# pymuvr Documentation 

Release 1.3.3

## Eugenio Piasini

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## Author Eugenio Piasini

Contact e.piasini@ucl.ac.uk
Documentation http://pymuvr.readthedocs.org
Source code https://github.com/epiasini/pymuvr
PyPI entry https://pypi.python.org/pypi/pymuvr
A Python package for the fast calculation of Multi-unit Van Rossum neural spike train metrics, with the kernelbased algorithm described in Houghton and Kreuz, On the efficient calculation of Van Rossum distances (Network: Computation in Neural Systems, 2012, 23, 48-58). This package started out as a Python wrapping of the original C++ implementation given by the authors of the paper, and evolved from there with bugfixes and improvements.

## Contents

### 1.1 Installation

### 1.1.1 Requirements

- CPython 2.7 or 3.x.
- NumPy>=1.7.
- C++ development tools and Standard Library (package build-essential on Debian).
- Python development tools (package python-dev on Debian).


### 1.1.2 Installing via pip

To install the latest release, run:

```
pip install pymuvr
```


### 1.1.3 Testing

From the root directory of the source distribution, run:

```
python setup.py test
```

(requires setuptools). Alternatively, if pymuvr is already installed on your system, look for the copy of the test_pymuvr.py script installed alongside the rest of the pymuvr files and execute it. For example:

```
python /usr/lib/pythonX.Y/site-packages/pymuvr/test/test_pymuvr.py
```


### 1.2 Mathematical methods

We define a compact formalism for multiunit spike-train metrics by opportunely characterising the space of multiunit feature vectors as a tensor product. Previous results from Houghton and Kreuz (2012, On the efficient calculation of van Rossum distances. Network: Computation in Neural Systems, 2012, 23, 48-58) on a clever formula for multiunit Van Rossum metrics are then re-derived within this framework, also fixing some errors in the original calculations.

### 1.2.1 A compact formalism for kernel-based multiunit spike train metrics

Consider a network with $C$ cells. Let

$$
\mathcal{U}=\left\{\boldsymbol{u}^{1}, \boldsymbol{u}^{2}, \ldots, \boldsymbol{u}^{C}\right\}
$$

be an observation of network activity, where

$$
\boldsymbol{u}^{i}=\left\{u_{1}^{i}, u_{2}^{i}, \ldots, u_{N_{u^{i}}}^{i}\right\}
$$

is the (ordered) set of times of the spikes emitted by cell $i$. Let $\mathcal{V}=\left\{\boldsymbol{v}^{1}, \boldsymbol{v}^{2}, \ldots, \boldsymbol{v}^{C}\right\}$ be another observation, different in general from $\mathcal{U}$.
To compute a kernel based multiunit distance between $\mathcal{U}$ and $\mathcal{V}$, we map them to the tensor product space $\mathcal{S} \doteq$ $\mathbb{R}^{C} \otimes L_{2}(\mathbb{R} \rightarrow \mathbb{R})$ by defining

$$
|\mathcal{U}\rangle=\sum_{i=1}^{C}|i\rangle \otimes\left|\boldsymbol{u}^{i}\right\rangle
$$

where we consider $\mathbb{R}^{C}$ and $L_{2}(\mathbb{R} \rightarrow \mathbb{R})$ to be equipped with the usual euclidean distances, consequently inducing an euclidean metric structure on $\mathcal{S}$ too.
Conceptually, the set of vectors $\{|i\rangle\}_{i=1}^{C} \subset \mathbb{R}^{C}$ represents the different cells, while each $\left|\boldsymbol{u}^{i}\right\rangle \in L_{2}(\mathbb{R} \rightarrow \mathbb{R})$ represents the convolution of a spike train of cell $i$ with a real-valued feature function $\phi: \mathbb{R} \rightarrow \mathbb{R}$,

$$
\langle t \mid \boldsymbol{u}\rangle=\sum_{n=1}^{N_{u}} \phi\left(t-u_{n}\right)
$$

