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# Zcode Documentation

*Release*

**Thierry Dumont**

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### 1.1 Node definition

```
template <std::size_t Dim, typename value_type = std::size_t>
struct definitions
```

#### Public Static Attributes

```
const int size = sizeof(value_type)*8
    size of Node in digits.

const int nbfreebits = 5
    number of freebits used for MR.

const int nblevelbits = max_level(dim, nbfreebits, size)
    number of digit for level.

const int nlevels = (size-nbfreebits-nblevelbits)/dim
    max number of tree levels.

const int treetype = 1<<dim
    bin (1d), quad(2d), octo (3d) trees.

const int nfakes = 2*dim
    number of faces of each element

const int nbgef = 1<<(dim-1)
    number of elements when you refine once on each face (1d: 1, 2d: 2, 3d: 4).

const int nbd = ipow(2, dim) << dim
    number max of bound. elements (1d: 2, 2d: 12, 3d: 56).

const int levelshift = size-nblevelbits
    amount of right shift needed to get level in the tree.
```

```
constexpr value_type levelone = one<<levelshift
    first digit marking levels:  

const value_type levelmask = AllSet2One<dim, nlevelbits, value_type>::value
    mask for extracting level:  

const value_type levelzone = (levelmask)<<levelshift
    mask the part used to store level  

constexpr value_type maskpos = AllSet2One<dim, dim*nlevels, value_type>::value
    mask for what is used for position:  

const int nbneighb = ipow(3, dim)
    how many neighbors for one Node (including itself).  

const value_type Xbit = one<<(dim*nlevels-1)
    bits used in nodes computations (Zbit not used -2d problem!-)
        leftmost digit for x position  

const value_type Ybit = (dim==1)? 0: (Xbit>>1)
        leftmost digit for y position  

const value_type Zbit = (dim==3)? (Xbit>>2): 0
        ! not used (for compatibility with the 3-d case).  

const value_type IntOne = one
        ! 1!  

const value_type AllExceptVoidbit = allone - voidbit
    mask for extracting all, but the void bit:
```

## 1.2 Node class

```
template <std::size_t Dim, typename Value = std::size_t>
struct Node  
Inherits from definitions<Dim, Value>
```

### Public Functions

```
bool is_max(direction d) const
    test if the node as max coordinate
```

#### Parameters

- *d*: the direction.

```
bool is_min(direction d) const
    test if the node as min coordinate
```

#### Parameters

- *d*: direction.

```
std::size_t lastlevel() const
    get the last level digits of a node in an int (flushed right).
```

**Note** this can be applied to hashed and non hashed Nodes.

#### Parameters

- node:

`bool is_minimal() const`

is a `Node` minimal (ie has minimal abscissa) in his set of Brothers?

`void setTags(Node &n) const`

set the tag part of a `Node`

**Note** we do not check V.

#### Parameters

- N: pointer to the `Node`.
- V: tag value

`Node hash() const`

return the hash code for nodes.

**Note** we do not test if x is already hashed, except if DEBUG is set.

#### Parameters

- x: `Node`

`Node unhash() const`

For a given hasehd representation of a `Node`, we return the non hashed representation.

#### Parameters

- x: `Node`

`bool isHashed() const`

Is a node hashed?

## 1.3 Node family

### Functions

`template <std::size_t dim, typename value_type>`

`Node<dim, value_type> firstSon(Node<dim, value_type> const &node)`

return the son of a `Node` which has the smallest abssissa (ie, the 1rst one in the son's brotherhood).

**Note** we return a non hashed `Node`.

#### Parameters

- u: `Node`.

`template <typename Node_type>`

`Node_type lastSon(Node_type const &node)`

return the son of a `Node` which has the largestlest abssissa (ie, the last one in the son's brotherhood).

