to fill the array by.
• **dtype** (*numpy.dtype*) – Element type.
• **stream** (*Stream*) – CUDA stream.

Returns Constant-filled GPU array allocated by memory pool.

Return type **GPUArray**

`chainer.cuda.full_like(array, fill_value, stream=None)`
Creates a constant-filled GPUArray object like the given array.

Parameters
• **array** (*GPUArray*) – Base array.
• **fill_value** – Constant value to fill the array by.
• **stream** (*Stream*) – CUDA stream.

Returns Constant-filled array.
Return type GPUArray

chainer.cuda.zeros(shape, dtype=<type 'numpy.float32'>, stream=None)

Creates a zero-filled GPUArray object.

This function is equivalent to full(shape, 0, dtype, stream).

chainer.cuda.zeros_like(array, stream=None)

Creates a zero-filled GPUArray object like the given array.

This function is equivalent to full_like(array, 0, stream).

chainer.cuda.ones(shape, dtype=<type 'numpy.float32'>, stream=None)

Creates a zero-filled GPUArray object.

This function is equivalent to full(shape, 1, dtype, stream).

chainer.cuda.ones_like(array, stream=None)

Creates a one-filled GPUArray object like the given array.

This function is equivalent to full_like(array, 1, stream).

chainer.cuda.to_cpu(array)

Copies the given GPU array to host CPU.

Parameters array – Array to be sent to GPU.

Returns

Array on CPU.

If given array is already on CPU, then this function just returns array without performing any copy.

Return type ndarray

chainer.cuda.to_cpu_async(array, stream=None)

Copies the given GPU array asynchronously to host CPU.

Parameters

• array – Array to be sent to GPU.

• stream (Stream) – CUDA stream.

Returns

Array on CPU.

If given array is already on CPU, then this function just returns array without performing any copy.

Return type ndarray

chainer.cuda.to_gpu(array, device=None)

Copies the given CPU array to specified device.

Parameters

• array – Array to be sent to GPU.

• device – Device specifier.

Returns

Array on GPU.
If array is already on GPU, then this function just returns array without performing any copy. Note that this function does not copy GPUArray into specified device.

**Return type**  
GPUArray

`chainer.cuda.to_gpu_async(array, stream=None)`  
Copies the given CPU array asynchronously to the current device.

**Parameters**  
- `array` – Array to be sent to GPU. If it is `ndarray`, then its memory must be pagelocked.
- `stream` (`Stream`) – CUDA stream.

**Returns**  
Array on GPU.

If given array is already on GPU, then this function just returns array without performing any copy.

**Return type**  
GPUArray

### Random number generators

`chainer.cuda.get_generator(device=None)`  
Gets the random number generator for the given device.

**Parameters**  
- `device` – Device specifier (an arugment of `get_device()`)

**Returns**  
Random number generator.

**Return type**  
`pycuda.curandom.XORWOWRandomNumberGenerator`

`chainer.cuda.seed(s=None, device=None)`  
Resets the random number generator of the specified device.

**Parameters**  
- `s` (**int or None**) – Seed value. If it is None, it initializes the generator without fixed seed.
- `device` – Device specifier (i.e. argument of `get_device()`).

### Kernel definition utilities

`chainer.cuda.elementwise(arguments, operation, name, keep=False, options=None, preamble='', loop_prep='', after_loop='')`  
Creates an elementwise kernel function.

This function uses `pycuda.tools.context_dependent_memoize()` to cache the resulting kernel object, i.e. the resulting kernel object is cached for each arguments and CUDA context.

The arguments are the same as those for `pycuda.elementwise.ElementwiseKernel()`, except that `name` argument is mandatory.

`chainer.cuda.reduce(arguments, map_expr, reduce_expr, neutral, name, dtype_out=<type 'numpy.float32'>, keep=False, options=None, preamble='')`  
Creates a global reduction kernel function.

This function uses `pycuda.tools.context_dependent_memoize()` to cache the resulting kernel object, i.e. the resulting kernel object is cached for each argument and CUDA context.
The arguments are the same as those for \texttt{pycuda.reduction.ReductionKernel()}, except that their order is different and \texttt{name} argument is mandatory.

### Interprocess communication on GPU

**class** \texttt{chainer.cuda.IPCEvent}

Event object for interprocess synchronization on GPU.

**class** \texttt{chainer.cuda.IPCArrayHandle}(array)

Converter between GPUArray and its Inter-Process Communication handle.

It holds IPC memory handle with shape and dtype information. The instance can be pickled, which means it can be passed through IPC path way, e.g. Pipe and Queue. The other process can extract shared GPUArray by calling \texttt{get()}. Also, the extracted array can be re-converted into another IPCArrayHandle.

### 2.2.2 Common algorithms

**class** \texttt{chainer.utils.WalkerAlias}(probs)

Implementation of Walker's alias method.

This method generates a random sample from given probabilities \(p_1, \ldots, p_n\) in \(O(1)\) time. It is more efficient than \texttt{choice()}. This class has sampling methods in CPU and in GPU.

**Parameters**

\texttt{probs} \texttt{(float list)} – Probabilities of entries. They are normalized with \texttt{sum(probs)}.

See: Wikipedia article

**sample** (shape)

Generates a random sample based on given probabilities.

**Parameters**

\texttt{shape} \texttt{(tuple of int)} – Shape of a return value.

**Returns**

Returns a generated array with the given shape. If a sampler is in CPU mode the return value is \texttt{ndarray}, and if it is in GPU mode the return value is \texttt{GPUArray}.

**to\_gpu**

Make a sampler GPU mode.

### 2.3 Assertion and Testing

Chainer provides some facilities to make debugging easy.

\texttt{Function} uses a systematic type checking of the \texttt{chainer.utils.type\_check} module. It enables users to easily find bugs of forward and backward implementations. You can find examples of type checking in some function implementations.

Most function implementations are numerically tested by \texttt{gradient checking}. This method computes numerical gradients of forward routines and compares their results with the corresponding backward routines. It enables us to make the source of issues clear when we hit an error of gradient computations. The \texttt{chainer.gradient\_check} module makes it easy to implement the gradient checking.