In practice, we will never use the feature functions directly, but we will be only interested in the inner products of the $|i\rangle$ and $|\boldsymbol{u}\rangle$ vectors. We call $c_{i j} \doteq\langle i \mid j\rangle=\langle i \mid j\rangle_{\mathbb{R}^{C}}=c_{j i}$ the multiunit mixing coefficient for cells $i$ and $j$, and $\langle\boldsymbol{u} \mid \boldsymbol{v}\rangle=\langle\boldsymbol{u} \mid \boldsymbol{v}\rangle_{L_{2}}$ the single-unit inner product,

$$
\begin{aligned}
\langle\boldsymbol{u} \mid \boldsymbol{v}\rangle & =\left\langle\left\{u_{1}, u_{2}, \ldots, u_{N}\right\} \mid\left\{v_{1}, v_{2}, \ldots, v_{M}\right\}\right\rangle= \\
& =\int \mathrm{d} t\langle\boldsymbol{u} \mid t\rangle\langle t \mid \boldsymbol{v}\rangle=\int \mathrm{d} t \sum_{n=1}^{N} \sum_{m=1}^{M} \phi\left(t-u_{n}\right) \phi\left(t-v_{m}\right) \\
& \doteq \sum_{n=1}^{N} \sum_{m=1}^{M} \mathcal{K}\left(u_{n}, v_{m}\right)
\end{aligned}
$$

where $\mathcal{K}\left(t_{1}, t_{2}\right) \doteq \int \mathrm{d} t\left[\phi\left(t-t_{1}\right) \phi\left(t-t_{2}\right)\right]$ is the single-unit metric kernel, and where we have used the fact that the feature function $\phi$ is real-valued. It follows immediately from the definition above that $\langle\boldsymbol{u} \mid \boldsymbol{v}\rangle=\langle\boldsymbol{v} \mid \boldsymbol{u}\rangle$.
Note that, given a cell pair $(i, j)$ or a spike train pair $(\boldsymbol{u}, \boldsymbol{v}), c_{i j}$ does not depend on spike times and $\langle\boldsymbol{u} \mid \boldsymbol{v}\rangle$ does not depend on cell labeling.
With this notation, we can define the multi-unit spike train distance as

$$
\||\mathcal{U}\rangle-|\mathcal{V}\rangle \|^{2}=\langle\mathcal{U} \mid \mathcal{U}\rangle+\langle\mathcal{V} \mid \mathcal{V}\rangle-2\langle\mathcal{U} \mid \mathcal{V}\rangle
$$

where the multi-unit spike train inner product $\langle\mathcal{V} \mid \mathcal{U}\rangle$ between $\mathcal{U}$ and $\mathcal{V}$ is just the natural bilinear operation induced on $\mathcal{S}$ by the tensor product structure:

$$
\begin{aligned}
\langle\mathcal{V} \mid \mathcal{U}\rangle & =\sum_{i, j=1}^{C}\langle i \mid j\rangle\left\langle\boldsymbol{v}^{i} \mid \boldsymbol{u}^{j}\right\rangle=\sum_{i, j=1}^{C} c_{i j}\left\langle\boldsymbol{v}^{i} \mid \boldsymbol{u}^{i}\right\rangle \\
& =\sum_{i=1}^{C}\left[c_{i i}\left\langle\boldsymbol{v}^{i} \mid \boldsymbol{u}^{i}\right\rangle+c_{i j}\left(\sum_{j<i}\left\langle\boldsymbol{v}^{i} \mid \boldsymbol{u}^{j}\right\rangle+\sum_{j>i}\left\langle\boldsymbol{v}^{i} \mid \boldsymbol{u}^{j}\right\rangle\right)\right]
\end{aligned}
$$