**Note** we return a non hashed `Node`.

**Parameters**

- u: *Node*.

```
template <typename Node_type>
Node_type father(Node_type const &node)
    compute the father of a node
```

**Parameters**

- node: node.

```
template <typename Node_type>
bool isAncestor(Node_type A, Node_type X)
    test if a Node A is an ancestor of a Node X.
```

**Note** each *Node* is its own ancestor, too.

**Parameters**

- A: *Node*
- X: *Node*

```
template <typename Node_type>
bool shareAncestor(Node_type A, Node_type B, std::size_t lv)
    Do 2 Nodes share the same ancestor of a given level ?
```

**Parameters**

- A: *Node*
- B: *Node*
- lv: the level.

```
template <typename Node_type, typename Node_array>
void brothers_impl(Node_type const &node, Node_array &Brothers, std::integral_constant<std::size_t,
    1>)
template <typename Node_type, typename Node_array>
void brothers_impl(Node_type const &node, Node_array &Brothers, std::integral_constant<std::size_t,
    2>)
template <typename Node_type, typename Node_array>
void brothers_impl(Node_type const &node, Node_array &Brothers, std::integral_constant<std::size_t,
    3>)
template <typename Node_type, typename Node_array>
void brothers(Node_type const &node, Node_array &Brothers)
```

Make the list of the brothers of a minimal node in a brothers set.

**Note** node *must* be minimal in his brothers set. *NOT TESTED*, except if DEBUG is set.

**Note** Brothers[0] == node.

**Note** the output array Brothers is ordered.

**Parameters**

- node: the node for which we build the list.
- Brothers: the list of brothers.

## 1.4 Node neighbors

### Functions

```

template <typename Node_type, std::size_t nx>
void neighbors (Node_type const &node, std::array<Node_type, nx> &node_array, std::array<int, nx>
                const &stencilx)
template <typename Node_type, std::size_t nx, std::size_t ny>
void neighbors (Node_type const &node, std::array<Node_type, nx *ny> &node_array, std::array<int, nx>
                const &stencilx, std::array<int, ny> const &stencily)
template <typename Node_type, std::size_t ns>
void neighbors (Node_type const &node, std::array<Node_type, ns> &node_array,
                std::array<std::array<int, 2>, ns> const &stencil)
template <typename Node_type, std::size_t ns>
void neighbors (Node_type const &node, std::array<Node_type, ns> &node_array,
                std::array<std::array<int, 3>, ns> const &stencil)
template <typename Node_type, std::size_t nx, std::size_t ny, std::size_t nz>
void neighbors (Node_type const &node, std::array<Node_type, nx *ny *nz> &node_array,
                std::array<int, nx> const &stencilx, std::array<int, ny> const &stencily, std::array<int, nz> const &stencilz)
template <std::size_t stencil, typename Node_type, typename Node_array>
void boxNeighbors_impl (Node_type const &n, Node_array &node_array,
                      std::integral_constant<std::size_t, 1>)
template <std::size_t stencil, typename Node_type, typename Node_array>
void boxNeighbors_impl (Node_type const &n, Node_array &node_array,
                      std::integral_constant<std::size_t, 2>)
template <std::size_t stencil, typename Node_type, typename Node_array>
void boxNeighbors_impl (Node_type const &n, Node_array &node_array,
                      std::integral_constant<std::size_t, 3>)
template <std::size_t stencil, typename Node_type, typename Node_array>
void boxNeighbors (Node_type const &n, Node_array &node_array)
    find a potential neighbor, depending on the position of u.

```

### Parameters

- u: node.
- P []: returned list(vector)

```

template <int stencil, typename Node_type, typename Node_array>
void starNeighbors_impl (Node_type const &n, Node_array &node_array,
                      std::integral_constant<std::size_t, 1>)
template <int stencil, typename Node_type, typename Node_array>
void starNeighbors_impl (Node_type const &n, Node_array &node_array,
                      std::integral_constant<std::size_t, 2>)
template <int stencil, typename Node_type, typename Node_array>
void starNeighbors_impl (Node_type const &n, Node_array &node_array,
                      std::integral_constant<std::size_t, 3>)
template <int stencil, typename Node_type, typename Node_array>
void starNeighbors (Node_type const &n, Node_array &node_array)
    find a potential neighbor, depending on the position of u.

```

### Parameters

- u: node.
- P []: returned list(vector)

## 1.5 Node refinement

### Functions

```
template <typename Node_type, typename Node_array>
void refine (Node_type const &n, Node_array &refined)
    refine n.
```

Results in refined[0: treetype-1].