### 2.3.1 Type checking utilites

**class** \texttt{chainer.utils.type\_check.Expr}(priority)

Abstract syntax tree of an expression.
It represents an abstract syntax tree, and isn’t a value. You can get its actual value with `eval()` function, and
get syntax representation with the `__str__()` method. Each comparison operator (e.g. `==`) generates a new
`Expr` object which represents the result of comparison between two expressions.

Example
Let `x` and `y` be instances of `Expr`, then

```python
>>> c = (x == y)
```

is also an instance of `Expr`. To evaluate and get its value, call `eval()` method:

```python
>>> c.eval()
True # when x.eval() == y.eval()
```

Call `str` function to get a representation of the original equation:

```python
>>> str(c)
'x + y' # when str(x) == 'x' and str(y) == 'y'
```

You can actually compare an expression with a value:

```python
>>> (x == 1).eval()
```

Note that you can’t use boolean operators such as `and`, as they try to cast expressions to boolean values:

```python
>>> x == y and y == z # raises an error
```

`eval()`
Evaluates the tree to get actual value.

Behavior of this function depends on an implementation class. For example, a binary operator `+` calls the
`__add__` function with the two results of `eval()` function.

`chainer.utils.type_check.expect(*bool_exprs)`
Evaluates and tests all given expressions.

This function evaluates given boolean expressions in order. When at least one expression is evaluated as `False`,
that means the given condition is not satisfied. You can check conditions with this function.

**Parameters**
`bool_exprs` (tuple of `Bool expressions`) -- Bool expressions you want to evaluate.

`chainer.utils.type_check.TypeInfo(shape, dtype)`
Type information of an input/gradient array.

It contains type information of an array, such as the shape of array and the number of dimensions. This information
is independent of CPU or GPU array.

`chainer.utils.type_check.TypeInfoTuple`
Type information of input/gradient tuples.

It is a sub-class of tuple containing `TypeInfo`. The i-th element of this object contains type information of the
i-th input/gradient data. As each element is `Expr`, you can easily check its validity.

`size()`
Returns an expression representing its length.

**Returns**
An expression object representing length of the tuple.

`Return type` `Expr`
2.3.2 Gradient checking utilities

chainer.gradient_check.assert_allclose(x, y, atol=1e-05, rtol=0.0001, verbose=True)

Asserts if some corresponding element of x and y differs too much.

This function can handle both CPU and GPU arrays simultaneously.

Parameters

• x – Left-hand-side array.
• y – Right-hand-side array.
• atol (float) – Absolute tolerance.
• rtol (float) – Relative tolerance.
• verbose (bool) – If True, it outputs verbose messages on error.

chainer.gradient_check.numerical_grad(f, inputs, grad_outputs, eps=0.001)

Computes numerical gradient by finite differences.

This function is used to implement gradient check. For usage example, see unit tests of chainer.functions.

Parameters

• f (function) – Python function with no arguments that runs forward computation and returns the result.
• inputs (tuple of arrays) – Tuple of arrays that should be treated as inputs. Each element of them is slightly modified to realize numerical gradient by finite differences.
• grad_outputs (tuple of arrays) – Tuple of arrays that are treated as output gradients.
• eps (float) – Epsilon value of finite differences.

Returns Numerical gradient arrays corresponding to inputs.

Return type tuple

2.4 Standard Function implementations

Chainer provides basic Function implementations in the chainer.functions package.

Non-parameterized functions are provided as plain Python functions. These can be used directly in forward computation without explicit handling of Function objects. On the other hand, parameterized functions should be used with explicit handling of Function objects.

2.4.1 Learnable connections

class chainer.functions.BinaryHierarchicalSoftmax(in_size, tree)
Implementation of hierarchical softmax (HSM).

In natural language applications, vocabulary size is too large to use softmax loss. Instead, the hierarchical softmax uses product of sigmoid functions. It costs only \(O(\log(n))\) time where \(n\) is the vocabulary size in average.

At first a user need to prepare a binary tree whose each leaf is corresponding to a word in a vocabulary. When a word \(x\) is given, exactly one path from the root of the tree to the leaf of the word exists. Let path(\(x\) =
\((e_1, b_1), \ldots, (e_m, b_m)\) be the path of \(x\), where \(e_i\) is an index of \(i\)-th internal node, and \(b_i \in \{-1, 1\}\) indicates direction to move at \(i\)-th internal node (-1 is left, and 1 is right). Then, the probability of \(x\) is given as below:

\[
P(x) = \prod_{(e_i, b_i) \in \text{path}(x)} P(b_i | e_i) = \prod_{(e_i, b_i) \in \text{path}(x)} \sigma(b_i x^T w_{e_i}),
\]

where \(\sigma(\cdot)\) is a sigmoid function, and \(w\) is a weight matrix.

This function costs \(O(\log(n))\) time as an average length of paths is \(O(\log(n))\), and \(O(n)\) memory as the number of internal nodes equals \(n - 1\).

**Parameters**
- \texttt{in\_size} (int) – Dimension of input vectors.
- \texttt{tree} – A binary tree made with tuples like \(((1, 2), 3)\).

See: Hierarchical Probabilistic Neural Network Language Model [Morin+, AISTAT2005].

```python
class chainer.functions.Convolution2D(in_channels, out_channels, ksize, stride=1, pad=0, wscale=1, bias=0, nobias=False, use_cudnn=True, initialW=None, initial_bias=None)
```

Two-dimensional convolution function.

The details of this function are described below the arguments description.

**Parameters**
- \texttt{in\_channels} (int) – Number of channels of input arrays.
- \texttt{out\_channels} (int) – Number of channels of output arrays.
- \texttt{ksize} (int or (int, int)) – Size of filters (a.k.a. kernels). \(ksize=k\) and \(ksize=(k, k)\) are equivalent.
- \texttt{stride} (int or (int, int)) – Stride of filter applications. \(stride=s\) and \(stride=(s, s)\) are equivalent.
- \texttt{pad} (int or (int, int)) – Spatial padding width for input arrays. \(pad=p\) and \(pad=(p, p)\) are equivalent.
- \texttt{wscale} (float) – Scaling factor of the initial weight.
- \texttt{bias} (float) – Initial bias value.
- \texttt{nobias} (bool) – If True, then this function does not use the bias term.
- \texttt{use\_cudnn} (bool) – If True, then this function uses CuDNN if available.
- \texttt{initialW} (4-D array) – Initial weight value. If \texttt{None}, then this function uses to initialize \(wscale\).
- \texttt{initial\_bias} (1-D array) – Initial bias value. If \texttt{None}, then this function uses to initialize \(bias\).