But $c_{i j}=c_{j i}$ and $\langle\boldsymbol{v} \mid \boldsymbol{u}\rangle=\langle\boldsymbol{u} \mid \boldsymbol{v}\rangle$, so

$$
\begin{aligned}
\sum_{i=1}^{C} \sum_{j<i} c_{i j}\left\langle\boldsymbol{v}^{i} \mid \boldsymbol{u}^{j}\right\rangle & =\sum_{j=1}^{C} \sum_{i<j} c_{j i}\left\langle\boldsymbol{v}^{j} \mid \boldsymbol{u}^{i}\right\rangle=\sum_{i=1}^{C} \sum_{j>i} c_{j i}\left\langle\boldsymbol{v}^{j} \mid \boldsymbol{u}^{i}\right\rangle=\sum_{i=1}^{C} \sum_{j>i} c_{i j}\left\langle\boldsymbol{v}^{j} \mid \boldsymbol{u}^{i}\right\rangle \\
& =\sum_{i=1}^{C} \sum_{j>i} c_{i j}\left\langle\boldsymbol{u}^{i} \mid \boldsymbol{v}^{j}\right\rangle
\end{aligned}
$$

and

$$
\langle\mathcal{V} \mid \mathcal{U}\rangle=\sum_{i=1}^{C}\left[c_{i i}\left\langle\boldsymbol{v}^{i} \mid \boldsymbol{u}^{i}\right\rangle+c_{i j} \sum_{j>i}\left(\left\langle\boldsymbol{v}^{i} \mid \boldsymbol{u}^{j}\right\rangle+\left\langle\boldsymbol{u}^{i} \mid \boldsymbol{v}^{j}\right\rangle\right)\right]
$$

Now, normally we are interested in the particular case where $c_{i j}$ is the same for all pair of distinct cells:

$$
c_{i j}= \begin{cases}1 & \text { if } i=j \\ c & \text { if } i \neq j\end{cases}
$$

and under this assumption we can write

$$
\langle\mathcal{V} \mid \mathcal{U}\rangle=\sum_{i=1}^{C}\left[\left\langle\boldsymbol{v}^{i} \mid \boldsymbol{u}^{i}\right\rangle+c \sum_{j>i}\left(\left\langle\boldsymbol{v}^{i} \mid \boldsymbol{u}^{j}\right\rangle+\left\langle\boldsymbol{u}^{i} \mid \boldsymbol{v}^{j}\right\rangle\right)\right]
$$

and

$$
\begin{aligned}
\||\mathcal{U}\rangle-|\mathcal{V}\rangle \|^{2}=\sum_{i=1}^{C} & \left\{\left\langle\boldsymbol{u}^{i} \mid \boldsymbol{u}^{i}\right\rangle+c \sum_{j>i}\left(\left\langle\boldsymbol{u}^{i} \mid \boldsymbol{u}^{j}\right\rangle+\left\langle\boldsymbol{u}^{i} \mid \boldsymbol{u}^{j}\right\rangle\right)+\right. \\
& +\left\langle\boldsymbol{v}^{i} \mid \boldsymbol{v}^{i}\right\rangle+c \sum_{j>i}\left(\left\langle\boldsymbol{v}^{i} \mid \boldsymbol{v}^{j}\right\rangle+\left\langle\boldsymbol{v}^{i} \mid \boldsymbol{v}^{j}\right\rangle\right)+ \\
& \left.-2\left[\left\langle\boldsymbol{v}^{i} \mid \boldsymbol{u}^{i}\right\rangle+c \sum_{j>i}\left(\left\langle\boldsymbol{v}^{i} \mid \boldsymbol{u}^{j}\right\rangle+\left\langle\boldsymbol{u}^{i} \mid \boldsymbol{v}^{j}\right\rangle\right)\right]\right\}
\end{aligned}
$$

Rearranging the terms

$$
\begin{aligned}
& \||\mathcal{U}\rangle-|\mathcal{V}\rangle \|^{2}=\sum_{i=1}^{C}\left[\left\langle\boldsymbol{u}^{i} \mid \boldsymbol{u}^{i}\right\rangle+\left\langle\boldsymbol{v}^{i} \mid \boldsymbol{v}^{i}\right\rangle-2\left\langle\boldsymbol{v}^{i} \mid \boldsymbol{u}^{i}\right\rangle+\right. \\
& \left.+2 c \sum_{j>i}\left(\left\langle\boldsymbol{u}^{i} \mid \boldsymbol{u}^{j}\right\rangle+\left\langle\boldsymbol{v}^{i} \mid \boldsymbol{v}^{j}\right\rangle-\left\langle\boldsymbol{v}^{i} \mid \boldsymbol{u}^{j}\right\rangle-\left\langle\boldsymbol{v}^{j} \mid \boldsymbol{u}^{i}\right\rangle\right)\right]
\end{aligned}
$$