### Parameters

- n: node.
- refined [ ]: the refined nodes.

# CHAPTER 2

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slot

---

```
template <std::size_t dim, typename node_value_type = std::size_t>
struct slot
```

slot structure, used to store Nodes with a hash code in an interval.

slot structures, store a set of Nodes.

Inherits from std::vector< Node< dim, node\_value\_type > >

## Public Functions

```
auto find(node_type const &node)
    find a Node.
```

**Note** we do not check if x is hashed.

### Parameters

- x: *Node* hashed

```
void put(node_type x)
    put a Node at the end.
```

### Parameters

- x: a *hashed* node (not checked).

```
template <typename container>
void put(container const &x)
    put a vector of Node's at the end.
```

### Parameters

- x: vector of *hashed* nodes (not checked).

```
int lastPos () const
    position of the last entered Node in v[]

void compress (node_type N = node_type::voidbit)
    compress: ie, supress void Nodes with a given value
```

#### Parameters

- *N*: supress nodes for which *N*&node !=0

```
void compressany ()
    compress all marked Nodes.

    ie, supress Nodes with any value in the FreeBitsPart or marked as void

void compress (node_type N, node_type M)
    compress: ie, supress void Nodes with given values
```

**Note** a *Node* *K* are supressed iff *K*&*N*==*N* or *K*&*M*==*M*

#### Parameters

- *N*: test value
- *M*: test value

```
void setMark (node_type N)
    mark the slot with some value.
```

#### Parameters

- *N*: associated value.

```
unsigned char getMark ()
    get the mark tag.
```

```
void unsetMark (node_type N)
    suppress a given mark
```

**Note** throw an exception if not marked “mark”.

#### Parameters

- *N*: the mark

```
bool markedOther (node_type mark)
    test if the slot has been marked by an other mark as “mark”
```

#### Parameters

- *mark*: for the test.

```
bool hasvoidNodes () const
    does this slot contains void Nodes ?
```

```
void sethasvoidNodes ()
    mark the slot as containing void Nodes.
```

---

void **And** (node\_type *N*)  
make a logical “and” of all Nodes with a given value.

**Parameters**

- *N*: the value.

void **setTag** (node\_type *N*)  
Tag, ie add some value to all Nodes.

**Note** a “and” with the value must be zero. Not tested if DEBUG is not set. We do not want to set a value to Nodes, but to tag them.

**Parameters**

- *N*: the value.

void **empty** ()  
empty the slot. Do not change s1 and s2, do not deallocate space.

auto **cut** (std::size\_t **const** *nc*)  
cut the slot in *nc* slots.

**Note** sizes of the resulting slots are not garanted to be equal.

**Parameters**

- *nc*: number of slots
- *s*: result. Array of *nc* slot\*.

auto **cutBefore** (std::size\_t *pos*, node\_type *s2new*)  
cut this slot in 2 slots, at position *pos*, and then shrink it.

the returned slot is the first part containing v[0,*pos*[

**Note** we do not check that *pos* is correct, except if DEBUG is set.

**Note** for *s2new*: position part only; tested only if DEBUG set.

**Parameters**

- *pos*:
- *s2new*: value for *s2* of the *new* slot, and *s1* of this slot.

void **fusion** (**const** *slot* &*s1*)  
fusion this slot with slot *s1*

**Parameters**

- *s1*: slot.

void **sort** ()  
sort by hash function.

bool **cutdown** (std::size\_t *lim* = 2)  
reallocate to reduce size;

**Note** return True iff slot is reduced.

### Parameters

- `lim`: we reduce size if `allocsize/size >= lim`

`void forgetFreeBits()`  
suppress all bits used to mark something (except voidbit).

`void uniq()`  
suppress ex-aquo.

**Note** slot must be sorted (tested only if DEBUG is set).

`bool testWellFormed(bool throwexept = true) const`  
test if all nodes have their abscissa between s1 and s2.

### Parameters

- `throwexept`: throw an exception if true.