This function holds at most two parameter arrays: \(W\) and \(b\), which indicate the filter weight and the bias vector, respectively.

The filter weight has four dimensions \((c_O, c_I, k_H, k_W)\) which indicate the number of output channels, the number of input channels, height and width of the kernels, respectively. The filter weight is initialized with i.i.d. Gaussian random samples, each of which has zero mean and deviation \(\sqrt{1/(c_I k_H k_W)}\) by default. The deviation is scaled by \(\texttt{wscale}\) if specified.
The bias vector is of size $c_O$. Each element of it is initialized by `bias` argument. If `nobias` argument is set to True, then this function does not hold the bias parameter.

The two-dimensional convolution function is defined as follows. Let $X$ be the input tensor of dimensions $(n, c_I, h, w)$, where $n$ is the batch size, and $(h, w)$ is spatial size of the input image. Then the `Convolution2D` function computes correlations between filters and patches of size $(k_H, k_W)$ in $X$. Note that correlation here is equivalent to the inner product between expanded vectors. Patches are extracted at positions shifted by multiples of `stride` from the first position `-pad` for each spatial axis. The right-most (or bottom-most) patches do not run over the padded spatial size.

Let $(s_Y, s_X)$ be the stride of filter application, and $(p_H, p_W)$ the spatial padding size. Then, the output size $(h_O, w_O)$ is determined by the following equations:

$$h_O = (h + 2p_H - k_H)/s_Y + 1,$$
$$w_O = (w + 2p_W - k_W)/s_X + 1.$$  

**class chainer.functions.EmbedID (in_size, out_size)**

Efficient linear function for one-hot input.

This is a parameterized function to embed the given discrete identifier (e.g. word) into a continuous vector space. This function just holds embedding vectors for all identifiers as one large matrix $W$, which is learnable. The identifiers are directly used as indexes of the matrix $W$.

**Parameters**

- `in_size` (int) – Number of different identifiers (a.k.a. vocabulary size).
- `out_size` (int) – Size of embedding vector.

**Note:** This function is non-differentiable with respect to the input identifiers.

**class chainer.functions.Linear (in_size, out_size, wscale=1, bias=0, nobias=False, initialW=None, initial_bias=None)**

Linear function (a.k.a. fully-connected layer or affine transformation).

This function holds a weight matrix $W$ and a bias vector $b$.

The weight matrix $W$ has shape $(out_size, in_size)$. This matrix is initialized with i.i.d. Gaussian samples, each of which has zero mean and deviation $\sqrt{1/}$

**Parameters**

- `in_size` (int) – Dimension of input vectors.
- `out_size` (int) – Dimension of output vectors.
- `wscale` (float) – Scaling factor of the weight matrix.
- `bias` (float) – Initial bias value.
- `nobias` (bool) – If True, then this function does not use the bias.
- `initialW` (2-D array) – Initial weight value. If None, then this function uses to initialize $wscale$.
- `initial_bias` (1-D array) – Initial bias value. If None, then this function uses to initialize $bias$.

**Note:** This function accepts an input variable of a non-matrix array. In this case, the leading dimension is treated as the batch dimension, and the other dimensions are reduced to one dimension.

**class chainer.functions.NegativeSampling (in_size, counts, sample_size, power=0.75)**

Implementation of negative sampling.

In natural language processing, especially language modeling, the number of vocabulary is very large. Therefore, you need to spend a lot of time to calculate the gradient of the embedding matrix.
Instead, in negative sampling trick, you only need to calculate the gradient for a few sampled negative examples. The objective function is below:

\[ f(x, p) = \log \sigma(x^T w_p) + kE_{i \sim P(i)}[\log \sigma(-x^T w_i)], \]

where \( \sigma(\cdot) \) is a sigmoid function, \( w_i \) is the weight vector for the word \( i \), and \( p \) is a positive example. It is approximated with \( k \) examples \( N \) sampled from probability \( P(i) \), like this:

\[ f(x, p) \approx \log \sigma(x^T w_p) + \sum_{n \in N} \log \sigma(-x^T w_n). \]

Each sample of \( N \) is drawn from the word distribution \( P(w) \). This is calculated as \( P(w) = \frac{1}{Z} c(w)^\alpha \), where \( c(w) \) is the unigram count of the word \( w \), \( \alpha \) is a hyper-parameter, and \( Z \) is the normalization constant.

**Parameters**

- `in_size (int)` – Dimension of input vectors.
- `counts (int list)` – Number of each identifiers.
- `sample_size (int)` – Number of negative samples.
- `power (float)` – Power factor \( \alpha \).

See: Distributed Representations of Words and Phrases and their Compositionality

```python
class chainer.functions.Parameter(array):
    Function that outputs its weight array.

    This is a parameterized function that takes no input and returns a variable holding a shallow copy of the parameter array.

    Parameters
    array -- Initial parameter array.
```

### 2.4.2 Array computation functions

```python
class chainer.functions.convolution_2d(x, W, b=None, stride=1, pad=0, use_cudnn=True):
    Two-dimensional convolution function.

    Parameters
    x (Variable) -- Input variable.
    W (Variable) -- Weight variable.
    b (Variable) -- Bias variable.
    stride (int or (int, int)) -- Stride of filter applications. stride=s and stride=(s, s) are equivalent.
    pad (int or (int, int)) -- Spatial padding width for input arrays. pad=p and pad=(p, p) are equivalent.
    use_cudnn (bool) -- If True, then this function uses CuDNN if available.

    Returns
    Output variable.
```

See also:

`Convolution2D`
chainer.functions.linear(x, W, b=None, stride=1, pad=0, use_cudnn=True)
Nonparameterized linear function.

Parameters
• x (Variable) – Input variable.
• W (Variable) – Weight variable.
• b (Variable) – Bias variable.

Returns Output variable.
Return type Variable

See also:
Linear

2.4.3 Array manipulation functions

chainer.functions.concat(xs, axis=1)
Concatenates given variables along an axis.

Parameters
• xs (tuple of Variables) – Variables to be concatenated.
• axis (int) – Axis that the input arrays are concatenated along.

Returns Output variable.
Return type Variable

chainer.functions.copy(x, dst)
Copies the input variable onto the specified device.