### 1.2.2 Van Rossum-like metrics

In Van Rossum-like metrics, the feature function and the single-unit kernel are, for $\tau \neq 0$,

$$
\begin{gathered}
\phi_{\tau}^{\mathrm{VR}}(t)=\sqrt{\frac{2}{\tau}} \cdot e^{-t / \tau} \theta(t) \\
\mathcal{K}_{\tau}^{\mathrm{VR}}\left(t_{1}, t_{2}\right)= \begin{cases}1 & \text { if } t_{1}=t_{2} \\
e^{-\left|t_{1}-t_{2}\right| / \tau} & \text { if } t_{1} \neq t_{2}\end{cases}
\end{gathered}
$$

where $\theta$ is the Heaviside step function (with $\theta(0)=1$ ), and we have chosen to normalise $\phi_{\tau}^{\mathrm{VR}}$ so that

$$
\left\|\phi_{\tau}^{\mathrm{VR}}\right\|_{2}=\sqrt{\int \mathrm{d} t\left[\phi_{\tau}^{\mathrm{VR}}(t)\right]^{2}}=1
$$

In the $\tau \rightarrow 0$ limit,

$$
\begin{gathered}
\phi_{0}^{\mathrm{VR}}(t)=\delta(t) \\
\mathcal{K}_{0}^{\mathrm{VR}}\left(t_{1}, t_{2}\right)= \begin{cases}1 & \text { if } t_{1}=t_{2} \\
0 & \text { if } t_{1} \neq t_{2}\end{cases}
\end{gathered}
$$

In particular, the single-unit inner product now becomes

$$
\langle\boldsymbol{u} \mid \boldsymbol{v}\rangle=\sum_{n=1}^{N} \sum_{m=1}^{M} \mathcal{K}^{\mathrm{VR}}\left(u_{n}, v_{m}\right)=\sum_{n=1}^{N} \sum_{m=1}^{M} e^{-\left|u_{n}-v_{m}\right| / \tau}
$$

## Markage formulas

For a spike train $\boldsymbol{u}$ of length $N$ and a time $t$ we define the index $\tilde{N}(\boldsymbol{u}, t)$

$$
\tilde{N}(\boldsymbol{u}, t) \doteq \max \left\{n \mid u_{n}<t\right\}
$$

which we can use to re-write $\langle\boldsymbol{u} \mid \boldsymbol{u}\rangle$ without the absolute values:

$$
\begin{aligned}
\langle\boldsymbol{u} \mid \boldsymbol{u}\rangle= & \sum_{n=1}^{N}\left(\sum_{m \mid v_{m}<u_{n}} e^{-\left(u_{n}-v_{m}\right) / \tau}+\sum_{m \mid v_{m}>u_{n}} e^{-\left(v_{m}-u_{n}\right) / \tau}+\sum_{m=1}^{M} \delta\left(u_{n}, v_{m}\right)\right) \\
= & \sum_{n=1}^{N}\left(\sum_{m \mid v_{m}<u_{n}} e^{-\left(u_{n}-v_{m}\right) / \tau}+\sum_{m \mid u_{m}<v_{n}} e^{-\left(v_{n}-u_{m}\right) / \tau}+\sum_{m=1}^{M} \delta\left(u_{n}, v_{m}\right)\right) \\
= & \sum_{n=1}^{N}\left[\sum_{m=1}^{\tilde{N}\left(\boldsymbol{v}, u_{n}\right)} e^{-\left(u_{n}-v_{m}\right) / \tau}+\sum_{m=1}^{\tilde{N}\left(\boldsymbol{u}, v_{n}\right)} e^{-\left(v_{n}-u_{m}\right) / \tau}+\delta\left(u_{n}, v_{\tilde{N}\left(\boldsymbol{v}, u_{n}\right)+1}\right)\right] \\
= & \sum_{n=1}^{N}\left[e^{-\left(u_{n}-v_{\tilde{N}\left(v, u_{n}\right)}\right) / \tau} \sum_{m=1}^{\tilde{N}\left(\boldsymbol{v}, u_{n}\right)} e^{-\left(v_{\tilde{N}\left(v, u_{n}\right)}-v_{m}\right) / \tau}+\right. \\
& +e^{-\left(v_{n}-u_{\tilde{N}\left(u, v_{n}\right) / \tau} \tilde{\tilde{N}\left(\boldsymbol{u}, v_{n}\right)} \sum_{m=1}^{-\left(u_{\tilde{N}\left(u, v_{n}\right)}-u_{m}\right) / \tau}+\right.} \\
& \left.+\delta\left(u_{n}, v_{\tilde{N}\left(\boldsymbol{v}, u_{n}\right)+1}\right)\right]
\end{aligned}
$$