`bool exaequo() const`  
look for ex-aquo

`void setStartRank(std::size_t r)`  
set starrank

### Parameters

- `r`:

`int slotrank() const`  
return slotrank.

`void setSlotrank(std::size_t r)`  
set the slot rank

### Parameters

- `r`:

`void dump(std::ofstream &f)`  
Write slot to a file, already open.  
\_param f the file.

`void restore(std::ifstream &f)`  
restore a slot from a dump.

### Parameters

- `file`: the file to restore from.

# CHAPTER 3

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## slotCollection

---

```
template <std::size_t dim, typename node_value_type>
struct slotCollection
Inherits from std::vector< std::shared_ptr< slot< dim, node_value_type > >>
```

### Public Functions

```
void copyInArray (std::vector<node_type> &array)
An other “copy init”.
```

Here we put the Nodes of each slot in a global array. This is supposed to reduce the number of allocations.  
We use this to store a local copy of a SlotCollection.

#### Parameters

- SC: slot collection to be copied.
- G: global array.

```
void clone (const slotCollection &C)
make a “clone”, ie copy all, but not the Nodes!
```

```
bool inInterval (node_type s1, node_type s2, node_type x) const
Is a Node abscissa in the interval [s1,s2[ ?
```

**Note** x must be *not* hashed.

#### Parameters

- s1:
- s2:
- x: *Node* to check.

```
void insert (node_type x, Cache<dim, node_value_type> &cache)
Store one node using a cache.
```

### Parameters

- x: the node to be inserted.
- cache: an external Cache.

void **insert** (node\_type *x*)

Store one node.

### Parameters

- x: the node to be inserted.

std::size\_t **nbNodes** () **const**

number of Nodes stored.

level\_count\_type **nbNodesByLevel** () **const**

Returns the number of nodes by level.

auto **ubound** (node\_type *x*) **const**

return a pointer to a slot which *possibly* contains a *Node*.

### Parameters

- x: *Node* not hashed

auto **ubound\_hashed** (node\_type *x*) **const**

return a pointer to a slot which *possibly* contains a *Node*.

### Parameters

- x: *Node* hashed

std::size\_t **findSlot** (node\_type *N*, std::size\_t *left*, std::size\_t *right*) **const**

Given a *Node*, find his slot.

**Note** we search in range [left,right] of the SlotCollection

**Note** returns the rank of the slot which contains N

### Parameters

- N: the *Node*
- left:
- right:

std::size\_t **count** (node\_type *x*, Cache<dim, node\_value\_type> &*cache*) **const**

Test if a *Node* exists within this *slotCollection*, using a cache.

**Return** the number of corresponding found node (either 0 or 1).

**Note** we do not directly check if the *Node* is really non hashed, but this is checked in “*xh=hash(x)*”.

### Parameters

- x: *Node* non hashed.
- cach: cache updated.

---

`std::size_t count (node_type x) const`  
 Test if a *Node* exists within this *slotCollection*.

**Return** the number of corresponding found node (either 0 or 1).

**Note** we do not directly check if the *Node* is really non hashed, but this is checked in “*xh=hash(x)*”.

#### Parameters

- *x*: *Node* non hashed.

`void forgetFreeBits ()`  
 remove all free bits from all nodes.

`void compress (node_type val = node_type::voidbit)`  
 suppress void Nodes, if any.  
 update the count of leaves.

`void clear ()`  
 empty all the slots.

`void makeExtern (SetNode &setN)`  
 make a copy (in a set) of the Nodes.

#### Parameters

- *setN*: the set.

`void finalize ()`  
 finalize: compute cumulsize (to allow rank function to work), and maximum size of slots;

`void relink ()`  
 compute ranks, ...

`std::size_t maxSlotSize () const`  
 return maximum size of slots.

### Public Members

`std::size_t slot_max_size`  
 size of slot which triggers decomposition of a slot.

`std::size_t slot_min_size`  
 size of slot which triggers fusion of two slots.

`struct ltNode`  
 define order on the Nodes.

We use the Peano-Hilbert curve for indexation, and thus, we must suppress all what is not position.



# CHAPTER 4

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## Indices and tables

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## Index

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