This function copies the array of input variable onto the device specified by dst if the original array is on GPU, and otherwise just copies the array within host memory.

Parameters
• x (Variable) – Variable to be copied.
• dst – Target device specifier.

Returns Output variable.
Return type Variable

chainer.functions.dropout(x, ratio=0.5, train=True)
Drops elements of input variable randomly.

This function drops input elements randomly with probability ratio and scales the remaining elements by factor \(1 / (1 - \text{ratio})\). In testing mode, it does nothing and just returns x.

Parameters
• x (Variable) – Input variable.
• ratio (float) – Dropout ratio.
• train (bool) – If True, executes dropout. Otherwise, does nothing.

Returns Output variable.
Return type Variable
See the paper by G. Hinton: Improving neural networks by preventing co-adaptation of feature detectors.

chainer.functions.identity(*inputs)
Just returns input variables.

chainer.functions.reshape(x, shape)
Reshapes an input variable without copy.

Parameters
• x (Variable) – Input variable.
• shape (tuple of ints) – Target shape.

Returns Variable that holds a reshaped version of the input variable.

Return type Variable

chainer.functions.split_axis(x, indices_or_sections, axis)
Splits given variables along an axis.

Parameters
• x (tuple of Variables) – Variables to be split.
• indices_or_sections (int or 1-D array) – If this argument is an integer, N, the array will be divided into N equal arrays along axis. If it is a 1-D array of sorted integers, it indicates the positions where the array is split.
• axis (int) – Axis that the input array is split along.

Returns Tuple of Variable objects if the number of outputs is more than 1 or Variable otherwise.

Return type tuple or Variable

Note: This function raises ValueError if at least one of the outputs is splitted to zero-size (i.e. axis-th value of its shape is zero).

2.4.4 Array computations

chainer.functions.matmul(a, b, transa=False, transb=False)
Computes the matrix multiplication of two arrays.

Parameters
• a (Variable) – The left operand of the matrix multiplication. A 1-D array of shape (N,) is considered as an Nx1 matrix. A 2-D array of shape (M, N) is considered as an MxN matrix.
• b (Variable) – The right operand of the matrix multiplication. Its array is treated as a matrix in the same way as a’s array.
• transa (bool) – If true, transpose a.
• transb (bool) – If true, transpose b.

Returns The result of the matrix multiplication as a 2-D array.

Return type Variable

chainer.functions.batch_matmul(a, b, transa=False, transb=False)
Computes the batch matrix multiplications of two sets of arrays.

Parameters
• **a** *(Variable)* – The left operand of the batch matrix multiplications. A 2-D array of shape \((B, N,)\) is considered as \(B \times 1\) matrices. A 3-D array of shape \((B, M, N)\) is considered as \(B \times M \times N\) matrices.

• **b** *(Variable)* – The right operand of the batch matrix multiplications. Its array is treated as matrices in the same way as a’s array.

• **transa** *(bool)* – If true, transpose each matrix in a.

• **transb** *(bool)* – If true, transpose each matrix in b.

**Returns** The result of the batch matrix multiplications as a 3-D array.

**Return type** *Variable*

### 2.4.5 Activation functions

**chainer.functions.exp**(x)

Elementwise exponential function.

**chainer.functions.leaky_relu**(x, slope=0.2)

Leaky Rectified Linear Unit function.

This function is expressed as \(f(x) = \max(x, ax)\), where a is a configurable slope value.

**Parameters**

• **x** *(Variable)* – Input variable.

• **slope** *(float)* – Slope value a.

**Returns** Output variable.

**Return type** *Variable*

**chainer.functions.log**(x)

Elementwise natural logarithm function.

**chainer.functions.lstm**(c_prev, x)

Long Short-Term Memory units as an activation function.

This function implements LSTM units with forget gates. Let the previous cell state \(c_{\text{prev}}\) and the incoming signal \(x\).

First, the incoming signal \(x\) is split into four arrays \(a, i, f, o\) of the same shapes along the second axis. It means that \(x\)'s second axis must have 4 times the length of \(c_{\text{prev}}\).

The splitted input signals are corresponding to:

• \(a\) : sources of cell input

• \(i\) : sources of input gate

• \(f\) : sources of forget gate

• \(o\) : sources of output gate

Second, it computes outputs as:

\[
c = \tanh(a) \cdot \text{sigmoid}(i) + c_{\text{prev}} \cdot \text{sigmoid}(f),
\]

\[
h = \tanh(c) \cdot \text{sigmoid}(o).
\]

These are returned as a tuple of two variables.

**Parameters**
• **c_prev** (Variable) – Variable that holds the previous cell state. The cell state should be a zero array or the output of the previous call of LSTM.

• **x** (Variable) – Variable that holds the incoming signal. It must have the second dimension four times of that of the cell state.

Returns Two Variable objects \(c\) and \(h\). \(c\) is the updated cell state. \(h\) indicates the outgoing signal.

Return type **tuple**

See the original paper proposing LSTM with forget gates: Long Short-Term Memory in Recurrent Neural Networks.

### Example

Assuming \(y\) is the current input signal, \(c\) is the previous cell state, and \(h\) is the previous output signal from an \(lstm\) function. Each of \(y\), \(c\) and \(h\) has \(n\_units\) channels. Most typical preparation of \(x\) is:

```python
>>> model = FunctionSet(w=F.Linear(n_units, 4 * n_units),
                      ... v=F.Linear(n_units, 4 * n_units),
                      ...)

>>> x = model.w(y) + model.v(h)

>>> c, h = F.lstm(c, x)
```

It corresponds to calculate the input sources \(a, i, f, o\) from the current input \(y\) and the previous output \(h\). Different parameters are used for different kind of input sources.

class **chainer.functions.PReLU** (\(shape=(), init=0.25\))

Parametric ReLU function.

PReLU function is written in elementwise equation as \(PReLU(x) = \text{max}(x, ax)\), where \(a\) is a parameter array.

When the PReLU function is combined with two-dimensional convolution, the elements of parameter \(a\) are typically shared across the same filter of different pixels. In order to support such usage, this function supports the shape of parameter array that indicates leading dimensions of input arrays except the batch dimension.

Parameters

• **shape** (tuple of ints) – Shape of the parameter array.

• **init** (float) – Initial parameter value.