For a spike train $\boldsymbol{u}$ of length $N$, we also define the the markage vector $\boldsymbol{m}$, with the same length as $\boldsymbol{u}$, through the following recursive assignment:

$$
\begin{aligned}
& m_{1}(\boldsymbol{u}) \doteq 0 \\
& m_{n}(\boldsymbol{u}) \doteq\left(m_{n-1}+1\right) e^{-\left(u_{n}-u_{n-1}\right) / \tau} \quad \forall n \in\{2, \ldots, N\}
\end{aligned}
$$

It is easy to see that

$$
\begin{aligned}
m_{n}(\boldsymbol{u}) & =\sum_{k=1}^{n-1} e^{-\left(u_{n}-u_{k}\right) / \tau}=\left(\sum_{k=1}^{n} e^{-\left(u_{n}-u_{k}\right) / \tau}\right)-e^{-\left(u_{n}-u_{n}\right) / \tau} \\
& =\sum_{k=1}^{n} e^{-\left(u_{n}-u_{k}\right) / \tau}-1
\end{aligned}
$$

and in particular

$$
\sum_{n=1}^{\tilde{N}(\boldsymbol{u}, t)} e^{-\left(u_{\tilde{N}(\boldsymbol{u}, t)}-u_{n}\right) / \tau}=1+m_{\tilde{N}(\boldsymbol{u}, t)}(\boldsymbol{u})
$$

With this definition, we get

$$
\begin{aligned}
\langle\boldsymbol{u} \mid \boldsymbol{v}\rangle=\sum_{n=1}^{N} & {\left[e^{-\left(u_{n}-v_{\tilde{N}\left(\boldsymbol{v}, u_{n}\right)}\right) / \tau}\left(1+m_{\tilde{N}\left(\boldsymbol{v}, u_{n}\right)}(\boldsymbol{v})\right)+\right.} \\
& +e^{-\left(v_{n}-u_{\tilde{N}\left(\boldsymbol{u}, v_{n}\right)}\right) / \tau}\left(1+m_{\tilde{N}\left(\boldsymbol{u}, v_{n}\right)}(\boldsymbol{u})\right)+ \\
& \left.+\delta\left(u_{n}, v_{\tilde{N}\left(\boldsymbol{v}, u_{n}\right)+1}\right)\right]
\end{aligned}
$$

Finally, note that because of the definition of the markage vector

$$
e^{-\left(u_{n}-u_{\tilde{N}\left(\boldsymbol{u}, u_{n}\right)}\right) / \tau}\left(1+m_{\tilde{N}\left(\boldsymbol{u}, u_{n}\right)}(\boldsymbol{u})\right)=e^{-\left(u_{n}-u_{n-1}\right) / \tau}(1+m(\boldsymbol{u}))=m_{n}(\boldsymbol{u})
$$

so that in particular

$$
\langle\boldsymbol{u} \mid \boldsymbol{u}\rangle=\sum_{n=1}^{N}\left(1+2 m_{n}(\boldsymbol{u})\right)
$$

A formula for the efficient computation of multiunit Van Rossum spike train metrics, used by pymuvr, can then be obtained by opportunely substituting these expressions for the single-unit scalar products in the definition of the multiunit distance.