See detail in paper: Delving Deep into Rectifiers: Surpassing Human-Level Performance on ImageNet Classification.

```python
chainer.functions.relu(x, use_cudnn=True)
```

Rectified Linear Unit function \(f(x) = \text{max}(0, x)\).

Parameters

• **x** (Variable) – Input variable.

• **use_cudnn** (bool) – If True and CuDNN is enabled, then this function uses CuDNN as the core implementation.

Returns Output variable.

Return type **Variable**

```python
chainer.functions.sigmoid(x, use_cudnn=True)
```

Elementwise sigmoid logistic function \(f(x) = (1 + \exp(-x))^{-1}\).

Parameters
• **x** (Variable) – Input variable.

• **use_cudnn** (bool) – If True and CuDNN is enabled, then this function uses CuDNN as the core implementation.

**Returns** Output variable.

**Return type** Variable

chainer.functions.softmax(x, use_cudnn=True)

Channelwise softmax function.

This function only accepts a two dimensional input array, and computes its softmax along the second axis. For each index \(i, j\) of the input matrix \(x\), it computes \(f_{ij}(x) = \frac{\exp(x_{ij})}{\sum_j \exp(x_{ij})}\).

**Parameters**

• **x** (Variable) – Input variable.

• **use_cudnn** (bool) – If True and CuDNN is enabled, then this function uses CuDNN as the core implementation.

**Returns** Output variable.

**Return type** Variable

chainer.functions.tanh(x, use_cudnn=True)

Elementwise hyperbolic tangent function.

**Parameters**

• **x** (Variable) – Input variable.

• **use_cudnn** (bool) – If True and CuDNN is enabled, then this function uses CuDNN as the core implementation.

**Returns** Output variable.

**Return type** Variable

### 2.4.6 Pooling functions

chainer.functions.average_pooling_2d(x, ksize, stride=None, pad=0, use_cudnn=True)

Spatial average pooling function.

This function acts similarly to Convolution2D, but it computes the average of input spatial patch for each channel without any parameter instead of computing the inner products.

**Parameters**

• **x** (Variable) – Input variable.

• **ksize** (int or (int, int)) – Size of pooling window. \(ksize=k\) and \(ksize=(k, k)\) are equivalent.

• **stride** (int or (int, int) or None) – Stride of pooling applications. \(ksize=k\) and \(ksize=(k, k)\) are equivalent. If None is specified, then it uses same stride as the pooling window size.

• **pad** (int or (int, int)) – Spatial padding width for the input array. \(pad=p\) and \(pad=(p, p)\) are equivalent.

• **use_cudnn** (bool) – If True and CuDNN is enabled, then this function uses CuDNN as the core implementation.
Returns Output variable.

Return type Variable

Note: This function currently does not support cover_all mode as max_pooling_2d(). Average pooling runs in non-cover-all mode.

chainer.functions.max_pooling_2d(x, ksize, stride=None, pad=0, cover_all=True, use_cudnn=True)

Spatial max pooling function.

This function acts similarly to Convolution2D, but it computes the maximum of input spatial patch for each channel without any parameter instead of computing the inner products.

Parameters

• x (Variable) – Input variable.
• ksize (int or (int, int)) – Size of pooling window. ksize=k and ksize=(k, k) are equivalent.
• stride (int or (int, int) or None) – Stride of pooling applications. ksize=k and ksize=(k, k) are equivalent. If None is specified, then it uses same stride as the pooling window size.
• pad (int or (int, int)) – Spatial padding width for the input array. pad=p and pad=(p, p) are equivalent.
• cover_all (bool) – If True, all spatial locations are pooled into some output pixels. It may make the output size larger.
• use_cudnn (bool) – If True and CuDNN is enabled, then this function uses CuDNN as the core implementation.

Returns Output variable.

Return type Variable

2.4.7 Normalization functions

class chainer.functions.BatchNormalization (size, decay=0.9, eps=1e-05)

Batch normalization on outputs of linear or convolution functions.

Parameters

• size (int or tuple of ints) – Size (or shape) of channel dimensions.
• decay (float) – Decay rate of moving average.
• eps (float) – Epsilon value for numerical stability.

See: Batch Normalization: Accelerating Deep Network Training by Reducing Internal Covariate Shift

__call__ (x, test=False, finetune=False)

Invokes the forward propagation of BatchNormalization.

BatchNormalization accepts additional arguments, which controls three different running mode.

Parameters

• x (Variable) – An input variable.
• test (bool) – If True, BatchNormalization runs in testing mode; it normalizes the input using precomputed statistics.
• **finetune** *(bool)* – If True, BatchNormalization runs in finetuning mode; it accumulates the input array to compute population statistics for normalization, and normalizes the input using batch statistics.

If test and finetune are both False, then BatchNormalization runs in training mode; it computes moving averages of mean and variance for evaluation during training, and normalizes the input using batch statistics.

chainer.functions.local_response_normalization*(x, n=5, k=2, alpha=0.0001, beta=0.75)*

Local response normalization across neighboring channels.

This function implements normalization across channels. Let $x$ an input image with $N$ channels. Then, this function computes an output image $y$ by following formula:

$$y_i = \frac{x_i}{\left( k + \alpha \sum_{j=\max\{1, i-n/2\}}^{\min\{N, i+n/2\}} x_j^2 \right)^\beta}.$$

Parameters

• **x** *(Variable)* – Input variable.

• **n** *(int)* – Normalization window width.

• **k** *(float)* – Smoothing parameter.

• **alpha** *(float)* – Normalizer scaling parameter.

• **beta** *(float)* – Normalizer power parameter.

Returns Output variable.

Return type Variable

See: SSect. 3.3 of ImageNet Classification with Deep Convolutional Neural Networks

### 2.4.8 Loss, evaluation and aggregation

chainer.functions.accuracy*(y, t)*

Computes muticlass classification accuracy of the minibatch.

Parameters

• **y** *(Variable)* – Variable holding a matrix whose $(i, j)$-th element indicates the score of the class $j$ at the $i$-th example.

• **t** *(Variable)* – Variable holding an int32 vector of groundtruth labels.

Returns A variable holding a scalar array of the accuracy.

Return type Variable

Note: This function is non-differentiable.

chainer.functions.mean_squared_error*(x0, x1)*

Mean squared error function.

This function computes mean squared error between two variables. The mean is taken over the minibatch. Note that the error is not scaled by $1/2$.

chainer.functions.sigmoid_cross_entropy*(x, t, use_cudnn=True)*

Computes cross entropy loss for sigmoid activations.

Parameters
- **x (Variable)** – A variable object holding a matrix whose (i, j)-th element indicates the un-normalized log probability of the j-th unit at the i-th example.

- **t (Variable)** – A variable object holding an int32 vector of groundtruth binary labels.

**Returns** A variable object holding a scalar array of the cross entropy loss.

**Return type** *Variable*

**Note:** This function is differentiable only by *x*.

```python
chainer.functions.softmax_cross_entropy(x, t, use_cudnn=True)
```

Computes cross entropy loss for pre-softmax activations.

**Parameters**
- **x (Variable)** – Variable holding a matrix whose (i, j)-th element indicates unnormalized log probability of the class j at the i-th example.
- **t (Variable)** – Variable holding an int32 vector of groundtruth labels.

**Returns** A variable holding a scalar array of the cross entropy loss.

**Return type** *Variable*

**Note:** This function is differentiable only by *x*.

```python
chainer.functions.sum(x)
```

Computes sum of all elements.

### 2.4.9 Reusable subnetwork of complex architectures

```python
class chainer.functions.Inception(in_channels, out1, proj3, out3, proj5, out5, proj_pool)
```

Inception module of GoogLeNet.

It applies four different functions to the input array and concatenates their outputs along the channel dimension. Three of them are 2D convolutions of sizes 1x1, 3x3 and 5x5. Convolution paths of 3x3 and 5x5 sizes have 1x1 convolutions (called projections) ahead of them. The other path consists of 1x1 convolution (projection) and 3x3 max pooling.

The output array has the same spatial size as the input. In order to satisfy this, Inception module uses appropriate padding for each convolution and pooling.

See: Going Deeper with Convolutions.

**Parameters**
- **in_channels (int)** – Number of channels of input arrays.
- **out1 (int)** – Output size of 1x1 convolution path.
- **proj3 (int)** – Projection size of 3x3 convolution path.
- **out3 (int)** – Output size of 3x3 convolution path.
- **proj5 (int)** – Projection size of 5x5 convolution path.
- **out5 (int)** – Output size of 5x5 convolution path.
- **proj_pool (int)** – Projection size of max pooling path.

**Returns** Output variable. Its array has the same spatial size and the same minibatch size as the input array. The channel dimension has size `out1 + out3 + out5 + proj_pool`.

## 2.4. Standard Function implementations
Return type: **Variable**

**Note:** This function inserts the full computation graph of the Inception module behind the input array. This function itself is not inserted into the computation graph.

```python
class chainer.functions.InceptionBN(in_channels, out1, proj3, out3, proj33, out33, pooltype, proj_pool=None, stride=1)
```

Inception module of the new GoogLeNet with BatchNormalization.

This class acts like `Inception`, while InceptionBN uses the `BatchNormalization` on top of each convolution, the 5x5 convolution path is replaced by two consecutive 3x3 convolution applications, and the pooling method is configurable.


**Parameters**
- `in_channels (int)` – Number of channels of input arrays.
- `out1 (int)` – Output size of the 1x1 convolution path.
- `proj3 (int)` – Projection size of the single 3x3 convolution path.
- `out3 (int)` – Output size of the single 3x3 convolution path.
- `proj33 (int)` – Projection size of the double 3x3 convolutions path.
- `out33 (int)` – Output size of the double 3x3 convolutions path.
- `pooltype (str)` – Pooling type. It must be either `max` or `avg`.
- `proj_pool (bool)` – If True, do projection in the pooling path.
- `stride (int)` – Stride parameter of the last convolution of each path.

See also:
- `Inception`

### 2.5 Optimizers

```python
class chainer.optimizers.AdaDelta(rho=0.95, eps=1e-06)
```

Zeiler’s ADADELTA.


```python
class chainer.optimizers.AdaGrad(lr=0.001, eps=1e-08)
```

AdaGrad implementation.


```python
class chainer.optimizers.Adam(alpha=0.001, beta1=0.9, beta2=0.999, lam=0.99999999, eps=1e-08)
```

Adam optimization algorithm.


```python
class chainer.optimizers.MomentumSGD(lr=0.01, momentum=0.9)
```

Classical momentum SGD.

```python
class chainer.optimizers.RMSprop(lr=0.01, alpha=0.99, eps=1e-08)
```

Hinton’s RMSprop.
class chainer.optimizers.SGD(lr=0.01)
Vanilla Stochastic Gradient Descent.

2.6 Caffe Reference Model Support

Caffe is a popular framework maintained by BVLC at UC Berkeley. It is widely used by computer vision communities, and aims at fast computation and easy usage without any programming. The BVLC team provides trained reference models in their Model Zoo, one of the reason why this framework gets popular.

Chainer can import the reference models and emulate the network by Function implementations. This functionality is provided by the chainer.functions.caffe.CaffeFunction class.

class chainer.functions.caffe.CaffeFunction(model_path)
Function using the model file of Caffe.

Given a binary protobuf file of a Caffe model, this function loads and emulates it on Variable objects. It supports the official reference models provided by BVLC.

Note: This function only supports Python 2.7, since the compiled module for protocol buffers only supports Python 2. The __init__ function raises an exception in Python 3.

Note: CaffeFunction ignores the following layers:
• Layers that CaffeFunction does not support (including data layers)
• Layers that have no top blobs
• Layers whose bottom blobs are incomplete (i.e., some or all of them are not given nor computed)

Warning: It does not support full compatibility against Caffe. Some layers and configurations are not implemented in Chainer yet, though the reference models provided by the BVLC team are supported except data layers.

Example
Consider we want to extract the (unnormalized) log class probability of given images using BVLC reference CaffeNet. The model can be downloaded from:
http://dl.caffe.berkeleyvision.org/bvlc_reference_caffenet.caffemodel

We want to compute the fc8 blob from the data blob. It is simply written as follows:

```
# Load the model
func = CaffeFunction('path/to/bvlc_reference_caffenet.caffemodel')

# Minibatch of size 10
x_data = numpy.ndarray((10, 3, 227, 227), dtype=numpy.float32)
...  # (Fill the minibatch here)

# Forward the pretrained net
x = Variable(x_data)
y, = func(inputs={'data': x}, outputs=['fc8'])
```

The result y contains the Variable corresponding to the fc8 blob. The computational graph is memorized as a usual forward computation in Chainer, so we can run backprop through this pretrained net.
Parameters **model_path** *(str)* – Path to the binary-proto model file of Caffe.