### 1.3 Usage

### 1.3.1 Examples

```
>>> import pymuvr
>>> # define two sets of observations for two cells
>>> observations_1 = [[[1.0, 2.3], # 1st observation, 1st cell
.. [0.2, 2.5, 2.7]], # 2nd cell
\cdots [[1.1, 1.2, 3.0], # 2nd observation
... []],
\cdots [[5.0, 7.8],
... [4.2, 6.0]]]
>>> observations_2 = [[[0.9],
    [0.7, 0.9, 3.3]],
    [[0.3, 1.5, 2.4],
    [2.5, 3.7]]]
>>> # set parameters for the metric
>>> cos=0.1
>>> tau = 1.0
>>> # compute distances between all observations in set I
>>> # and those in set 2
>>> pymuvr.dissimilarity_matrix(observations_1,
... observations_2,
... cos,
```

```
... tau,
... 'distance')
array([[ 2.40281585, 1.92780957],
    [ 2.76008964, 2.31230263],
    [ 3.1322069, 3.17216524]])
>>> # compute inner products
>>> pymuvr.dissimilarity_matrix(observations_1,
... observations_2,
... cos,
... tau,
... 'inner product')
array([[ 4.30817654, 5.97348384],
    [ 2.08532468, 3.85777053],
    [ 0.59639918, 1.10721323]])
>>> # compute all distances between observations in set 1
>>> pymuvr.square_dissimilarity_matrix(observations_1,
... cos,
... tau,
... 'distance')
array([[ 0. , 2.6221159 , 3.38230952],
    [ 2.6221159, 0. 3.10221811],
    [ 3.38230952, 3.10221811, 0. ]])
>>> # compute inner products
>>> pymuvr.square_dissimilarity_matrix(observations_1,
... cos,
... tau,
... 'inner product')
array([[ 8.04054275, 3.3022304 , 0.62735459],
    [ 3.3022304, 5.43940985, 0.23491838],
    [ 0.62735459, 0.23491838, 4.6541841 ]])
```

See the examples and test directories in the source distribution for more detailed examples of usage. These should also have been installed alongside the rest of the pymuvr files.
The script examples/benchmark_versus_spykeutils.py compares the performance of pymuvr with the pure Python/NumPy implementation of the multiunit Van Rossum distance in spykeutils.

### 1.3.2 Reference

pymuvr.dissimilarity_matrix(observationsl, observations2, cos, tau, mode)
Return the bipartite (rectangular) dissimilarity matrix between the observations in the first and the second list.

## Parameters

- observations1, observations2 (list) - Two lists of multi-unit spike trains to compare. Each observations parameter must be a thrice-nested list of spike times, with $o b$ servations $[i][j][k]$ representing the time of the kth spike of the jth cell of the ith observation.
- $\cos (f l o a t)$ - mixing parameter controlling the interpolation between labelled-line mode $(\cos =0)$ and summed-population mode ( $\cos =1$ ). It corresponds to the cosine of the angle between the vectors used for the euclidean embedding of the multiunit spike trains.
- tau (float) - time scale for the exponential kernel, controlling the interpolation between pure coincidence detection (tau=0) and spike count mode (very large tau). Note that setting tau $=0$ is always allowed, but there is a range ( 0 , epsilon) of forbidden values that tau is not allowed to assume. The upper bound of this range is proportional to the absolute value of the largest spike time in observations, with the proportionality constant being systemdependent. As a rule of thumb tau and the spike times should be within 4 orders of magni-
tude of each other; for example, if the largest spike time is 10 s a value of tau $>1 \mathrm{~ms}$ will be expected. An exception will be raised if tau falls in the forbidden range.
- mode (string) - type of dissimilarity measure to be computed. Must be either 'distance' or 'inner product'.
Returns A len(observations1) x len(observations2) numpy array containing the dissimilarity (distance or inner product) between each pair of observations that can be formed by taking one observation from observations 1 and one from observations 2.


## Return type numpy.ndarray

## Raises

- IndexError - if the observations in observations 1 and observations 2 don't have all the same number of cells.
- OverflowError - if tau falls in the forbidden interval.
pymuvr.square_dissimilarity_matrix (observations, cos, tau, mode)
Return the all-to-all (square) dissimilarity matrix for the given list of observations.