**fs**

*FunctionSet*

A set of functions corresponding to parameterized layers of Caffe. The names of its attributes are same as the layer names of the given network.

**forwards**

*dict*

A mapping from layer names to corresponding functions.

**__call__**(inputs, outputs, disable=[], train=True)

Executes a subnetwork of the network.

This function acts as an interpreter of the network definition for Caffe. On execution, it interprets each layer one by one, and if the bottom blobs are already computed, then emulates the layer and stores output blobs as `Variable` objects.

Parameters

- **inputs** *(dict)* – A dictionary whose key-value pairs indicate initial correspondences between blob names and `Variable` objects.
- **outputs** *(Iterable)* – A list of blob names whose corresponding `Variable` objects are returned.
- **disable** *(Iterable)* – A list of layer names that will be ignored during the forward computation.
- **train** *(bool)* – If True, this function emulates the TRAIN phase of the Caffe layers. Otherwise, it emulates the TEST phase.

Returns A tuple of output `Variable` objects corresponding to elements of the *outputs* argument.

Return type tuple

### 2.7 Visualization of Computational Graph

As neural networks get larger and complicated, it gets much harder to confirm if their architectures are constructed properly. Chainer supports visualization of computational graphs. Users can generate computational graphs by invoking `build_computational_graph()`. Generated computational graphs are dumped to specified format (Currently Dot Language is supported).

Basic usage is as follows:

```python
import chainer.computational_graph as c
...
g = c.build_computational_graph(vs)
with open('path/to/output/file', 'w') as o:
    o.write(g.dump())
```

where `vs` is list of `Variable` instances and `g` is an instance of `ComputationalGraph`. This code generates the computational graph that are backward-reachable (i.e. reachable by repetition of steps backward) from at least one of `vs`.

Here is an example of (a part of) the generated graph (inception(3a) in GoogLeNet). This example is from example/imagenet.
chainer.computational_graph.build_computational_graph(outputs, remove_split=True)

Builds a graph of functions and variables backward-reachable from outputs.

Parameters

- **outputs** (list) – nodes from which the graph is constructed. Each element of outputs must be either `Variable` object or `Function` object.

- **remove_split** (bool) – If it is True, this function hides `Split` functions and related variables from the graph.

Returns

A graph consisting of nodes and edges that are backward-reachable from at least one of outputs.

If `unchain_backward` was called in some variable in the computational graph before this function, backward step is stopped at this variable.

For example, suppose that computational graph is as follows:

```
|--> x' ----> f ----> y
x ----> (splitter) ++
```

Let `outputs = [y, z]`. If `remove_split` is False, this method generates the graph itself. On the other hand, if `remove_split` is True, `splitter`, `x'` and `x''` are removed from the graph and `x` is directly connected to `f` and `g`. Resulting graph will be:

```
|--> f ----> y
x +
|--> g ----> z
```

Next, let `outputs = [y]`. Note that `z`, `g`, and `x''` are not backward-reachable from `y`. If `remove_split` is False, this function removes these unreachable nodes to get:
x ---> (splitter) ---> x' ---> f ---> y

If remove_split is True, we further remove splitter and x' to get:

x ---> f ---> y

See TestGraphBuilder for details.

Return type  ComputationalGraph
class chainer.computational_graph.ComputationalGraph(nodes, edges)
Class that represents computational graph.

Note: We assume that the computational graph is directed and acyclic.

dump(format='dot')
Dumps graph as a text.

Parameters

• format (str) – The graph language name of the output.

• it must be 'dot'. (Currently.) –

Returns  The graph in specified format.

Return type  str
This is a guide for all contributions to Chainer. The development of Chainer is running on the official repository at GitHub. Anyone that wants to register an issue or to send a pull request should read through this document.

### 3.1 Classification of Contributions

There are several ways to contribute to Chainer community:

1. Registering an issue
2. Sending a pull request (PR)
3. Sending a question to Chainer User Group
4. Open-sourcing an external example
5. Writing a post about Chainer

This document mainly focuses on 1 and 2, though other contributions are also appreciated.

### 3.2 Release and Milestone

We are using GitHub Flow as our basic working process. In particular, we are using the master branch for our development, and releases are made as tags.

Releases are classified into three groups: major, minor, and revision. This classification is based on following criteria:

- A **major** release contains catastrophic changes on the interface that may break existing user codes.
- A **minor** release contains additions and modifications on the interface. It may break some existing user codes, though they must be fixed by small efforts.
- A **revision** release contains changes that does not affect the documented interface. It mainly consists of bug fixes, implementation improvements, and test/document/example updates.

The release classification is reflected into the version number x.y.z, where x, y, and z corresponds to major, minor, and revision updates, respectively.

We sets milestones for some future releases. A milestone for a revision release is set right after the last release. On the other hand, a milestone for a minor or major release is set four weeks prior to its due.
3.3 Issues and PRs

Issues and PRs are classified into following categories:

- **Bug**: bug reports (issues) and bug fixes (PRs)
- **Enhancement**: implementation improvements without breaking the interface
- **Feature**: feature requests (issues) and their implementations (PRs)
- **Test**: test fixes and updates
- **Document**: document fixes and improvements
- **Example**: fixes and improvements on the examples
- **Other**: other issues and PRs

Issues and PRs are labeled by these categories. This classification is often reflected into its corresponding release category: Feature issues/PRs are contained into minor/major releases, while other issues/PRs can be contained into any releases including revision ones.

On registering an issue, write precise explanations on what you want Chainer to be. Bug reports must include necessary and sufficient conditions to reproduce the bugs. Feature requests must include what you want to do (and why you want to do, if needed). You can contain your thoughts on how to realize it into the feature requests, though what part is most important for discussions.

**Warning:** If you have a question on usages of Chainer, it is highly recommended to send a post to Chainer User Group instead of the issue tracker. The issue tracker is not a place to share knowledge on practices. We may redirect question issues to Chainer User Group.