## Parameters

- observations (list) - A list of multi-unit spike trains to compare.
- $\boldsymbol{\operatorname { c o s }}(f l \circ a t)$ - mixing parameter controlling the interpolation between labelled-line mode ( $\cos =0$ ) and summed-population mode ( $\cos =1$ ).
- tau (float) - time scale for the exponential kernel, controlling the interpolation between pure coincidence detection (tau=0) and spike count mode (very large tau).
- mode (string) - type of dissimilarity measure to be computed. Must be either 'distance' or 'inner product'.

Returns A len(observations) x len(observations) numpy array containing the dissimilarity (distance or inner product) between all possible pairs of observations.

## Return type numpy.ndarray

## Raises

- IndexError - if the observations in observations don't have all the same number of cells.
- OverflowError - if tau falls in the forbidden interval.

Effectively equivalent to dissimilarity_matrix(observations, observations, cos, tau), but optimised for speed. See pymuvr.dissimilarity_matrix() for details.
pymuvr.distance_matrix (trains1, trains2, cos, tau)
Return the bipartite (rectangular) distance matrix between the observations in the first and the second list.
Convenience function; equivalent to dissimilarity_matrix(trains1, trains2, cos, tau,
"distance"). Refer to pymuvr. dissimilarity_matrix() for full documentation.
pymuvr.square_distance_matrix (trains, cos, tau)
Return the all-to-all (square) distance matrix for the given list of observations.
Convenience function; equivalent to square_dissimilarity_matrix(trains, cos, tau, "distance"). Refer to pymuvr.square_dissimilarity_matrix() for full documentation.

### 1.4 C++ API reference

## class ConvolvedSpikeTrain

A class representing a single-unit spike train for which several helper vectors relating to a Van Rossum-like exponential convolution have been calculated.

## Public Functions

```
ConvolvedSpikeTrain()
Default constructor.
ConvolvedSpikeTrain (std::vector<double> spikes, double tau)
Constructor accepting a spike train.
```


## Parameters

- spikes: A vector of spike times.
- tau: Time scale for the exponential kernel. There is a limit to how small tau can be compared to the absolute value of the spike times. An exception will be raised if this limit is exceeded; its value is system-dependent, but as a rule of thumb tau and the spike times should be within 4 orders of magnitude of each other.

| Warning: doxygenfunction: Unable to resolve multiple matches for function "distance" with arguments |
| :--- |
| (std::vector< std::vector< ConvolvedSpikeTrain $\gg \&$, double, double **) in doxygen xml output for project |
| "pymuvr" from directory:_doxygen/xml. Potential matches: |



Warning: doxygenfunction: Unable to resolve multiple matches for function "inner_product" with arguments (std::vector< std::vector< ConvolvedSpikeTrain $\gg \&$, double, double ${ }^{* *}$ ) in doxygen xml output for project "pymuvr" from directory: _doxygen/xml. Potential matches:

- void inner_product (std: : vector<std: : vector<ConvolvedSpikeTrain>>\&, double, double $*$ )
- void inner_product (std::vector<std::vector<ConvolvedSpikeTrain>>\&, std::vector<std: \{vector<Convol

Warning: doxygenfunction: Unable to resolve multiple matches for function "inner_product" with arguments (std::vector< std::vector< ConvolvedSpikeTrain \gg \& , std::vector< std::vector< ConvolvedSpikeTrain \gg \& , double, double ${ }^{* *}$ ) in doxygen xml output for project "pymuvr" from directory: _doxygen/xml. Potential matches:

```
- void inner_product(std::vector<std::vector<ConvolvedSpikeTrain>>&, double, double * f)
_ void inner_product(std::vector<std::vector<ConvolvedSpikeTrain>>&, std::vector<std:{vector<Convol
```


### 1.5 License

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### 1.6 Acknowledgements

This software has been developed at the Silver Lab, University College London, with support from the EU Marie Curie Initial Training Network CEREBNET (FP7-ITN-PEOPLE-2008; 238686).

Thanks to Robert Pröpper (author of spykeutils) for testing under Windows and providing bugfixes.

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