If you can write codes to fix an issue, send a PR to the master branch. Before writing your codes for PRs, read through the **Coding Guidelines**. The description of any PR must contain a precise explanation of what and how you want to do; it is the first documentation of your codes for developers, a very important part of your PR.

Once you send a PR, it is automatically tested on Travis CI. After the automatic test passes, some of the core developers will start reviewing your codes. Note that this automatic PR test only includes CPU tests.

**Note:** We are also running continuous integrations with GPU tests for the master branch. Since this service is running on our internal server, we do not use it for automatic PR tests to keep the server secure.

Even if your codes are not complete, you can send a pull request as a **work-in-progress PR** by putting the [WIP] prefix to the PR title. If you write a precise explanation about the PR, core developers and other contributors can join the discussion about how to proceed the PR.

3.4 Coding Guidelines

We use PEP8 and a part of OpenStack Style Guidelines related to general coding style as our basic style guidelines.

Before checking your code, you can use automatic formatter to set appropriate spacing, etc. We recommend you to install the pyformat and isort packages, and run the following commands:

```
$ pyformat -i path/to/your/code.py
$ isort path/to/your/code.py
```

Note that these formatters do not cover all part of the style guidelines.

To check your code, use flake8 command installed by hacking package:
The `flake8` command lets you know the part of your code not obeying our style guidelines. Before sending a pull request, be sure to check that your code passes the `flake8` checking.

Note that `flake8` command is not perfect. It does not check some of the style guidelines. Here is a (not-complete) list of the rules that `flake8` cannot check.

- Relative imports are prohibited. [H304]
- Importing non-module symbols is prohibited.
- Import statements must be organized into three parts: standard libraries, third-party libraries, and internal imports. [H306]

In addition, we restrict the usage of shortcut symbols in our code base. They are symbols imported by packages and subpackages of `chainer`. For example, `chainer.Variable` is a shortcut of `chainer.variable.Variable`. It is not allowed to use such shortcuts in the "`chainer`" library implementation. Note that you can still use them in `tests` and `examples` directories.

Once you send a pull request, your coding style is automatically checked by Travis-CI. The reviewing process starts after the check passes.

### 3.5 Testing Guidelines

Testing is one of the most important part of your code. You must test your code by unit tests following our testing guidelines.

We are using `nose` package to run unit tests. You can run unit tests simply by running `nosetests` command under the repository root. It requires CUDA by default. In order to run unit tests that do not require CUDA, pass `--attr='!gpu'` option to the `nosetests` command:

```bash
$ nosetests path/to/your/test.py --attr='!gpu'
```

Tests are put into the `tests` directory. This directory has the same structure as the `chainer` directory. In order to enable test runner to find test scripts correctly, we are using special naming convention for the test subdirectories and the test scripts.

- The name of each subdirectory of `tests` must end with the `_tests` suffix.
- The name of each test script must start with the `test_` prefix.

Following this naming convention, you can run all the tests by just typing `nosetests` at the repository root:

```bash
$ nosetests
```

If you modify the code related to existing unit tests, you must run this command.

There are many examples of unit tests under the `tests` directory. They simply use the `unittest` package of the standard library.

If your patch includes GPU-related code, your tests must run with and without GPU capability. Test functions that requires CUDA must be tagged by the `chainer.testing.attr.gpu` decorator:

```python
import unittest
from chainer.testing import attr

class TestMyFunc(unittest.TestCase):
    ...
```
The functions tagged by the `chainer.testing.attr.gpu` decorator are skipped if --attr=!gpu is given.

We also have the `chainer.testing.attr.cudnn` decorator to let nosetests know that the test depends on CuDNN.

Once you send a pull request, your code is automatically tested by Travis-CI with --attr=!gpu option. Since Travis-CI does not support CUDA, we cannot check your CUDA-related code automatically. The reviewing process starts after the test passes. Note that reviewers will test your code without the option to check CUDA-related code.
Tips and FAQs

4.1 Installation

4.1.1 I cannot install pycuda

You need to set `PATH` to CUDA bin path if you get the error below when you use `pip install chainer-cuda-deps`:

```
src/cpp/cuda.hpp:14:18: fatal error: cuda.h: No such file or directory
 #include <cuda.h>
 ^
compilation terminated.
error: command 'x86_64-linux-gnu-gcc' failed with exit status 1
```

Chainer-cuda-deps only installs pycuda and other dependent libraries. In `setup.py` of pycuda, it checks the path of `nvcc` command and guesses the path of CUDA (https://github.com/inducer/pycuda/blob/v2015.1.2/setup.py#L30). If `setup.py` couldn’t find CUDA, it causes an error like that.

Please try to set `PATH` before `pip install chainer-cuda-deps`. If you use NVIDIA’s official installer, `nvcc` command is located at `/usr/local/cuda/bin`:

```
$ export PATH=/usr/local/cuda/bin:$PATH
$ pip install chainer-cuda-deps
```

4.1.2 I cannot install pycuda with `sudo`

`sudo` changes `PATH` environment variable for security. You need to set `PATH` inside `sudo`. For example use `sh` command:

```
$ sudo sh -c "PATH=/usr/local/cuda/bin:\$PATH pip install chainer-cuda-deps"
```

Or, install as a root user:

```
$ su - root
% export PATH=/usr/local/cuda/bin:$PATH
% pip install chainer-cuda-deps
```

We recommend to install Chainer in your local environment with `--user` option if possible. You don’t need to use `sudo` in this case:
You can also use `pyenv` to create your local environment.
Comparison with Other Frameworks

5.1 A table for quick comparison

This table compares Chainer with other popular deep learning frameworks. We hope it helps you to choose an appropriate framework for the demand.

Note: This chart may be out-dated, since the developers of Chainer do not perfectly follow the latest development status of each framework. Please report us if you find an out-dated cell. Requests for new comparison axes are also welcome.
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### 5.2 Benchmarks

We are preparing for the benchmarks.

---

¹We are preparing for changing the GPU array backend to CuPy. It enables us to write one code for both CPU and GPU arrays.
²They are also developing libgpuarray
³Stateful RNN is a type of RNN implementation that maintains states in the loops. It should enable us to use the states arbitrarily to update them.
⁴This row shows whether each array API supports unified codes for CPU and GPU.
⁵The array backend of Theano does not have compatible interface with NumPy, though most users write code on theano variables, which is generic for CPU and GPU.
⁶Depending on the frameworks.
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